

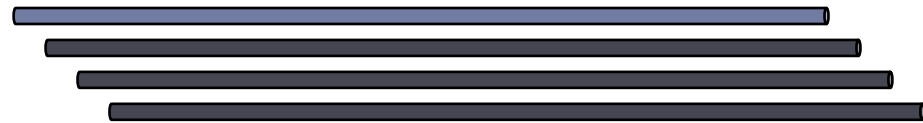
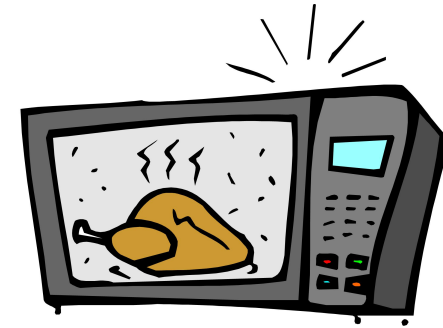
MIMO Systems

How Do We Increase Throughput in Wireless?

- ▶ Increase Power!

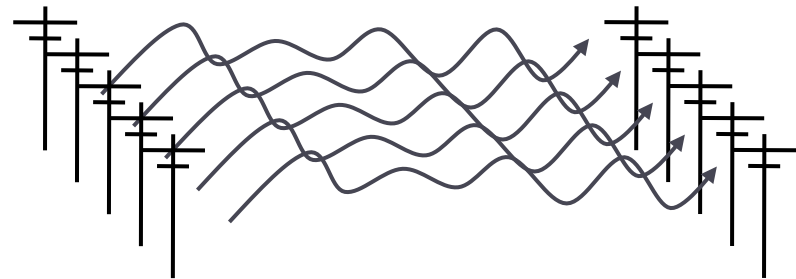
- ▶ Wired world

 - ▶ pull more wires!



- ▶ Wireless world

 - ▶ use concurrent streams!



Why MIMO

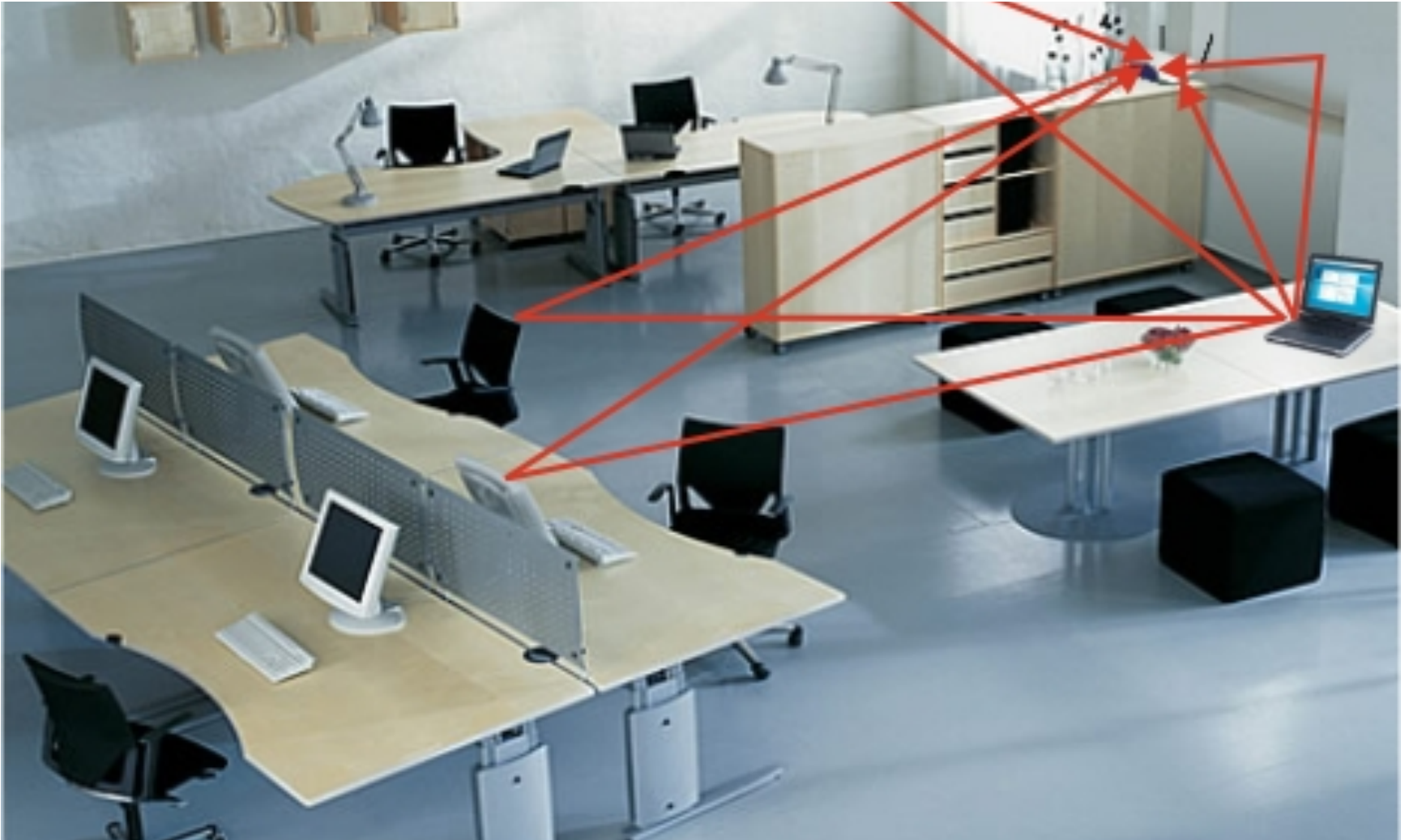
- ▶ **Motivation: current wireless systems**
 - ▶ Capacity constrained networks
 - ▶ Issues related to quality and coverage
- ▶ **MIMO exploits the space dimension to improve wireless systems**
 - ▶ capacity, range and reliability
- ▶ **MIMO-OFDM – the corner stone of future broadband wireless access**
 - ▶ WiFi – 802.11n 802.11ac
 - ▶ WiMAX – 802.16e (a.k.a 802.16-2005)
 - ▶ 3G / 4G



