

CS 225

Data Structures

Feb. 23 – BST Remove

Wade Fagen-Ulmschneider

Interactive Lecture Questions

- **Ask Questions:** Ask in-lecture questions using [this Google Form!](#) Questions are reviewed and answered live during lecture.
- **Detailed Answers After Lecture:** If we didn't get to answer your question in lecture, we provide detailed answers to common questions [here](#).
- You must be logged in with an account to use this form. If you are not logged in, you will be asked to log in.

Lecture Videos

- Recorded on [echo360.org](#), log in to watch.

Schedule

Monday

January 15
MLK Day

January 22
Memory

[slides](#) | [handout](#) | [pointers.pdf](#) | [code](#) | [TA Notes](#)

[slides](#) | [handout](#) | [Binky Pointer Fun](#) | [code](#) | [TA Notes](#)

[slides](#) | [handout](#) | [arrays.pdf](#) | [parameters](#) | [code](#) | [TA Notes](#)

CS 225 - Lecture Questions

Your email address ([waf@illinois.edu](#)) will be recorded when you submit this form. Not you? [Switch account](#)

* Required

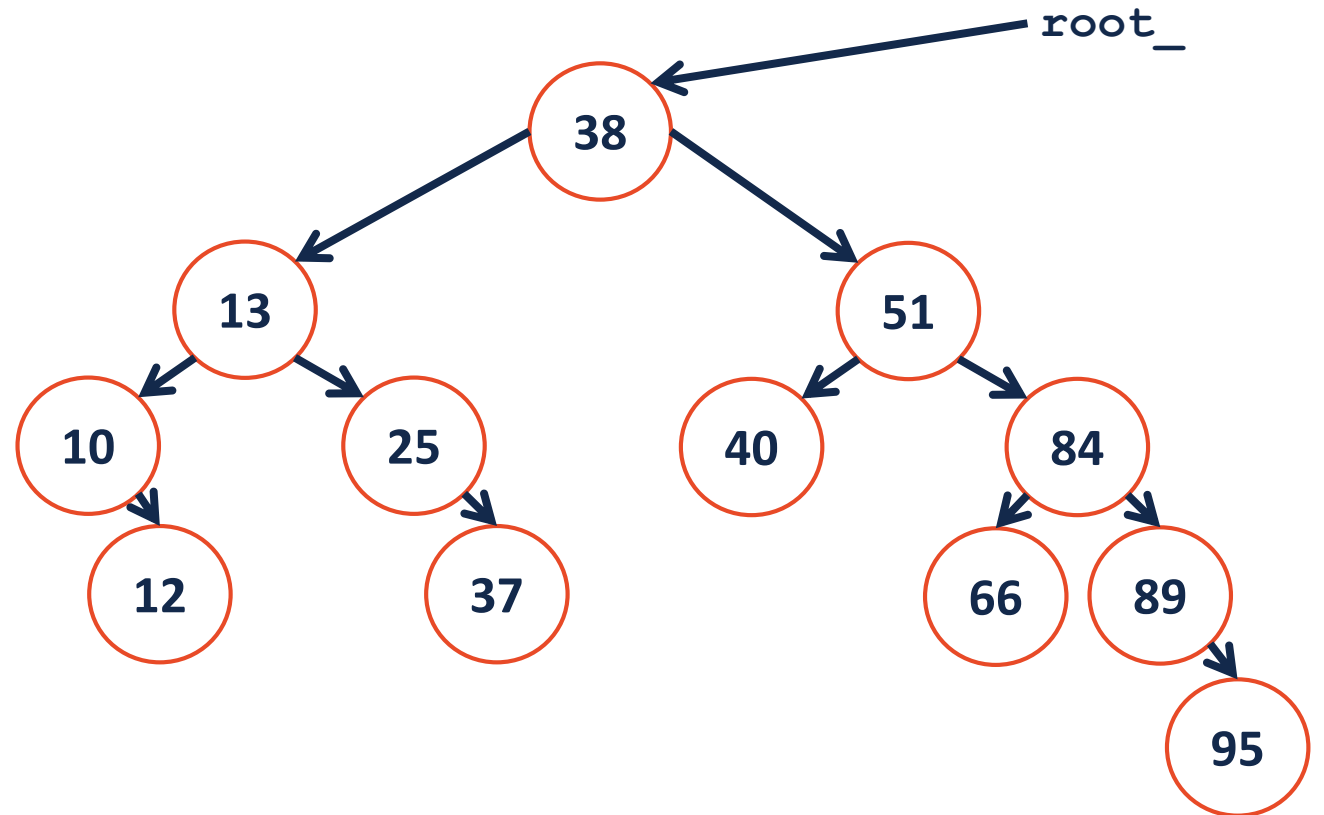
Question for Lecture: *

Your answer

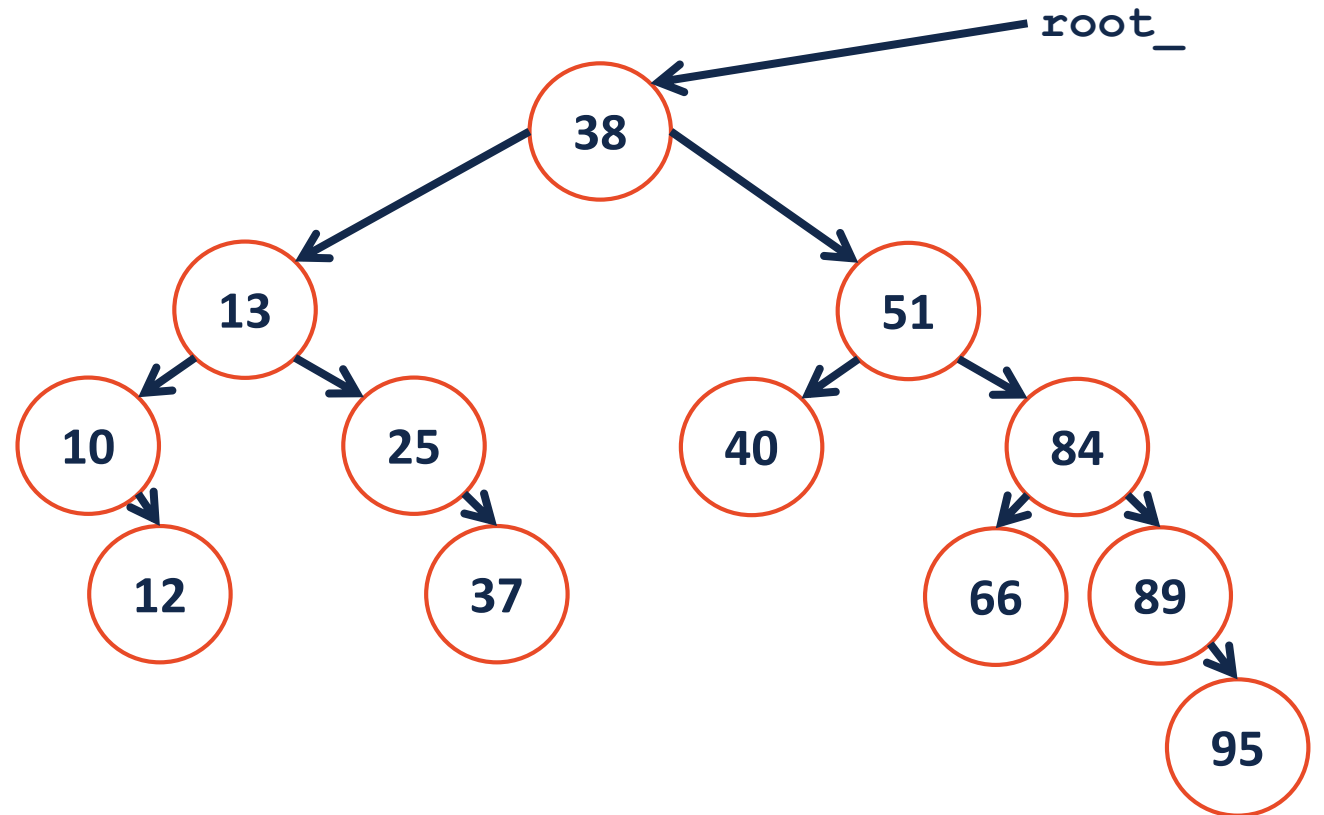
SUBMIT

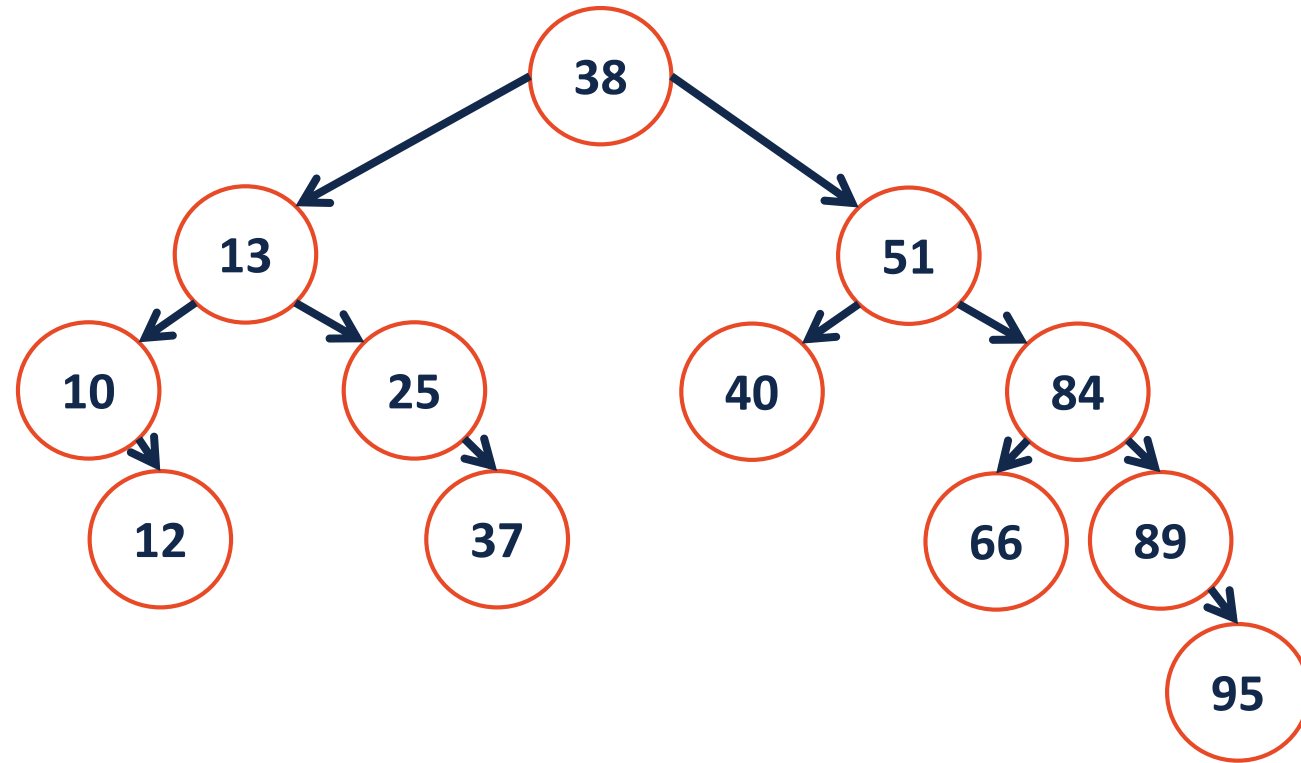
Never submit passwords through Google Forms.

