Physics 101: Lecture 08 Centripetal Acceleration and Circular Motion

http://www.youtube.com/watch?v=ZyF5WsmXRaI

 Today's lecture will cover Chapter 5

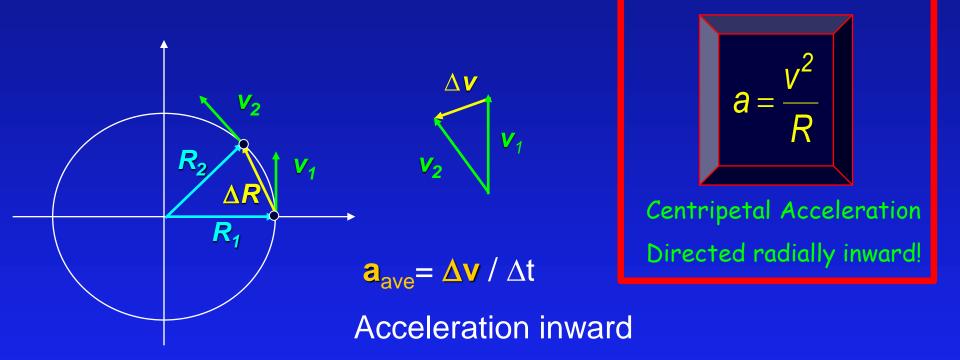


Circular Motion Act

Answer: B

A ball is going around in a circle attached to a string. If the string breaks at the instant shown, which path will the ball follow (demo)? Physics 101: Lecture 8, Pg 2

Acceleration in Uniform Circular Motion

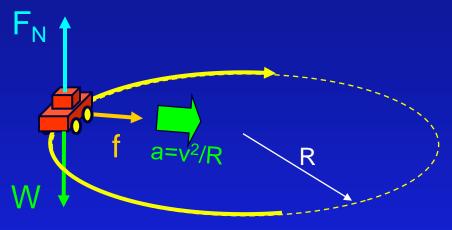


Acceleration is due to change in direction, not speed. Since the object turns "toward" center, there must be a force toward center: "Centripetal Force"

Checkpoint

Consider the following situation: You are driving a car with constant speed around a horizontal circular track. On a piece of paper, draw a Free Body Diagram (FBD) for the car. How many forces are acting on the car?

- A) 1 B) 2 C) 3
- D) 4 E) 5



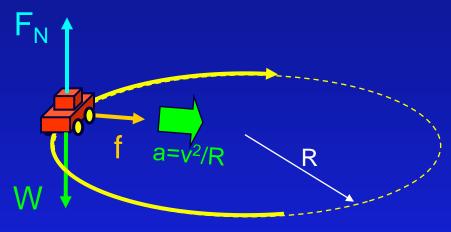
 $F_{Net} = ma = mv^2/R$

"Centripetal Force" is NOT an additional force!

Draw your FBD as normal, and one of the forces will be the Centripetal Force!

Checkpoint

Consider the following situation: You are driving a car with constant speed around a horizontal circular track. On a piece of paper, draw a Free Body Diagram (FBD) for the car. The net force on the car is



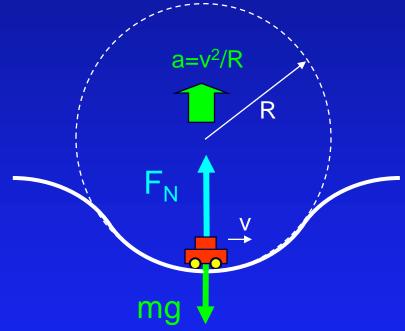
A. ZeroB. Pointing radially inwardC. Pointing radially outward

 $F_{Net} = ma = mv^2/R$

ACT

Suppose you are driving through a valley whose bottom has a circular shape. If your mass is m, what is the magnitude of the normal force F_N exerted on you by the car seat as you drive past the bottom of the hill

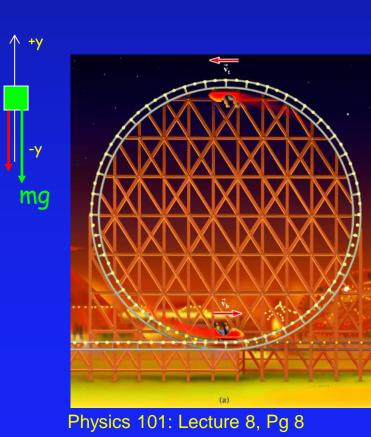
A. $F_N < mg$ B. $F_N = mg$ C. $F_N > mg$

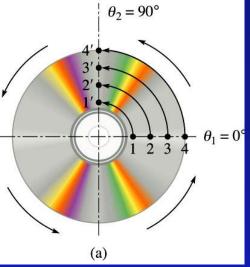


Roller Coaster Example

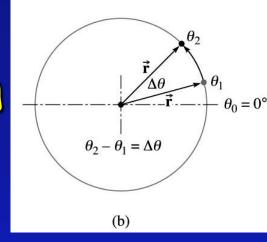
What is the minimum speed you must have at the top of a 20 meter roller coaster loop, to keep the wheels on the track?

