For each of the following languages over the alphabet  $\Sigma = \{0,1\}$ , either prove the language is regular (by giving an equivalent regular expression, DFA, or NFA) or prove that the language is not regular (using a fooling set argument). Exactly half of these languages are regular.

Version: 1.01

- $1 \quad \{0^n 10^n \mid n \ge 0\}$
- **2**  $\{0^n 10^n w \mid n \ge 0 \text{ and } w \in \Sigma^*\}$
- $3 \quad \{w0^n10^nx \mid w \in \Sigma^* \text{ and } n \ge 0 \text{ and } x \in \Sigma^*\}$
- 4 Strings in which the number of 0s and the number of 1s differ by at most 2.
- 5 Strings such that in every prefix, the number of 0s and the number of 1s differ by at most 2.
- 6 Strings such that in every substring, the number of 0s and the number of 1s differ by at most 2.