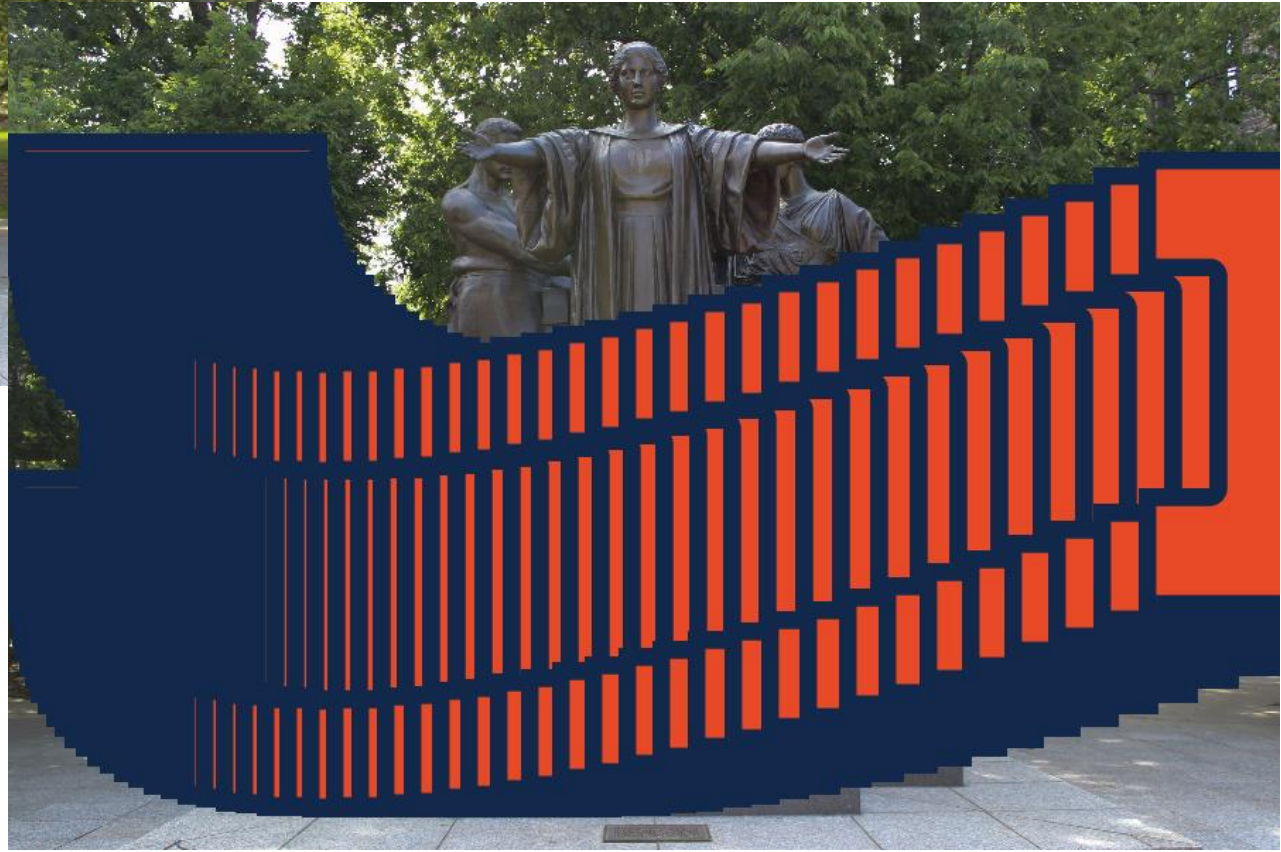
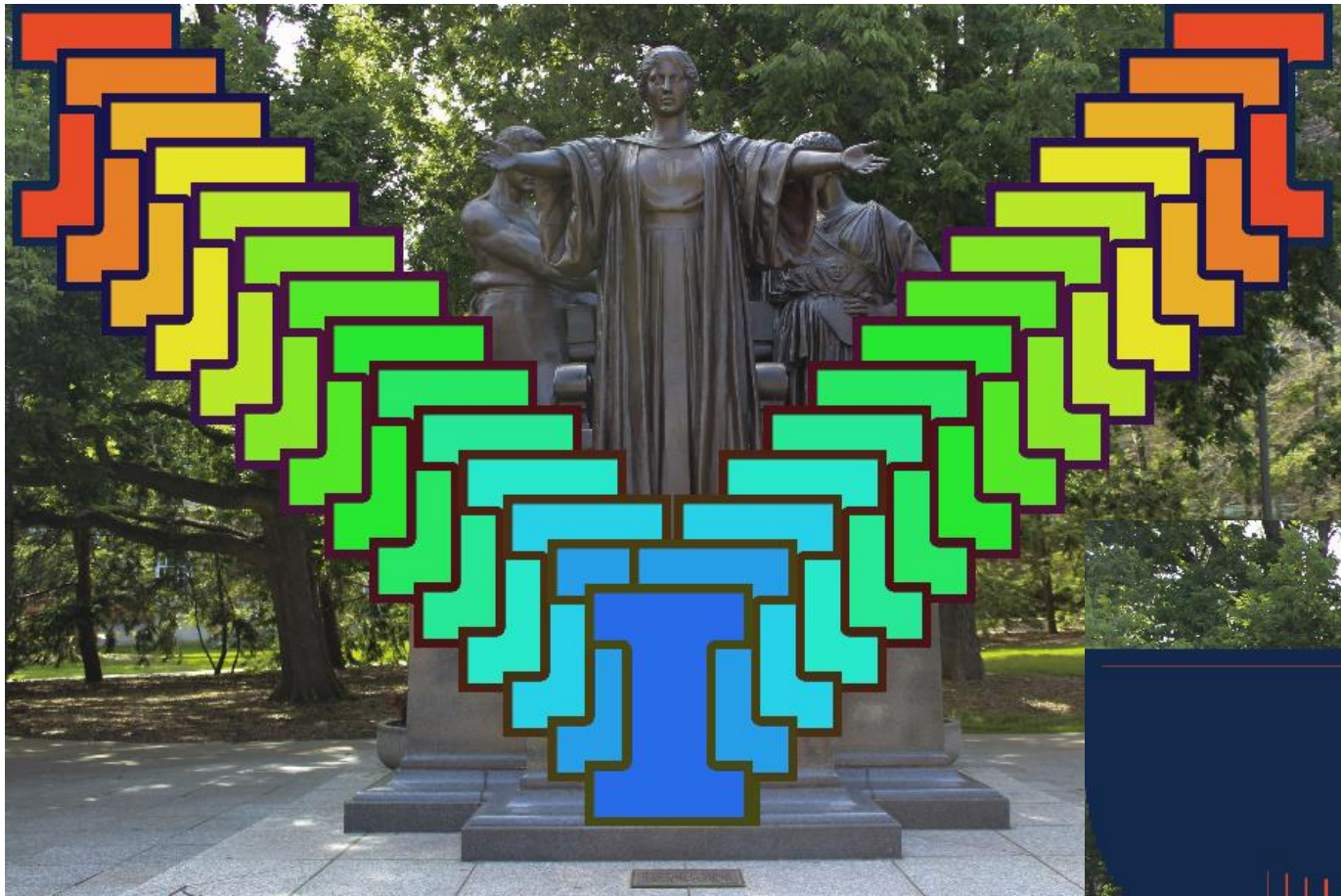
```
1 template<typename K, typename V>
2
3 void BST::_insert(TreeNode *& root, K & key, V & value) {
4     TreeNode *t = _find(root, key);
5     t = new TreeNode(key, value);
6 }
```



```
