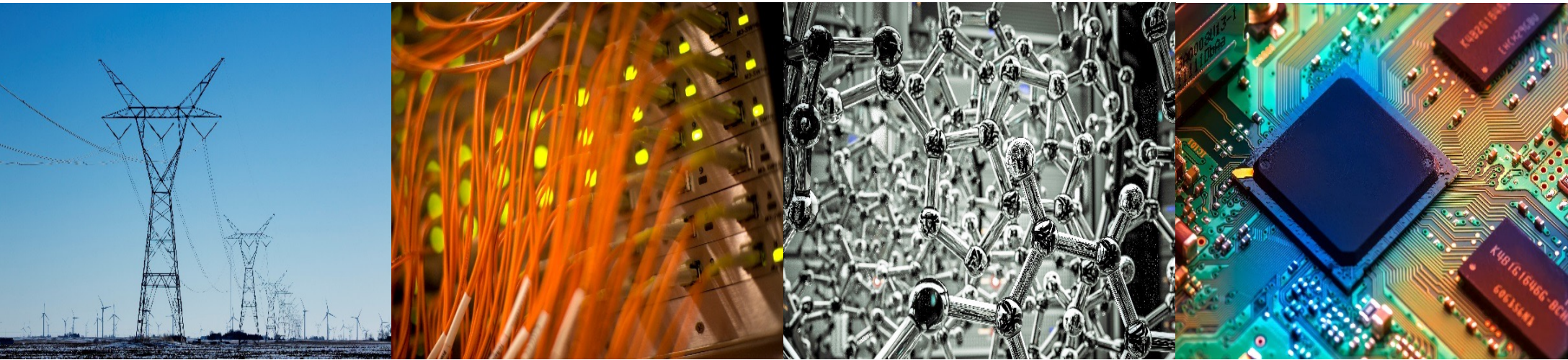


ECE 220 Computer Systems & Programming

Lecture 4 – Programming with Stack



- LC-3 practice is available on PrairieLearn
- Mock quiz should be taken next week @ CBTF
- Quiz1 (LC-3 programming) is available for reservation

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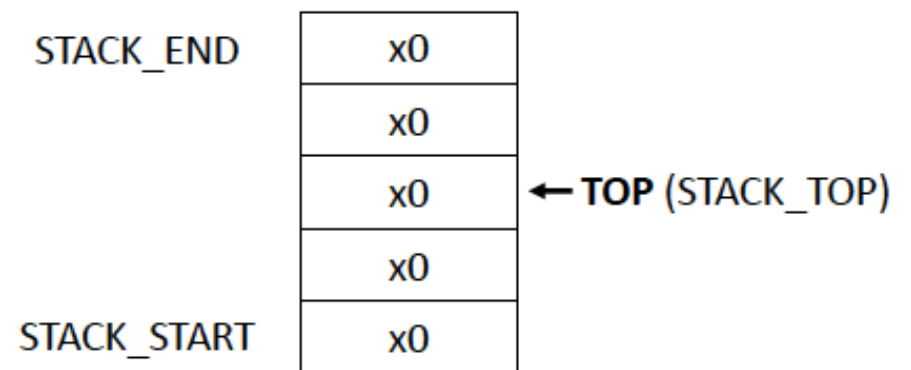
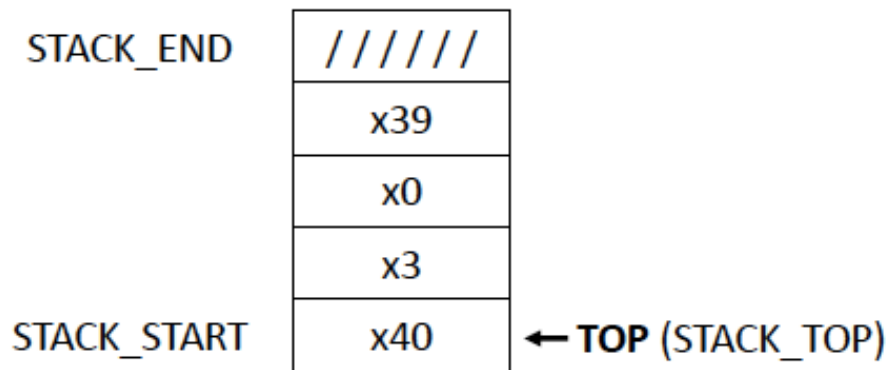
Electrical & Computer Engineering

