

Programming Languages and Compilers (CS 421)

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<https://courses.engr.illinois.edu/cs421/fa2017/CS421A>

Based in part on slides by Mattox Beckman, as updated
by Vikram Adve, Gul Agha, and Elsa Gunter

Contact Information – Sasa Misailovic

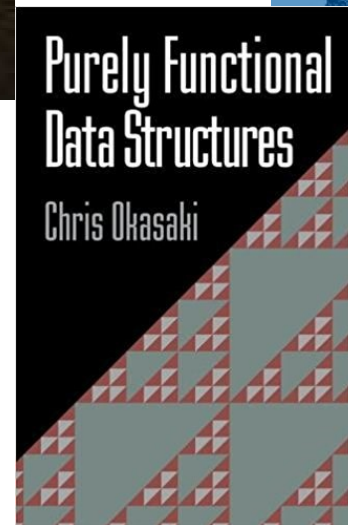
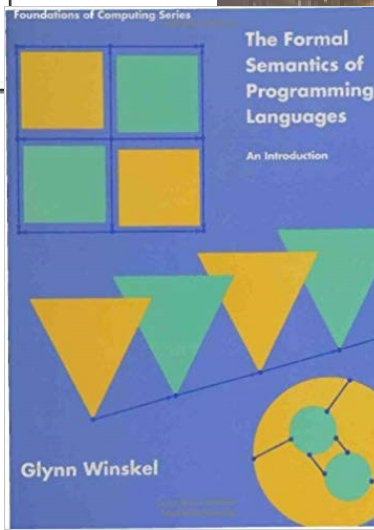
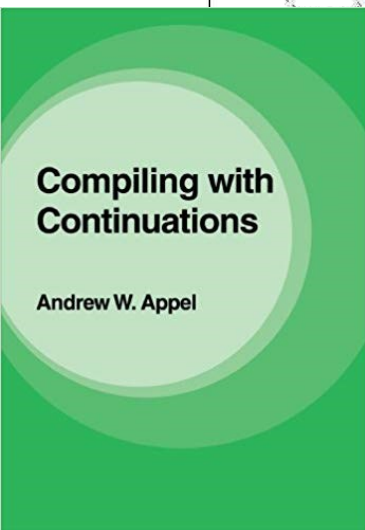
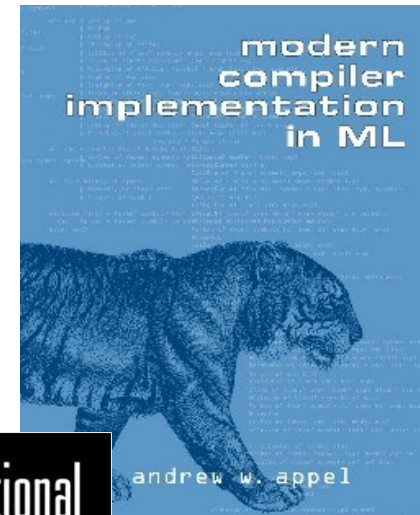
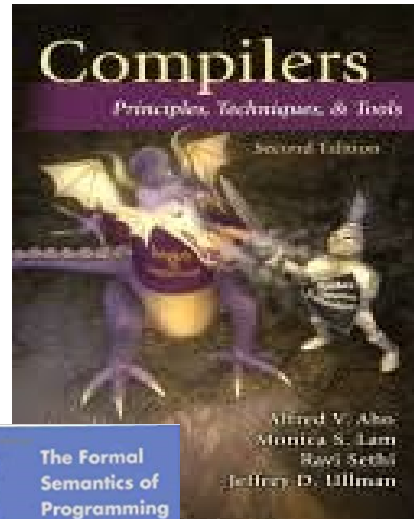
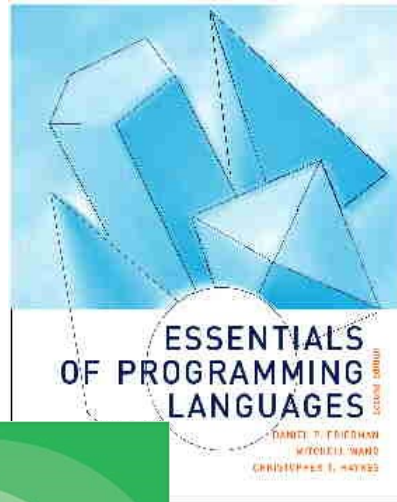
- Office: 4110 SC
- Office hours:
 - Tuesday, Thursday 8:30am – 9:30am
 - Also by appointment
- Email: misailo@illinois.edu

Course Website

- <https://courses.engr.illinois.edu/cs421/fa2018/CS421A>
- Main page - summary of news items
- Policy - rules governing course
- Lectures - syllabus and slides
- MPs - information about assignments
- Exams
- Unit Projects - for 4 credit students
- Resources - tools and helpful info
- FAQ

Some Course References

- No required textbook
- Some suggested references



Course Grading

- Assignments 20%
 - About 12 Web Assignments (WA) (~7%)
 - About 6 MPs (in Ocaml) (~7%)
 - About 5 Labs (~6%)
 - All WAs and MPs Submitted through **PrairieLearn**
 - Late submission penalty: 20%
 - Labs in Computer-Based Testing Center (Grainger)
 - Self-scheduled over a three day period
 - No extensions beyond the three day period
 - Fall back: Labs become MPs

Course Grading

- 2 Midterms - 20% each
 - Labs in Computer-Based Testing Center (Grainger)
 - Self-scheduled over a three day period
 - No extensions beyond the three day period
 - Dates: **Oct 2-4 (Midterm 1) Nov 6-8 (Midterm 2)**
 - Fall back: In class backup dates – Oct 9, Nov 13
 - **DO NOT MISS EXAM DATES!**
- Final 40% - Dec 19, 8:00am – 11:00am (nominally)
- Will likely use CBTF for Final (3 day window)
- Percentages are approximate

