

A Review of Major Data Structures so Far

Array-based	List/Pointer-based
<ul style="list-style-type: none"> <li>- Sorted Array</li> <li>- Unsorted Array</li> <li>- Stacks</li> <li>- Queues</li> <li>- Hashing</li> <li>- Heaps</li> <li>- Priority Queues</li> <li>- UpTrees</li> <li>- Disjoint Sets</li> </ul>	<ul style="list-style-type: none"> <li>- Singly Linked List</li> <li>- Doubly Linked List</li> <li>- Skip Lists</li> <li>- Trees</li> <li>- BTree</li> <li>- Binary Tree</li> <li>- Huffman Encoding</li> <li>- kd-Tree</li> <li>- AVL Tree</li> </ul>

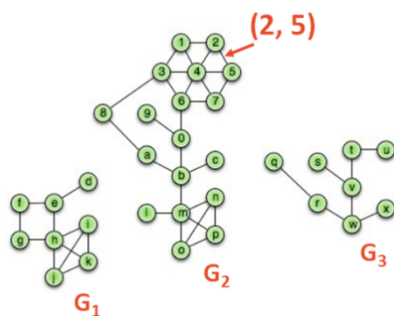
Motivation:

Graphs are awesome data structures that allow us to represent an enormous range of problems. To study these problems, we need:

1. A common vocabulary to talk about graphs
2. Implementation(s) of a graph
3. Traversals on graphs
4. Algorithms on graphs

Graph Vocabulary

Consider a graph  $G$  with vertices  $V$  and edges  $E$ ,  $G=(V,E)$ .



Incident Edges:

$$I(v) = \{ (x, v) \text{ in } E \}$$

Degree(v):  $|I|$

Adjacent Vertices:

$$A(v) = \{ x : (x, v) \text{ in } E \}$$

Path( $G_2$ ): Sequence of vertices connected by edges

Cycle( $G_1$ ): Path with a common begin and end vertex containing at least three vertices.

Simple Graph( $G$ ): A graph with no self loops or multi-edges.

Subgraph( $G$ ):  $G' = (V', E')$ :

$$V' \in V, E' \in E, \text{ and } (u, v) \in E \rightarrow u \in V', v \in V'$$

Graphs that we will study this semester include:

- Complete subgraph( $G$ )
- Connected subgraph( $G$ )
- Connected component( $G$ )
- Acyclic subgraph( $G$ )
- Spanning tree( $G$ )

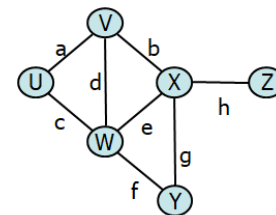
Size and Running Times

Running times are often reported by  $n$ , the number of vertices, but often depend on  $m$ , the number of edges.

For arbitrary graphs, the minimum number of edges given a graph that is:

Not Connected:

Minimally Connected\*:



The maximum number of edges given a graph that is:

Simple:

Not Simple:

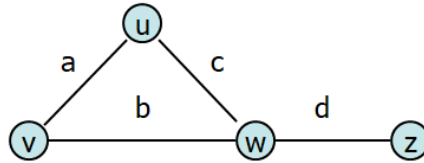
The relationship between the degree of the graph and the edges:

## Graph ADT

Data	Functions
1. Vertices	<code>insertVertex(K key);</code>
2. Edges	<code>insertEdge(Vertex v1, Vertex v2, K key);</code>
3. Some data structure maintaining the structure between vertices and edges.	<code>removeVertex(Vertex v);</code> <code>removeEdge(Vertex v1, Vertex v2);</code>
	<code>incidentEdges(Vertex v);</code> <code>areAdjacent(Vertex v1, Vertex v2);</code>
	<code>origin(Edge e);</code> <code>destination(Edge e);</code>

## Graph Implementation #1: Edge List

Vert.	Edges
u	a
v	b
w	c
z	d



### Data Structures:

Vertex Collection:

Edge Collection:

### Operations on an Edge List implementation:

`insertVertex(K key):`

- What needs to be done?

`removeVertex(Vertex v):`

- What needs to be done?

`incidentEdges(Vertex v):`

- What needs to be done?

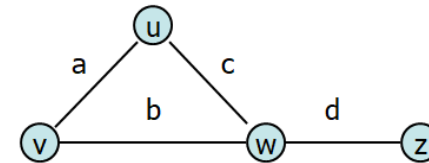
`areAdjacent(Vertex v1, Vertex v2):`

- Can this be faster than `G.incidentEdges(v1).contains(v2)`?

`insertEdge(Vertex v1, Vertex v2, K key):`

- What needs to be done?

## Graph Implementation #2: Adjacency Matrix



Vert.	Edges	Adj. Matrix
u	a	
v	b	
w	c	
z	d	

	u	v	w	z
u				
v				
w				
z				

## CS 225 – Things To Be Doing:

1. mp\_mazes out now EC due Monday Nov. 8
2. Final Project teams being contacted now.
3. Daily POTDs are ongoing!