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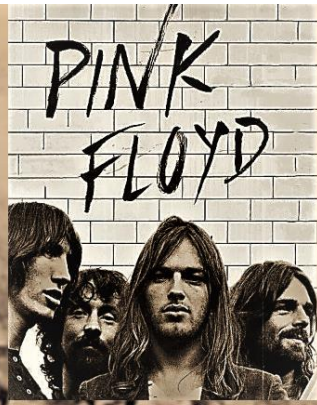




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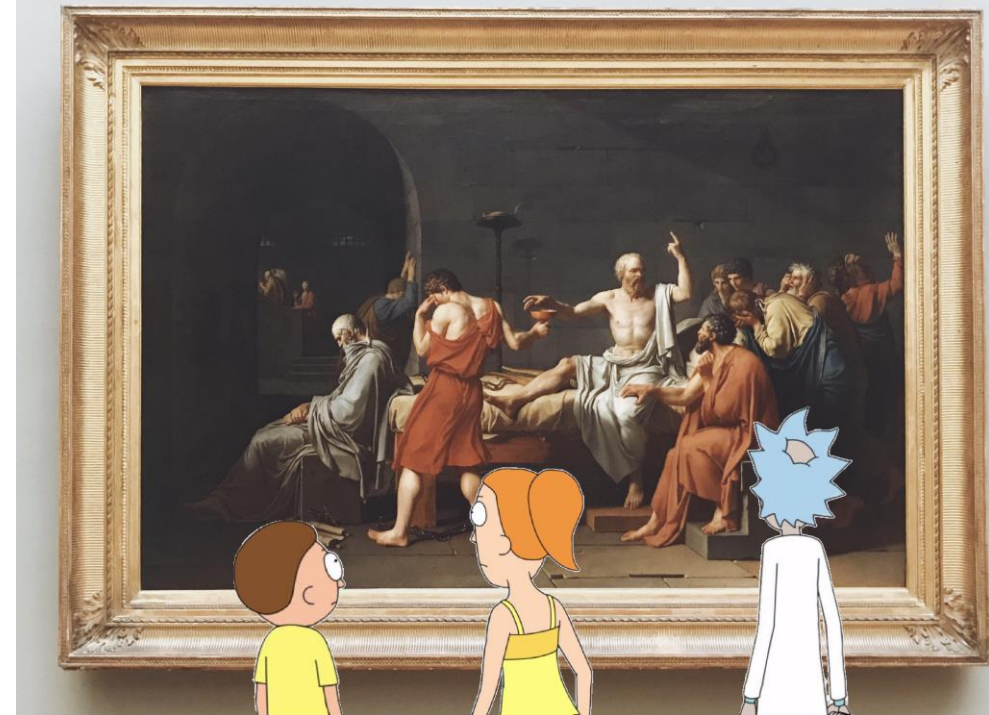
♥ HAPPY
Valentine's
DAY ♥





LONG LIVE
ROCK 'N' ROLL





EASY TO LEARN



LOOKS LAME

LOOKS COOL



HARD TO LEARN

EASY TO LEARN



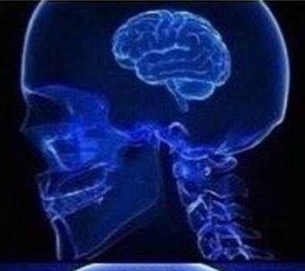