Course Assignments – WA & MP

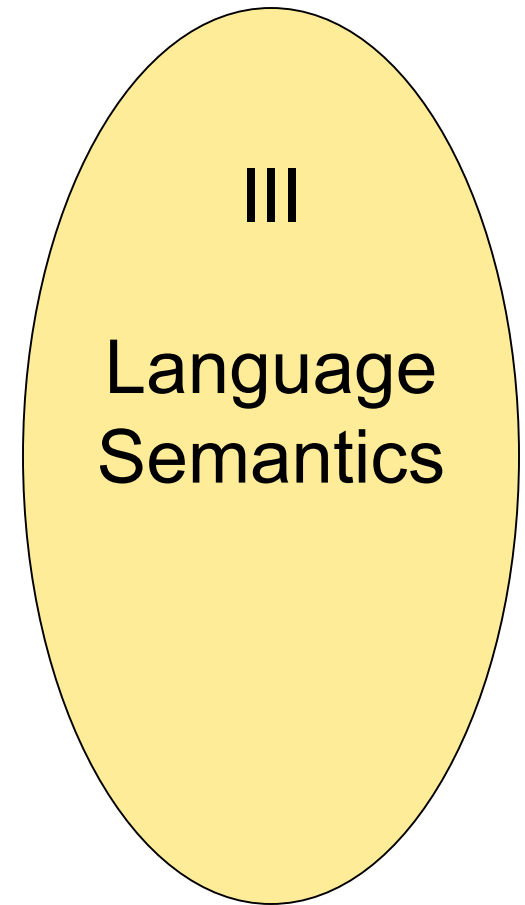
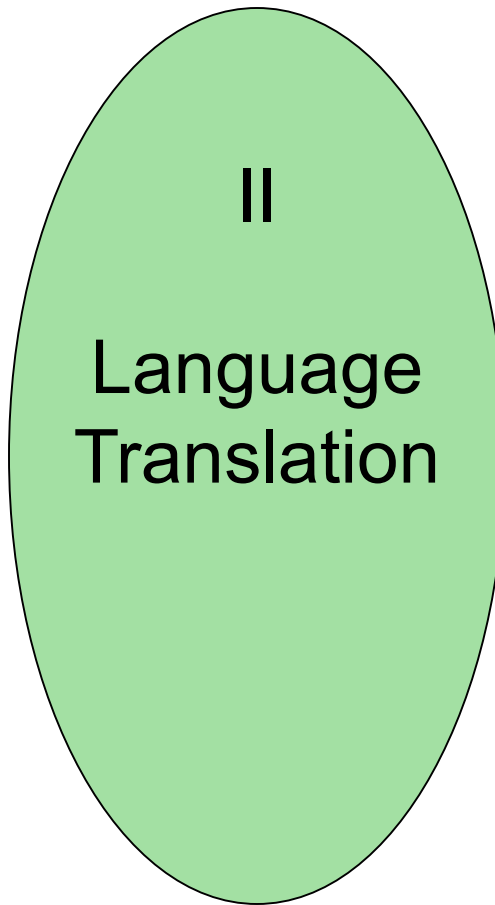
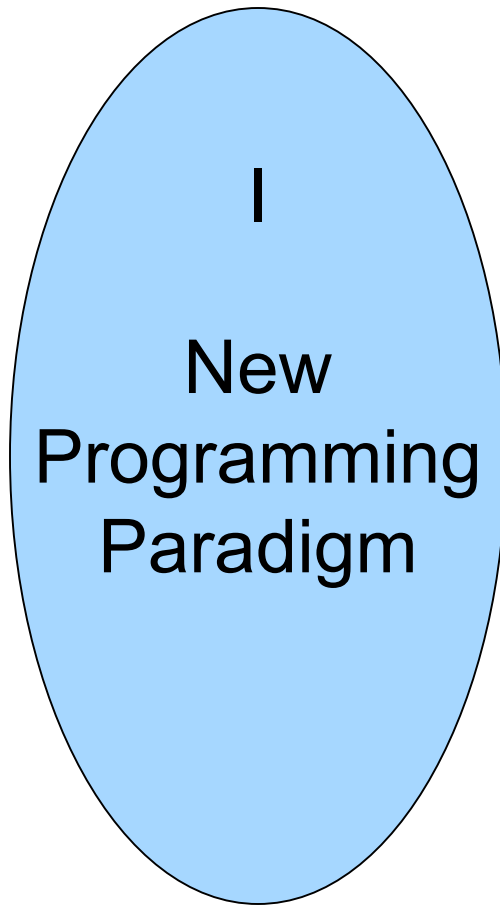
- You may discuss assignments and their solutions with others
- You may work in groups, but you must **list members with whom you worked** if you share solutions or solution outlines
- **Each student must write up and turn in their own solution separately**
- You may look at examples from class and other similar examples from any source – **cite appropriately**
 - Note: University policy on plagiarism still holds - cite your sources if you are not the sole author of your solution

Course Objectives

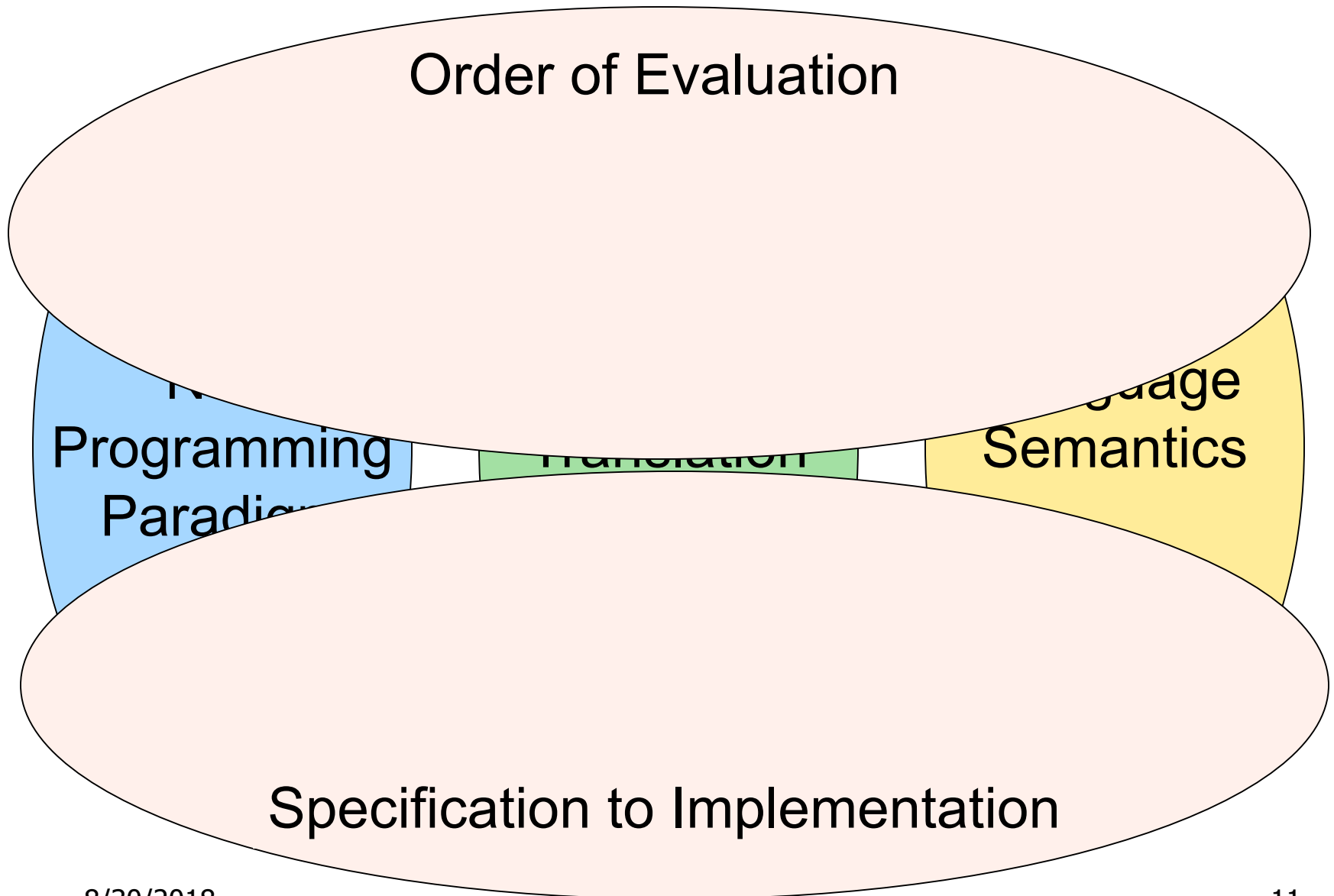
- **New programming paradigm**
 - Functional programming
 - Environments and Closures
 - Patterns of Recursion
 - Continuation Passing Style
- **Phases of an interpreter / compiler**
 - Lexing and parsing
 - Type systems
 - Interpretation
- **Programming Language Semantics**
 - Lambda Calculus
 - Operational Semantics
 - Axiomatic Semantics

