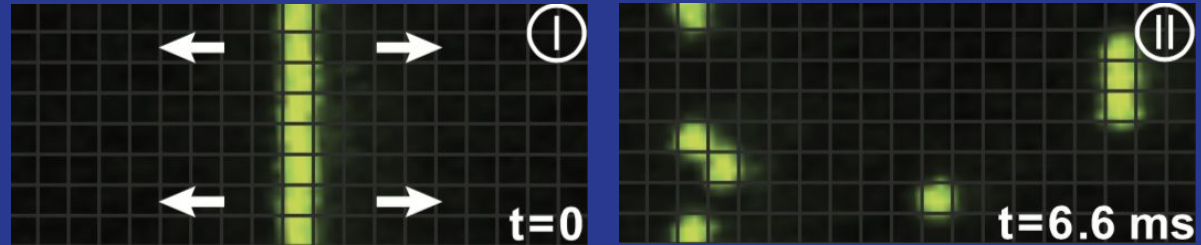


It's a Boson! No wait, it's two Bosons!

Quantum Walks in Optical Lattices

Team 5 (LLLK):
Nicholas Kowalski
David Lee
Ryan Levy
Min Li



The Paper

Strongly correlated quantum walks in optical lattices

Philipp M. Preiss¹, Ruichao Ma¹, M. Eric Tai¹, Alexander Lukin¹, Matthew Rispoli¹, Philip Zupancic^{1,*}, Yoav Lahini², Rajibul Islam¹, Markus Greiner^{1,†}

+ Author Affiliations

↩[†]Corresponding author. E-mail: greiner@physics.harvard.edu

↩^{*} Present address: Institute for Quantum Electronics, ETH Zürich, 8093 Zürich, Switzerland.

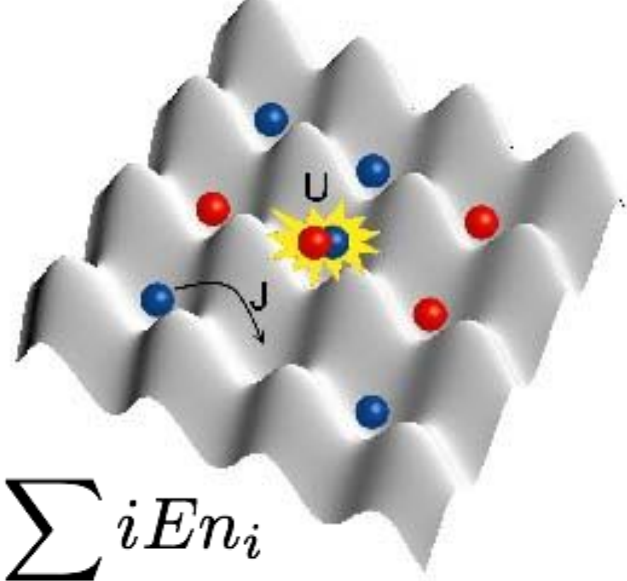
Science 13 Mar 2015:
Vol. 347, Issue 6227, pp. 1229-1233
DOI: 10.1126/science.1260364

Introduction

- Cold atoms experiments realize toy model Hamiltonians
 - Strong collaborations between theorists and experimentalists
 - Ability to observe weakly interacting many-body systems to strongly correlated dynamics
 - *Bose-Hubbard Model* - simple theoretical model of interacting bosons on optical lattice
- Can probe interesting physics
 - Many-body localization and dynamics of interacting quantum disordered systems
 - Universal and efficient quantum computation
 - Quantum effects when more than one particle participates in the quantum walk simultaneously - Hanbury Brown and Twiss (HBT) effect

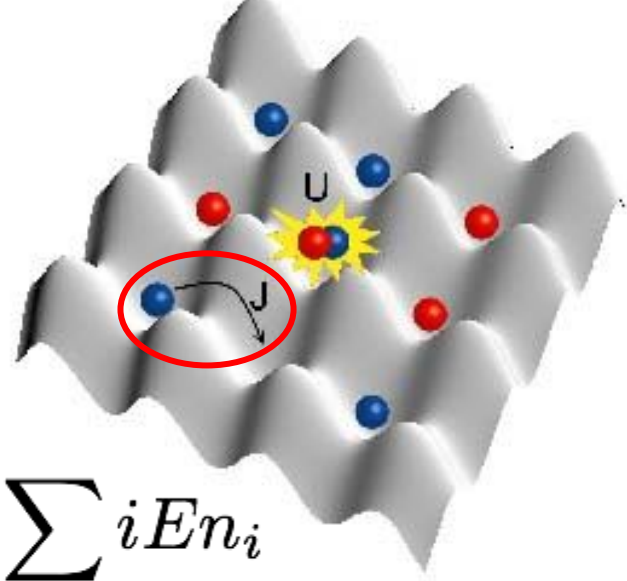


Hamiltonian for interacting bosons on a lattice.