LOOKS LAME

LOOKS COOL



HARD TO LEARN

Creating memes with photoshop



Creating memes with microsoft word



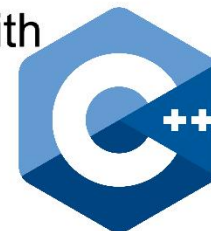
Creating memes with MS paint

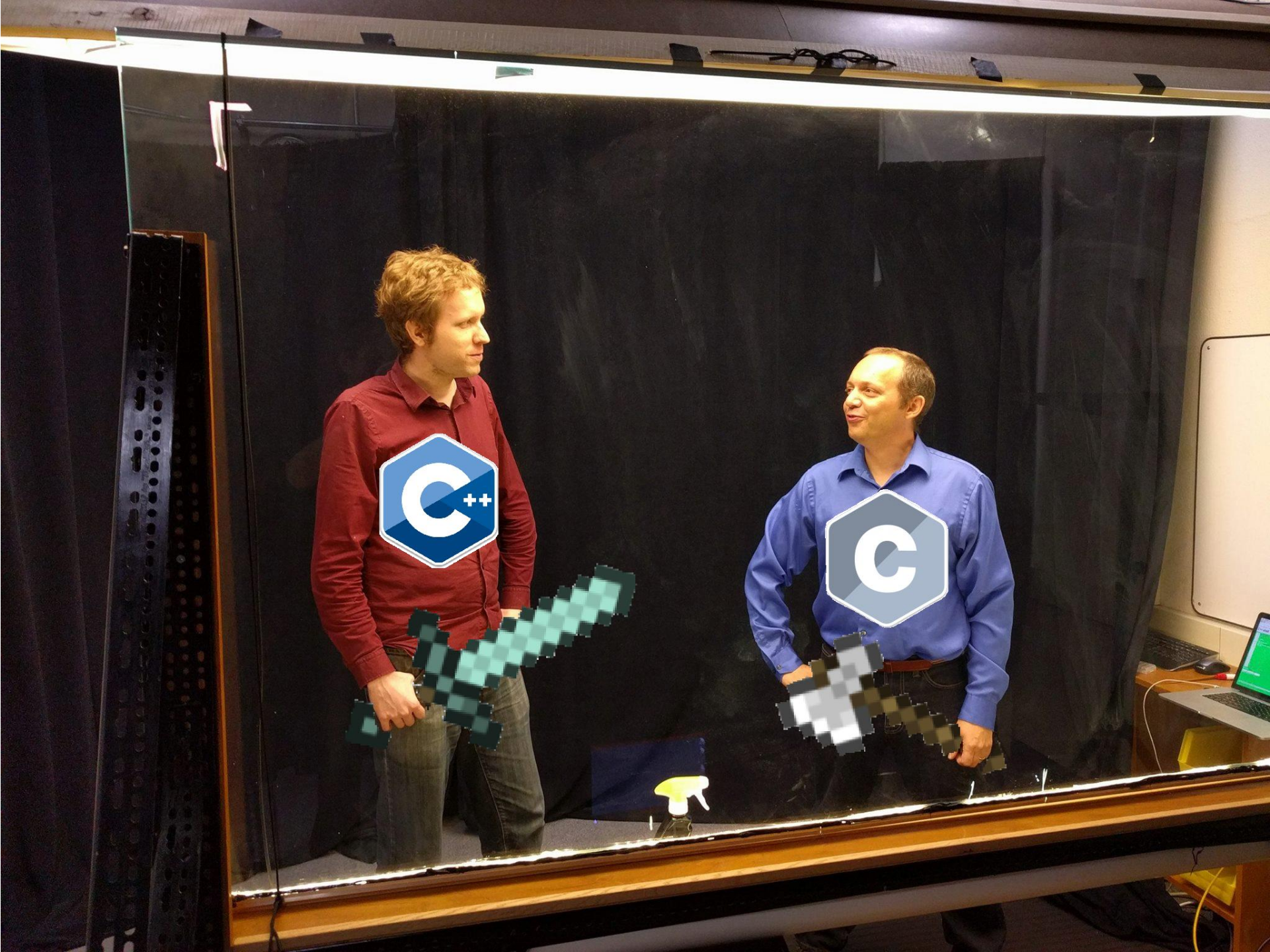


Creating memes with LibreOffice



Creating memes with





Tonight's the night when we forget about