Y Direction: $F_{Net} = ma$ $-N - mg = m a = m v^2/R$ Let N = 0, just touching $-mg = -m v^2/R$ $g = v^2 / R$ $v = sqrt(g^*R) = 9.9 m/s$





Circular Motion

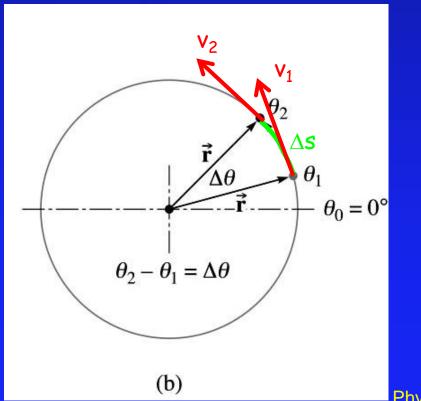


Angular displacement Δθ = θ₂-θ₁
 →How far it has rotated
 →Units radians (2π = 1 revolution)

Angular velocity ω = Δθ/Δt
 How fast it is rotating
 Units radians/second

Period =1/frequency T = 1/f = 2π / ω
 Time to complete 1 revolution

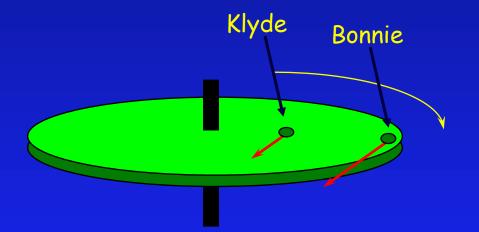
• Displacement $\Delta s = r \Delta \theta$ (θ in radians) • Speed $|v| = \Delta s / \Delta t = r \Delta \theta / \Delta t = r \omega$ • Direction of v is tangent to circle



Physics 101: Lecture 8, Pg 10

Merry-Go-Round ACT

- Bonnie sits on the outer rim of a merry-go-round with radius 3 meters, and Klyde sits midway between the center and the rim. The merry-go-round makes one complete revolution every two seconds (demo).
 - Klyde's speed is:

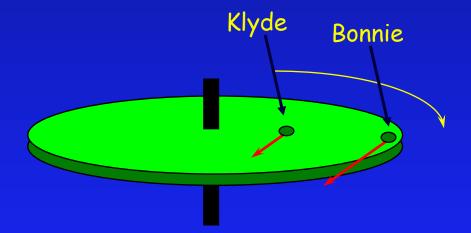


- (a) the same as Bonnie's
- (b) twice Bonnie's
- (c) half Bonnie's

Merry-Go-Round ACT II

 Bonnie sits on the outer rim of a merry-go-round, and Klyde sits midway between the center and the rim. The merry-goround makes one complete revolution every two seconds.
 Klyde's angular velocity is:

- (a) the same as Bonnie's
- (b) twice Bonnie's
- (c) half Bonnie's



Angular Acceleration

• Angular acceleration is the change in angular velocity ω divided by the change in time.

$$\overline{\alpha} \equiv \frac{\omega_f - \omega_0}{\Delta t}$$

If the speed of a roller coaster car is 15 m/s at the top of a 20 m loop, and 25 m/s at the bottom. What is the cars average angular acceleration if it takes 1.6 seconds to go from the top to the bottom?

$$\omega = \frac{V}{R} \qquad \omega_f = \frac{25}{10} = 2.5 \qquad \omega_0 = \frac{15}{10} = 1.5$$
$$\overline{\alpha} = \frac{2.5 - 1.5}{1.6} = 0.64 \text{ rad/s}^2$$

Summary (with comparison to 1-D kinematics)

Linear	
a = constant	
$v = v_0 + at$	
$x = x_0 + v_0 t + \frac{1}{2} a t^2$	
And for a point at a distance <i>R</i> from the rotation axis:	
$a = \alpha R$ $a = \alpha R$	

CD Player Example

• The CD in a disk player spins at about 20 radians/second. If it accelerates uniformly from rest with angular acceleration of 15 rad/s², how many revolutions does the disk make before it is at the proper speed?

$$\omega_{0} = 0$$

$$\omega_{f} = 20 \text{ rad/s}$$

$$\alpha = 15 \text{ rad/s}^{2}$$

$$\Delta \theta = ?$$

$$\omega_{f}^{2} = \omega_{0}^{2} + 2\alpha \Delta \theta$$

$$\frac{\omega_{f}^{2} - \omega_{0}^{2}}{2\alpha} = \Delta \theta$$

$$\frac{20^{2} - 0^{2}}{2\alpha} = \Delta \theta$$

 2×15

$$\omega_0 + 2\alpha\Delta\theta$$

 $\Delta\theta$

= 13.3 radians 1 Revolutions = 2π radians $\Delta \theta = 13.3$ radians

= 2.12 revolutions

Summary of Concepts

- Uniform Circular Motion
 - Speed is constant
 - Direction is changing
 - \rightarrow Acceleration toward center a = v² / r
 - Newton's Second Law F = ma
- Circular Motion
 - $\rightarrow \theta$ = angular position radians
 - $\rightarrow \omega$ = angular velocity radians/second
 - $\Rightarrow \alpha$ = angular acceleration radians/second²
 - \rightarrow Linear to Circular conversions $s = r \theta$
- Uniform Circular Acceleration Kinematics
 Similar to linear!