

Give regular expressions for each of the following languages over the alphabet $\{0, 1\}$.

1. All strings containing the substring **000**.
2. All strings *not* containing the substring **000**.
3. All strings in which every run of **0**s has length at least 3.
4. All strings in which every substring **000** appears after every **1**.
5. All strings containing at least three **0**s.
6. Every string except **000**. [*Hint: Don't try to be clever.*]

Work on these later:

7. All strings w such that *in every prefix of w* , the number of **0**s and **1**s differ by at most 1.
- *8. All strings containing at least two **0**s and at least one **1**.
- *9. All strings w such that *in every prefix of w* , the number of **0**s and **1**s differ by at most 2.
- *10. All strings in which the substring **000** appears an even number of times.
(For example, **0001000** and **0000** are in this language, but **00000** is not.)