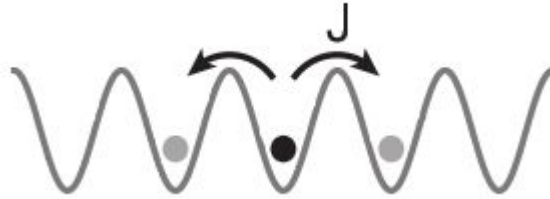
$$H_{BH} = \sum_{\langle i,j \rangle} J a_i^\dagger a_j + \sum_i \frac{U}{2} n_i (n_i - 1) + \sum_i \epsilon E n_i$$

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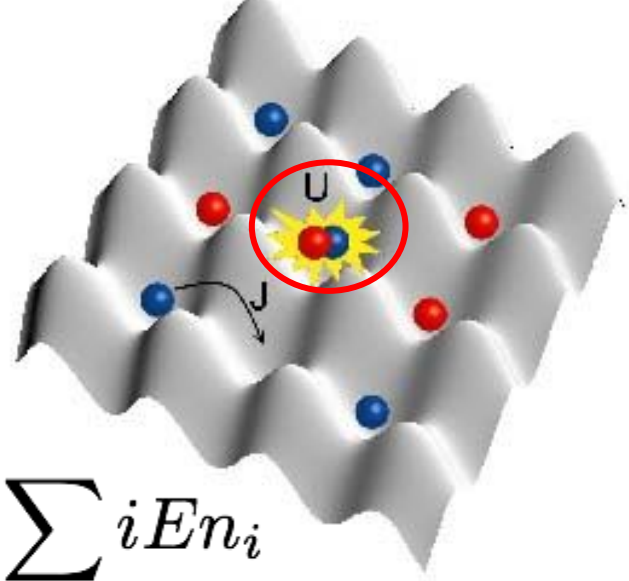


$$H_{BH} = \boxed{\sum_{\langle i,j \rangle} J a_i^\dagger a_j} + \sum_i \frac{U}{2} n_i (n_i - 1) + \sum_i \epsilon E n_i$$

J -tunneling amplitude
between lattice sites



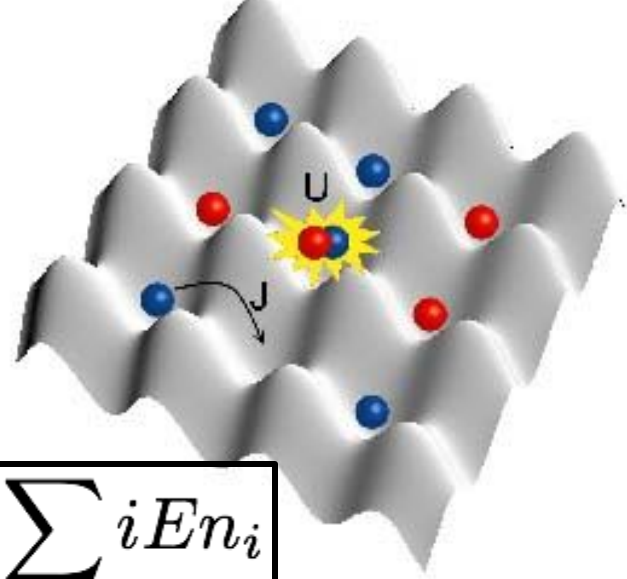
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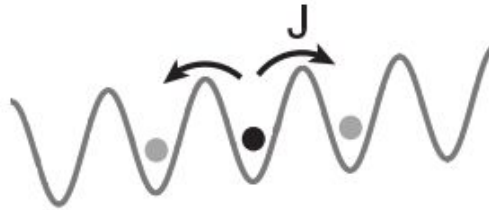
U -repulsive on site interaction

Hamiltonian for interacting bosons on a lattice.

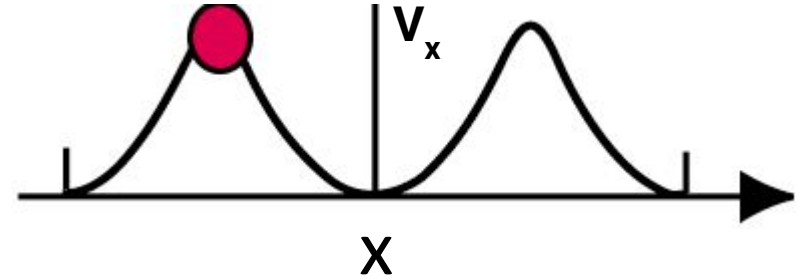


$$H_{BH} = \sum_{\langle i,j \rangle} J a_i^\dagger a_j + \sum_i \frac{U}{2} n_i (n_i - 1) + \boxed{\sum_i i E n_i}$$

E -energy shift
per lattice site

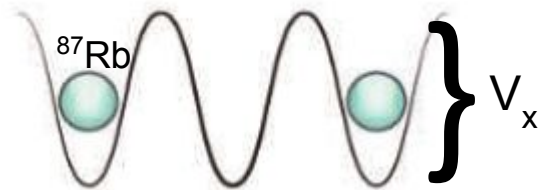


Potential Gradient Induces Bloch Oscillations



- Oscillations of a quantum particle within a small length scale in position space when exposed to external force
- Dispersion of probability distribution in position space
- Refocuses to initial position after one oscillation period

Experimental Setup



- Ultracold Bosonic ^{87}Rb atoms in an optical lattice
- Atoms initially prepared in 2D Mott Insulator (1-2 atoms per site)
- Potential is flattened in one direction to allow quantum walk (performed at reduced lattice depth V_x)
- Fluorescence imaging in deep optical lattice
- Pairs separated by magnetic field along direction of quantum walk prior to imaging

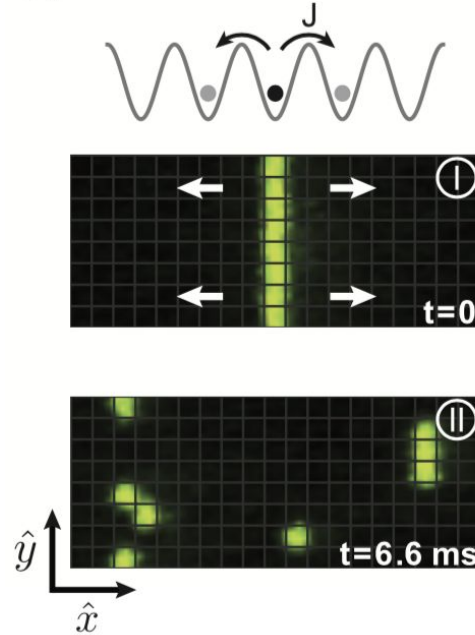


Single Particle Quantum Walk

- A: Without potential

- Particles spread linearly
- Interference leads to coherent wavefront rather than Gaussian like classical walk

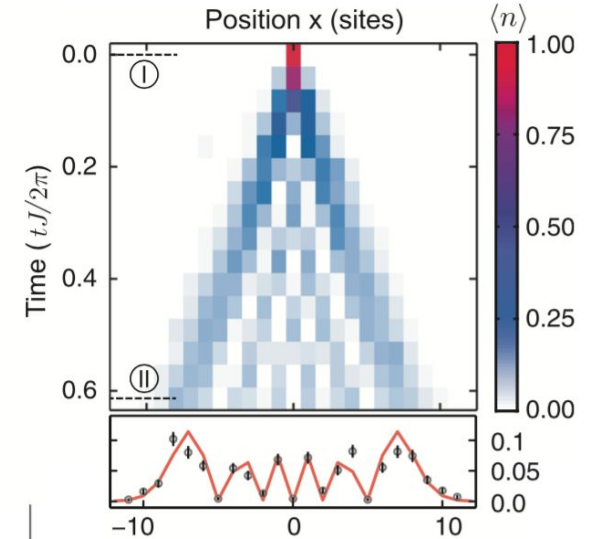
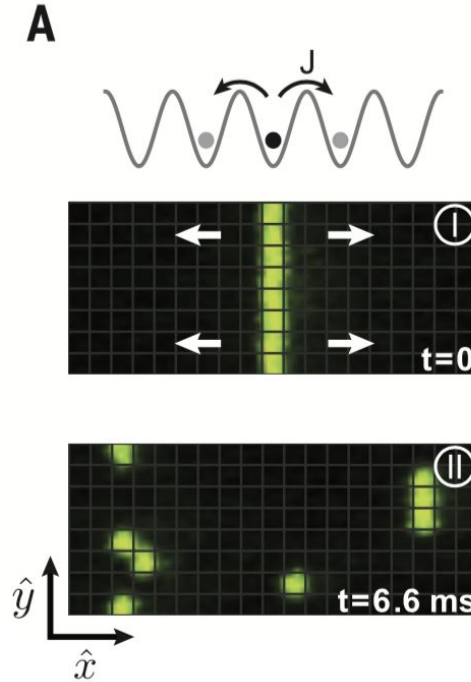
A



Single Particle Quantum Walk

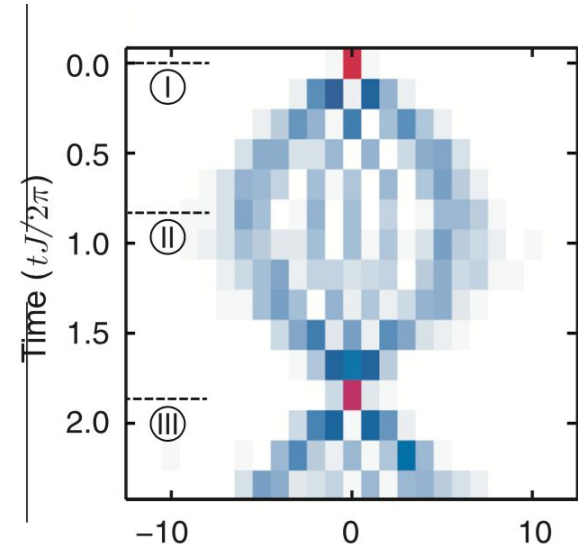
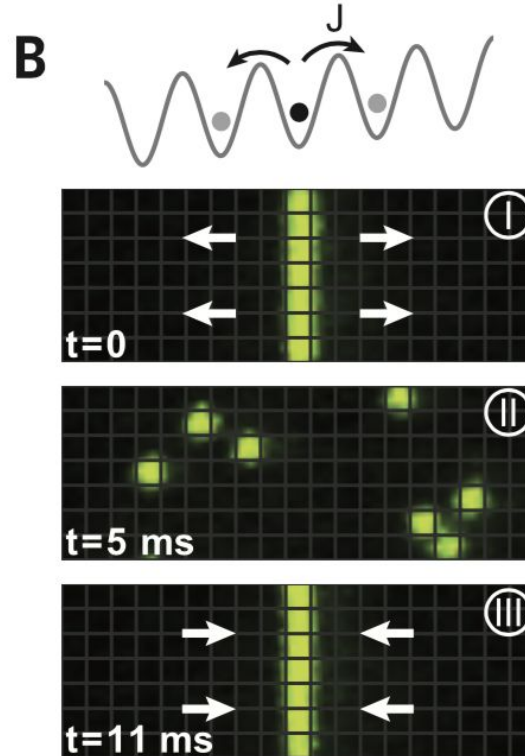
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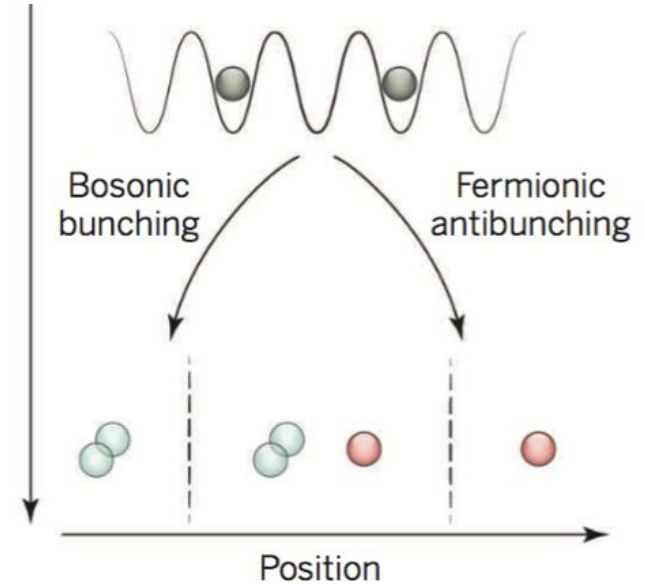
Single Particle Quantum Walk

- B: With potential
 - Particles undergo Bloch oscillation
 - Particles localized to small volume

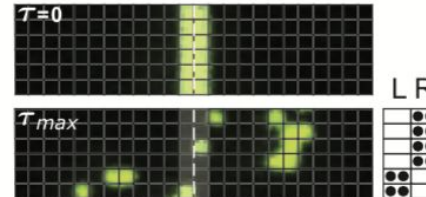


Two-Particle Quantum Walk

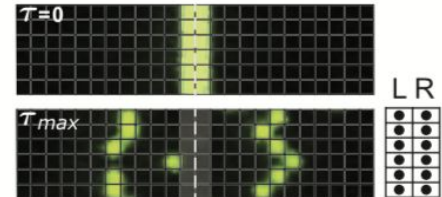
- Particles undergo Hanbury Brown and Twiss interference
- Bosons add constructively in close proximity
 - Leads to bunching
- Fermions add destructively
 - Leads to antibunching
- With strong repulsive interactions, bosonic particle pairs undergo “fermionization”



(I) weakly interacting bosons

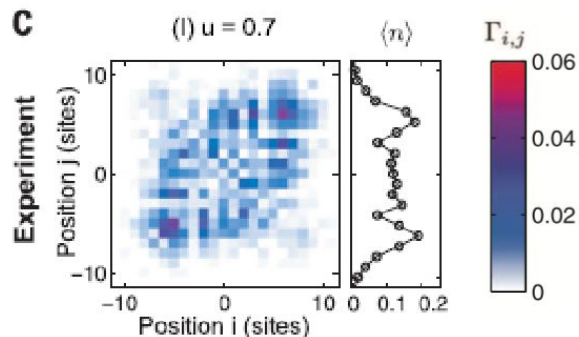


(II) strongly interacting bosons
fermionized regime



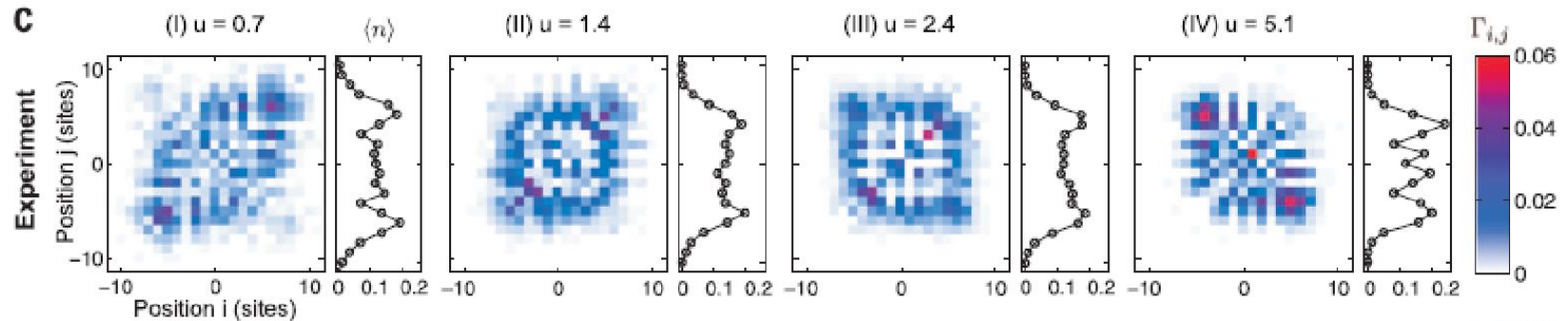
Two-Particle Fermionization

- Two particles starting in adjacent sites $a_0^\dagger a_1^\dagger |0\rangle$
- As interaction strength increases, repulsive interactions compete with and overcome HBT interference



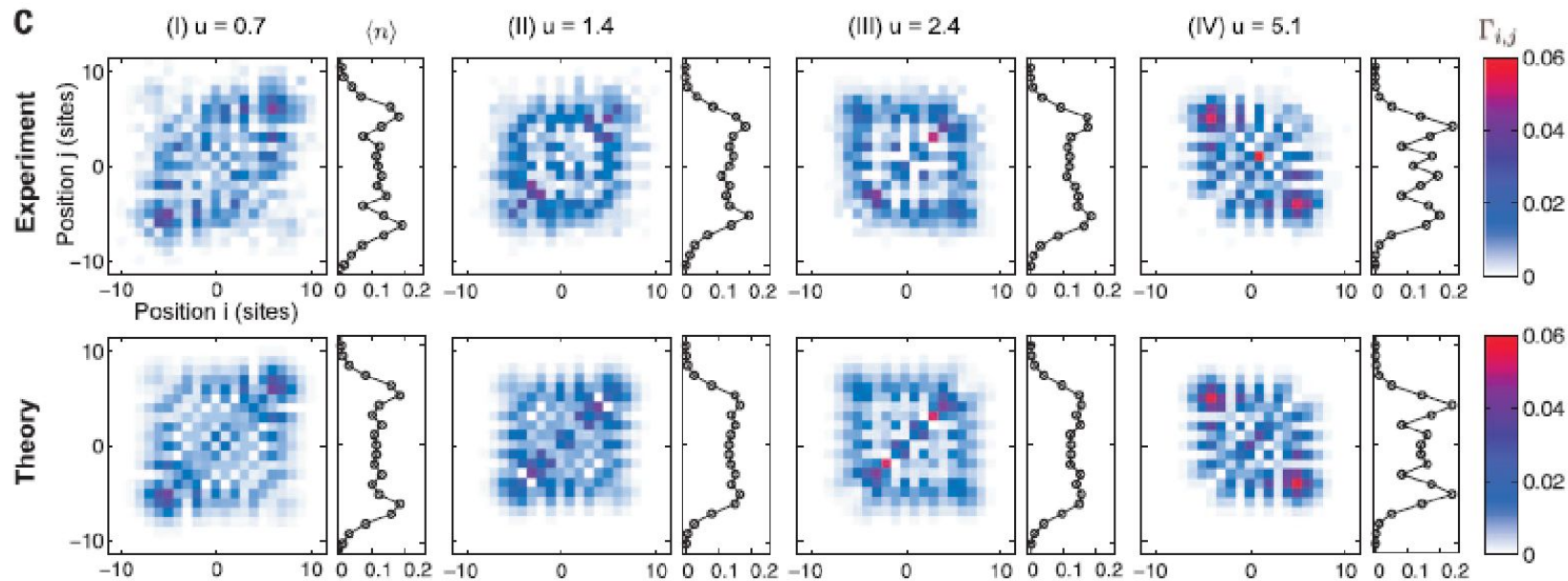
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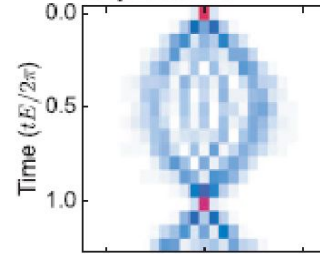
Strong Interactions: Repulsively Bound Pairs

- Two particles starting in same state $(1/\sqrt{2})a_0^\dagger a_0^\dagger |0\rangle$
- For weak interactions, particles act independently

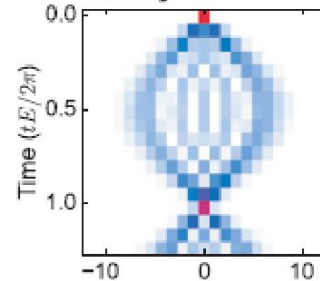


(I) $u = 0.3$

Experiment



Theory



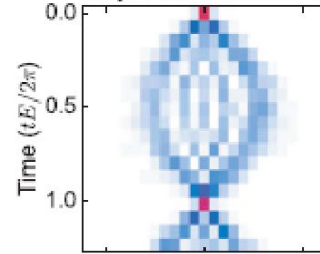
Strong Interactions: Repulsively Bound Pairs

- Two particles starting in same state $(1/\sqrt{2})a_0^\dagger a_0^\dagger |0\rangle$
- For weak interactions, particles act independently
- For strong interactions, particles move together as a repulsively bound pair

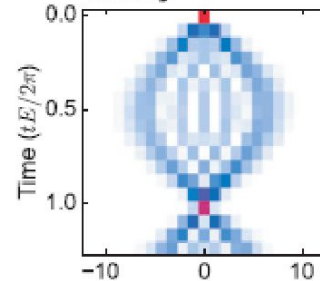


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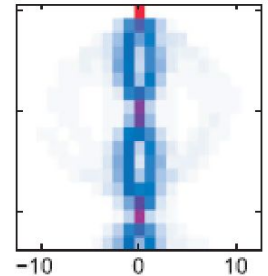
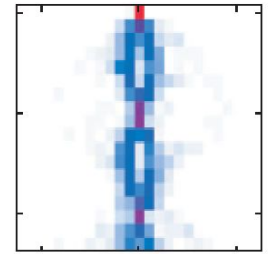
Theory



Position (sites)

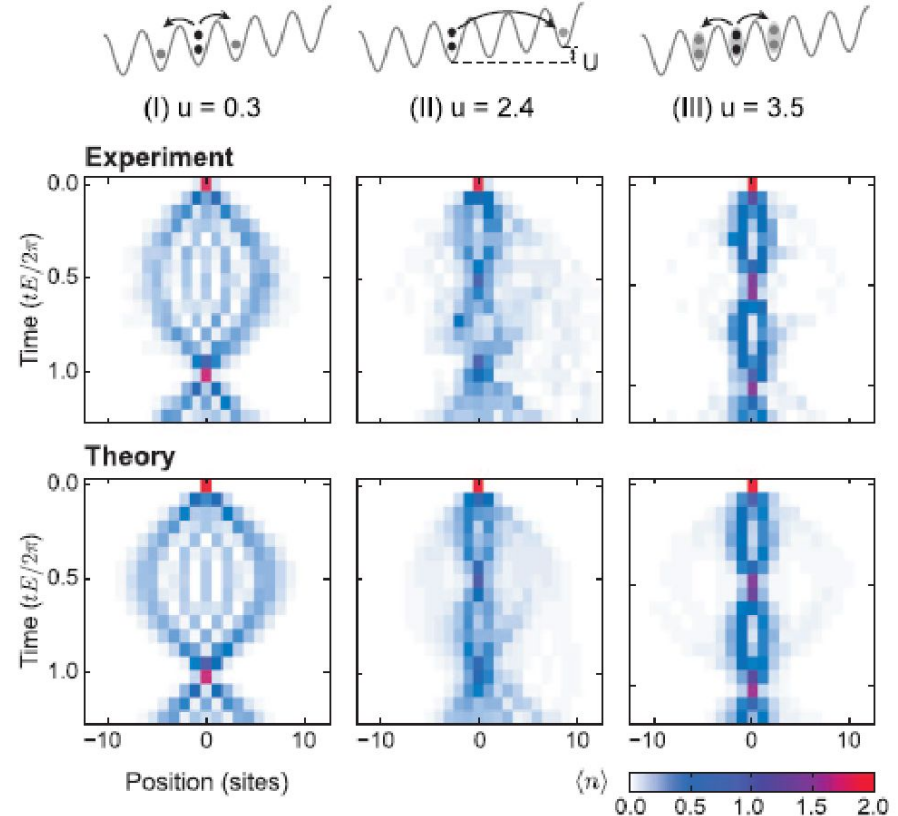


(III) $u = 3.5$

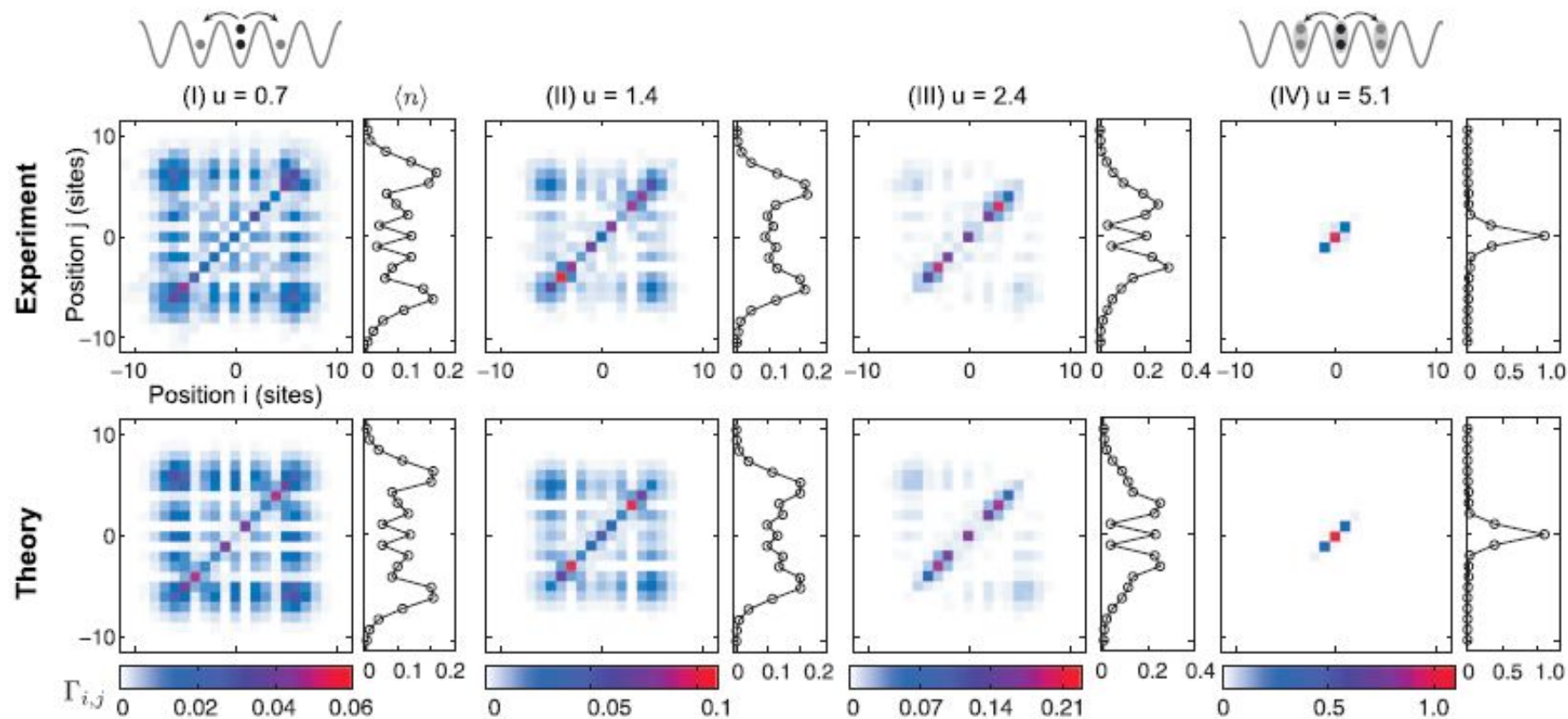


Strong Interactions: Repulsively Bound Pairs

- Two particles starting in same state $(1/\sqrt{2})a_0^\dagger a_0^\dagger |0\rangle$
- For weak interactions, particles act independently
- For strong interactions, particles move together as a repulsively bound pair
- Complicated dynamics in intermediate regime



Repulsively Bound Pairs (cont.)



Citation Analysis

- Paper Birthday: March 2015 (~1 year 9 months)
- 59 citations
 - ~50% experimental, ~50% theoretical
 - 3 papers specifically proposed new methods of studying similar systems
 - 4 papers from the same group
 - Many papers that provided more complex conditions:
 - cylindrical environments
 - fermionic atoms (Ytterbium atoms!)
 - polarized atoms



Citation Analysis - Notable Papers

- Most cited citing paper:

- Site-Resolved Imaging of Fermionic ${}^6\text{Li}$ in an Optical Lattice

Maxwell F. Parsons, Florian Huber, Anton Mazurenko, Christie S. Chiu, Widagdo Setiawan, Katherine Wooley-Brown, Sebastian Blatt, and Markus Greiner

Phys. Rev. Lett. **114**, 213002 – Published 28 May 2015

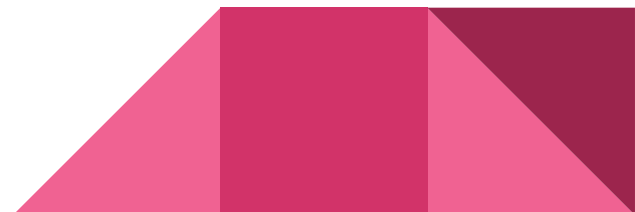
- 34 citations and same corresponding author
- Many more Lithium papers among citing (common cold atom)

- Extra interesting paper:

Quantum coherent oscillations in the early universe

Igor Pikovski and Abraham Loeb

Phys. Rev. D **93**, 101302(R) – Published 25 May 2016



Paper Critique

- Good:
 - Really great data!
 - Well polished paper
 - Publicly accessible abstract included
- Bad:
 - Lots of acronyms with little help for those outside the field
 - Does not describe methods in great detail (nor citations)



Conclusion

- Preiss, *et al.*, developed a system to create *2-particle* bosonic random walks in an optical lattice
- This system matched theoretical predictions and principal effects both non-interacting and a strongly correlated system
 - Observed Bloch oscillations and HBT effects
- This technique provides access to the exploration of fundamental condensed matter systems
 - Ex: Microscopies of complicated systems, such as ones with disorder and rapid changes (quench)