the deadlines, it's time, uh oh
I don't know about you, but
I'm FAILING 225



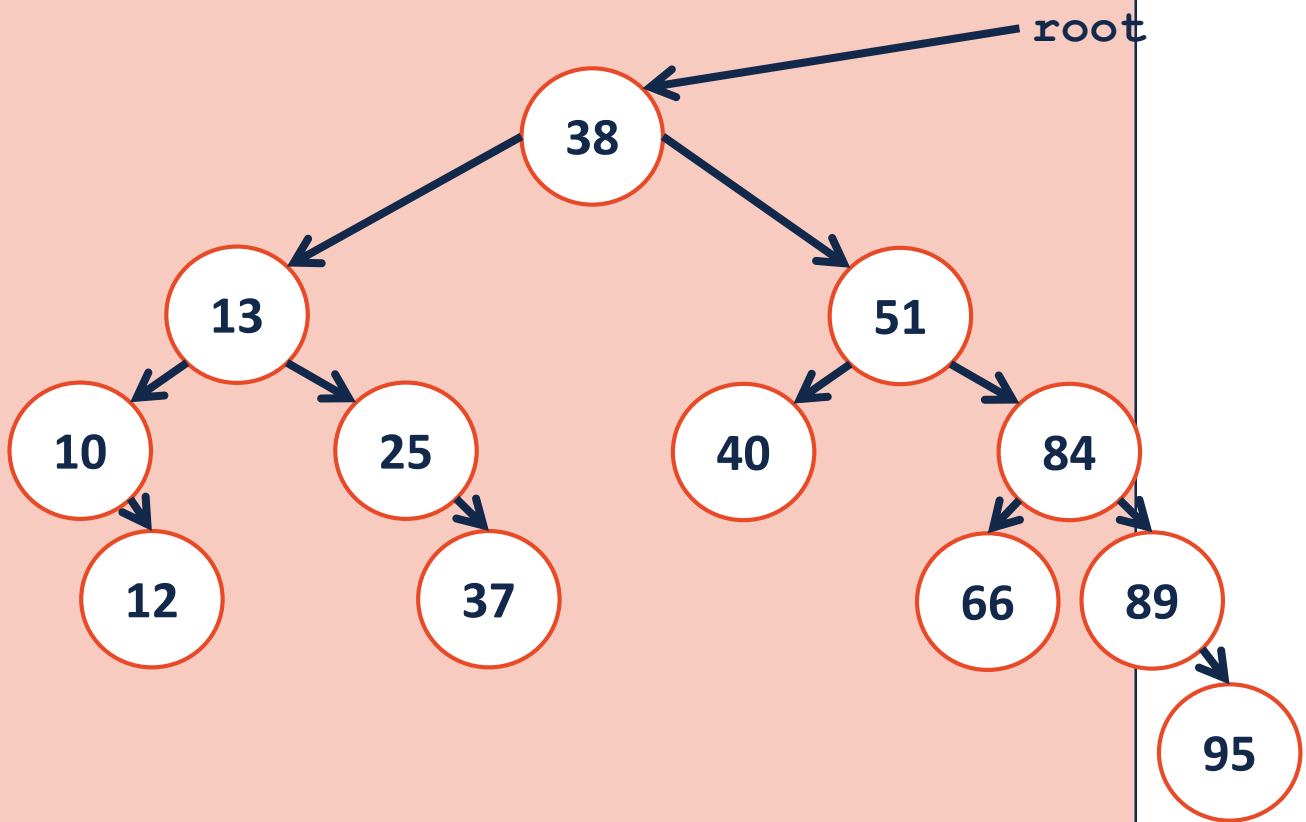
segmentation fault

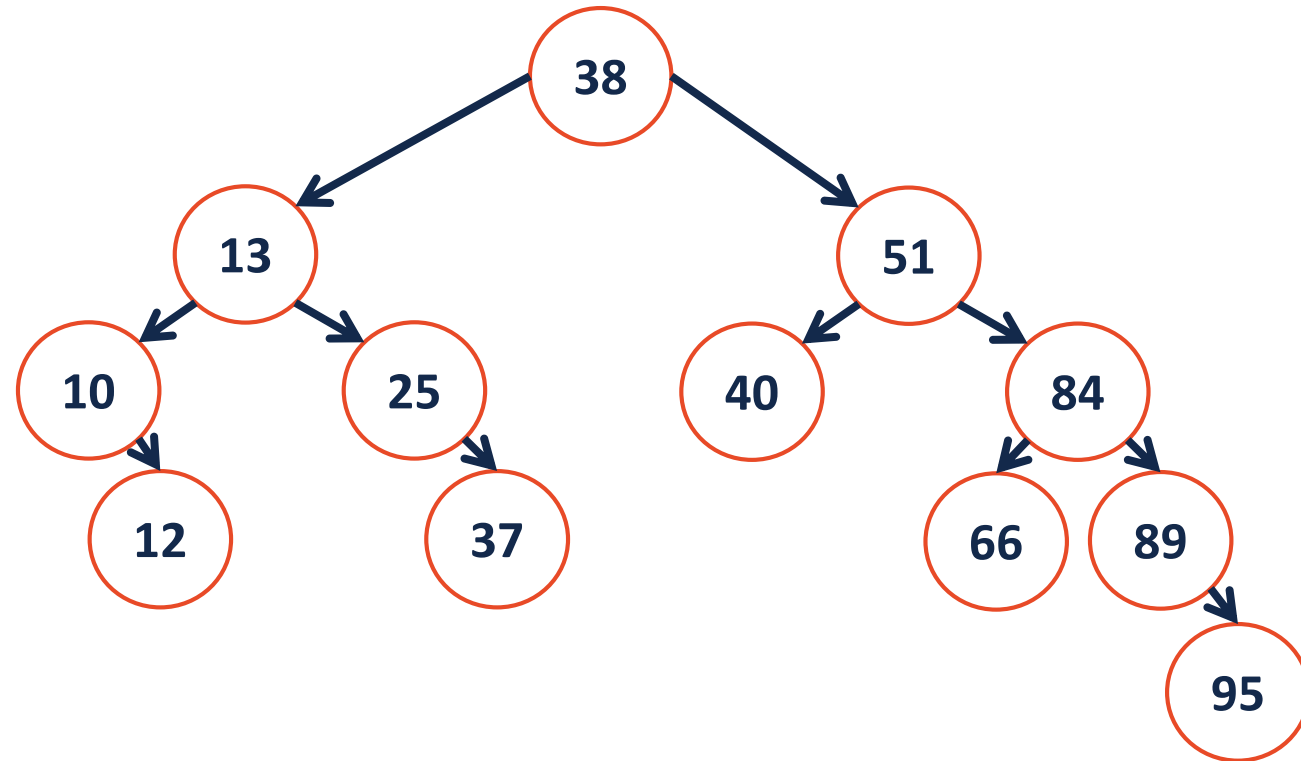
segmentation fault

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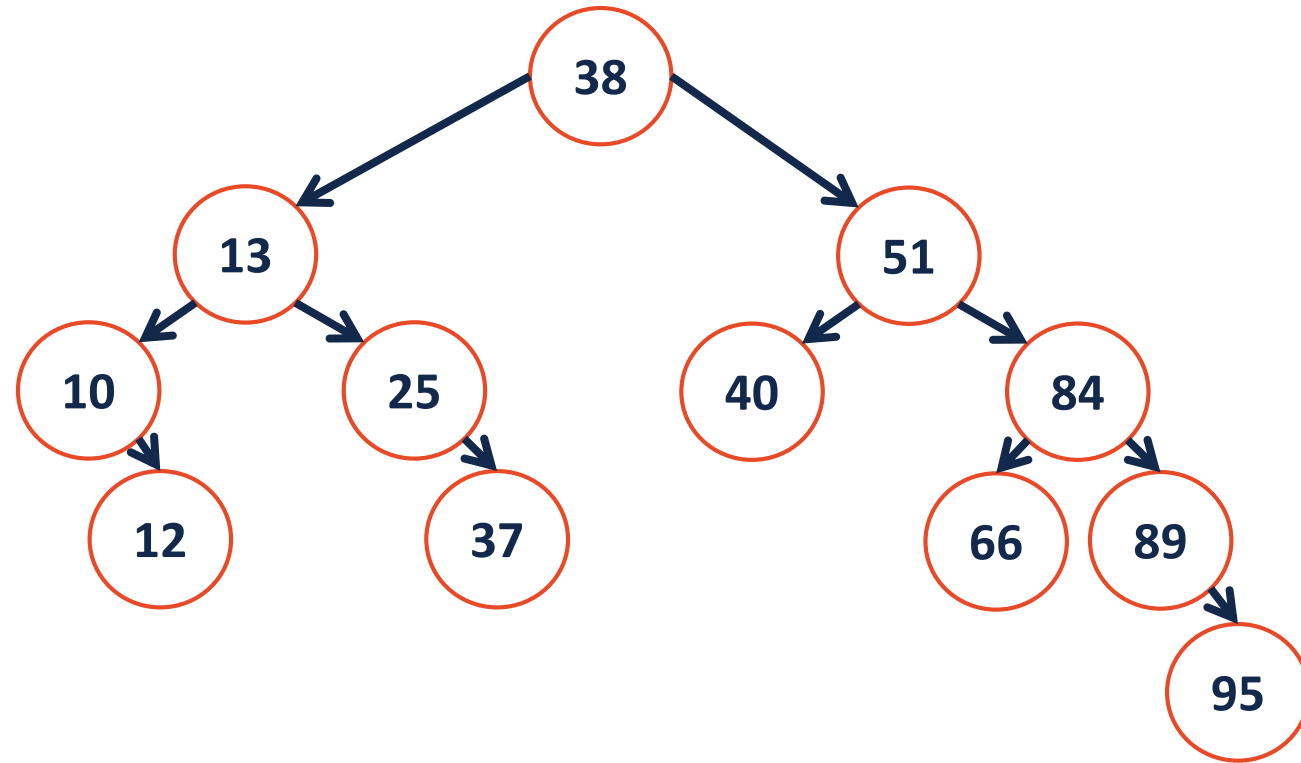