Programming Languages & Compilers

Three Main Topics of the Course

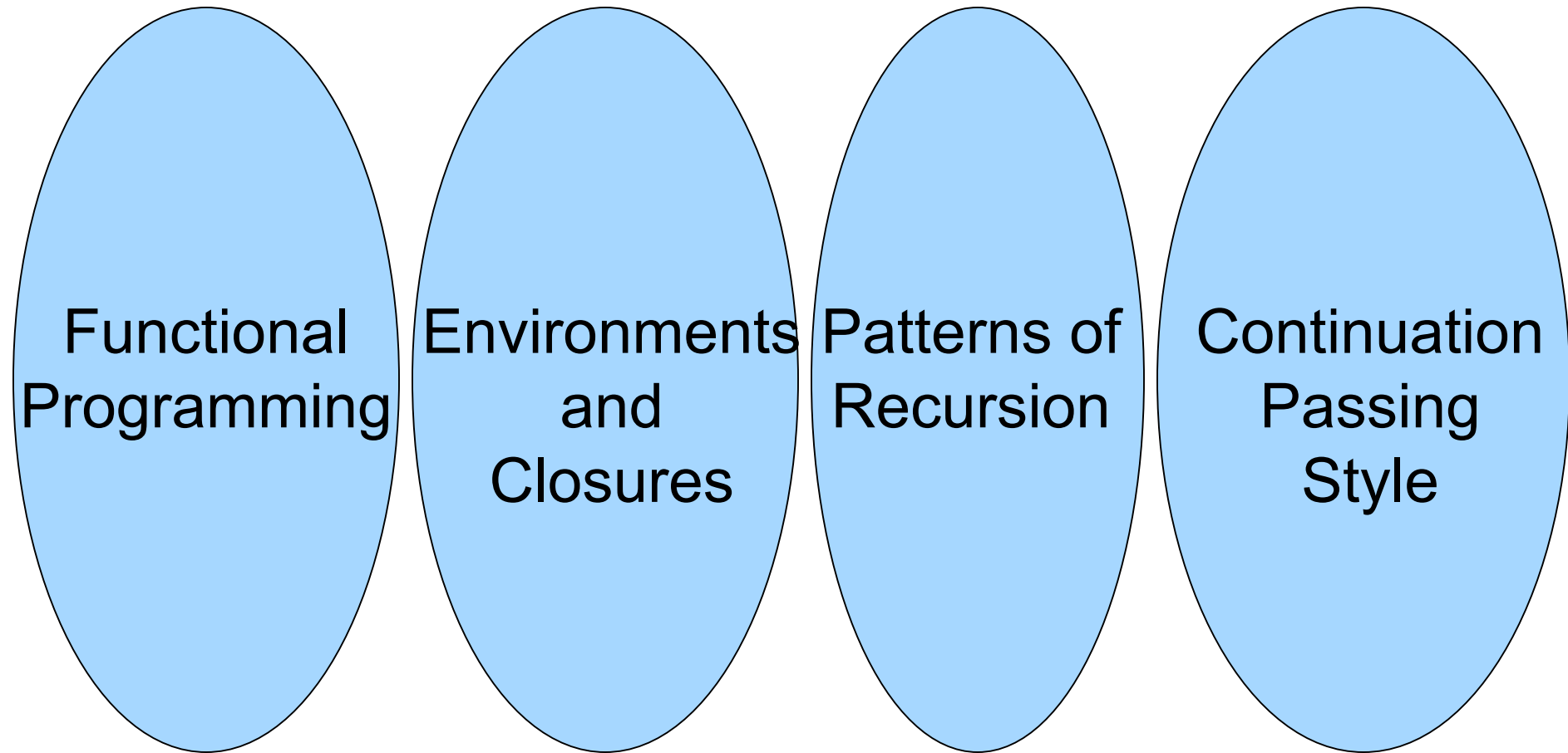


Programming Languages & Compilers



Programming Languages & Compilers

I : New Programming Paradigm



Programming Languages & Compilers

Order of Evaluation

Functional
Programming

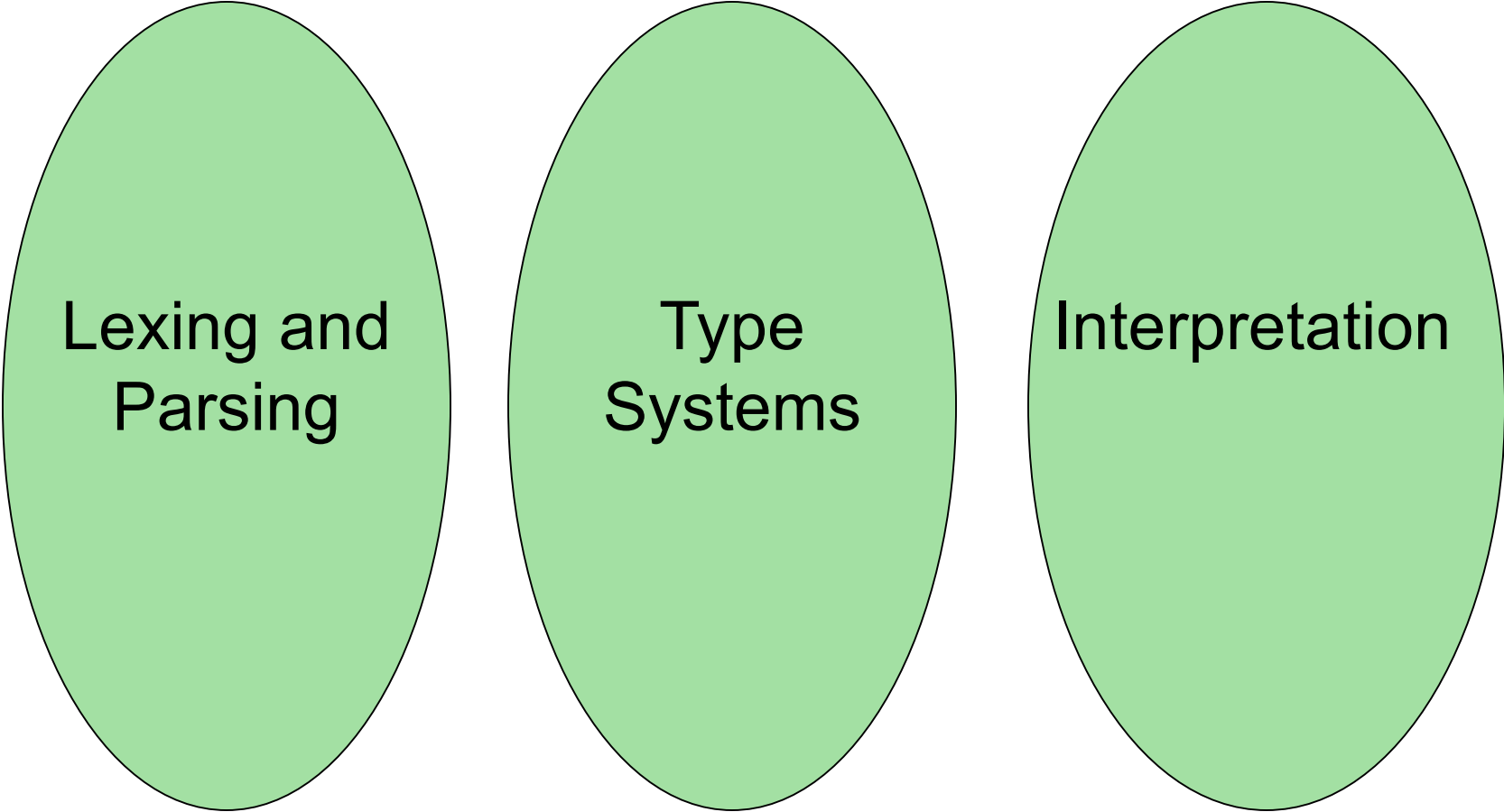
and Recursion

Continuation
Passing
Style

Specification to Implementation

Programming Languages & Compilers

II : Language Translation

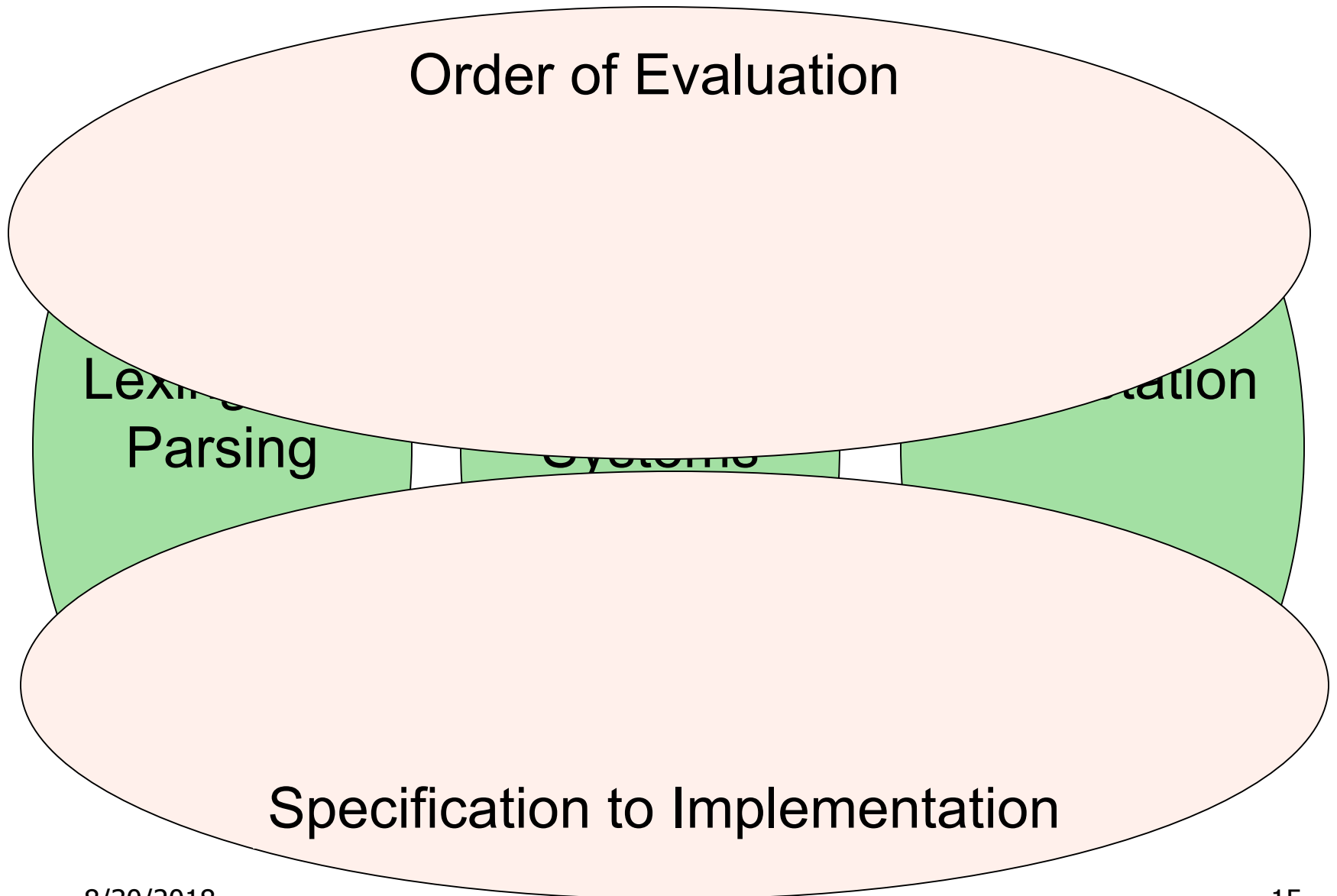


Lexing and
Parsing

Type
Systems

Interpretation

Programming Languages & Compilers



Programming Languages & Compilers

III : Language Semantics

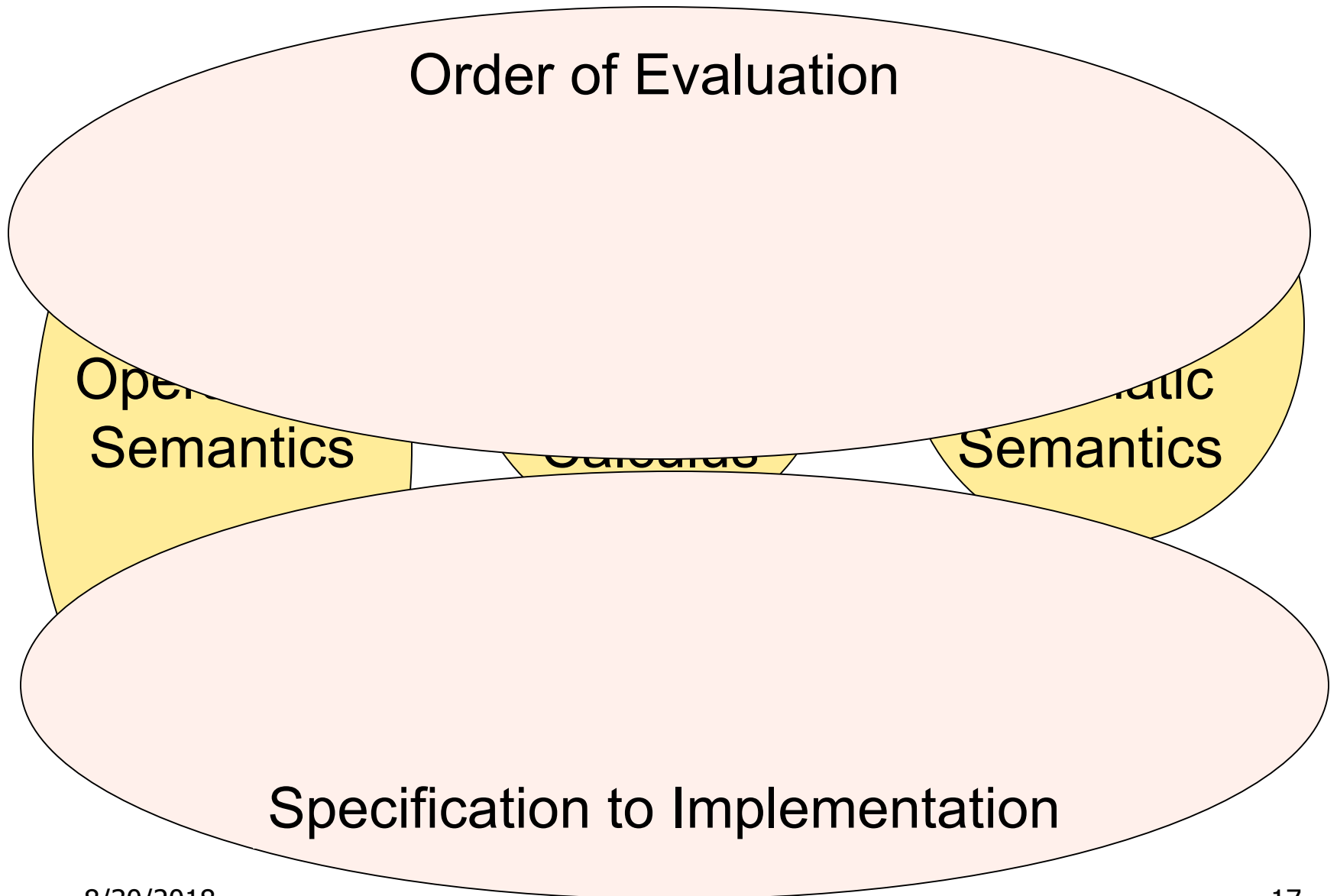


Operational
Semantics

Lambda
Calculus

Axiomatic
Semantics

Programming Languages & Compilers



OCAML

■ Locally:

- Compiler is on the EWS-linux systems at
/usr/local/bin/ocaml
- Be sure to **module load ocaml/2.07.0** in EWS!

■ Globally:

- Main CAML home: <http://ocaml.org>
- To install OCAML on your computer see:
<http://ocaml.org/docs/install.html>
- Or use one of the online OCAML compilers...

References for OCaml

- Supplemental texts (not required):
- The Objective Caml system release 4.07, by Xavier Leroy, online manual
- Introduction to the Objective Caml Programming Language, by Jason Hickey
- Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O' Reilly
 - Available online from course resources

Why learn OCAML?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCAML is particularly efficient for programming tasks involving languages (eg parsing, compilers, user interfaces)

Why Learn OCAML?

- Industrially Relevant: Jane Street trades billions of dollars per day using OCaml programs
