

**Theory Exam 2 - TA Review Session**  
7:30pm – 9:00pm · Tomorrow, Tuesday, Oct. 9, 2018  
1404 Siebel Center

**Binary Search Tree (BST) Finale**

**Q:** How does our data determine the height?

1 3 2 4 5 7 6      vs.      4 2 3 6 7 1 5

**Q:** How many different ways are there to insert data into a BST?

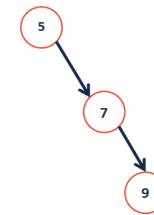
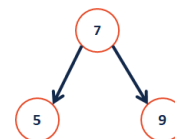
**Q:** What is the average height of every arrangement?

....what's the intuition for this argument?

operation	BST Avg. Case	BST Worst Case	Sorted Array	Sorted List
find				
insert				
delete				
traverse				

**Height Balance on BST**

What tree makes you happier?

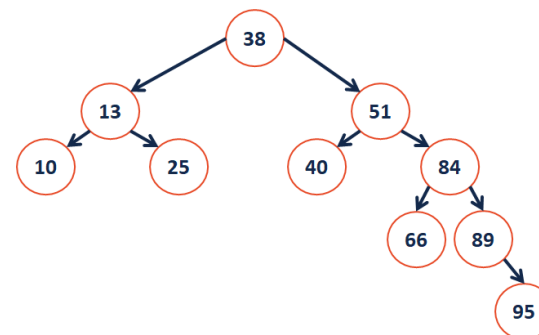


Let us describe the **balance (b)** of a BST to be:

- If **b** is negative:
- If **b** is positive:

We define a BST tree T to be **height balanced** if:

A node is considered to be **out of balance** if it's not height balanced. What is the lowest node that is out of balance?



## Brining a tree back into balance

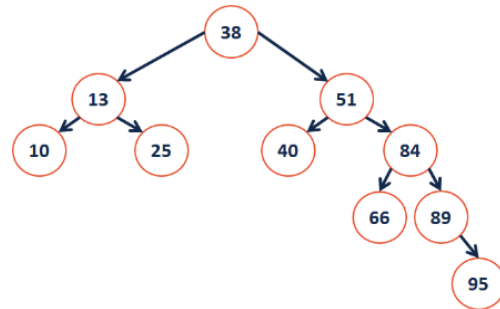
Goal: Create a strategy to bring a BST back into balance after an operation has caused the tree to be out of balance.

A **Tree Rotation** is an operation that maintains two properties:

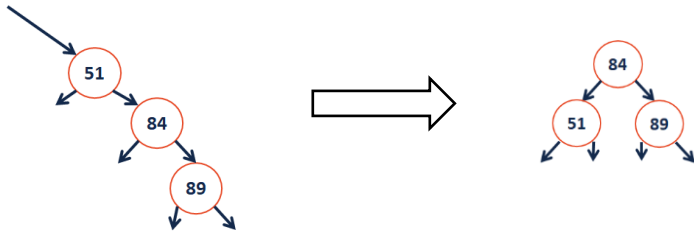
- 1.
- 2.

### Example 1: Defining a Rotation

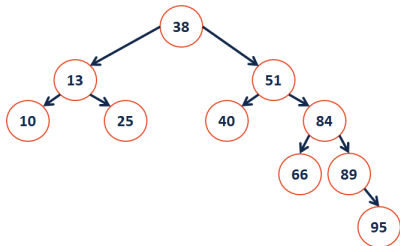
1. Where is the deepest point of imbalance in the tree: →



2. Perform a left rotation to balance this tree:

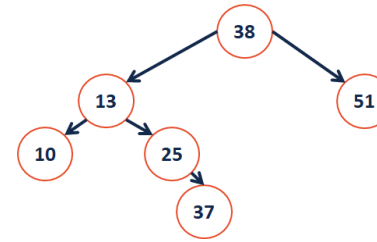


### Implementing a left rotation:



## Example 2: A Complex Rotation

Rotation #1:



Rotation #2:

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### BST Rotation Summary:

1. Four kinds of rotations (L, R, LR, and RL)
2. All rotations are local
3. All rotations run in constant time,  $O(1)$
4. BST property is maintained!

### Overall Goal:

...and we call these trees:

CS 225 – Things To Be Doing:
<ol style="list-style-type: none"><li>1. Theory Exam 2 starts next Thursday (topic list is online)</li><li>2. MP3 due <b>tonight</b>; MP4 released on Tuesday</li><li>3. lab_huffman released Wednesday</li><li>4. Daily POTDs</li></ol>