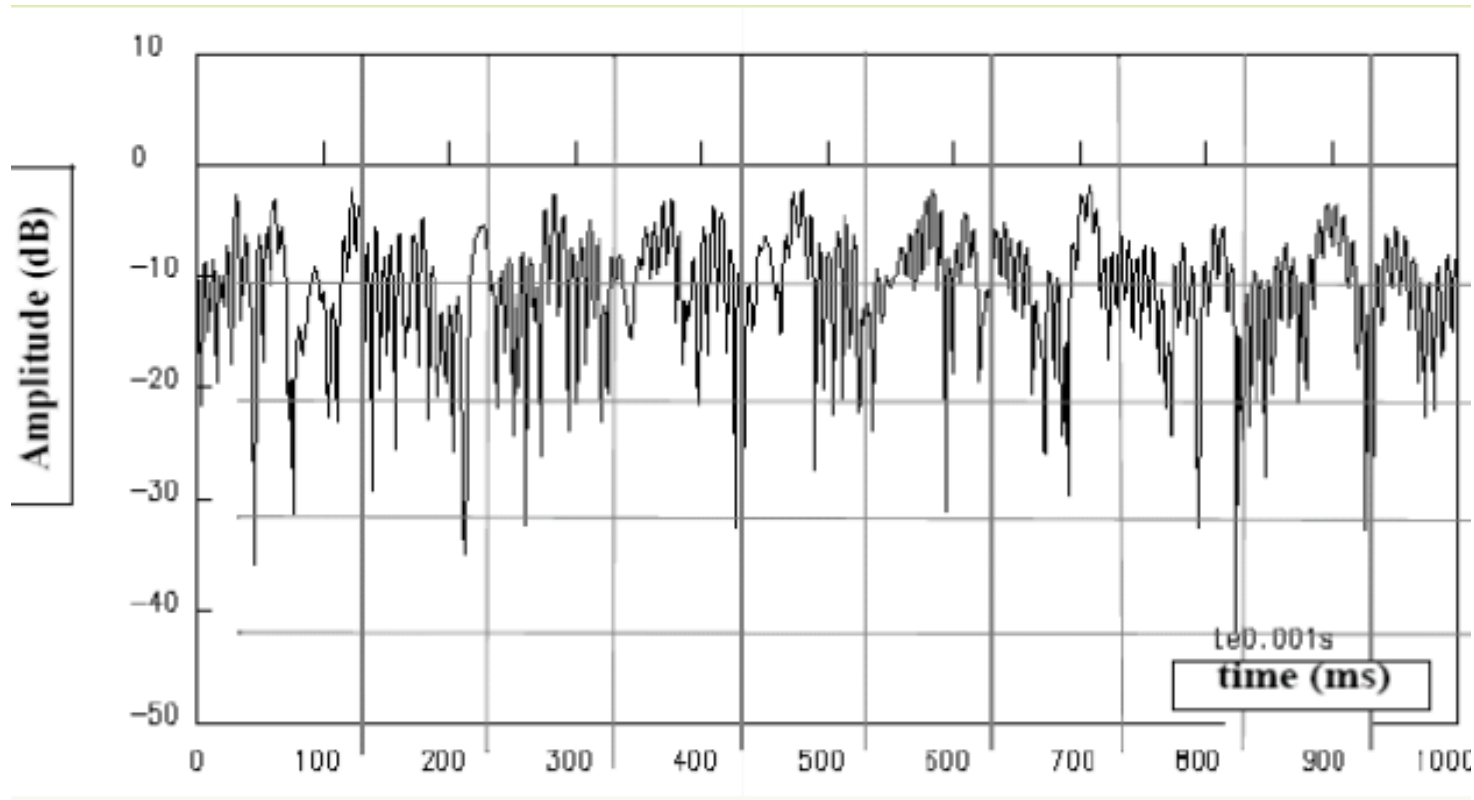
SISO - Single Input/Single Output

Method	Capacity
SISO	$B \log_2(1 + r)$

Multipath is Unavoidable



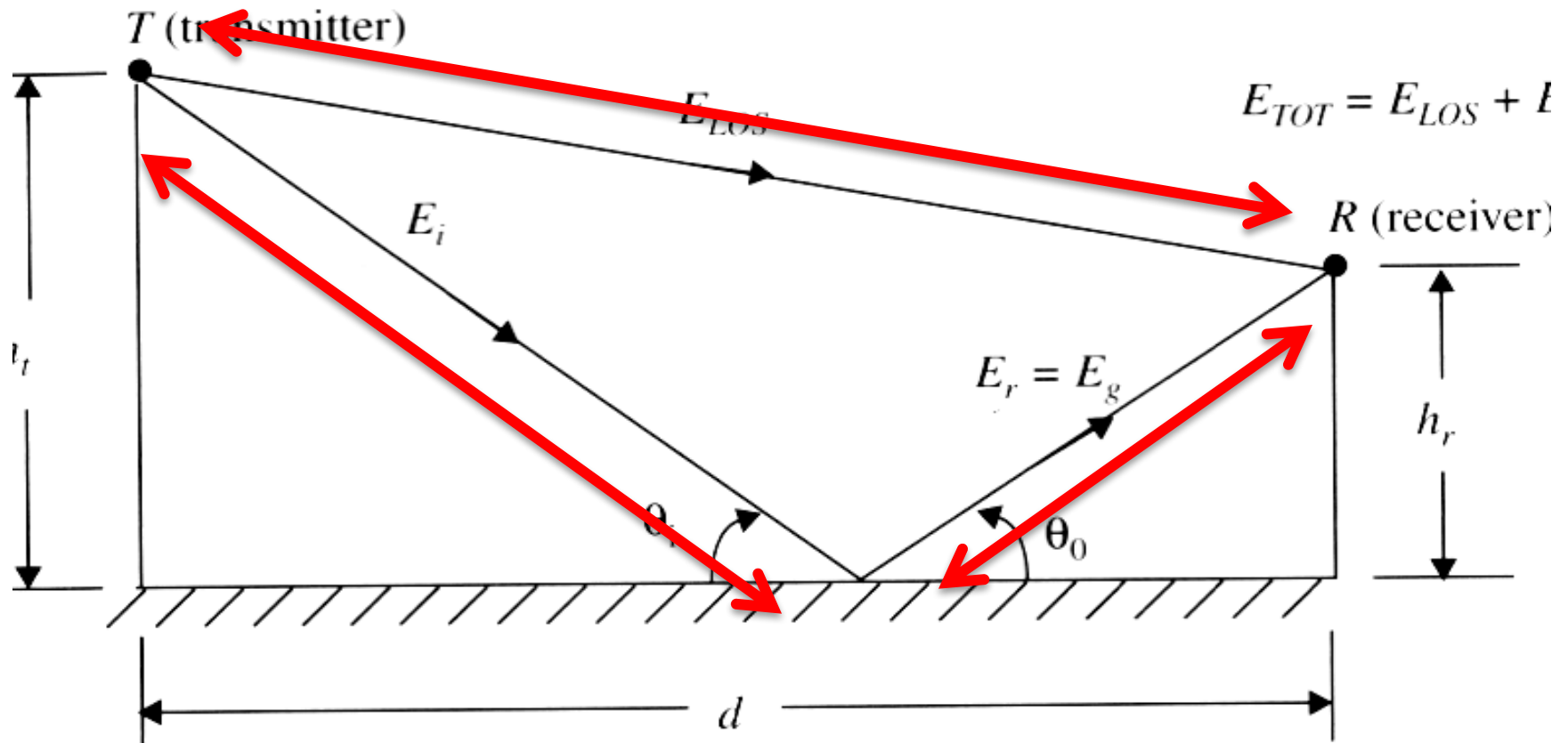
Fading becomes time-variant



Received SNR influenced by:

- Tx and Rx location
- Variation of channel fading over time

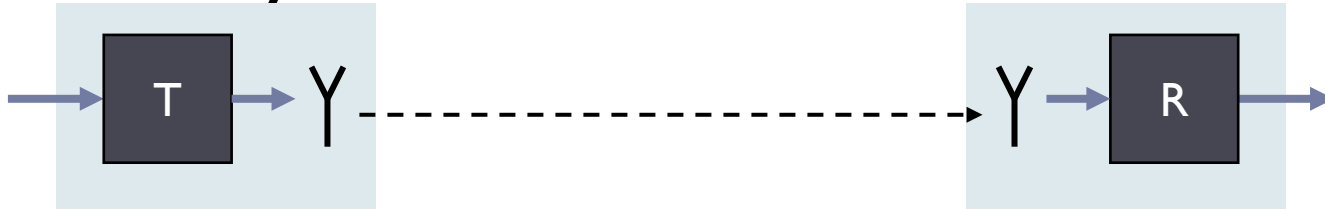
Different Propagation time



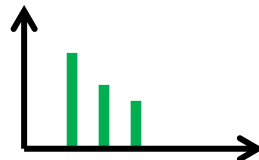
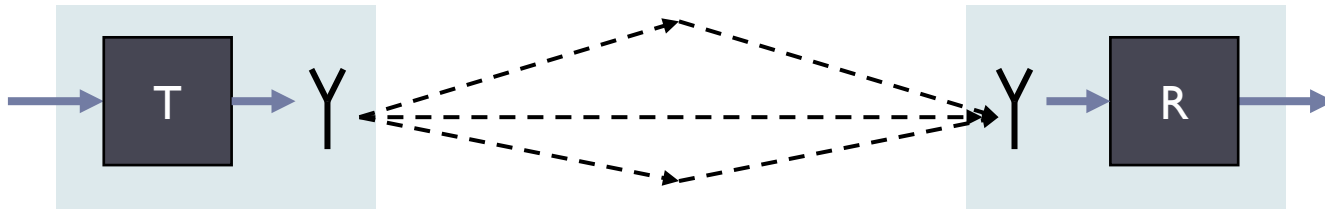
Two-ray ground reflection model.

Simple Channel Model

► No diversity:

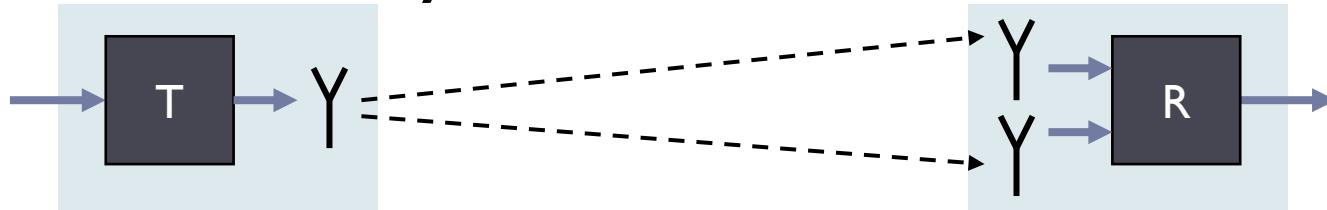


► Adding multi-path:

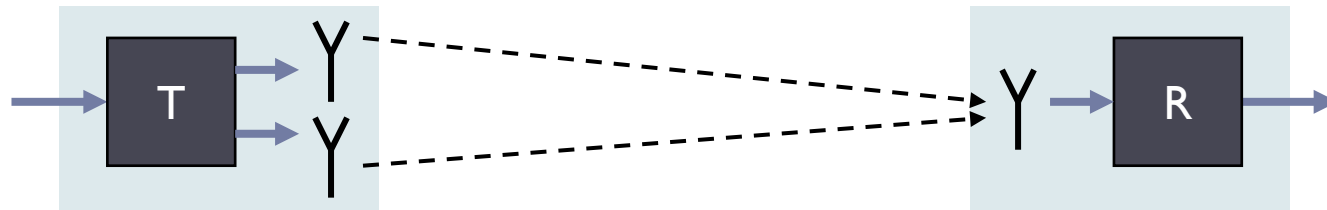


Can we Benefit from This?

► Receive diversity:



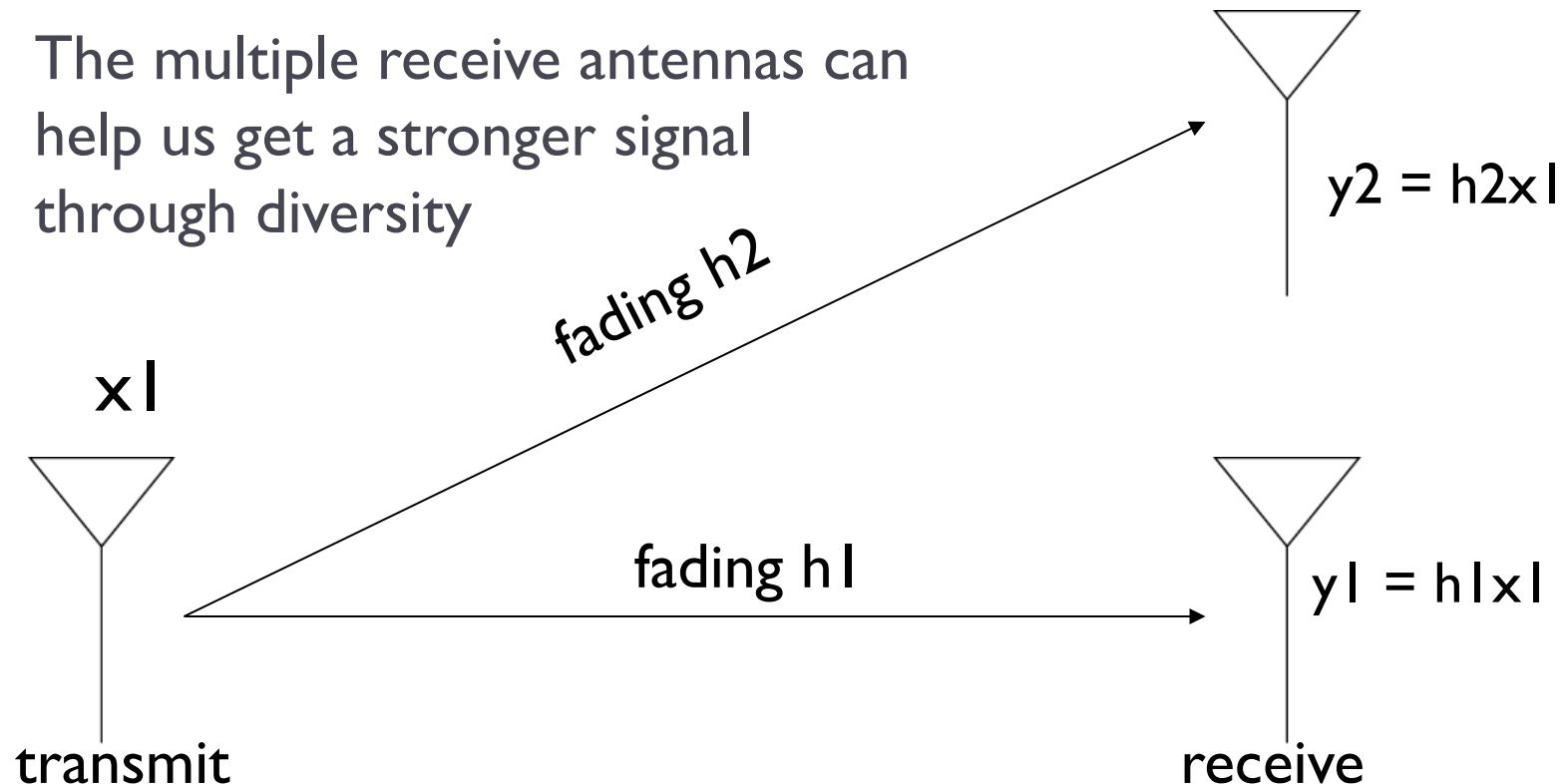
► Transmit diversity:



SIMO - Single Input/Multiple Output

► Spatial Diversity

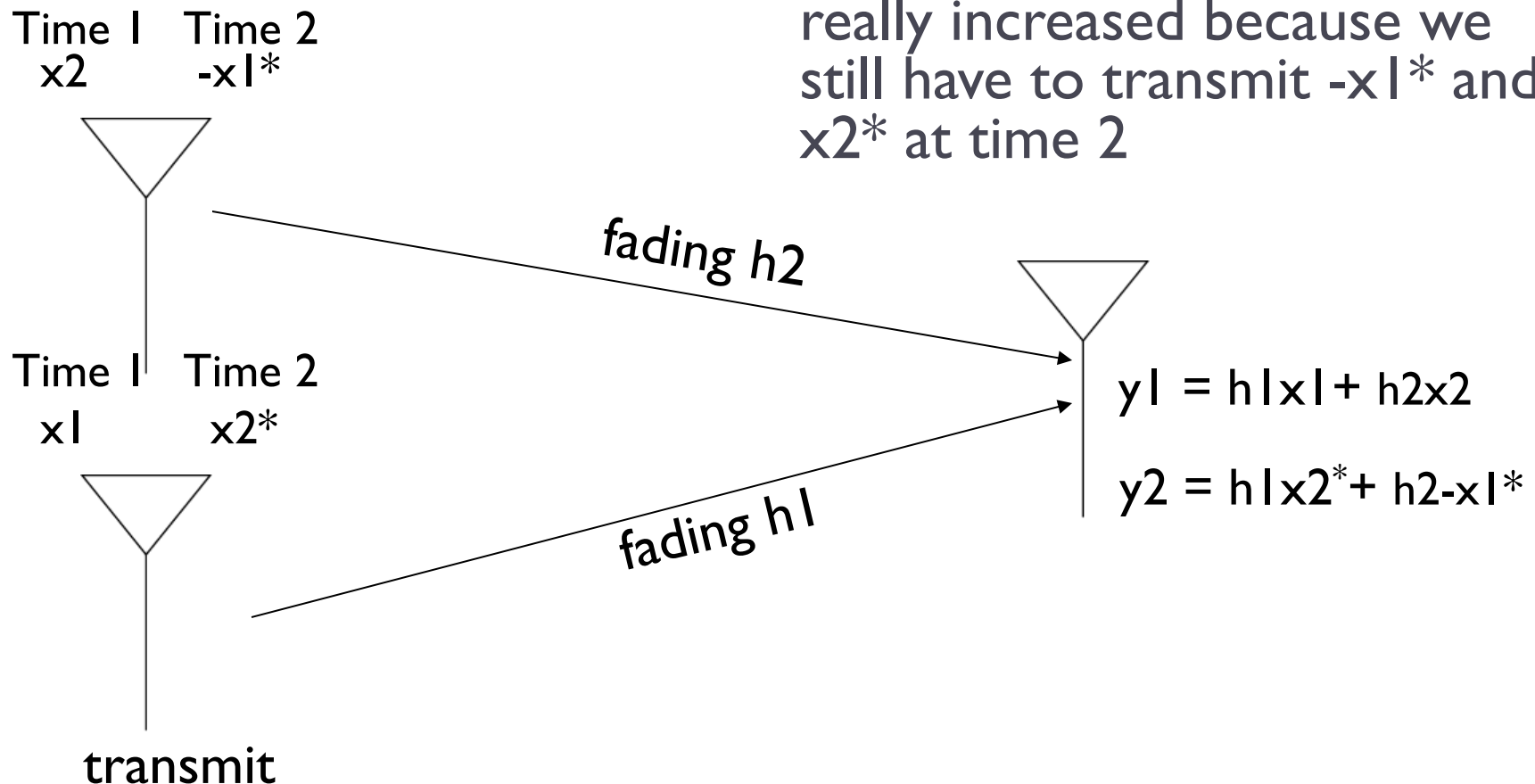
- The channel capacity has NOT increased
- The multiple receive antennas can help us get a stronger signal through diversity



MISO - Multiple Input/Single Output

► Time Diversity

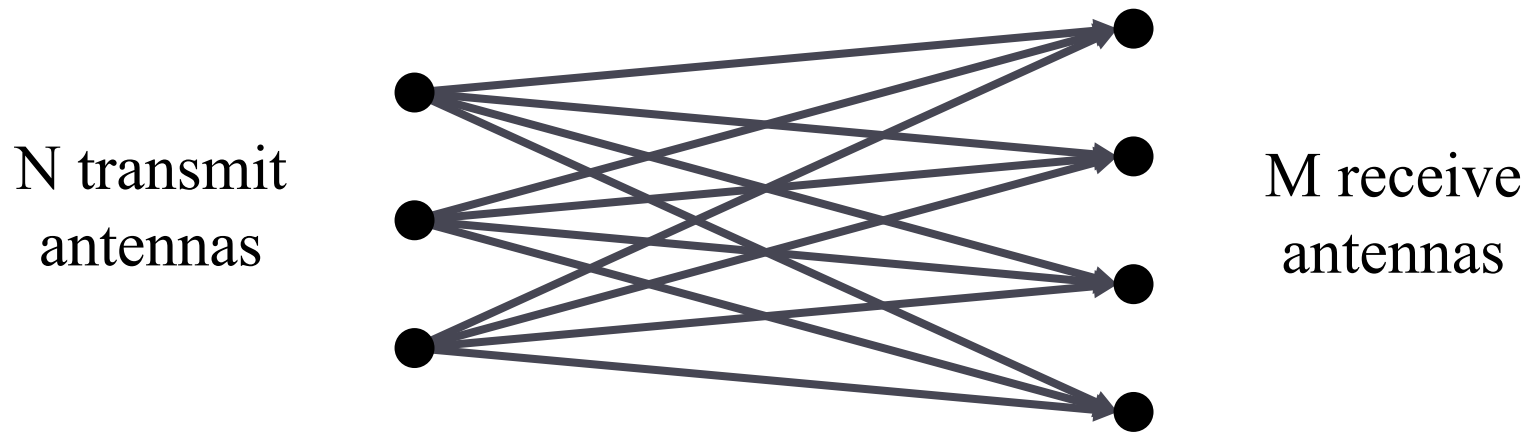
- The channel capacity has not really increased because we still have to transmit $-x_1^*$ and x_2^* at time 2



Channel Capacity for SISO, MISO, SIMO

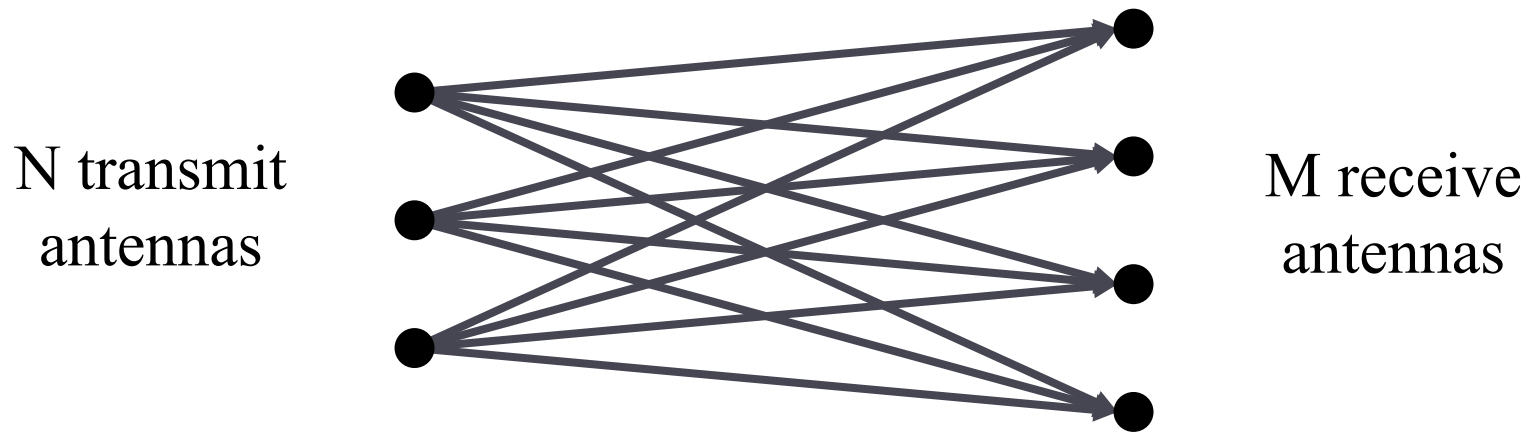
Method	Capacity
SISO	$B \log_2(1 + r)$
Diversity ($1 \times N$ or $N \times 1$)	$B \log_2(1 + rN)$
Diversity ($N \times N$)	$B \log_2(1 + rN^2)$

MIMO - Multiple Input/Multiple Output



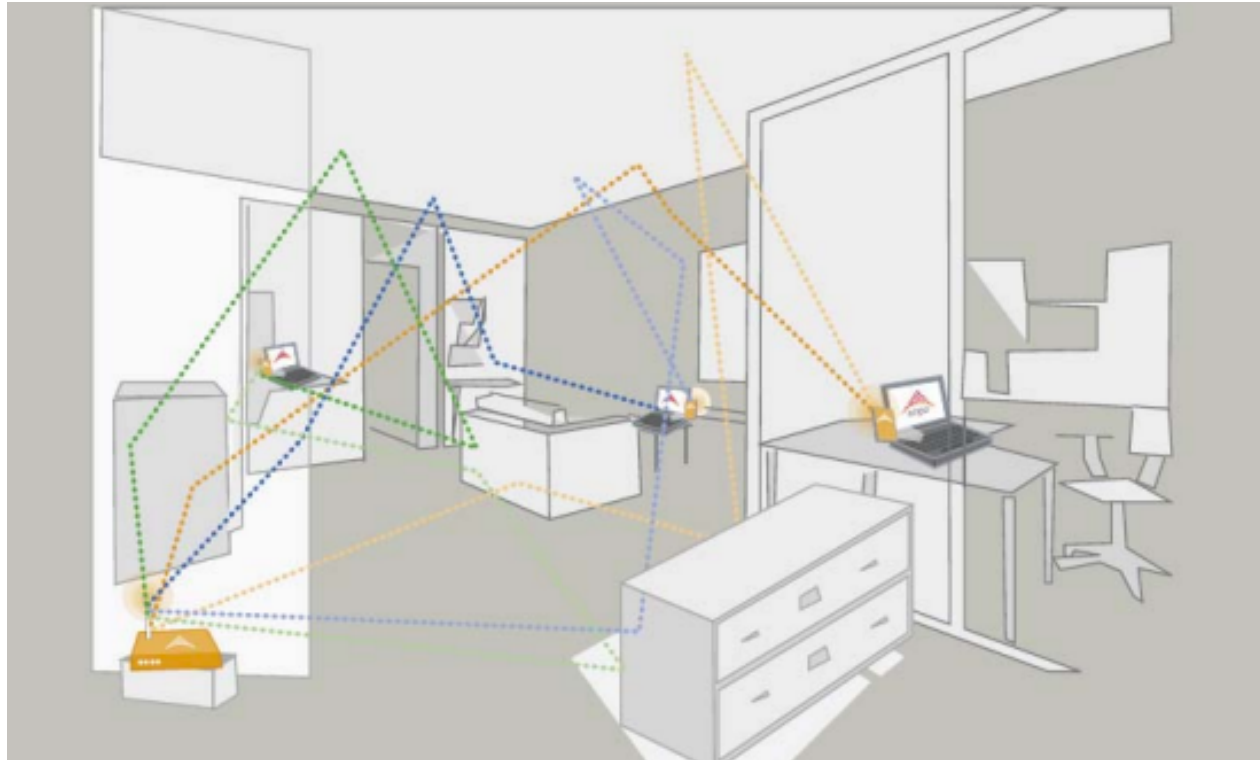
- ▶ $N \times M$ subchannels
- ▶ Fading on channels is largely independent
 - ▶ Assuming antennas are separate $\frac{1}{2}$ wavelength or more

MIMO - Multiple Input/Multiple Output



- ▶ Combines ideas from spatial and time diversity
 - ▶ e.g. $I \times N$ and $N \times I$
- ▶ Very effective if there is no direct line of sight
 - ▶ Subchannels become more independent

MIMO Increases Range

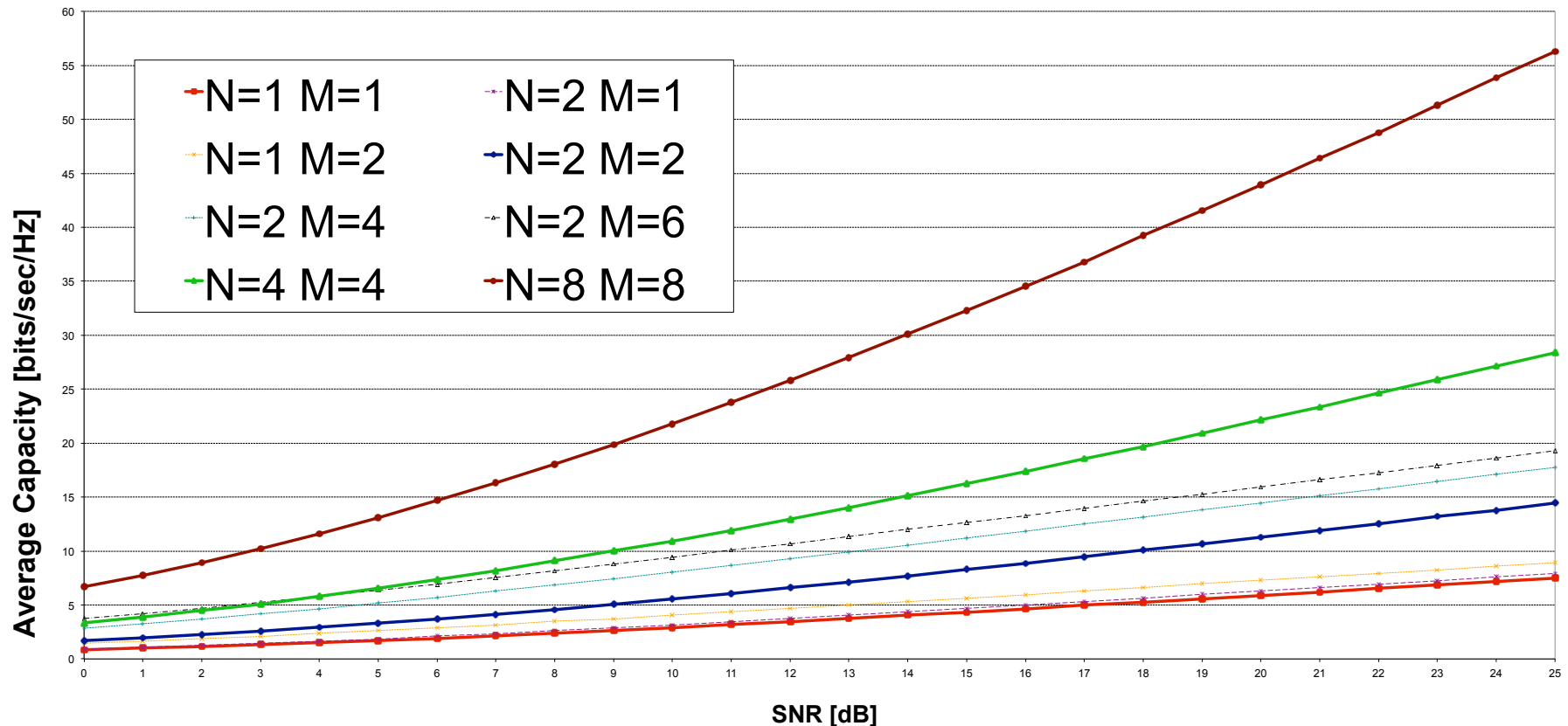


- ▶ Each multipath route is separate channel
- ▶ Traditional radios are confused by this multipath, while MIMO takes advantage of these “echoes”

Channel Capacity for MIMO

Method	Capacity
SISO	$B \log_2(1 + r)$
Diversity ($1 \times N$ or $N \times 1$)	$B \log_2(1 + rN)$
Diversity ($N \times N$)	$B \log_2(1 + rN^2)$
Multiplexing	$NB \log_2(1 + r)$

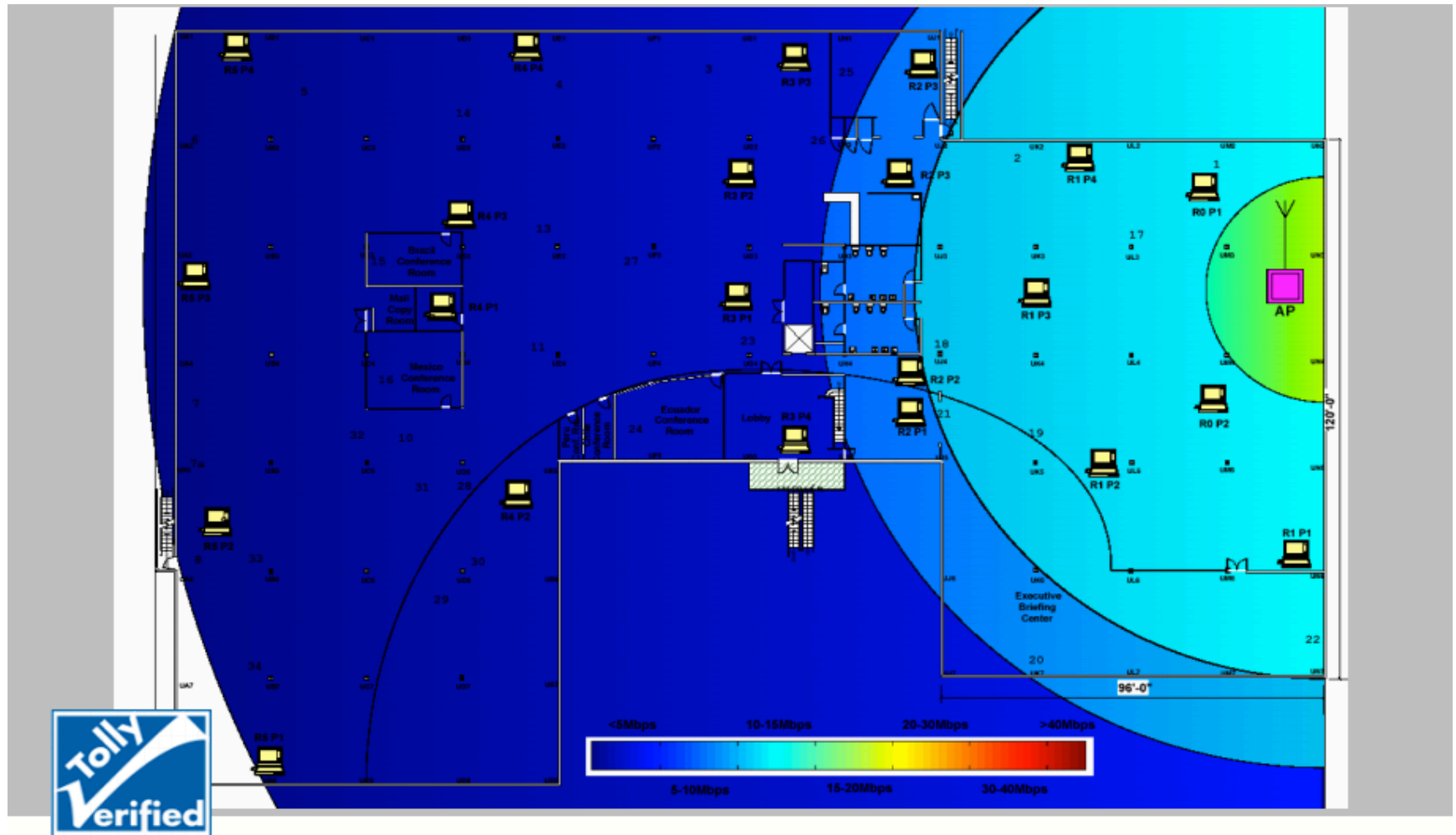
Average capacity of a MIMO Rayleigh fading channel



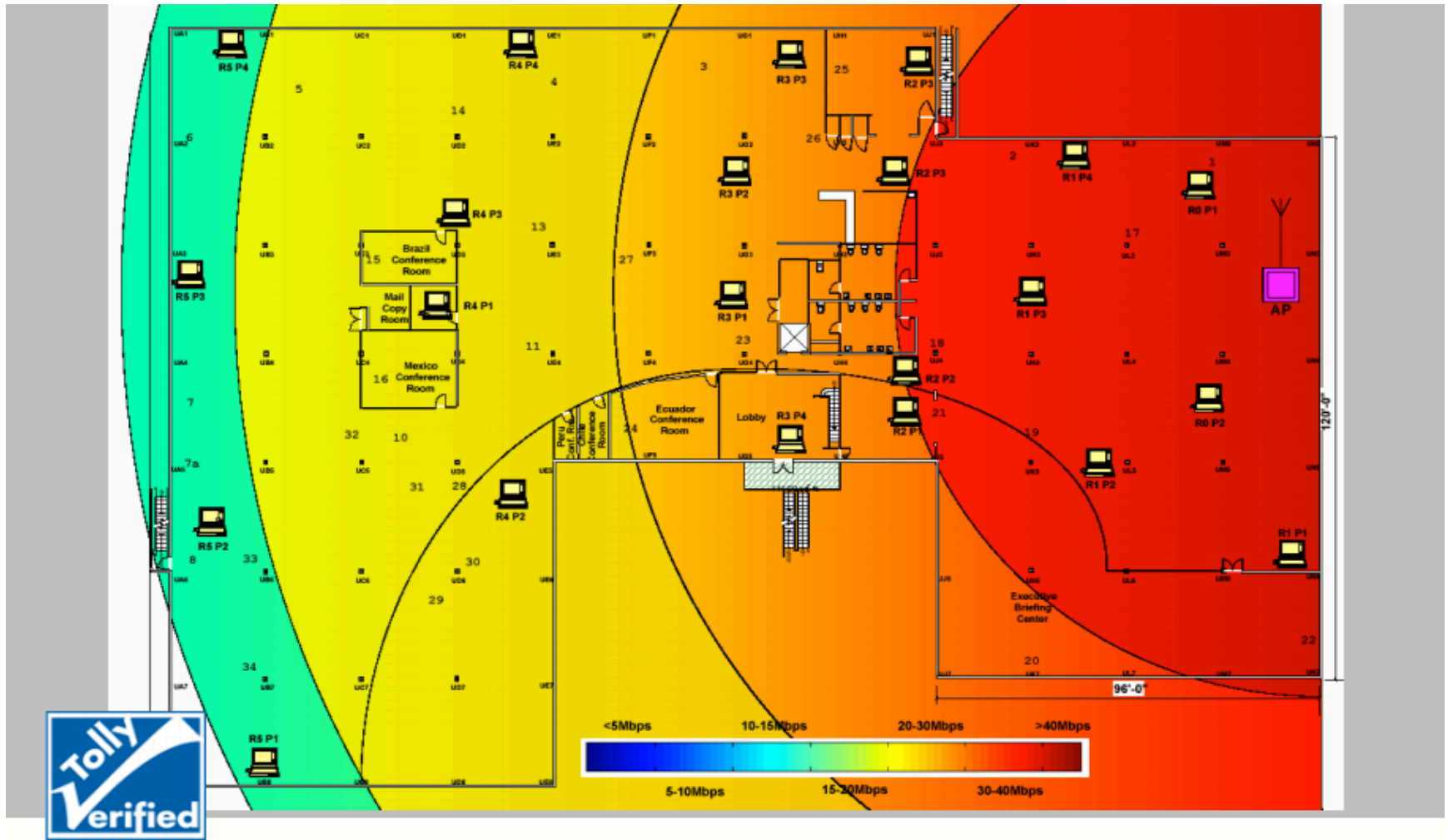
Source: R.A. Carrasco, Space-time Diversity Codes for fading Channel, *Staffordshire University*



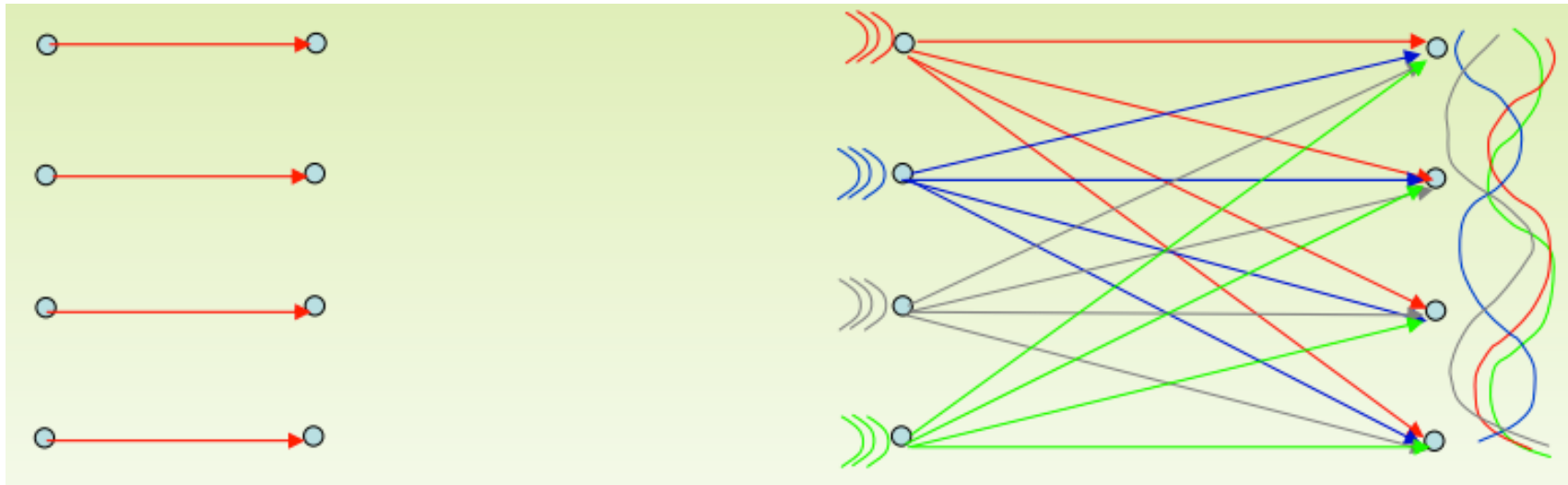
SISO in Office Space



MIMO in Office Space



How To Separate Multiple Streams

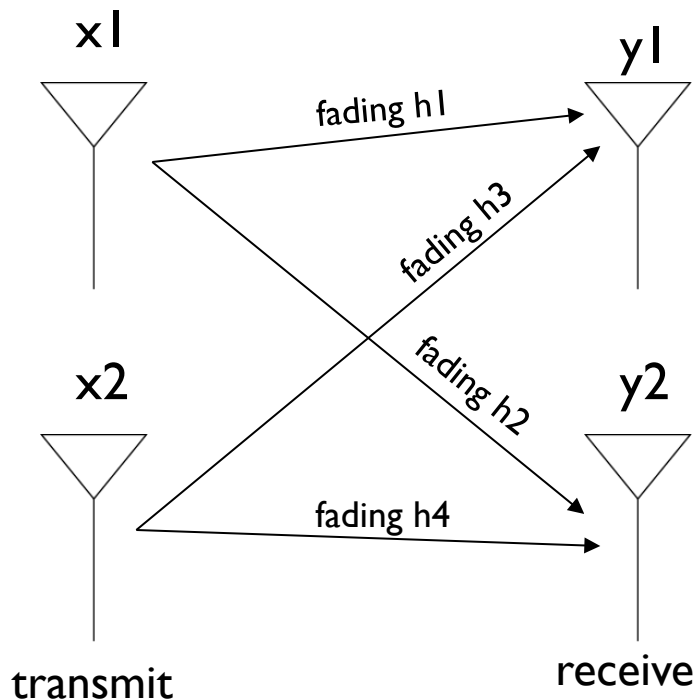


Laser diodes

Wireless Signals

MIMO - An Intuition

- ▶ 2 transmitting and 2 receiving antennas adds a degree of freedom
 - ▶ Assumption: h coefficients of fading are independent, and uncorrelated.



$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} h_1 & h_2 \\ h_3 & h_4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$y_1 = h_1 x_1 + h_2 x_2$$

$$y_2 = h_3 x_1 + h_4 x_2$$

We have a set of linear equations

$$y = Hx + w$$

All 2 degrees of freedom are being utilized in the MIMO case, giving us **Spatial Multiplexing**.

Impact of Channel Model

- ▶ MIMO performance is very sensitive to channel matrix invertibility
- ▶ The following degrades the conditioning of the channel matrix:
 - ▶ Antenna correlation caused by:
 - ▶ small antenna spacing, or
 - ▶ small angle spread
 - ▶ Line of sight component compared with multipath fading component:
 - ▶ multipath fading component, close to i.i.d. random, is well conditioned
 - ▶ Line of sight component is very poorly conditioned.



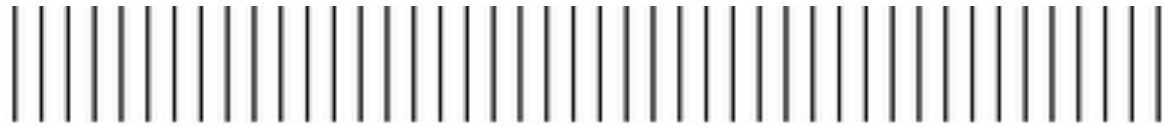
MIMO Discussion

- ▶ Need channel matrix H : use training with known signal
- ▶ MIMO is used in 802.11n in the 2.4 GHz band
 - ▶ Can use two of the non-overlapping “WiFi channels”
 - ▶ Raises lots of compatibility issues
 - ▶ Potential throughputs of 100 of Mbps
- ▶ IEEE 802.11ac can use up to 160MHz channels
- ▶ Not only maximizing throughput between two nodes:
 - ▶ Beamforming
 - ▶ Multi-User MIMO

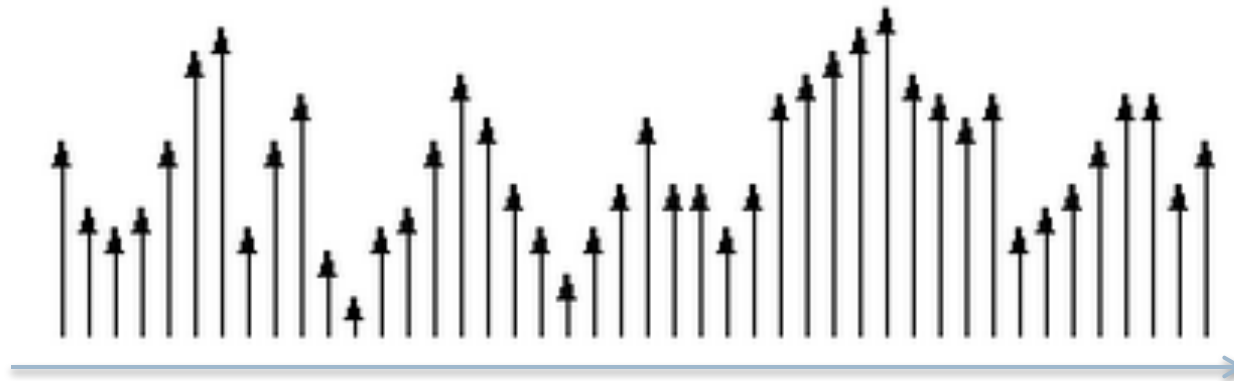


Orthogonal Frequency Division Multiplexing (OFDM)

Frequency Selective Fading



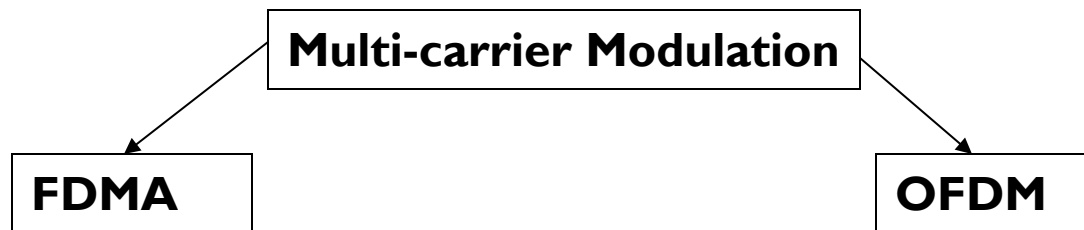
Carrier amplitude before fading



Frequency

Orthogonal Frequency Division Multiplexing (OFDM)

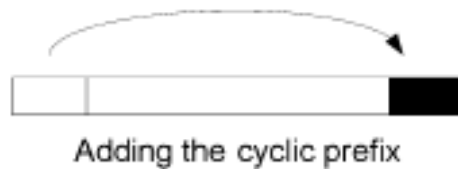
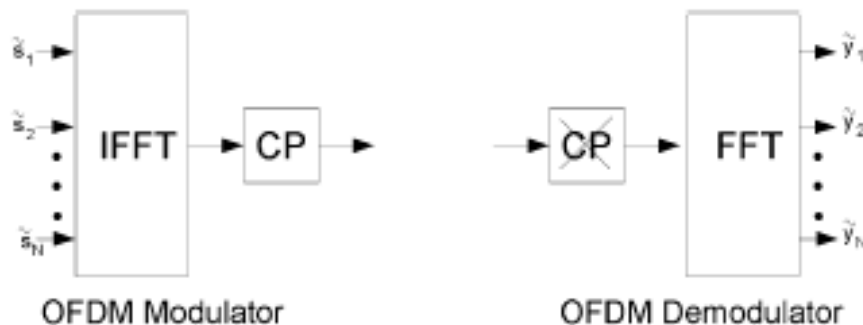
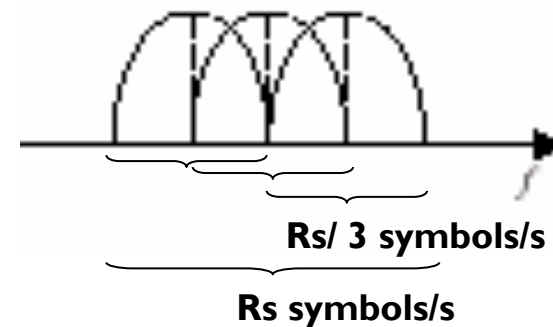
- ▶ Frequency selective fading causes Inter-Symbol Interference:
 - ▶ heavy degradation
- ▶ Most popular solution to compensate for ISI: equalizers
- ▶ Hdata rates (i.e. > 1 Mbps), equalizer complexity grows:
 - ▶ channel changes before you can compensate for it!
- ▶ Alternate solution:
 - ▶ Multi-carrier Modulation (MCM)



OFDM Spectral Efficiency

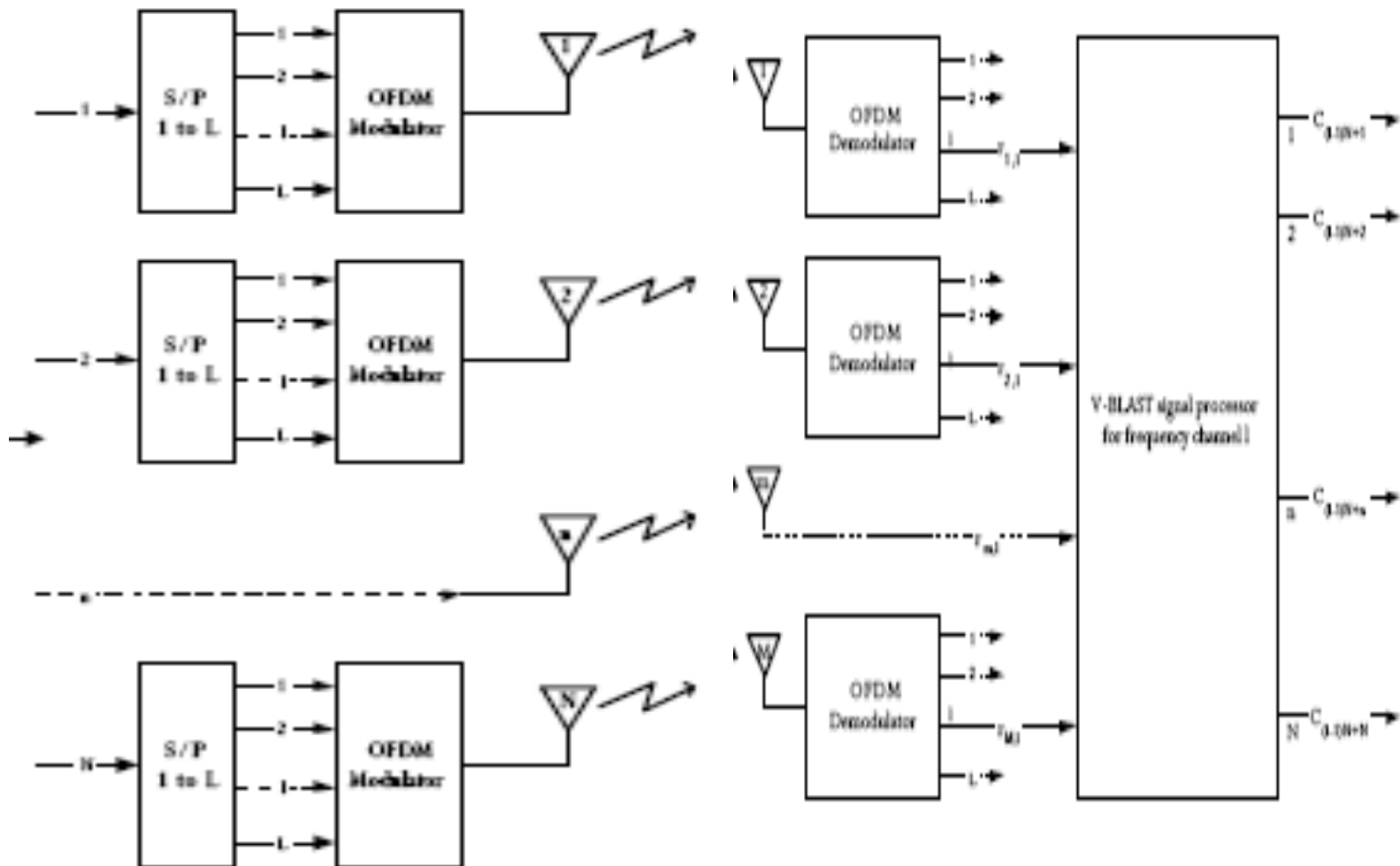
- ▶ The spectral efficiency of an OFDM-(PSK/ASK) system is same as compared to using the (PSK/ASK) system alone
 - ▶ Spec eff = $\log_2 M$ bits/s/Hz
- ▶ However, makes the difference between unusable and good channel

OFDM spectrum



- easy to implement
- Used in IEEE 802.11A, .11G, HiperLAN, IEEE 802.16

MIMO-OFDM



Channel State Information Matrix

► In a MIMO-OFDM system:

- M Transmitting antennas
- N Receiving antennas
- Q subcarriers per channel

$H = M \times N \times Q$ elements (complex values)

$h_{m,n,q}$ is a complex number which represents the phase shifting and fading for a specific sub-channel