GRAINGER COLLEGE OF ENGINEERING

Lecture 3 Review: Stack

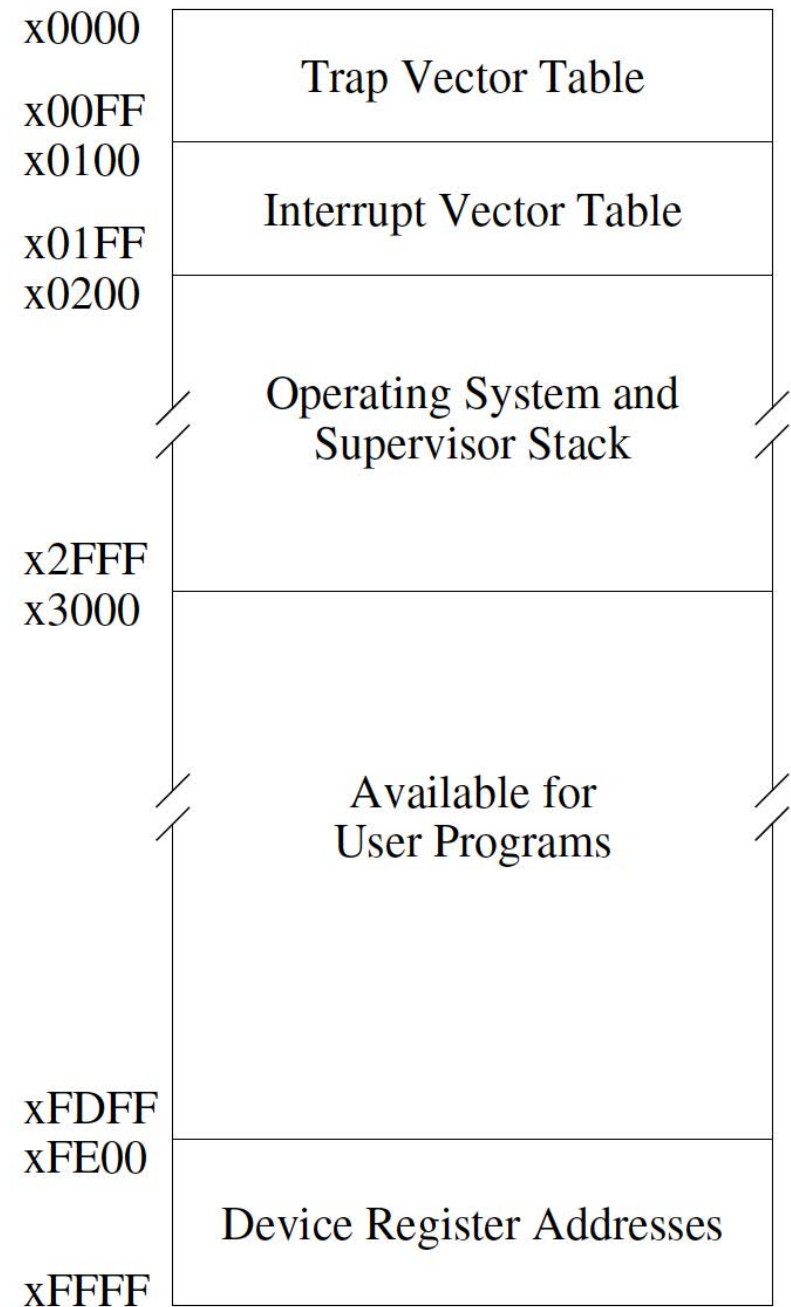
- ❑ Order of Access
- ❑ Two Main Operations
- ❑ Overflow vs. Underflow
- ❑ Hardware vs. Software Implementation
- ❑ Top of Stack Pointer (stack pointer)

➤ In the following two figures, which stack is empty? (Note: STACK_TOP points to the next available spot.)



Run-Time Stack

- Information of an invoked function (subroutine) is stored in a memory template called the **activation record** or **stack frame**.
- Functions' activation records are pushed onto the Run-Time Stack in the order they are invoked.
- ❖ **Supervisor Stack** is different from Run-Time Stack (more details at the end of the semester).



Balanced Parentheses Check Using a Stack

Examples of balanced parentheses:

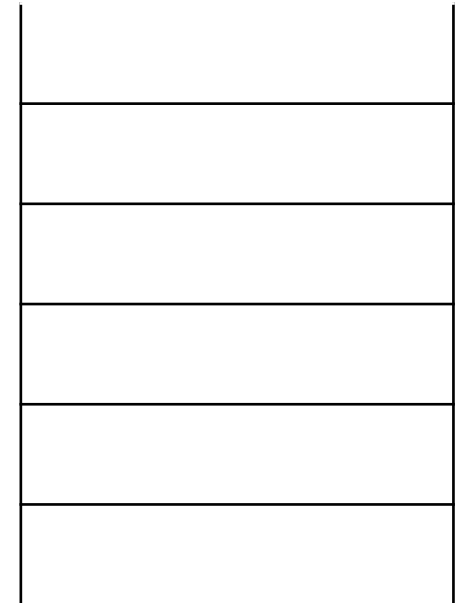
$((() ()))$ $((((()))))$ $((() ((())) ()))$

Examples of unbalanced parentheses:

$(((((((())))))))$ $(()))$ $((() () (()))$

Open parenthesis ' (' – _____ to the Stack

Close parenthesis ') ' – _____ from the stack



Assuming the expression would fit into the stack, unbalanced expression can be found under two situations:

1. At the end of the expression –
2. While entering expression –

Palindrome Check Using a Stack

A word, phrase, number or other sequence of characters which **reads the same forward or backward.**

- Madam
- Kayak
- Was it a car or a cat I saw
- 123456654321

➤ How can we perform a palindrome check using a stack?

Postfix Expression (input is single digit operand)

Infix

$(3+4)-5$

$2^{(8-4)}$

$7+(9-6)/3$

Postfix

$34+5-$

$512+4^*+3-$



Note: '12-' is 1-2 not 2-1

- Are these inputs valid postfix expressions? How would your program know?
 - 46^*-
 - $13+57$

Arithmetic Using a Stack

Compute $(A+B)*(C+D)$ and store the result in R0

; Implementation using registers

```
LD R0, A
LD R1, B
ADD R1, R0, R1
LD R2, C
LD R3, D
ADD R3, R2, R3
JSR MULT
HALT
```

** MULT subroutine*

(Input: R1, R3; Output: R0)

; Implementation using a Stack

; PUSH, POP, ADD & MULT subroutines are given

```
LD R0, A
JSR PUSH
```

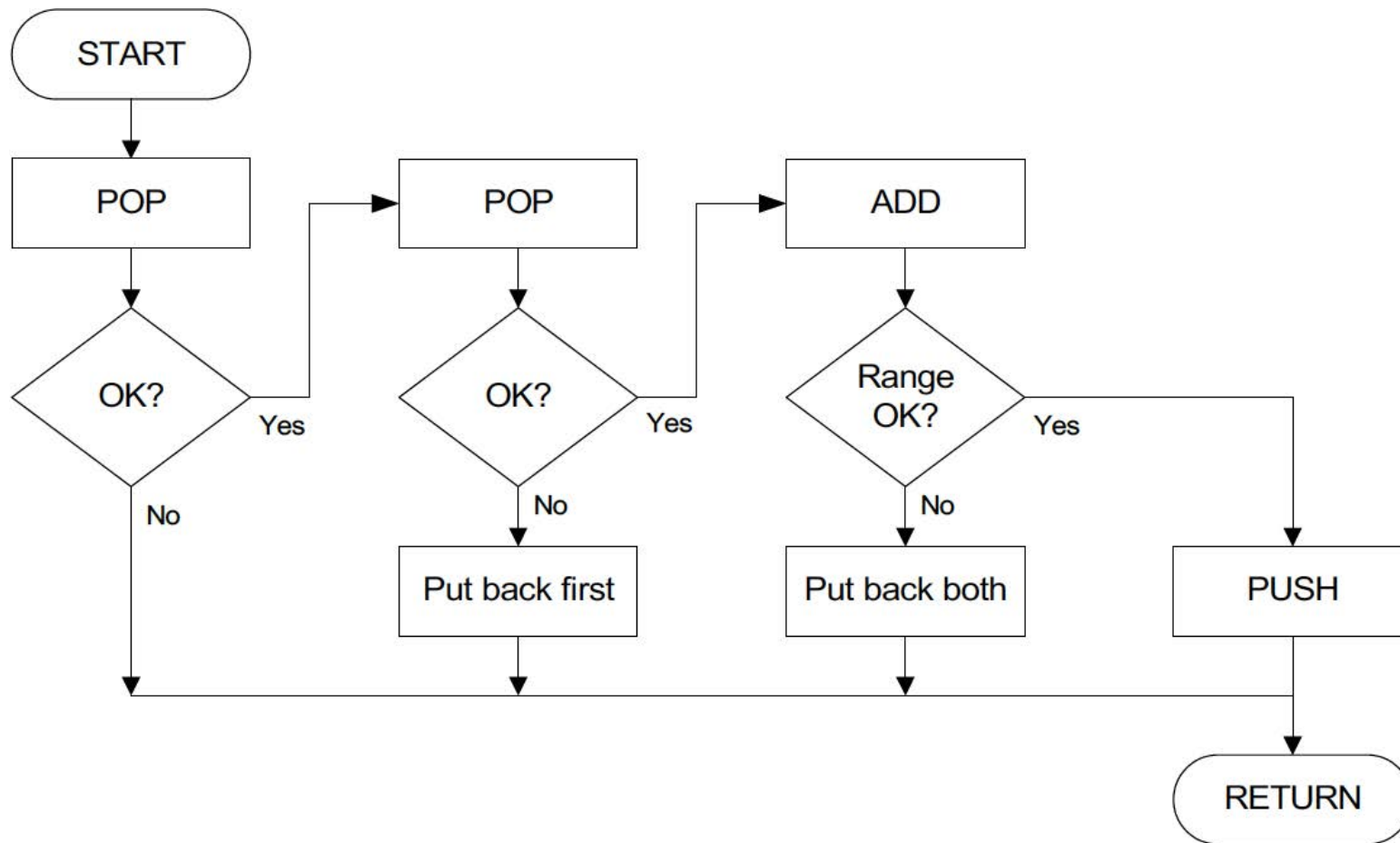
***PUSH: from R0 to stack; POP: from stack to R0**

***ADD: POP 2 numbers, compute and then PUSH result back**

***MULT: POP 2 numbers, compute and then PUSH result back**

Arithmetic Using a Stack

Implement an ADD subroutine that pops two numbers from a stack and perform the add operation (see flowchart below).



Implement ADD Subroutine

- **R6** should be used as stack pointer (points to the **next available spot** on the stack)
- Assume **PUSH**, **POP** and **CHECK_RANGE** subroutines are given & callee-saved

; PUSH

; Input: R0 (value to be stored on stack)

; Output: R5 (0 - success, 1 - failure)

; POP

; Output: R0 (value to be loaded from stack)

; Output: R5 (0 - success, 1 - failure)

; CHECK_RANGE: return 0 if value is within -100 to 100 decimal,

; otherwise return 1

; Input: R0 (value to be checked)

; Output: R5 (0 - success, 1 - failure)

- What do we need to consider when implementing the ADD subroutine?

```
; ADD subroutine - pop two numbers from stack,  
; perform '+' operation and then push result back to the stack  
; Output: R5 (0 - success, 1 - failure)
```

```
; save registers
```

```
; Initialize R5
```

```
; first pop
```

```
; check return value of first pop, go to EXIT if failed (R5 = 1)
```

```
; second pop
```

```
; check result of second pop, go to RESTORE_1 if it failed
```

```
; add two numbers
```

```
; check range of sum, go to RESTORE_2 if it failed
```

```
; everything is good, push sum to stack
```

```
RESTORE_1  
; put back first number
```

```
RESTORE_2  
; put back both numbers
```

```
EXIT  
; restore registers
```

```
RET  
STACK_START      .FILL x4000  
STACK_END        .FILL x3FF0  
STACK_TOP        .FILL x4000
```