Name:												
NetID:				Le	ectur	e:	\mathbf{A}	В				
Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6

(15 points) When senators enter the Magical Senate, the scanner outputs W for a wizard, E for an elf, G for a goblin. The Magical Senate cannot do business unless at least two wizards, one elf, and one goblin are present. Draw a state machine that reads a sequence of characters from the scanner. When it has seen enough participants of each type, it should enter an end state and stay there.

For readability, your drawing should show only transitions that move from one state to another. The house elves will add all required self-loops later, when they implement this in hardware. Your design should use no more than 16 states and, if you can, no more than 13.

Name:												
NetID:				Le	ecture	e:	\mathbf{A}	В				
Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6

(5 points) Amber Industries makes a line of necklaces featuring a mama brown bear leading an infinite line of baby bears. The baby bears get smaller and smaller, so the whole necklace is only 6 inches long. Each baby bear has either brown or cream fur, with no restrictions on the pattern of baby bear colors in the necklace. Is the set of possible necklaces countable or uncountable? Briefly justify your answer.

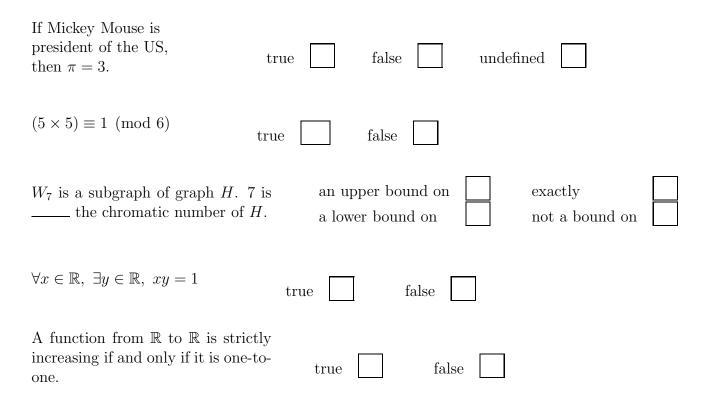
(10 points) Check the (single) box that best characterizes each item.

The interval $[2,3]$ of the real line.	finite countably infinite uncountable
If $f: A \to B$ is one-to-one	$ A < B \qquad A \le B \qquad A = B $
All infinite sequences of emojis	finite countably infinite uncountable
All partitions of the set of natural numbers less than 10,000.	finite countably infinite uncountable
We can build a program that decides whether an input program halts.	true false not known

Name:												
NetID:					ectur	e:	\mathbf{A}	В				
Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6

(5 points) Hermione Grainger has 7000 socks in her magically expanding drawer. The socks are colored purple, magenta, shocking pink, and neon green. How many socks must she pull out of the drawer before she is guaranteed to have two socks of the same color. Briefly justify your answer.

(10 points) Check the (single) box that best characterizes each item.



Name:												
NetID:					ecture	e:	\mathbf{A}	В				
Discussion:	Thursday	Friday	9	10	11	12	1	2	3	4	5	6

(5 points) Recall that the symmetric difference of two sets A and B written $A \oplus B$ contains all the elements that are in one of the two sets but not the other. That is $A \oplus B = (A - B) \cup (B - A)$. For any set of integers A, let $[A] = \{B \in \mathbb{P}(\mathbb{Z}) \mid A \oplus B \text{ is finite }\}$

Explain clearly what is in $[\{1, 2, 3\}]$. Also, is it true that $[\mathbb{Z}] = [\mathbb{N}]$? Briefly justify your answer.

(10 points) Check the (single) box that best characterizes each item.