- Similar languages: Microsoft F#, SML, Haskell, Scala, Scheme
- Who uses functional programming?
 - Google – MapReduce
 - Microsoft – LinQ
 - Twitter – Scala
 - Bonus: who likes set comprehensions in Python?

```
>>> squares = [x**2 for x in range(10)]
```

OCAML Background

- CAML is European descendant of original ML
 - American/British version is SML
 - **O** is for object-oriented extension
- ML stands for **Meta-Language**
- ML family designed for implementing theorem provers (back in 1970s)
 - It was the meta-language for programming the “object” language of the theorem prover
 - Despite obscure original application area, OCAML is a full general-purpose programming language

Session in OCAML

```
% ocaml
```

```
Objective Caml version 4.07
```

```
# _  
# (* Read-eval-print loop; expressions and declarations *)  
  2 + 3;;    (* Expression *)  
- : int = 5  
# 3 < 2;;  
- : bool = false
```

No Overloading for Basic Arithmetic Operations

```
# 15 * 2;;
```

```
- : int = 30
```

```
# 1.35 + 0.23;; (* Wrong type of addition *)
```

Characters 0-4:

```
1.35 + 0.23;; (* Wrong type of addition *)
```

```
^^^^
```

Error: This expression has type **float** but an expression was expected of type **int**

```
# 1.35 +. 0.23;;
```

```
- : float = 1.58
```

No Implicit Coercion

1.0 * 2;; (* No Implicit Coercion *)

Characters 0-3:

1.0 * 2;;

^^^

Error: This expression has type float but an expression was expected of type int

1.0 *. 2;; (* No Implicit Coercion *)

Characters 7-8:

1.0 *. 2;;

^^

Error: This expression has type int but an expression was expected of type float

Sequencing Expressions

```
# "Hi there";; (* has type string *)
```

```
- : string = "Hi there"
```

```
# print_string "Hello world\n";; (* has type unit *)
```

```
Hello world
```

```
- : unit = ()
```

```
# (print_string "Bye\n"; 25);; (* Sequence of exp *)
```

```
Bye
```

```
- : int = 25
```

Declarations; Sequencing of Declarations

```
# let x = 2 + 3;; (* declaration *)
```

```
val x : int = 5
```

```
# let test = 3 < 2;;
```

```
val test : bool = false
```

```
# let a = 1 let b = a + 4;; (* Sequence of dec *)
```

```
val a : int = 1
```

```
val b : int = 5
```

Environments

- *Environments* record what value is associated with a given identifier
- Central to the semantics and implementation of a language
- Notation

$$\rho = \{\text{name}_1 \rightarrow \text{value}_1, \text{name}_2 \rightarrow \text{value}_2, \dots\}$$

Using set notation, but describes a partial function

- Implementation: Often stored as list, or stack
 - To find value start from left and take first match

Environments

$X \rightarrow 3$

$\text{name} \rightarrow \text{"Steve"}$

...

$y \rightarrow 17$

$\text{region} \rightarrow (5.4, 3.7)$

$b \rightarrow \text{true}$

$\text{id} \rightarrow \{\text{Name} = \text{"Paul"},$
 $\text{Age} = 23,$
 $\text{SSN} = 999888777\}$

Global Variable Creation

```
# 2 + 3;;    (* Expression *)
```

```
// doesn't affect the environment
```

```
# let test = 3 < 2;;    (* Declaration *)
```

```
val test : bool = false
```

```
//  $\rho_1 = \{\text{test} \rightarrow \text{false}\}$ 
```

```
# let a = 1 let b = a + 4;; (* Seq of dec *)
```

```
//  $\rho_2 = \{b \rightarrow 5, a \rightarrow 1, \text{test} \rightarrow \text{false}\}$ 
```

New Bindings Hide Old

```
//  $\rho_2 = \{b \rightarrow 5, a \rightarrow 1, test \rightarrow false\}$ 
```

```
let test = 3.7;;
```

- What is the environment after this declaration?

New Bindings Hide Old

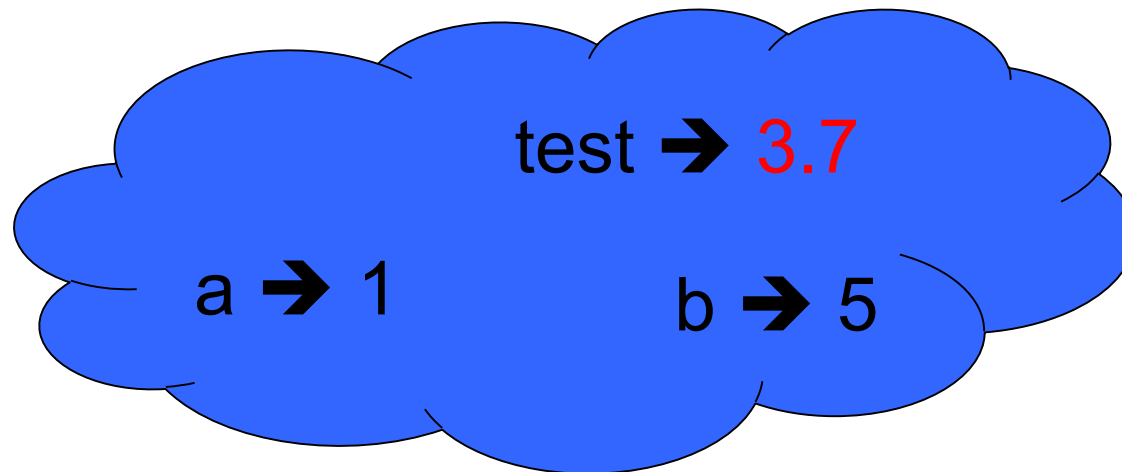
// $\rho_2 = \{b \rightarrow 5, a \rightarrow 1, \mathbf{test} \rightarrow \mathbf{false}\}$

let test = 3.7;;

- What is the environment after this declaration?

// $\rho_3 = \{\mathbf{test} \rightarrow \mathbf{3.7}, a \rightarrow 1, b \rightarrow 5\}$

Environments



Local Variable Creation

// $\rho_3 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

let $b = 5 * 4$

// $\rho_4 = \{b \rightarrow 20, \text{test} \rightarrow 3.7, a \rightarrow 1\}$

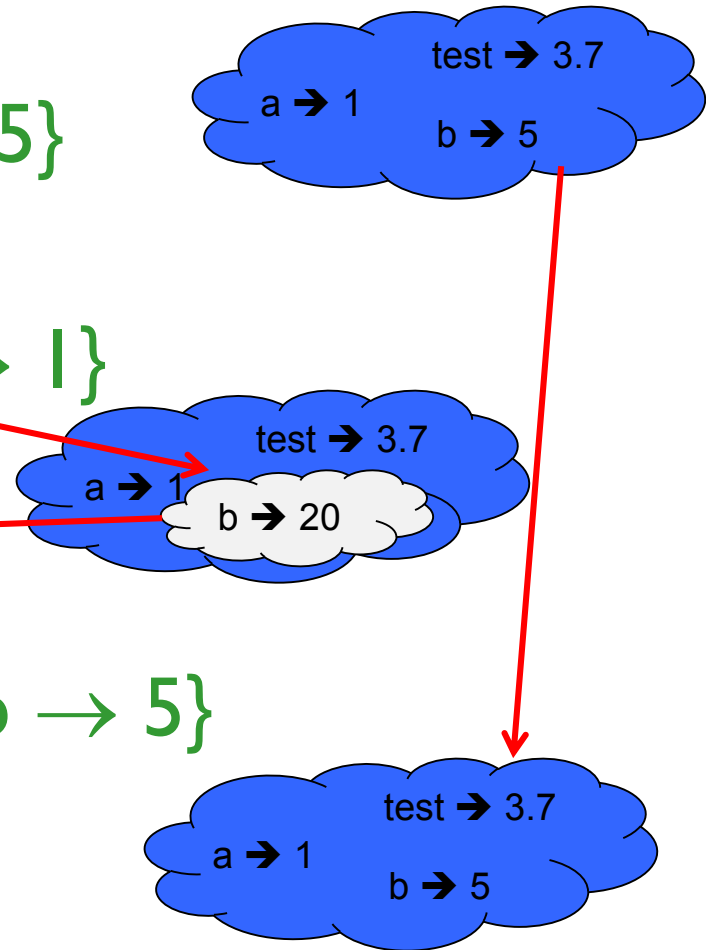
in $2 * b;$

- : int = 40

// $\rho_5 = \rho_3 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

b;

- : int = 5



Local let binding

// $\rho_5 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

let c =

let b = a + a

in b * b;;

b;;

Local let binding

// $\rho_5 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

let c =

let b = a + a

// $\rho_6 = \{b \rightarrow 2\} + \rho_5$

// $= \{b \rightarrow 2, \text{test} \rightarrow 3.7, a \rightarrow 1\}$

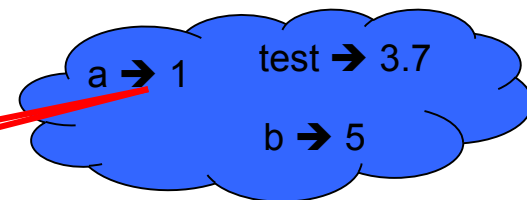
in b * b;;

val c : int = 4

// $\rho_7 = \{c \rightarrow 4, \text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

b;;

- : int = 5



Local let binding

// $\rho_5 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

let c =

let b = a + a

// $\rho_6 = \{b \rightarrow 2\} + \rho_5$

// = $\{b \rightarrow 2, \text{test} \rightarrow 3.7, a \rightarrow 1\}$

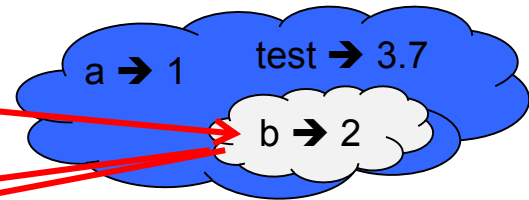
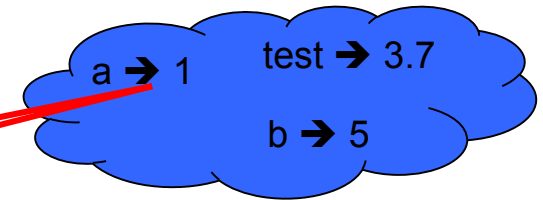
in b * b;;

val c : int = 4

// $\rho_7 = \{c \rightarrow 4, \text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

b;;

- : int = 5



Local let binding

// $\rho_5 = \{\text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

let c =

let b = a + a

// $\rho_6 = \{b \rightarrow 2\} + \rho_5$

// = $\{b \rightarrow 2, \text{test} \rightarrow 3.7, a \rightarrow 1\}$

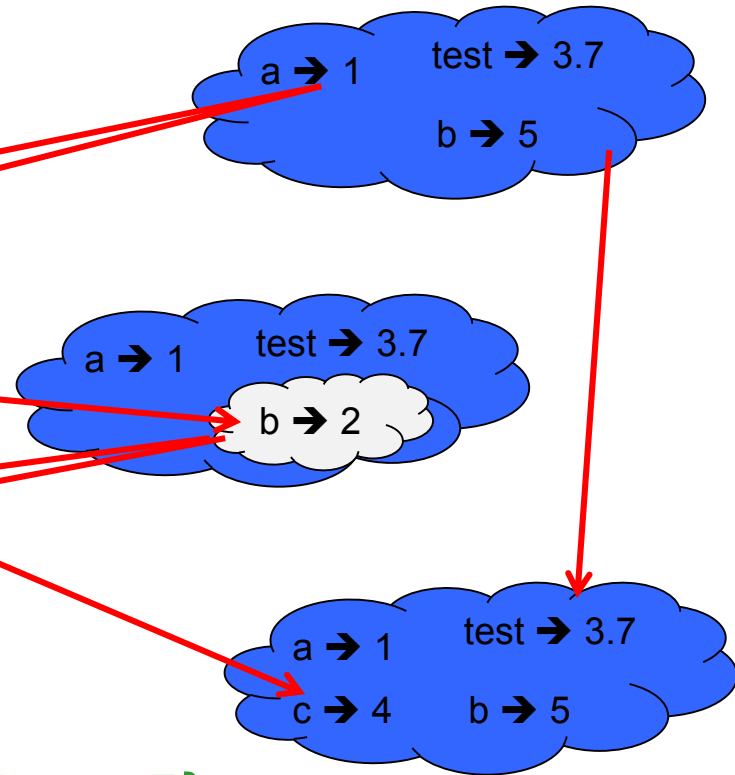
in b * b;;

val c : int = 4

// $\rho_7 = \{c \rightarrow 4, \text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$

b;;

- : int = 5



Booleans (aka Truth Values)

```
# true;;
```

```
- : bool = true
```

```
# false;;
```

```
- : bool = false
```

```
//  $\rho_7 = \{c \rightarrow 4, \text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\}$ 
```

```
# if b > a then 25 else 0;;
```

```
- : int = 25
```

Booleans and Short-Circuit Evaluation

```
# 3 > 1 && 4 > 6;;
```

```
- : bool = false
```

```
# 3 > 1 || 4 > 6;;
```

```
- : bool = true
```

```
# not (4 > 6);;
```

```
- : bool = true
```

```
# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
```

```
Hi
```

```
- : bool = true
```

```
# 3 > 1 || (print_string "Bye\n"; 4 > 6);;
```

```
- : bool = true
```

Tuples as Values

```
//  $\rho_0 = \{c \rightarrow 4, a \rightarrow 1, b \rightarrow 5\}$ 
```

```
# let s = (5, "hi", 3.2);;
```

```
val s : int * string * float = (5, "hi", 3.2)
```

```
//  $\rho = \{s \rightarrow (5, "hi", 3.2), c \rightarrow 4, a \rightarrow 1, b \rightarrow 5\}$ 
```


Pattern Matching with Tuples

```
// ρ = {s → (5, "hi", 3.2), a → 1, b → 5, c → 4}
```

```
# let (a,b,c) = s;;          (* (a,b,c) is a pattern *)
```

```
val a : int = 5
```

```
val b : string = "hi"
```

```
val c : float = 3.2
```

```
# let (a, _, _) = s;;
```

```
val a : int = 5
```

```
# let x = 2, 9.3;;          (* tuples don't require parens in Ocaml *)
```

```
val x : int * float = (2, 9.3)
```

Nested Tuples

```
# (*Tuples can be nested *)
# let d = ((1,4,62),("bye",15),73.95);;
val d : (int * int * int) * (string * int) * float =
  ((1, 4, 62), ("bye", 15), 73.95)

# (*Patterns can be nested *)
# let (p, (st,_), _) = d;;
      (* _ matches all, binds nothing *)
val p : int * int * int = (1, 4, 62)
val st : string = "bye"
```

Functions

```
# let plus_two n = n + 2;;
```

```
val plus_two : int -> int = <fun>
```

```
# plus_two 17;;
```

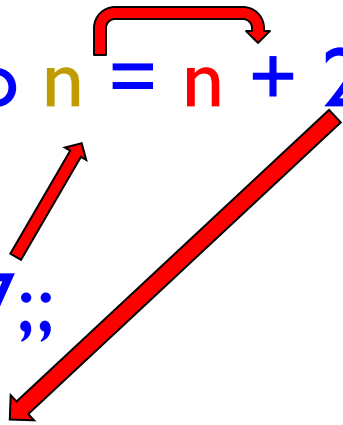
```
- : int = 19
```

Functions

```
let plus_two n = n + 2;;
```

```
plus_two 17;;
```

```
- : int = 19
```



Nameless Functions (aka Lambda Terms)

```
fun n -> n + 2;;
```

```
(fun n -> n + 2) 17;;
```

```
- : int = 19
```



Functions

```
# let plus_two n = n + 2;;
```

```
val plus_two : int -> int = <fun>
```

```
# plus_two 17;;
```

```
- : int = 19
```

```
# let plus_two = fun n -> n + 2;;
```

```
val plus_two : int -> int = <fun>
```

```
# plus_two 14;;
```

```
- : int = 16
```

First definition syntactic sugar for second

Using a nameless function

(* An application *)

```
# (fun x -> x * 3) 5;;
```

```
: int = 15
```

(* As data *)

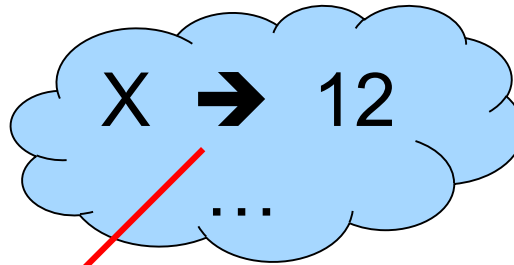
```
# ((fun y -> y +. 2.0), (fun z -> z * 3));;
```

```
- : (float -> float) * (int -> int) = (<fun>, <fun>)
```

Note: in `fun v -> exp(v)`, scope of variable is only the body `exp(v)`

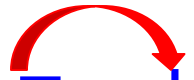
Values fixed at declaration time

```
# let x = 12;;
```



```
val x : int = 12
```

```
# let plus_x y = y + x;;
```



```
val plus_x : int -> int = <fun>
```

```
# plus_x 3;;
```

What is the result?

Values fixed at declaration time

```
# let x = 12;;
```

```
val x : int = 12
```

```
# let plus_x y = y + x;;
```

```
val plus_x : int -> int = <fun>
```

```
# plus_x 3;;
```

```
- : int = 15
```

Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an update *)
```

```
val x : int = 7
```

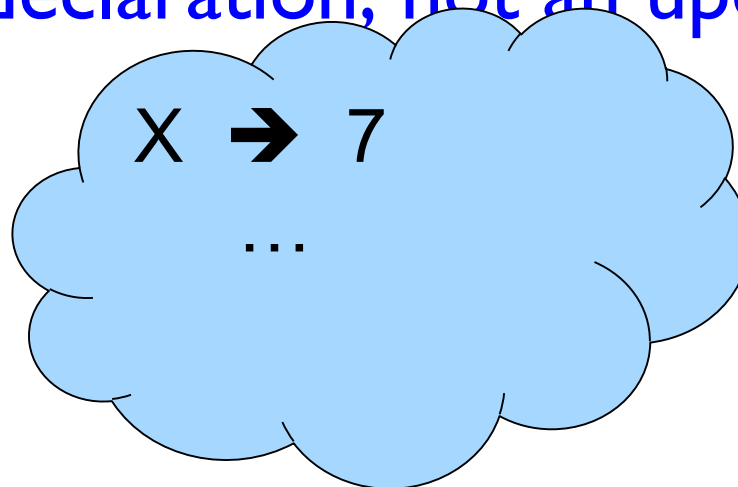
```
# plus_x 3;;
```

What is the result this time?

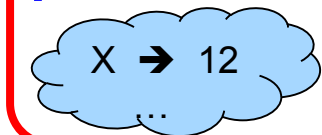
Values fixed at declaration time

let x = 7;; (* New declaration, not an update *)

val x : int = 7



plus_x 3;;



What is the result this time?

Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an update *)
```

```
val x : int = 7
```

```
# plus_x 3;;
```

```
- : int = 15
```

Question

- Observation: Functions are **first-class values** in this language
- Question: What value does the environment record for a function variable?
- Answer: **a closure**

Save the Environment!

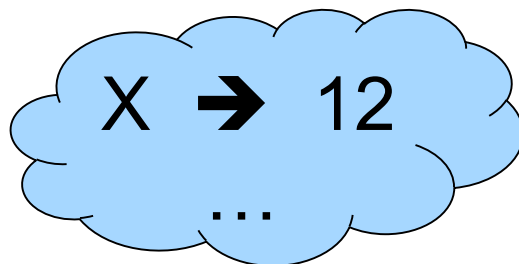
- A **closure** is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:

$$\langle (v_1, \dots, v_n) \rightarrow \text{exp}, \rho \rangle$$

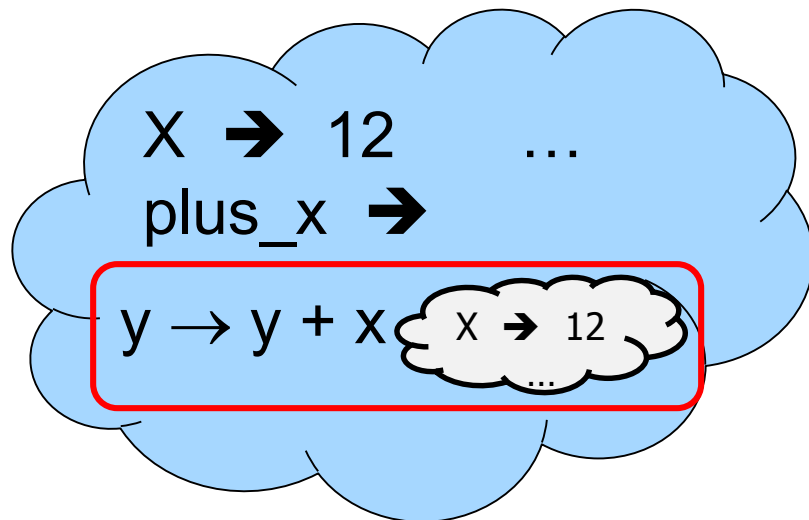
- Where ρ is the environment in effect when the function is defined (for a simple function)

Recall: let plus_x = fun x => y + x

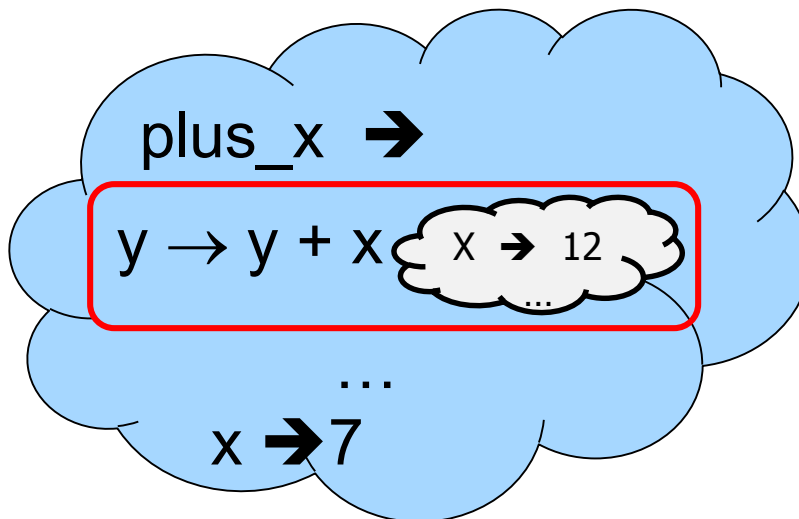
let x = 12



let plus_x = fun y -> y + x



let x = 7



Closure for plus_x

- When plus_x was defined, had environment:

$$\rho_{\text{plus_x}} = \{\dots, x \rightarrow 12, \dots\}$$

- Recall: `let plus_x y = y + x`

is really `let plus_x = fun y -> y + x`

- Closure for `fun y -> y + x`:

$$\langle y \rightarrow y + x, \rho_{\text{plus_x}} \rangle$$

- Environment just after plus_x defined:

$$\{\text{plus_x} \rightarrow \langle y \rightarrow y + x, \rho_{\text{plus_x}} \rangle\} + \rho_{\text{plus_x}}$$

Like set union!
(but subtle differences;
new decl. replaces old)

Functions with more than one argument

```
# let add_three x y z = x + y + z;;  
val add_three : int -> int -> int -> int = <fun>
```

```
# let t = add_three 6 3 2;;  
val t : int = 11
```

```
# let add_three =  
    fun x -> (fun y -> (fun z -> x + y + z));;  
val add_three : int -> int -> int -> int = <fun>
```

Again, first syntactic sugar for second

Functions on tuples

```
# let plus_pair (n,m) = n + m;;  
val plus_pair : int * int -> int = <fun>
```

```
# plus_pair (3,4);;  
- : int = 7
```

```
# let twice x = (x,x);;  
val twice : 'a -> 'a * 'a = <fun>
```

```
# twice 3;;  
- : int * int = (3, 3)
```

```
# twice "hi";;  
- : string * string = ("hi", "hi")
```

Curried vs Uncurried

■ Recall

```
# let add_three u v w = u + v + w;;
```

```
val add_three : int -> int -> int -> int = <fun>
```

■ How does it differ from

```
# let add_triple (u,v,w) = u + v + w;;
```

```
val add_triple : int * int * int -> int = <fun>
```

■ add_three is **curried**;

■ add_triple is **uncurried**

Curried vs Uncurried

```
# add_three 6 3 2;;
```

```
- : int = 11
```

```
# add_triple (6,3,2);;
```

```
- : int = 11
```

```
# add_triple 5 4;;
```

```
Characters 0-10: add_triple 5 4;;
```

```
^^^^^^^^^^
```

This function is applied to too many arguments,
maybe you forgot a `;`

```
# fun x -> add_triple (5,4,x);;
```

```
: int -> int = <fun>
```

Partial application of functions

```
let add_three x y z = x + y + z;;
```

```
# let h = add_three 5 4;;  
val h : int -> int = <fun>
```

```
# h 3;;  
- : int = 12
```

```
# h 7;;  
- : int = 16
```

Partial application also called *sectioning*

Match Expressions

```
# let triple_to_pair triple =
```

```
  match triple
```

```
  with (0, x, y) -> (x, y)
```

```
  | (x, 0, y) -> (x, y)
```

```
  | (x, y, _) -> (x, y);;
```

- Each clause: pattern on left, expression on right
- Each x, y has scope of only its clause
- Use first matching clause

```
val triple_to_pair : int * int * int -> int * int =
```

```
<fun>
```