## Algorithms & Models of Computation

CS/ECE 374, Fall 2020

# **21.6.3** 2SAT

### What about **2SAT**?

**2SAT** can be solved in polynomial time! (specifically, linear time!)

No known polynomial time reduction from **SAT** (or **3SAT**) to **2SAT**. If there was, then **SAT** and **3SAT** would be solvable in polynomial time.

#### Why the reduction from 3SAT to 2SAT fails?

Consider a clause  $(x \lor y \lor z)$ . We need to reduce it to a collection of 2CNF clauses. Introduce a face variable  $\alpha$ , and rewrite this as

$$(x \lor y \lor \alpha) \land (\neg \alpha \lor z)$$
 (bad! clause with 3 vars) or  $(x \lor \alpha) \land (\neg \alpha \lor y \lor z)$  (bad! clause with 3 vars).

(In animal farm language: **2SAT** good, **3SAT** bad.)

#### What about 2SAT?

A challenging exercise: Given a **2SAT** formula show to compute its satisfying assignment...

(Hint: Create a graph with two vertices for each variable (for a variable x there would be two vertices with labels x=0 and x=1). For ever 2CNF clause add two directed edges in the graph. The edges are implication edges: They state that if you decide to assign a certain value to a variable, then you must assign a certain value to some other variable.

Now compute the strong connected components in this graph, and continue from there...)