```
1  template<typename K, typename V>
2  _____ _remove(TreeNode *& root, const K & key) {
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24
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26 }
```

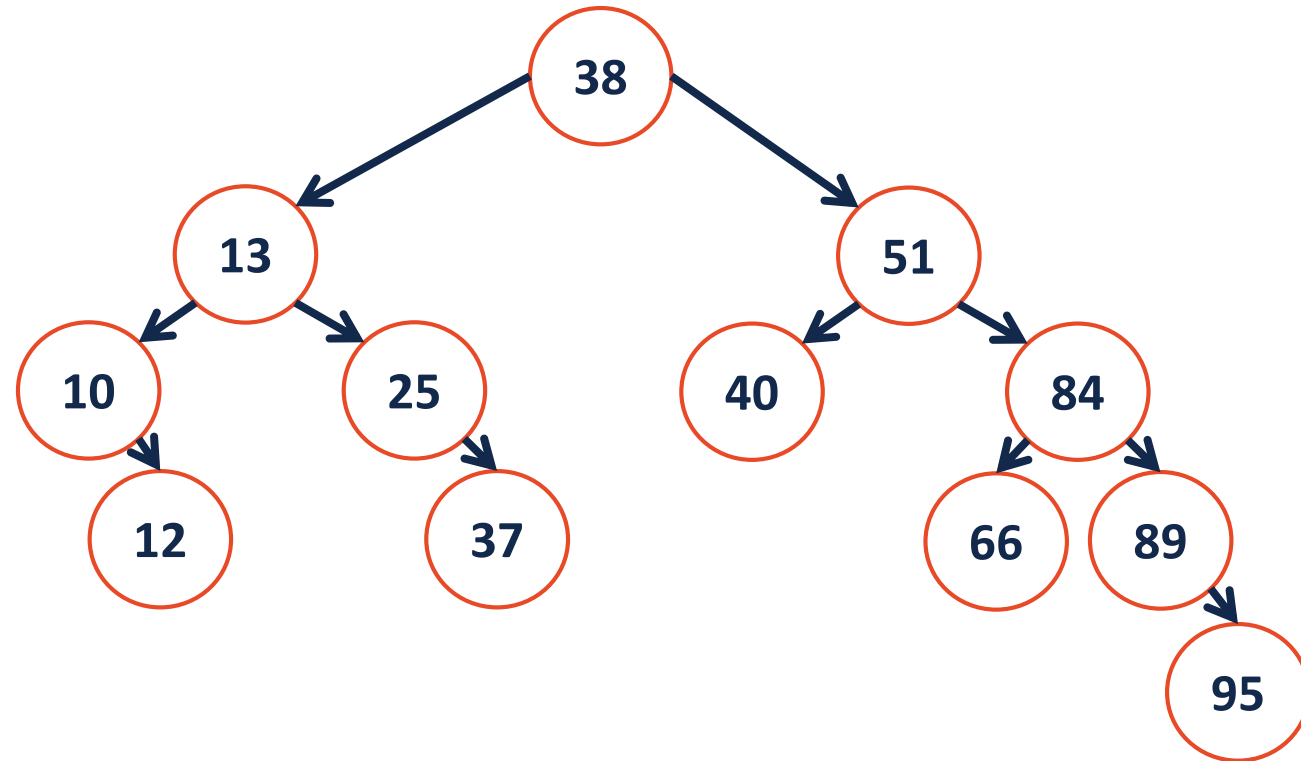




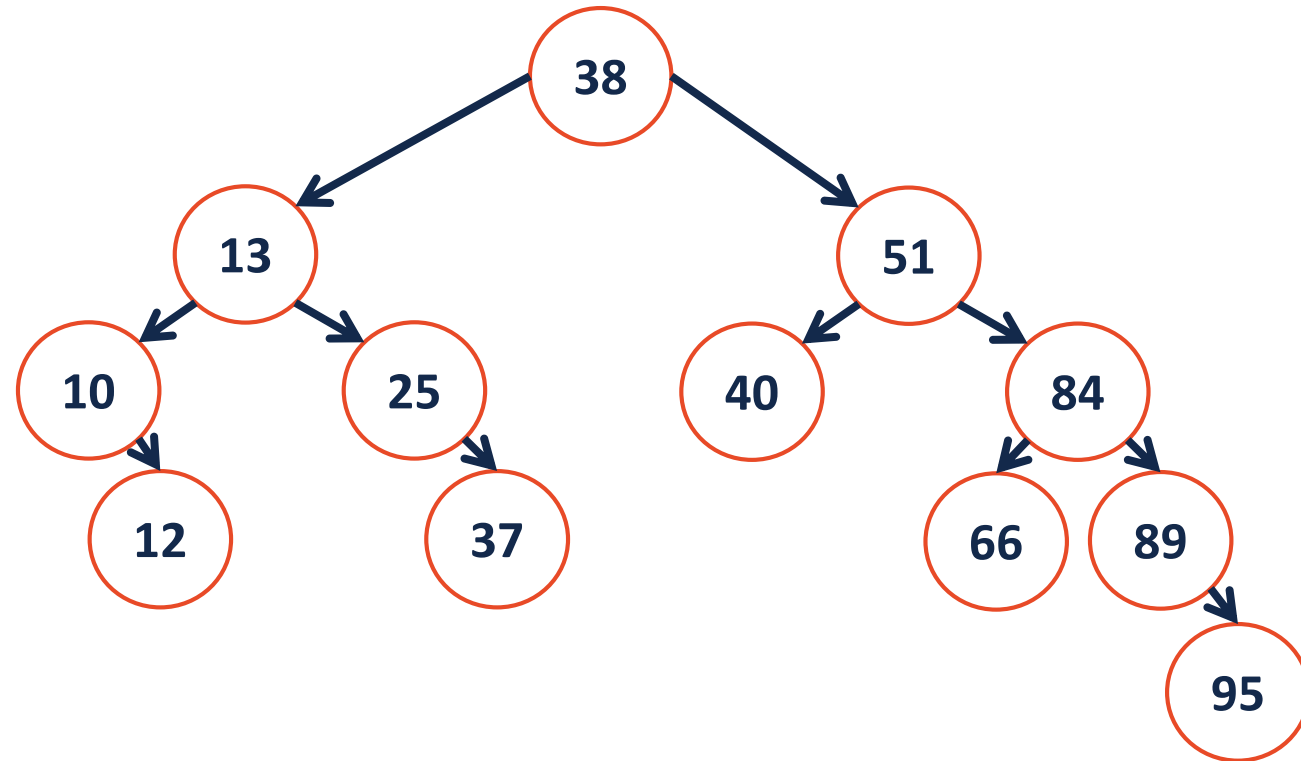
`remove(40);`



remove (25) ;



`remove(10);`



`remove (13) ;`

BST Analysis – Running Time

Operation	BST Worst Case
find	
insert	
delete	
traverse	

BST Analysis

Every operation that we have studied on a BST depends on the height of the tree: **$O(h)$** .

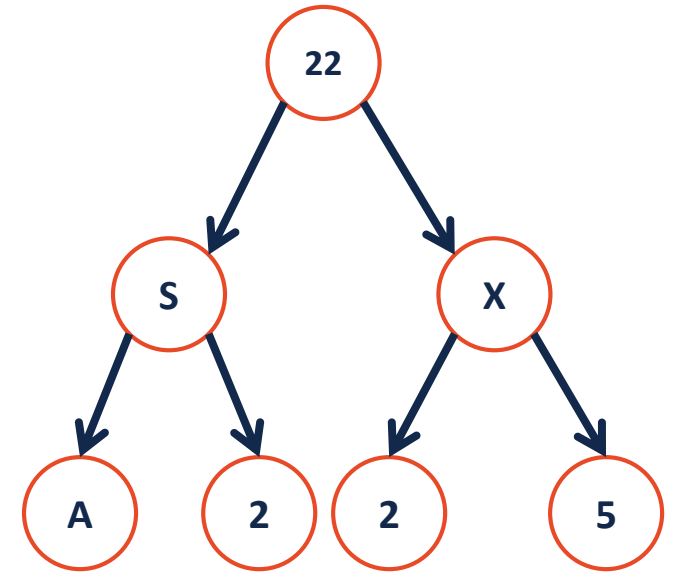
...what is this in terms of **n** , the amount of data?

We need a relationship between h and **n** :

$$f(n) \leq h \leq g(n)$$

BST Analysis

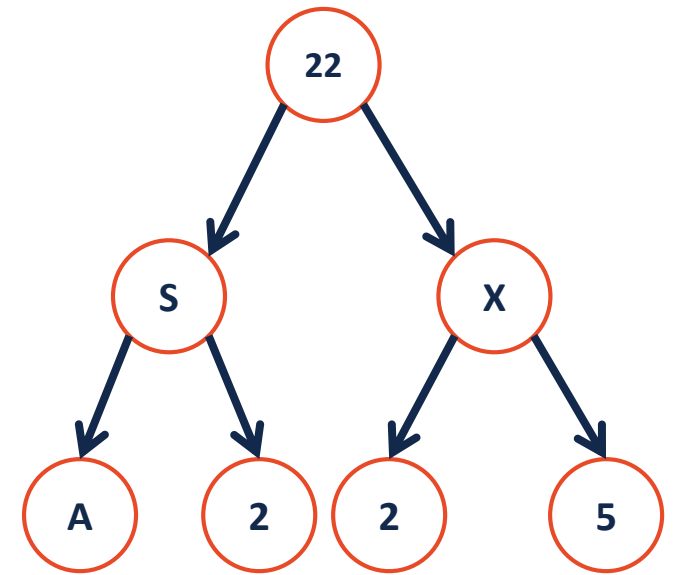
Q: What is the maximum number of nodes in a tree of height **h**?



BST Analysis

Q: What is the minimum number of nodes in a tree of height **h**?

