

Physic 102 formula sheet

Kinematics and mechanics

$$x = x_0 + v_0 t + \frac{1}{2} a t^2 \qquad v = v_0 + a t \qquad v^2 = v_0^2 + 2a \Delta x$$

$$F = m a \qquad a_c = \frac{v^2}{r}$$

$$E_{\text{tot}} = K + U \qquad K = \frac{1}{2} m v^2 = \frac{p^2}{2m} \qquad p = m v \qquad W_F = F d \cos \theta \qquad P = F v \cos \theta$$

Electrostatics

$$F_{12} = k \frac{q_1 q_2}{r^2} \qquad E = \frac{F}{q_0} \qquad U_{12} = k \frac{q_1 q_2}{r} \qquad V \equiv \frac{U}{q_0} \qquad W_E = -\Delta U = -W_{\text{you}}$$

$$\text{Point charge} \qquad E = k \frac{q}{r^2} \qquad V = k \frac{q}{r}$$

$$\text{Electric dipole} \qquad p = q d \qquad \tau_{\text{dip}} = p E \sin \theta \qquad U_{\text{dip}} = -p E \cos \theta$$

Resistance

$$R = \frac{V}{I} \qquad I = \frac{\Delta q}{\Delta t} \qquad \text{Physical resistance: } R = \rho \frac{L}{A}$$

$$P = IV = I^2 R = \frac{V^2}{R} \qquad R_S = R_1 + R_2 + \dots \qquad \frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

Capacitance

$$C = \frac{Q}{V} \qquad \text{Parallel plate capacitor: } C = \frac{\kappa \epsilon_0 A}{d} \qquad E = \frac{Q}{\epsilon_0 A} \qquad V = E d$$

$$U_C = \frac{1}{2} Q V = \frac{1}{2} C V^2 = \frac{1}{2} \frac{Q^2}{C} \qquad C_P = C_1 + C_2 + \dots \qquad \frac{1}{C_S} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

Circuits

$$\sum \Delta V = 0 \qquad \sum I_{\text{in}} = \sum I_{\text{out}}$$

$$q(t) = q_{\infty} (1 - e^{-t/\tau}) \qquad q(t) = q_0 e^{-t/\tau} \qquad I(t) = I_0 e^{-t/\tau} \qquad \tau = RC$$

Magnetism

$$F = q v B \sin \theta \qquad r = \frac{m v}{q B} \qquad F_{\text{wire}} = I L B \sin \theta \qquad \tau_{\text{loop}} = N I A B \sin \varphi$$

$$\text{Magnetic dipole:} \qquad \mu = N I A \qquad \tau_{\text{dip}} = \mu B \sin \varphi \qquad U_{\text{dip}} = -\mu B \cos \varphi$$

$$B_{\text{wire}} = \frac{\mu_0 I}{2 \pi r} \qquad B_{\text{sol}} = \mu_0 n I$$

Electromagnetic induction

$$\mathcal{E} = -N \frac{\Delta \Phi}{\Delta t} \qquad \Phi = B A \cos \varphi$$

$$|\mathcal{E}_{\text{bar}}| = B L v \qquad \mathcal{E}_{\text{gen}} = \mathcal{E}_{\text{max}} \sin \omega t = \omega N A B \sin \omega t \qquad \omega = 2 \pi f$$

$$V_{\text{rms}} = \frac{V_{\text{max}}}{\sqrt{2}} \qquad I_{\text{rms}} = \frac{I_{\text{max}}}{\sqrt{2}} \qquad \frac{V_p}{V_s} = \frac{I_s}{I_p} = \frac{N_p}{N_s}$$

Right-hand rule (RHR) reminders

Find the force on a moving positive charge:

1. Fingers point along the velocity direction
2. Curl fingers toward the magnetic field
3. Magnetic force points in the direction of your thumb

Find the direction of a magnetic field due to a current:

1. Thumb points along the (positive) current
2. The curl of your fingers shows the orientation of the magnetic field around the current

Electromagnetic waves

$$\lambda = \frac{c}{f} \qquad E = cB$$

$$u_E = \frac{1}{2}\epsilon_0 E^2 \qquad u_B = \frac{1}{2\mu_0} B^2 \qquad \bar{u} = \frac{1}{2}\epsilon_0 E_{\text{rms}}^2 + \frac{1}{2\mu_0} B_{\text{rms}}^2 = \epsilon_0 E_{\text{rms}}^2 = \frac{B_{\text{rms}}^2}{\mu_0} \qquad S = I = \bar{u}c = \frac{P}{A}$$

$$f_0 = f_e \sqrt{\frac{1 + v_{\text{rel}}/c}{1 - v_{\text{rel}}/c}} \approx f_e \left(1 + \frac{v_{\text{rel}}}{c}\right) \qquad I = I_0 \cos^2 \theta \qquad E_{\text{rms}}^2 = E_0^2/2$$

Reflection and refraction

$$\theta_r = \theta_i \qquad \frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \qquad f = \pm \frac{R}{2} \qquad m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \qquad v = \frac{c}{n} \qquad \sin \theta_c = \frac{n_2}{n_1} \qquad M = \frac{\theta'}{\theta} \approx \frac{d_{\text{near}}}{f}$$

$$\text{Compound microscope:} \qquad m_{\text{obj}} = \frac{L_{\text{tube}}}{f_{\text{obj}}} \qquad M_{\text{eye}} = \frac{d_{\text{near}}}{f_{\text{eye}}} \qquad M_{\text{tot}} = M_{\text{eye}} m_{\text{obj}}$$

Interference and diffraction

$$\text{Double-slit interference:} \qquad d \sin \theta = m\lambda \qquad d \sin \theta = \left(m + \frac{1}{2}\right)\lambda \qquad m = 0, \pm 1, \pm 2, \dots$$

$$\text{Single-slit diffraction:} \qquad a \sin \theta = m\lambda \qquad m = 0, \pm 1, \pm 2, \dots$$

$$\text{Circular aperture:} \qquad D \sin \theta \approx 1.22\lambda$$

Constants and unit conversion

$$g = 9.8 \text{ m/s}^2 \qquad e = 1.60 \times 10^{-19} \text{ C}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2 \qquad k \equiv \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2 \qquad \mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$$

$$c = \frac{1}{\sqrt{\epsilon_0\mu_0}} = 3 \times 10^8 \text{ m/s} \qquad h = 6.626 \times 10^{-34} \text{ J} \cdot \text{s} \qquad hc = 1240 \text{ eV} \cdot \text{nm}$$

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J} \qquad m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg} = 511 \text{ keV}/c^2$$

$$m_{\text{proton}} = 1.673 \times 10^{-27} \text{ kg} = 938 \text{ MeV}/c^2 \qquad m_{\text{neutron}} = 1.675 \times 10^{-27} \text{ kg} = 939.5 \text{ MeV}/c^2$$

SI Prefixes

Power	Prefix	Symbol
10^9	giga	G
10^6	mega	M
10^3	kilo	k
10^0	—	—
10^{-3}	milli	m
10^{-6}	micro	μ
10^{-9}	nano	n
10^{-12}	pico	p