

1-Body Motion	$\vec{f} = \dot{\vec{p}} = m\ddot{\vec{r}}$	$\vec{p} = m\vec{v} = m\dot{\vec{r}}$	Rocket Motion	$m\dot{v} = -\dot{m}v_{ex} + F^{ext}$
$\vec{l} \equiv \vec{r} \times \vec{p}$	$\vec{\tau} \equiv \vec{r} \times \vec{f} = \dot{\vec{l}}$	$\vec{f}_{EM} = q(\vec{E} + \vec{v} \times \vec{B})$	Miscellaneous	$1 \text{ m/s} \approx 2 \text{ mph}$
$\vec{f}_{air} = -(bv + cv^2)\hat{v} = \vec{f}_{lin} + \vec{f}_{quad}$		$\text{Reynolds } R \equiv Dv\rho / \eta$	$f_{friction} = \mu F_N$	$\vec{f}_{grav} = -\frac{GMm}{r^2}\hat{r}$
sphere, diameter D: $b = \beta D$	$c = \gamma D^2$	$R = 48 f_{quad} / f_{lin}$		

Collective Motion * assuming Newton's 3rd Law $\rightarrow F^{int}$ cancel

Notation for collective properties

- unsubscripted capital letter \rightarrow "TOTAL", except for ...
- unsubscripted capital position, velocity, accel \rightarrow "OF THE CM"
- ◊ subscript \neq coordinate index \rightarrow "OF"
- ◆ no superscript \rightarrow "RELATIVE TO ORIGIN"
- ◆ superscript () \rightarrow "RELATIVE TO (POINT)"
- ◆ superscript prime' \rightarrow "RELATIVE TO THE CM"

$$\text{CM: } M\vec{R} \equiv \sum_i m_i \vec{r}_i \quad \vec{P} = M\dot{\vec{R}} \quad \vec{L}_{CM} = \vec{R} \times \vec{P}$$

Rotating Body: for any BODY-FIXED vector \vec{B} , $\dot{\vec{B}} = \vec{\omega} \times \vec{B}$

Moment of Inertia: for any BODY-FIXED point B ,

$$I_{\hat{\omega}}^{(B)} \equiv \sum_i m_i |\vec{r}_i^{(B)} \times \hat{\omega}|^2 \quad L_{\omega}^{(B)} = I_{\hat{\omega}}^{(B)} \omega \quad T^{(B)} = \frac{1}{2} I_{\hat{\omega}}^{(B)} \omega^2$$

Uniform Gravity: If $\vec{f}^{ext} = m\vec{g}$ only $\rightarrow \vec{F}^{ext} = M\vec{g} \quad \vec{\tau}^{ext} = \vec{R} \times M\vec{g} \quad \vec{\tau}'^{ext} = 0 \quad U^{ext} = MgH$

Variational Calc / Mech * Gen. coord q_i must be indep

$$S \equiv \int_{t_1, \vec{q}_1}^{t_2, \vec{q}_2} dt L(q_i, \dot{q}_i, t) \quad \delta S = 0 \rightarrow \frac{\partial L}{\partial q_i} = \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_i} \right) \text{ for each } q_i$$

$H \equiv \dot{q}_i (\partial L / \partial \dot{q}_i) - L$ conserved when $\partial L / \partial t = 0$

Mechanics Principle of Least Action : $L = T - U \rightarrow \delta S = 0 @ \text{ true } \{q_i(t)\}$

$$\text{Gen. force } Q_i \equiv \frac{\partial L}{\partial q_i}, \text{ momentum } p_i \equiv \frac{\partial L}{\partial \dot{q}_i}$$

$$H \equiv p_i \dot{q}_i - L \text{ equals } T+U \text{ when } \vec{r}_a = \vec{r}_a(q_i)$$