What is the maximum height for a tree of **n** nodes?



BST Analysis

Therefore, for all BST:

Lower bound:

Upper bound:

BST Analysis

The height of a BST depends on the order in which the data is inserted into it.

ex: 1 3 2 4 5 7 6

vs.

4 2 3 6 7 1 5

Q: How many different ways are there to insert keys into a BST?

Q: What is the average height of all the arrangements?

BST Analysis

Q: How many different ways are there to insert keys into a BST?

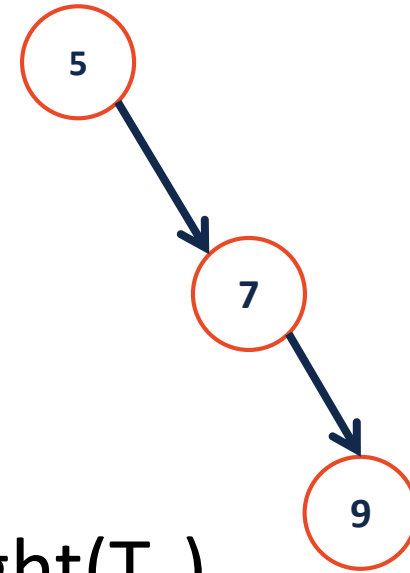
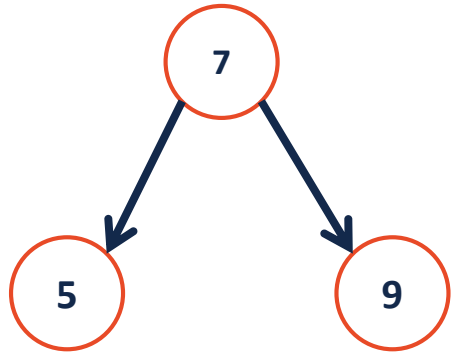
Q: What is the average height of all the arrangements?

BST Analysis – Running Time

Operation	BST Average case	BST Worst case	Sorted array	Sorted List
find				
insert				
delete				
traverse				

Height-Balanced Tree

What tree makes you happier?



Height balance: $b = \text{height}(T_L) - \text{height}(T_R)$

A tree is height balanced if: