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## CS 374 LAB 9: CHURCH-TURING THESIS

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**Problem 1.** [Category: Design] A  $k$ -tape Turing machine is a TM that can read and write onto  $k$ -tapes. It starts out with the input being written on the first tape, and the remaining  $k - 1$  tapes being blank. Formally,  $M = (Q, \Sigma, \Gamma, \square, \delta, \text{start}, \text{accept}, \text{reject})$ , where  $Q$  is a finite set of states,  $\Sigma$  is the input alphabet,  $\Gamma$  is the tape alphabet,  $\square \in \Gamma \setminus \Sigma$  is the blank symbol,  $\delta$  is the transition function, and start, accept and reject are the start, accept and reject states, respectively.

1. What is the domain and co-domain of the function  $\delta$ ?
2. What does a configuration of such a machine look like?
3. Given an arbitrary  $k$ -tape TM  $M$ , sketch out the construction of a 1-tape TM  $N$  that accepts the same language as  $M$ .

**Problem 2.** [Category: Design] A Random Access Machine (RAM) is a computing device that has finite many registers that can store numbers, and infinitely many memory locations each of which can store an arbitrary natural number. Initially the RAM has a program (sequence of instructions) stored in the first few cell of the the memory; all other memory locations, and all registers initially contain 0. A RAM program consists of the following instructions.

- **add X, Y:** Add the contents of registers  $X$  and  $Y$  and store the result in  $X$ .
- **loadc X, I:** Place the constant  $I$  in register  $X$ .
- **load X, M:** Load the contents of memory location  $M$  into register  $X$ .
- **loadI X, M:** Load the contents of the location “pointed to” by the contents of  $M$  into register  $X$ .
- **store X, M:** store the contents of register  $X$  in memory location  $M$ .
- **jmp M:** The next instruction to be executed is in location  $M$ .
- **jmz X, M:** If register  $X$  is 0, then jump to instruction  $M$ .
- **halt:** Halt execution.

Prove that an RAM can be simulated by a  $k$ -tape TM (for some  $k$ ).