

Announcements

- **MP4** is out. Due on Nov 6 @ 11:59pm.

Final project upcoming deadlines:

- Nov 13, a short video of your progress.
- Dec 16, final project presentation.

Grades are out for:

- Midterm 1
- Project abstract and picture-title

Tracking Systems in VR

What do we want to track? Think about rigid bodies:

1. Head wearing HMD
2. Eyes
3. Palms of hands
4. Fingers
5. Entire body
6. Movable objects - controller, coffee cup, desk
7. Other people in the space

Tracking Systems in VR

What do we want to track:

For each rigid body, estimate

Rotation:

Position:

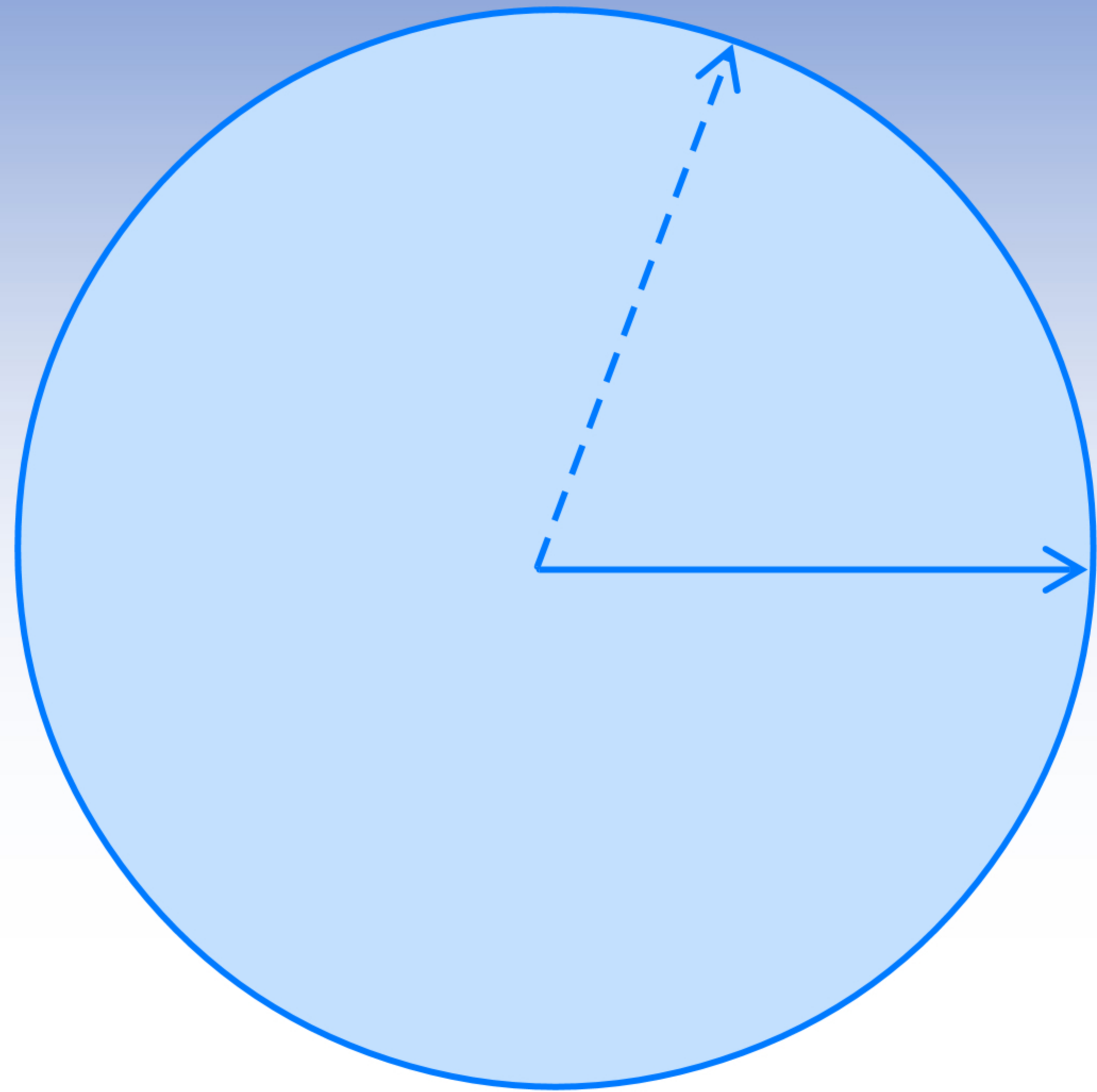
OR

Homogeneous
transformation
matrix:

Task:

Tracking Systems in VR: Estimating 2D Orientation

easy?



