

**BTree Properties**

For a BTree of order **m**:

1. All keys within a node are ordered.
2. All leaves contain no more than **m-1** nodes.
3. All internal nodes have exactly **one more children than keys**.
4. Root nodes can be a leaf or have [**2, m**] children.
5. All non-root, internal nodes have [**ceil(m/2), m**] children.
6. All leaves are on the same level.

**BTree Analysis**

The height of the BTree determines maximum number of \_\_\_\_\_ possible in search data.

...and the height of our structure:

**Therefore**, the number of seeks is no more than: \_\_\_\_\_.

*...suppose we want to prove this!*

**BTree Proof #1**

In our AVL Analysis, we saw finding an **upper bound** on the height (**h** given **n**, aka **h = f(n)**) is the same as finding a **lower bound** on the keys (**n** given **h**, aka **f<sup>-1</sup>(h)**).

**Goal:** We want to find a relationship for BTrees between the number of keys (**n**) and the height (**h**).

**BTree Strategy:**

1. Define a function that counts the minimum number of nodes in a BTree of a given order.
  - a. Account for the minimum number of keys per node.

2. Proving a minimum number of nodes provides us with an upper-bound for the maximum possible height.

**Proof:**

**1a.** The minimum number of nodes for a BTree of order **m** at each level is as follows:

root:

level 1:

level 2:

level 3:

...

level h:

**1b.** The minimum total number of nodes is the sum of all levels:

**2.** The minimum number of keys:

**3.** Finally, we show an upper-bound on height:

### So, how good are BTrees?

Given a BTree of order 101, how much can we store in a tree of height=4?

Minimum:

Maximum:

---

---

This space Intentionally left blank

#### CS 225 – Things To Be Doing:

1. Enjoy Break stay healthy
2. Mp\_lists is due March 27 by 11:59pm;
3. Daily POTDs stopped for break
4. Check out tools from the survey