

1-Body Motion $\vec{f} = \dot{\vec{p}} = m\ddot{\vec{r}} \quad \vec{p} = m\vec{v} = m\dot{\vec{r}}$

$\vec{l} \equiv \vec{r} \times \vec{p} \quad \vec{\tau} \equiv \vec{r} \times \vec{f} = \dot{\vec{l}} \quad \vec{f}_{EM} = q(\vec{E} + \vec{v} \times \vec{B})$

$\vec{f}_{air} = -(bv + cv^2)\hat{v} = \vec{f}_{lin} + \vec{f}_{quad} \quad \text{Reynolds } R \equiv Dv\rho / \eta$

sphere, diameter D: $b = \beta D \quad c = \gamma D^2 \quad R = 48 f_{quad} / f_{lin}$

Rocket Motion $m\dot{v} = -\dot{m}v_{ex} + F^{EXT}$

Miscellaneous $1 \text{ m/s} \approx 2 \text{ mph}$

$f_{friction} = \mu F_N \quad \vec{f}_{grav} = -\frac{GMm}{r^2}\hat{r}$

Collective Motion * assuming Newton's 3rd Law $\rightarrow F^{INT}$ cancel

Notation for collective properties

- unsubscripted capital letter \rightarrow "TOTAL", except for ...
- unsubscripted capital position, velocity, accel \rightarrow "OF THE CM"
- ◇ subscript \neq coordinate index \rightarrow "OF"
- ◆ no superscript \rightarrow "RELATIVE TO ORIGIN"
- ◆ superscript () \rightarrow "RELATIVE TO (POINT)"
- ◆ superscript prime' \rightarrow "RELATIVE TO THE CM"

CM: $M\vec{R} \equiv \sum_i m_i \vec{r}_i \quad \vec{P} = M\dot{\vec{R}} \quad \vec{L}_{CM} = \vec{R} \times \vec{P}$

Rotating Body: for any BODY-FIXED vector \vec{B} , $\dot{\vec{B}} = \vec{\omega} \times \vec{B}$

Moment of Inertia: for any BODY-FIXED point B,

$I_{\hat{\omega}}^{(B)} \equiv \sum m_i |\vec{r}_i^{(B)} \times \hat{\omega}|^2 \quad L_{\hat{\omega}}^{(B)} = I_{\hat{\omega}}^{(B)} \omega \quad T^{(B)} = \frac{1}{2} I_{\hat{\omega}}^{(B)} \omega^2$

Uniform Gravity: If $\vec{f}^{EXT} = m\vec{g}$ only $\rightarrow \vec{F}^{EXT} = M\vec{g} \quad \vec{\tau}^{EXT} = \vec{R} \times M\vec{g} \quad \vec{\tau}'^{EXT} = 0 \quad U^{EXT} = MgH$

EOM in Inertial Frames

$\vec{F}^{EXT} = \dot{\vec{P}}$

$\vec{\tau}^{EXT, (A)} = \dot{\vec{L}}^{(A)}$ if reference point A

- is the CM, or
- is not accelerating, or
- $\ddot{\vec{r}}_A \parallel (\vec{R} - \vec{r}_A)$

$T + U^{EXT} + U^{INT} = \text{conserved for conservative forces}$

Decompositions

$\vec{P} = \vec{P}_{CM} \quad I_{\hat{\omega}}^{(B)} = I_{CM, \hat{\omega}}^{(B)} + I'_{\hat{\omega}}$

$\vec{L} = \vec{L}_{CM} + \vec{L}' \quad \vec{\tau}_{CM}^{EXT} = \dot{\vec{L}}_{CM}$

$T = T_{CM} + T' \quad T = T^{(\text{stationary point})}$