Initial conditions

For constant velocity

For variable velocity

Discrete-time approximation

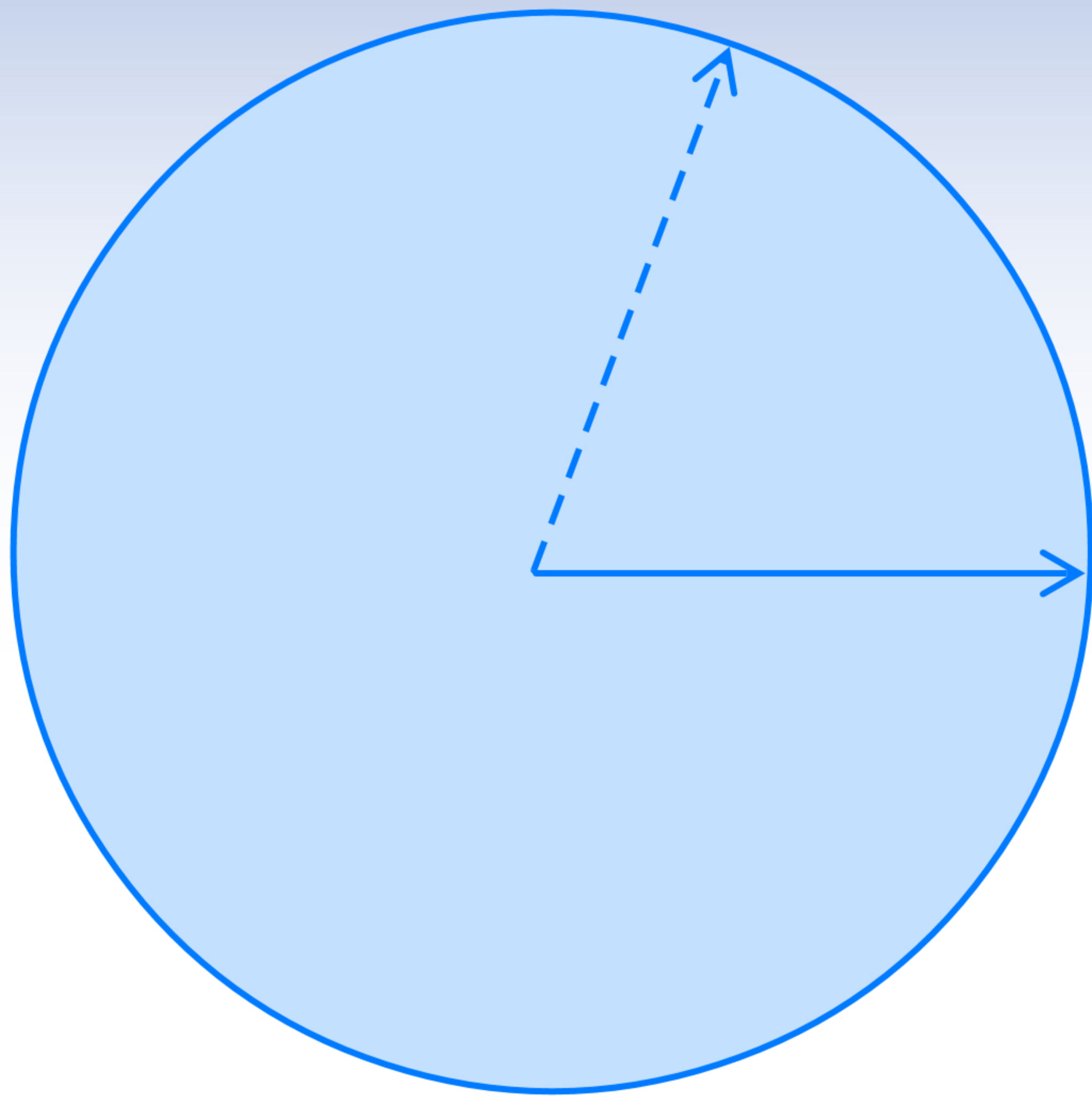
Tracking Systems in VR: Estimating 2D Orientation

Discrete-time approximation

$$\begin{aligned}\theta_k &\approx \theta_0 + \sum_{i=1}^k \Delta\theta_i = \\ &= \theta_0 + \sum_{i=1}^k \omega_i \Delta t\end{aligned}$$

$$\Delta t = 1 \text{ msec}$$

$$\omega_i = \omega((i-1)\Delta t)$$



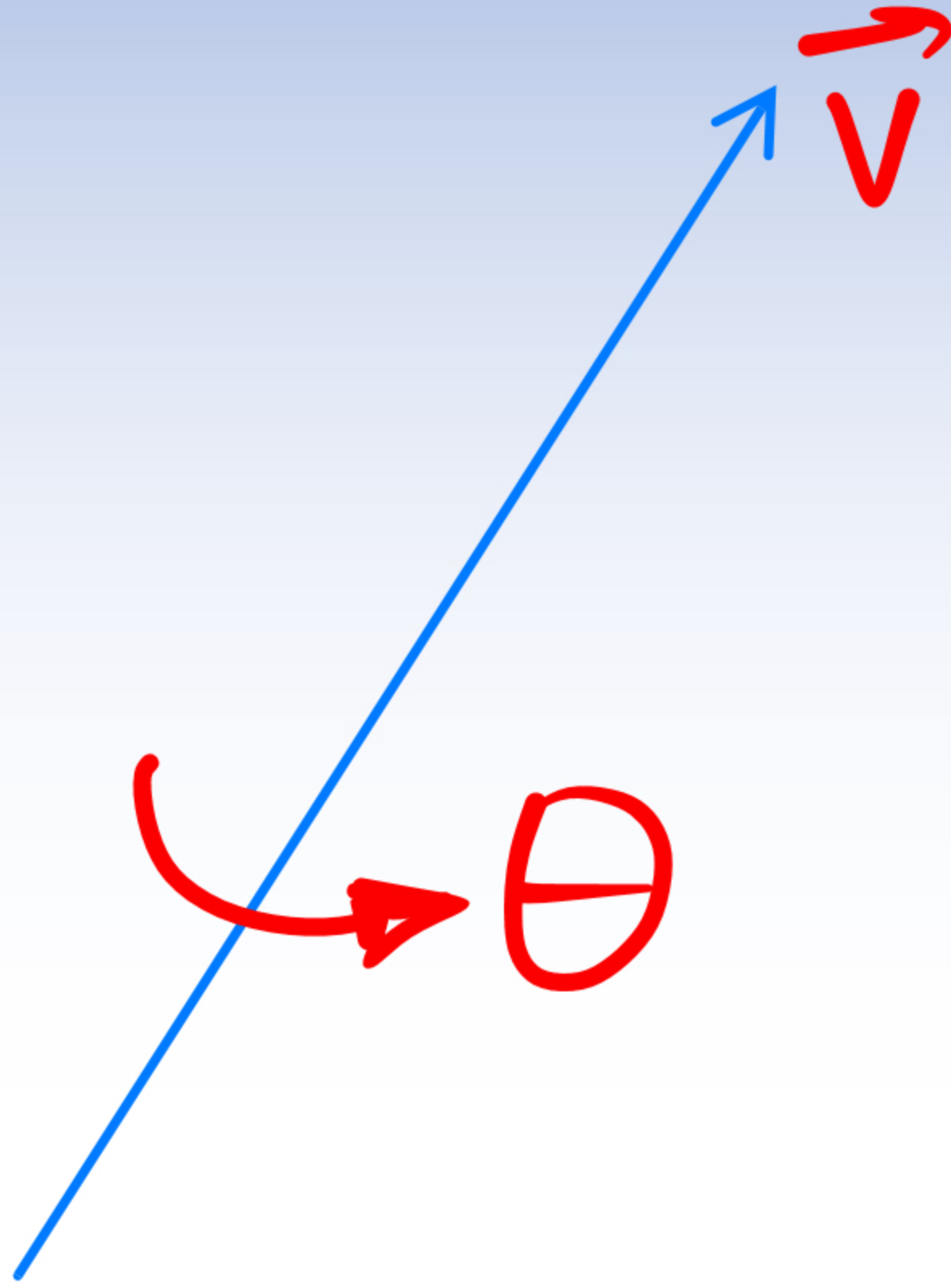
Estimation given sensor readings ω_i every Δt

Q1: does it matter where we put the gyroscope on the disk?

Q2: How many lines of code to implement this estimation?

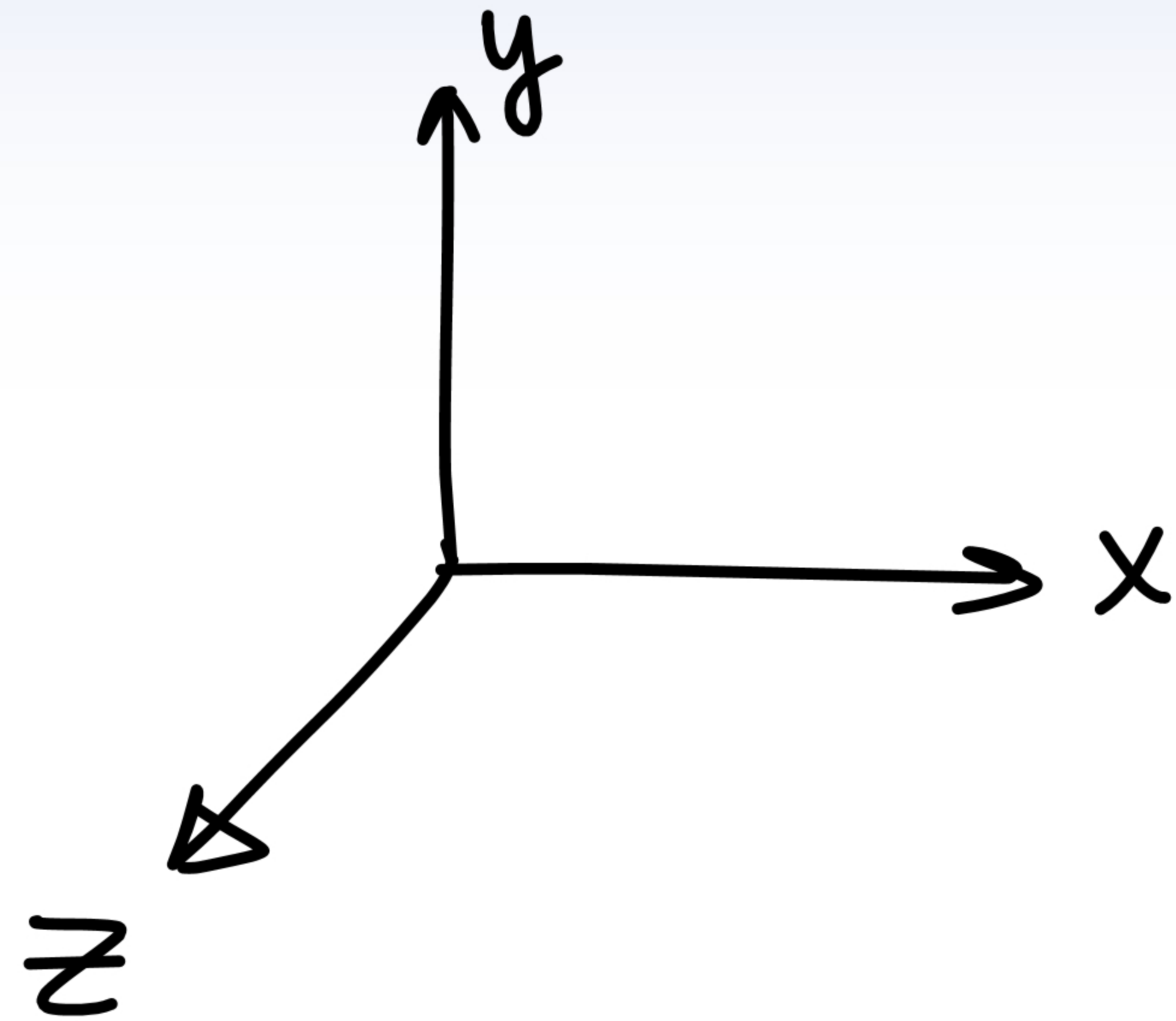
Tracking Systems in VR: Estimating 3D Orientation

Axis-angle:



3-axis gyroscope measures:

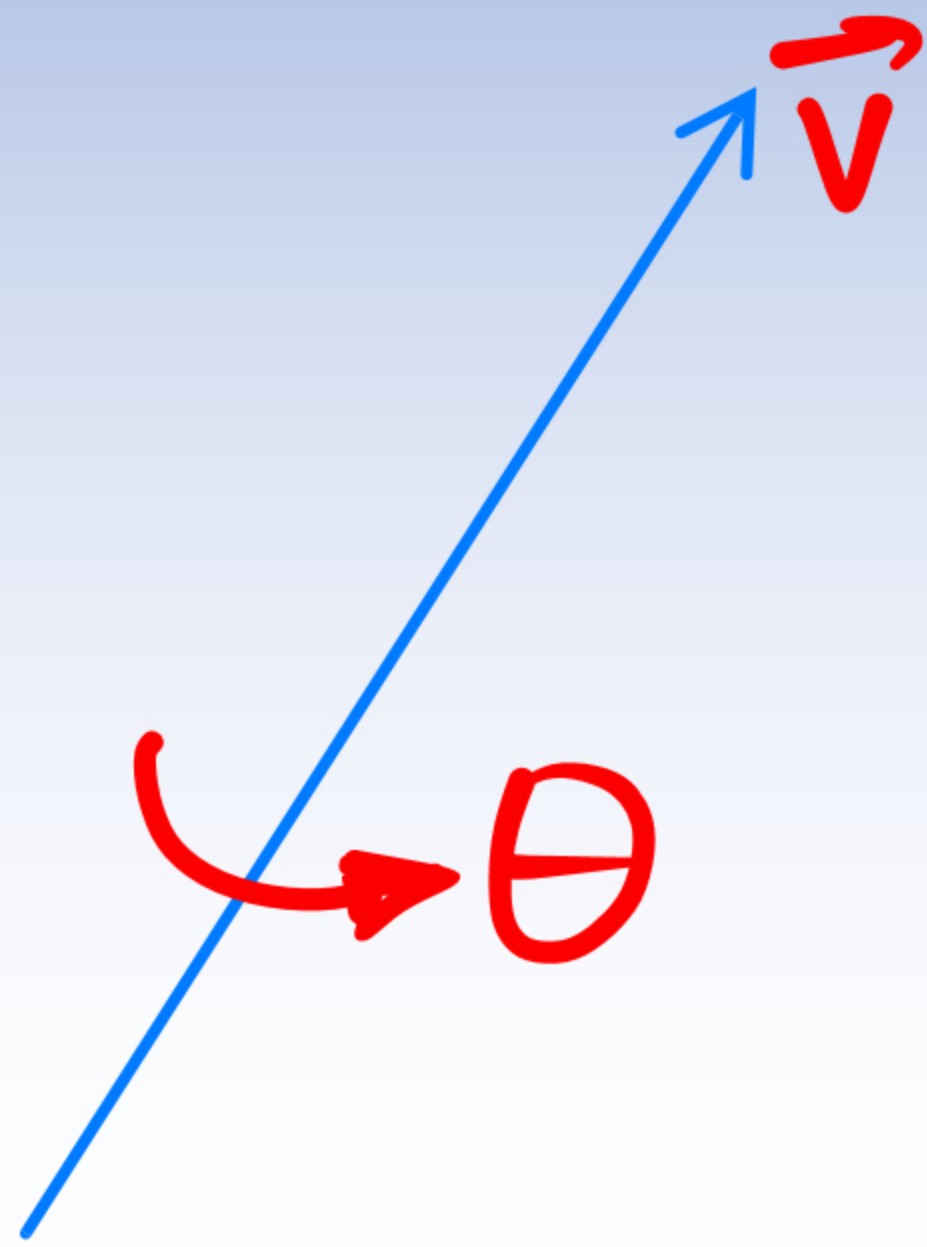
$$\omega =$$



Examples of VR systems with IMU only tracking:

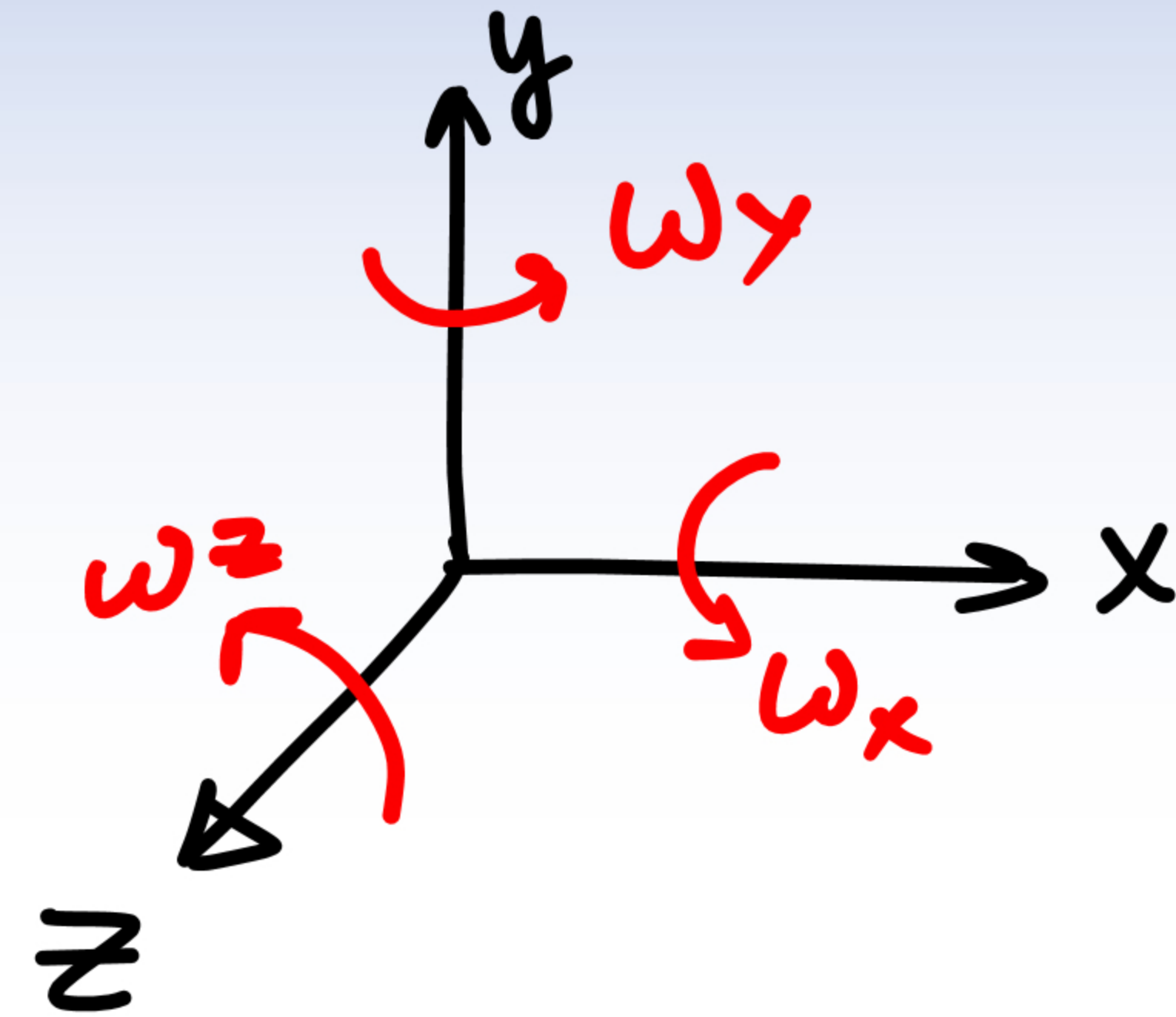
Tracking Systems in VR: Estimating 3D Orientation

Axis-angle: (\vec{v}, θ)



3-axis gyroscope measures:

$$\vec{\omega} = (\omega_x, \omega_y, \omega_z)$$



How large is ΔQ_i ?

Tracking Systems in VR: Estimating 3D Orientation

Integrate sensor readings to estimate orientation:

Recall 2D: $\hat{\theta}_k = \theta_0 + \sum_{i=1}^k \Delta \hat{\theta}_i =$
 $= \theta_0 + \Delta \hat{\theta}_1 + \Delta \hat{\theta}_2 + \dots + \Delta \hat{\theta}_k$

3D: $\hat{Q}_k =$

Recursively/Incrementally: 2D: $\hat{\theta}_{\text{current}} =$

3D: $\hat{Q}_{\text{current}} =$

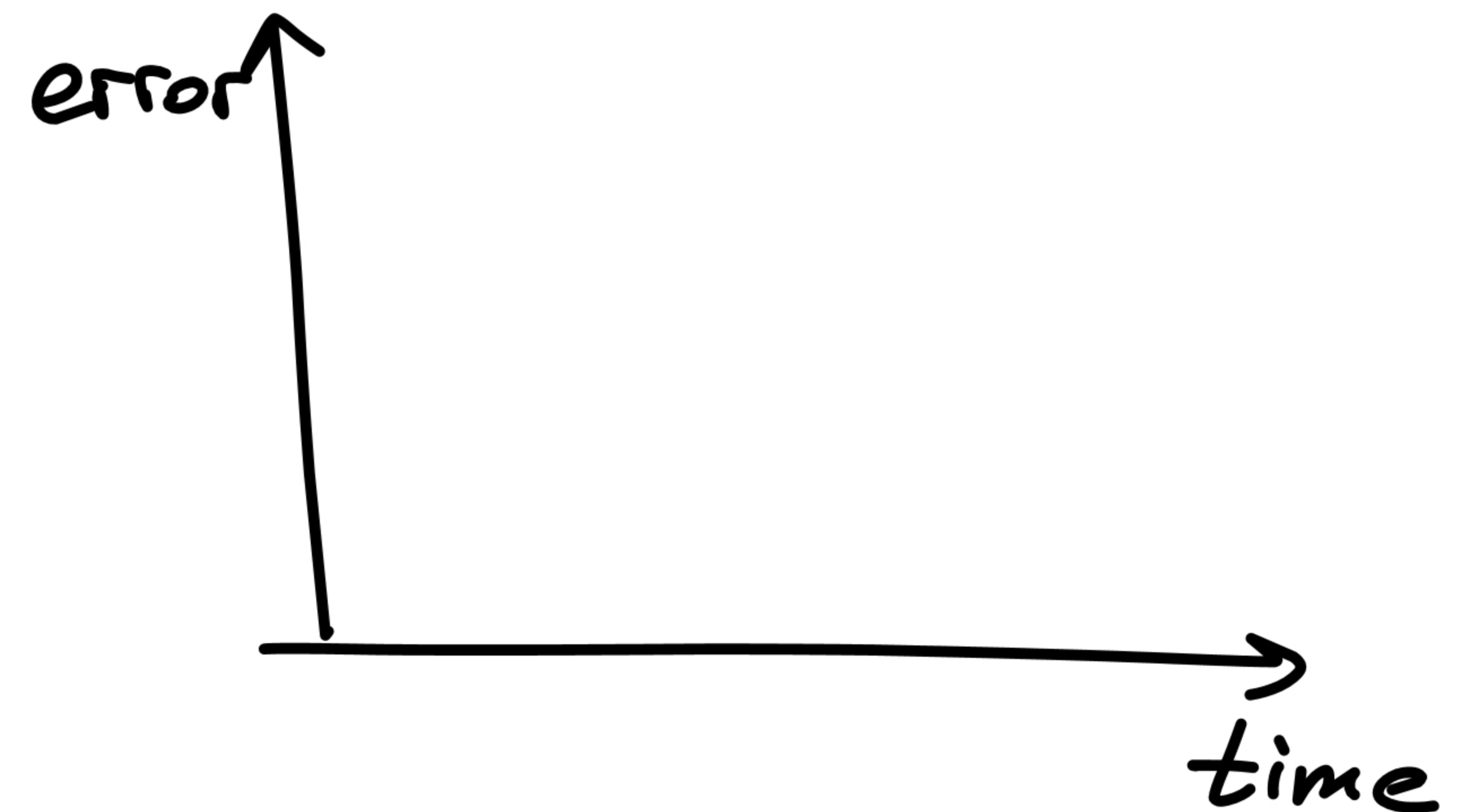
Problem:

Estimating 3D Orientation: Drift Correction

Expression for drift error:

$$2D: d_k =$$

$$3D: d_k =$$



An unusual quantity to have for an error!

Estimating 3D Orientation: Drift Correction

Correcting for drift errors challenge:

1) Use another sensor _____

2) Gradually apply corrections

- Fast enough to _____

- Slow enough to _____

Estimating 3D Orientation: Drift Correction

Separate the rotational drift error into **two components**:

1)

To correct:

2)

To correct: