
ECE 333 – Green Electric Energy

Recitation: Economics Applications

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OUTLINE

- ❑ Time value of money
- ❑ Net present value
- ❑ Internal rate of return
- ❑ Inflation impacts
- ❑ Total *PV* system cost estimation
- ❑ *LCOE* determination of a *PV* system
- ❑ The *PV* system tax incentive impacts on the *LCOE*
- ❑ The *PV* system tax benefits and rebate program impacts

ENERGY ECONOMICS CONCEPTS

- ❑ **The economic evaluation of a renewable energy resource requires a meaningful quantification of the cost elements**
 - **fixed costs**
 - **variable costs**
- ❑ **We use engineering economics notions for this purpose since they provide the means to compare on a consistent basis**
 - **two different projects; or,**
 - **the costs with and without a given project**

TIME VALUE OF MONEY

- ❑ Basic underlying notion: a dollar today is not the same as a dollar in a year
- ❑ We represent the time value of money by the standard approach of *discounted cash flows*
- ❑ The notation is
 - $P = \textit{principal}$
 - $i = \textit{interest value}$
- ❑ We use the convention that every payment occurs at the *end of a period*

SIMPLE EXAMPLE

loan P for 1 year

repay $P + iP = P(1+i)$ at the end of 1 year

year 0 P

year 1 $P(1+i)$

loan P for n years

year 0 P

year 1 $(1+i)P$ repay/reborrow

year 2 $(1+i)^2 P$ repay/reborrow

year 3 $(1+i)^3 P$ repay/reborrow

⋮

⋮

⋮

year n $(1+i)^n P$ repay

COMPOUND INTEREST

<i>end of period</i>	<i>amount owed</i>	<i>interest for next period</i>	<i>amount owed at the beginning of the next period</i>
0	P	Pi	$P + Pi = P(1+i)$
1	$P(1+i)$	$P(1+i)i$	$P(1+i) + P(1+i)i = P(1+i)^2$
2	$P(1+i)^2$	$P(1+i)^2 i$	$P(1+i)^2 + P(1+i)^2 i = P(1+i)^3$
3	$P(1+i)^3$	$P(1+i)^3 i$	$P(1+i)^3 + P(1+i)^3 i = P(1+i)^4$
⋮	⋮		
$n-1$	$P(1+i)^{n-1}$	$P(1+i)^{n-1} i$	$P(1+i)^{n-1} + P(1+i)^{n-1} i = P(1+i)^n$
n	$P(1+i)^n$		

the value in the last column at the *e.o.p.* ($k-1$) provides the amount in the first column for the *period* k

TERMINOLOGY

$$F = P \underbrace{(1 + i)^n}_{\text{compound interest}}$$

*lump sum repayment at the
end of n periods*

need not be integer-valued

TERMINOLOGY

□ We call $(1 + i)^n$ the single payment compound amount factor

□ We define

$$\beta \triangleq (1 + i)^{-1}$$

□ Then,

$$\beta^n = (1 + i)^{-n}$$

is the single payment present worth factor

□ F denotes the *future worth*; P denotes the *present worth or present value* at interest i of a future sum F

CASH FLOWS

- A *cash-flow* is a transfer of an amount A_t from one entity to another at the *e.o.p.* t
- We consider the cash-flow set $\{A_0, A_1, A_2, \dots, A_n\}$
- This set corresponds to the set of the transfers in the periods $\{0, 1, 2, \dots, n\}$

CASH FLOWS

- We associate the transfer A_t at the *e.o.p.* t ,
 $t = 0, 1, 2, \dots, n$
- The convention for cash flows is
 - + *inflow*
 - *outflow*
- Each cash flow requires the specification of:
 - amount;
 - time; and,
 - sign

EXAMPLE

□ Consider an investment that returns

\$ 1,000 at the *e.o.y.* 1

\$ 2,000 at the *e.o.y.* 2

$i = 10\%$

rate at which
money can be
freely lent or
borrowed



□ We evaluate P

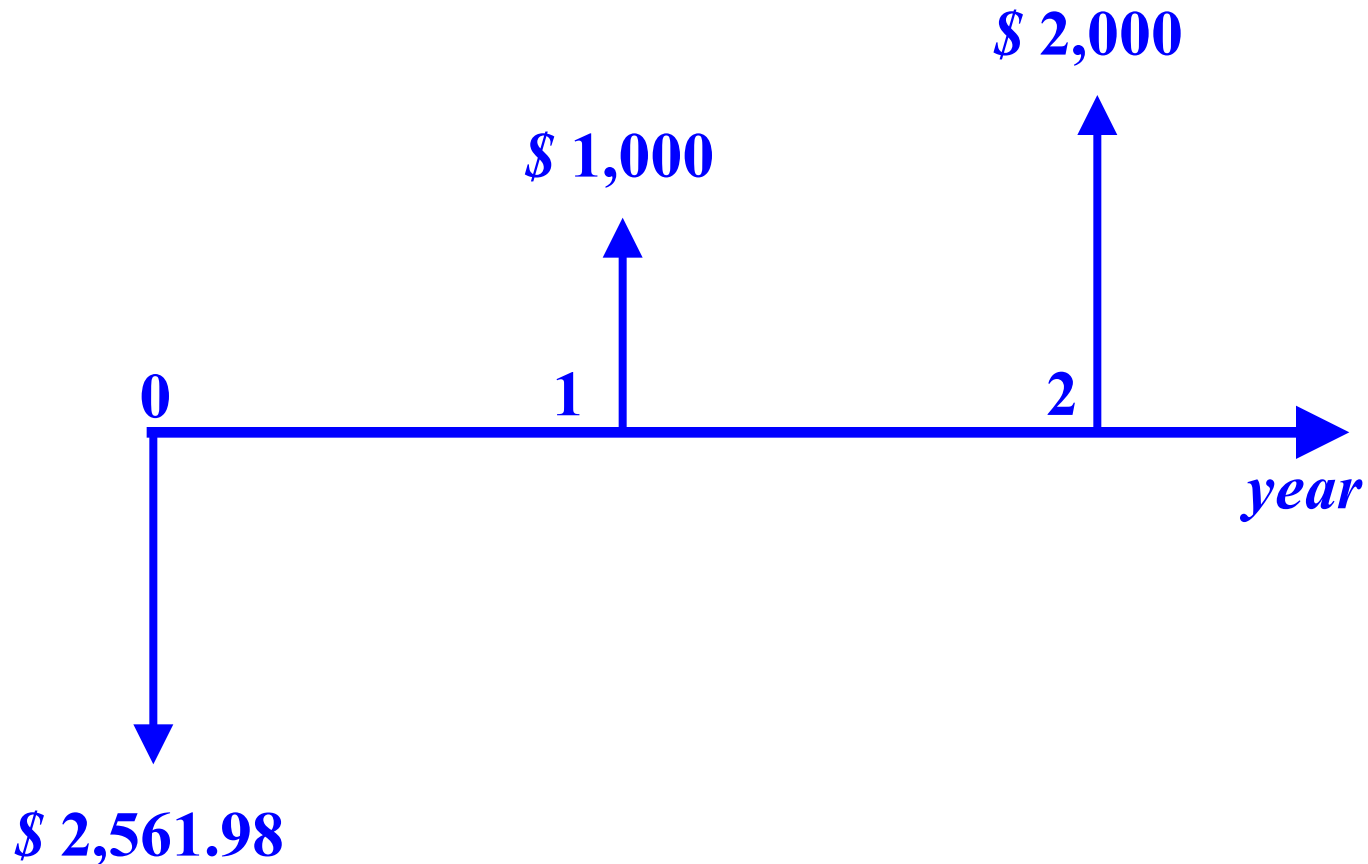
$$P = \$ 1,000 \underbrace{(1 + .1)^{-1}}_{\beta} + \$ 2,000 \underbrace{(1 + .1)^{-2}}_{\beta^2}$$

$$= \$ 909.9 + \$ 1,652.09$$

$$= \$ 2,561.98$$

EXAMPLE

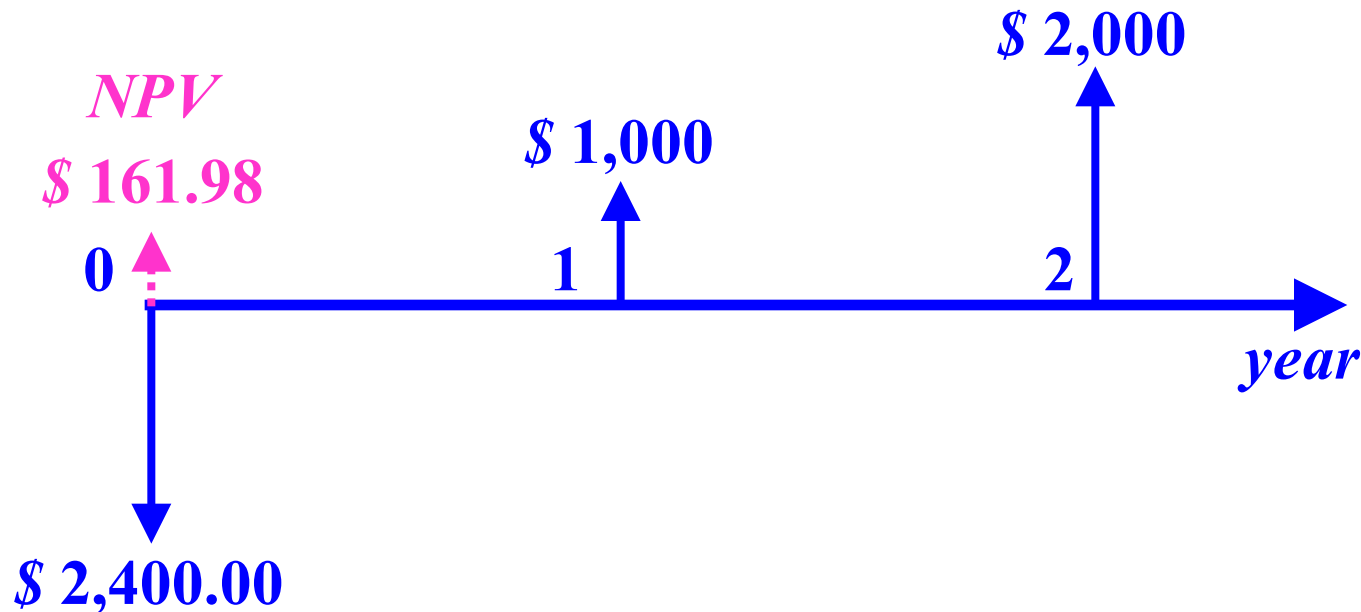
- We review this example with a *cash – flow diagram*



NET PRESENT VALUE

- Next, suppose that this investment requires \$ 2,400 now and so at 10 % we say that the investment has a *net present value* or

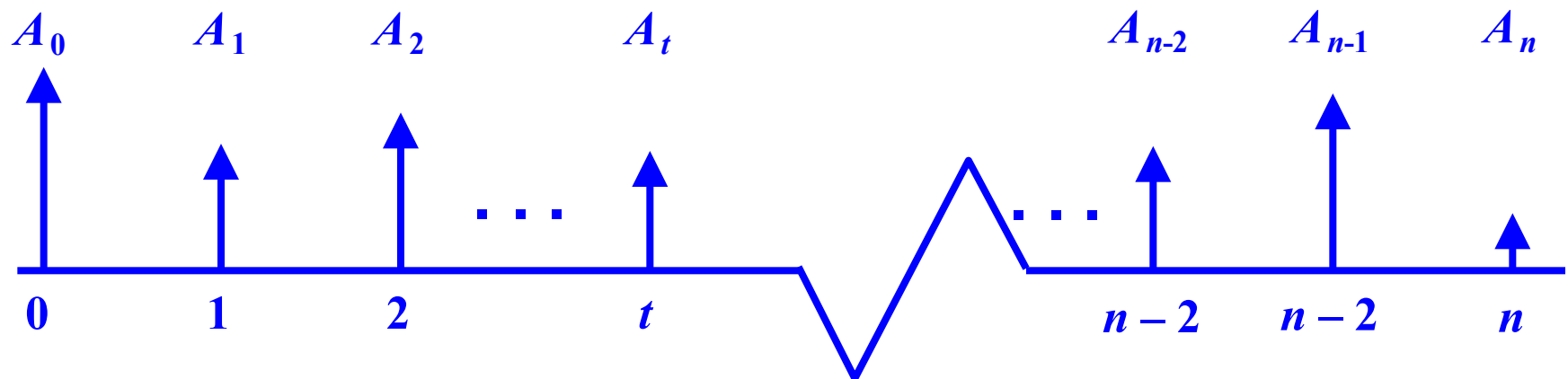
$$NPV = \$ 2,561.98 - \$ 2,400 = \$ 161.98$$



CASH FLOWS : FUTURE WORTH

- Given a cash-flow set $\{A_0, A_1, A_2, \dots, A_n\}$ we define the future worth F_n of the cash flow set at the *e.o.y.* n as

$$F_n = \sum_{t=0}^n A_t (1 + i)^{n-t}$$



CASH FLOWS : FUTURE WORTH

- Note that each cash flow A_t in the $(n + 1)$ period set contributes differently to F_n :

$$\begin{array}{rcl} A_0 & \rightarrow & A_0 (1+i)^n \\ A_1 & \rightarrow & A_1 (1+i)^{n-1} \\ A_2 & \rightarrow & A_2 (1+i)^{n-2} \\ \vdots & & \vdots \\ A_t & \rightarrow & A_t (1+i)^{n-t} \\ \vdots & & \vdots \\ A_n & \rightarrow & A_n \end{array}$$

CASH FLOWS : PRESENT WORTH

- We define the present worth P of the cash – flow set as

$$P = \sum_{t=0}^n A_t \beta^t = \sum_{t=0}^n A_t (1+i)^{-t}$$

- Note that

$$\begin{aligned} P &= \sum_{t=0}^n A_t (1+i)^{-t} \\ &= \sum_{t=0}^n A_t (1+i)^{-t} \underbrace{(1+i)^n (1+i)^{-n}}_1 \end{aligned}$$

CASH FLOWS

$$= \underbrace{(1+i)^{-n}}_{\beta^n} \underbrace{\sum_{t=0}^n A_t (1+i)^{n-t}}_{F_n}$$

$$= \beta^n F_n$$

or, equivalently,

$$F_n = (1+i)^n P$$

UNIFORM CASH-FLOW SET

□ Consider the cash-flow set $\{A_1, A_2, \dots, A_n\}$ with

$$A_t = A \quad t = 1, 2, \dots, n$$

□ Such a set is called an *equal payment cash flow set*

□ We compute the present worth at $t = 0$

$$P = \sum_{t=1}^n A_t \beta^t = A \sum_{t=1}^n \beta^t = A\beta [1 + \beta + \beta^2 + \dots + \beta^{n-1}]$$

UNIFORM CASH-FLOW SET

□ Now, for $0 < \beta < 1$, we have the identity

$$\sum_{j=0}^{\infty} \beta^j = \frac{1}{1 - \beta}$$

□ It follows that

$$\begin{aligned} 1 + \beta + \dots + \beta^{n-1} &= \sum_{j=0}^{\infty} \beta^j - \beta^n \left[\overbrace{1 + \beta + \beta^2 + \dots + \beta^{n-1} + \dots}^{\sum_{j=0}^{\infty} \beta^j} \right] \\ &= (1 - \beta^n) \sum_{j=0}^{\infty} \beta^j \end{aligned}$$

UNIFORM CASH-FLOW SET

$$= \frac{1 - \beta^n}{1 - \beta}$$

□ Therefore

$$P = A\beta \frac{1 - \beta^n}{1 - \beta}$$

□ But

$$\beta = (1 + d)^{-1}$$

and so

UNIFORM CASH-FLOW SET

$$1 - \beta = 1 - \frac{1}{1+d} = \frac{d}{1+d} = \beta d$$

□ We write

$$P = A \frac{1 - \beta^n}{d}$$

and we call $\frac{1 - \beta^n}{d}$ the *equal payment series*

present worth factor

EQUIVALENCE

□ We consider two cash – flow sets

$$\{A_t^a: t = 0, 1, 2, \dots, n\} \quad \text{and} \quad \{A_t^b: t = 0, 1, 2, \dots, n\}$$

under a given discount rate d

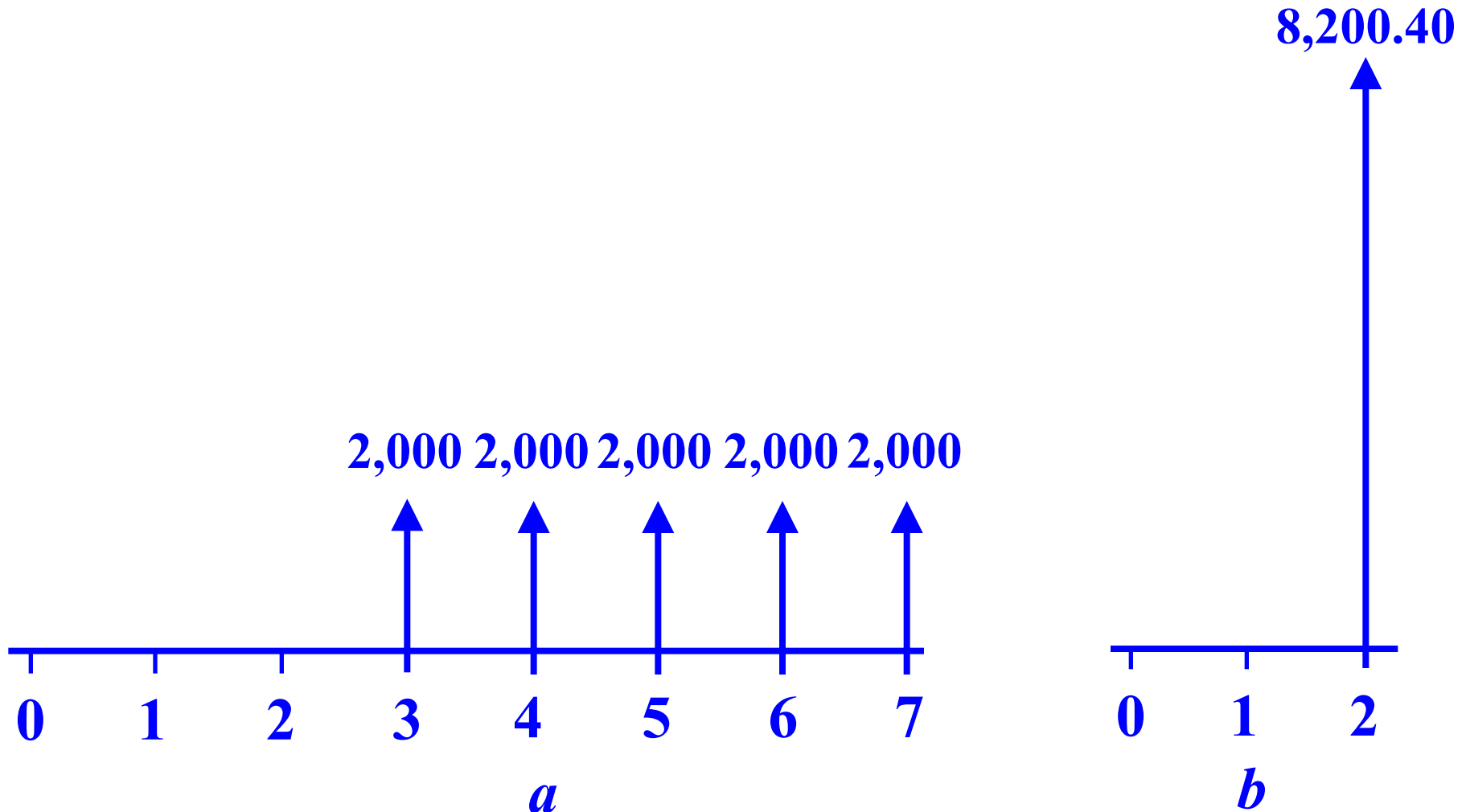
□ We say $\{A_t^a\}$ and $\{A_t^b\}$ are *equivalent* cash – flow

sets if and only if

$$F_m \text{ of } \{A_t^a\} = F_m \text{ of } \{A_t^b\} \text{ for each value of } m$$

EQUIVALENCE EXAMPLE

□ Consider the two cash-flow sets under $d = 7\%$



EQUIVALENCE

□ We compute

$$P^a = 2,000 \sum_{t=3}^7 \beta^t = 7,162.55$$

and

$$P^b = 8,200.40 \quad \beta^2 = 7,162.55$$

□ Therefore, $\{A_t^a\}$ and $\{A_t^b\}$ are equivalent cash

flow sets under $d = 7\%$

DISCOUNT RATE

- The interest rate i is, typically, referred to as the *discount rate* and is denoted by d
- In converting the future amount F to the present worth P we can view the *discount rate* as the interest rate that may be earned from the best investment alternative
- A postulated savings of \$10,000 in a project in 5 years is worth at present

$$P = F_5 \beta^5 = 10,000(1 + d)^{-5}$$

DISCOUNT RATE

□ For $d = 0.1$

$$P = \$ 6,201,$$

while for $d = 0.2$

$$P = \$ 4,019$$

□ In general, for a specified future worth, the lower the discount factor, the higher the present worth is

INTERNAL RATE OF RETURN

- We consider a cash–flow set

$$\{A_t = A : t = 0, 1, 2, \dots\}$$

- The value of d for which

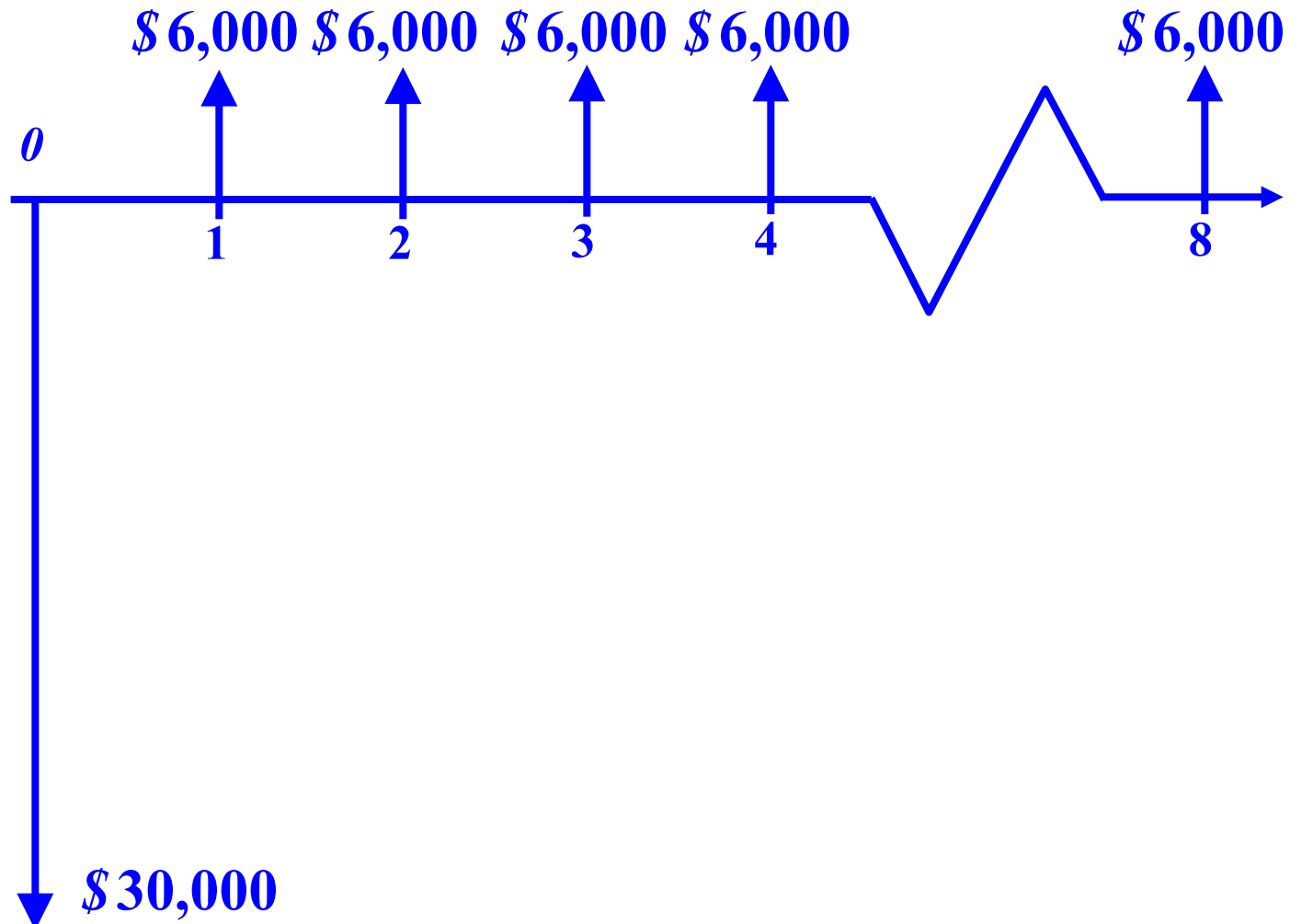
$$P - \sum_{t=0}^n A_t \beta^t = 0$$

is called the *internal rate of return (IRR)*

- The *IRR* is a measure of how fast we recover an investment, or stated differently, the speed with or rate at which the returns recover an investment

EXAMPLE: INTERNAL RATE OF RETURN

□ Consider the following cash–flow set



INTERNAL RATE OF RETURN

- The present value

$$P = -30,000 + 6,000 \frac{1 - \beta^8}{d} = 0$$

has the solution

$$d \approx 12\%$$

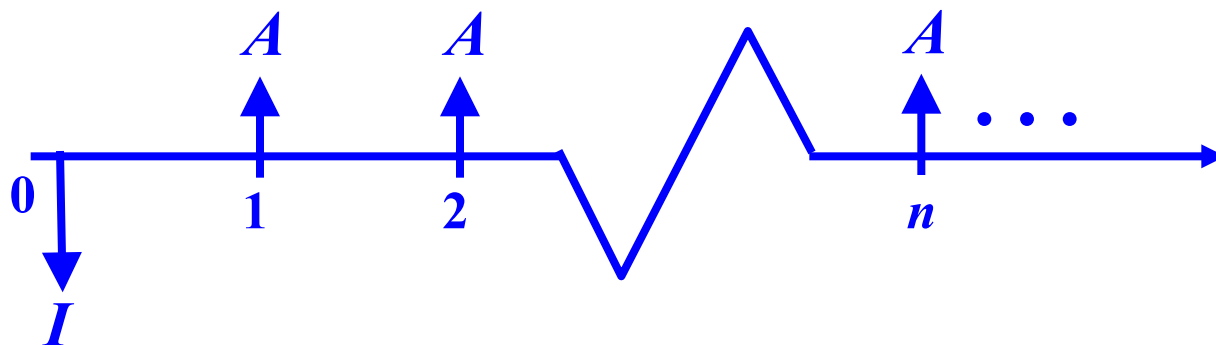
- The interpretation is that under a 12 % *discount rate*,

the *present value* of the cash – flow set is 0 and so

$d \approx 12\%$ is the *IRR* for the given cash – flow set

INTERNAL RATE OF RETURN

- Consider an infinite horizon simple investment



- Therefore

$$d = \frac{A}{I}$$

ratio of annual return
to initial investment

INTERNAL RATE OF RETURN

□ Consider

$$I = \$ 1,000$$

$$A = \$ 200$$

and

$$d = 20 \%$$

we interpret that the returns capture 20 % of the investment each year or equivalently that we have a *simple payback period of 5 years*

IRR TABLE

Life (years)	9%	11%	13%	15%	17%	19%	21%	23%	25%	27%	29%	31%	33%	35%	37%	39%
1	0.92	0.90	0.88	0.87	0.85	0.84	0.83	0.81	0.80	0.79	0.78	0.76	0.75	0.74	0.73	0.72
2	1.76	1.71	1.67	1.63	1.59	1.55	1.51	1.47	1.44	1.41	1.38	1.35	1.32	1.29	1.26	1.24
3	2.53	2.44	2.36	2.28	2.21	2.14	2.07	2.01	1.95	1.90	1.84	1.79	1.74	1.70	1.65	1.61
4	3.24	3.10	2.97	2.85	2.74	2.64	2.54	2.45	2.36	2.28	2.20	2.13	2.06	2.00	1.94	1.88
5	3.89	3.70	3.52	3.35	3.20	3.06	2.93	2.80	2.69	2.58	2.48	2.39	2.30	2.22	2.14	2.07
6	4.49	4.23	4.00	3.78	3.59	3.41	3.24	3.09	2.95	2.82	2.70	2.59	2.48	2.39	2.29	2.21
7	5.03	4.71	4.42	4.16	3.92	3.71	3.51	3.33	3.16	3.01	2.87	2.74	2.62	2.51	2.40	2.31
8	5.53	5.15	4.80	4.49	4.21	3.95	3.73	3.52	3.33	3.16	3.00	2.85	2.72	2.60	2.48	2.38
9	6.00	5.54	5.13	4.77	4.45	4.16	3.91	3.67	3.46	3.27	3.10	2.94	2.80	2.67	2.54	2.43
10	6.42	5.89	5.43	5.02	4.66	4.34	4.05	3.80	3.57	3.36	3.18	3.01	2.86	2.72	2.59	2.47
15	8.06	7.19	6.46	5.85	5.32	4.88	4.49	4.15	3.86	3.60	3.37	3.17	2.99	2.83	2.68	2.55
20	9.13	7.96	7.02	6.26	5.63	5.10	4.66	4.28	3.95	3.67	3.43	3.21	3.02	2.85	2.70	2.56
25	9.82	8.42	7.33	6.46	5.77	5.20	4.72	4.32	3.98	3.69	3.44	3.22	3.03	2.86	2.70	2.56
30	10.27	8.69	7.50	6.57	5.83	5.23	4.75	4.34	4.00	3.70	3.45	3.22	3.03	2.86	2.70	2.56

EXAMPLE: *IRR* FOR *HVAC* RETROFIT WITH INFLATION

- ❑ An energy efficiency retrofit of a commercial site reduces the *HVAC* load consumption to 0.8 *GWh* from 2.3 *GWh* and the peak demand by 0.15 *MW*
- ❑ Electricity costs are 60 $\$/MWh$ and demand charges are 7,000 $\$/(MW\text{-}mo)$ and these prices escalate at an annual rate of $j = 5\%$
- ❑ The retrofit requires a \$ 500,000 investment today and is planned to have a 15 – *year* lifetime

EXAMPLE: *IRR* FOR *HVAC* RETROFIT WITH INFLATION

□ We evaluate the *IRR* for this project

□ The annual savings are

$$\text{energy} : (2.3 - 0.8) \text{GWh} (60 \$ / \text{MWh}) = \$ 90,000$$

$$\text{demand} : (.15 \text{MW}) (7000 \$ / (\text{MWh} - \text{mo})) 12 \text{mo} = \$ 12,600$$

$$\text{total} : 90,000 + 12,600 = \$ 102,600$$

□ The *IRR* is the value of d' that results in

EXAMPLE: *IRR* FOR *HVAC* RETROFIT WITH INFLATION

$$0 = -500,000 + 102,600 \frac{1 - (\beta')^{15}}{d'}$$

□ The table look up produces the d' of 19 % and

with inflation factored in, we have

$$(1 + d) = (1 + j)(1 + d')$$

$$= (1.05)(1.19)$$

$$= 1.25$$

resulting in a combined *IRR* of 25 %

INFLATION IMPACTS

- ❑ Inflation is a general *increase* in the level of prices in an economy; equivalently, we may view inflation as a general *decline* in the value of the purchasing power of money
- ❑ Inflation is measured using prices: different products may have distinct escalation rates
- ❑ Typically, indices such as the *CPI* – the *consumer price index* – use a market basket of goods and

INFLATION IMPACTS

services as a proxy for the entire *US* economy

- reference basis is the year 1967 with the price of \$ 100 for the basket $\longrightarrow L_0$
- in the year 1990, the same basket cost \$ 374 $\longrightarrow L_{21}$
- the average inflation rate j is estimated from

$$(1 + j)^{23} = \frac{374}{100} = 3.74$$

and so

$$j = (3.74)^{\frac{1}{23}} - 1 \approx 0.059$$

INFLATION RATE

- The inflation rate contributes to the *overall market interest rate* i , sometimes called the *combined interest rate*
- We write, using d for i

$$(1 + d) = (1 + j) (1 + d')$$

combined interest rate *inflation rate* *real interest rate*

INFLATION

□ We obtain the following identities

$$d' = \frac{d - j}{1 + j}$$

and

$$j = \frac{d - d'}{1 + d'}$$

CASH – FLOWS INCORPORATING INFLATION

- We express the cash – flow in the set

$\{A_t: t = 0, 1, 2, \dots, n\}$ in then current dollars

- The following is synonymous terminology

current \equiv *then current* \equiv *inflated* \equiv *after inflation*

- An *indexed* or *constant – worth* cash – flow is one

that does **not explicitly** take inflation into

CASH – FLOWS INCORPORATING INFLATION

account, i.e., whatever amount in current inflated dollars will buy the same goods and services as in the reference year, typically, the year 0

□ The following terms are synonymous

constant \equiv *indexed* \equiv *inflation free* \equiv *before inflation*

and we use them interchangeably

CASH – FLOWS INCORPORATING INFLATION

- We define the set of constant currency flows

$$\{W_t : t = 0, 1, 2, \dots, n\}$$

corresponding to the set

$$\{A_t : t = 0, 1, 2, \dots, n\}$$

with each element A_t given in period t currency

CASH – FLOWS INCORPORATING INFLATION

□ We use the relationship

$$A_t = W_t (1 + j)^t$$

or equivalently

$$W_t = A_t (1 + j)^{-t}$$

with W_t expressed in reference year 0 (today's)

dollars

CASH – FLOWS INCORPORATING INFLATION

□ We have

$$\begin{aligned} P &= \sum_{t=0}^n A_t \beta^t \\ &= \sum_{t=0}^n W_t (i+j)^t (i+d)^{-t} \\ &= \sum_{t=0}^n W_t (i+j)^t (i+j)^{-t} (i+d')^{-t} \\ &= \sum_{t=0}^n W_t (i+d')^{-t} \end{aligned}$$

CASH – FLOWS INCORPORATING INFLATION

□ Therefore, the *real interest rate* d' is used to

discount the indexed cash – flows

□ In summary,

we discount current *dollar* cash – flow at d

we discount indexed *dollar* cash – flow at d'

CASH – FLOWS INCORPORATING INFLATION

- Whenever inflation is taken into account, it is convenient to carry out the analysis in *present worth* rather than future worth or on a *cash – flow basis*
- Under inflation ($j > 0$), it follows that a uniform set of cash flows $\{A_t = A: t = 1, 2, \dots, n\}$ implies a real decline in the cash flows

EXAMPLE: INFLATION CALCULATIONS

- Consider an annual inflation rate of $j = 4\%$ and the cost for a piece of equipment is assumed constant for the next 3 years in terms of today's \$

$$W_0 = W_1 = W_2 = W_3 = \$1,000$$

- The corresponding cash flows in current \$ are

$$A_0 = \$1,000$$

$$A_1 = 1,000(1 + .04) = \$1,040$$

EXAMPLE: INFLATION CALCULATIONS

$$A_2 = 1,000(1 + .04)^2 = \$ 1,081.60$$

$$A_3 = 1,000(1 + .04)^3 = \$ 1,124.86$$

□ The interpretation of A_3 is that under 4 % inflation,

$\$ 1,125$ in 3 years will have the same value as

$\$ 1,000$ today; it must **not** be confused with the

present worth calculation

MOTOR ASSESSMENT EXAMPLE

- For the motor *a* or *b* purchase example, we consider the escalation of electricity at an annual rate of $j = 5\%$
- We compute the *NPV* taking into account the inflation (price escalation of 5%) and $d = 10\%$
- Then,

$$d' = \frac{d - j}{1 + j} = \frac{.10 - .05}{1 + .05} = \frac{.05}{1.05} = 0.04762$$

MOTOR ASSESSMENT

- The savings of \$ 192 per year are in constant dollars

$$P_{savings} = \sum_{t=1}^{20} W_t (1 + d')^{-t} \leftarrow 0.04762$$

and so

$$P_{savings} = \$2,442$$

- The total savings are

$$P = -500 + P_{savings} = \$1,942$$

which are larger than those of \$ 1,135 without electricity price escalation

ANNUALIZED INVESTMENT

- ❑ A capital investment, such as a renewable energy project, requires funds, either borrowed from a bank, or obtained from investors, or taken from the owner's own accounts**
- ❑ Conceptually, we may view the investment as a loan that converts the investment costs into a series of equal annual payments to pay back the loan with the interest**

ANNUALIZED INVESTMENT

- For this purpose, we use a uniform cash – flow set and use the relation

$$P = A \underbrace{\frac{1 - \beta^n}{d}}$$

The diagram shows the equation $P = A \frac{1 - \beta^n}{d}$ with three arrows pointing from labels below to variables in the equation. The first arrow points from 'present worth' to P . The second arrow points from 'equal payment term' to A . The third arrow points from 'equal payment series present worth factor' to the fraction $\frac{1 - \beta^n}{d}$.

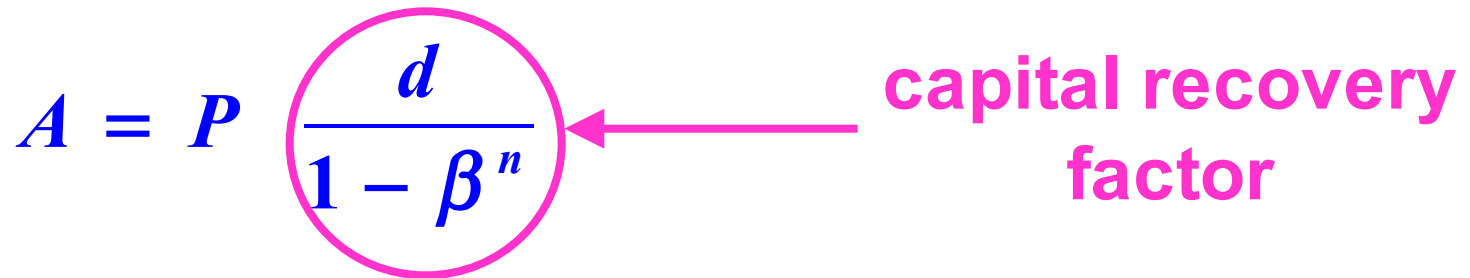
present worth equal payment term equal payment series present worth factor

ANNUALIZED INVESTMENT

- Therefore, the equal payment is given by

$$A = P \left(\frac{d}{1 - \beta^n} \right)$$

capital recovery factor



- The capital recovery factor measures the speed

with which the initial investment is repaid

EXAMPLE: EFFICIENT AIR CONDITIONER

- ❑ An efficiency upgrade of an air conditioner incurs a \$ 1,000 investment and results in savings of \$ 200 *per year*
- ❑ The \$ 1,000 is obtained as a 10 – *year* loan repaid at 7 % interest
- ❑ The repayment on the loan is done as a uniform cash flow

$$A = 1,000 \frac{0.07}{1 - \beta^{10}} = \$ 142.38$$

EXAMPLE: EFFICIENT AIR CONDITIONER

- The annual net savings are

$$200 - 142.38 = \$ 57.62$$

and not only are the savings sufficient to pay back the loan in 10 *years*, they also provide a yearly surplus of \$ 57.62

- The *benefits/costs ratio* is

$$\frac{200}{142.38} = 1.4$$

EXAMPLE: PV SYSTEM

- We consider a 3 – kW PV system whose capacity factor $K = 0.25$
- The investment incurred \$ 10,000 and the funds are obtained as a 20 – year 6 % loan
- The annual loan repayments are

$$A = 10,000 \frac{0.06}{1 - \beta^{20}} = 10,000(0.0872) = \$ 872$$

EXAMPLE: PV SYSTEM

- The annual energy generated is

$$(3)(0.25)(8,760) = 6,570 \text{ kWh}$$

- We can compute the unit costs of electricity for break-even operation to be

$$\frac{872}{6,570} = 0.133 \text{ \$ / kWh}$$

PV SYSTEM TOTAL COST ESTIMATION

- ❑ The *PV* system for a Boulder house is designed to generate roughly 4,000 *kWh* annually
- ❑ The key cost components are

<i>component</i>	<i>costs (\$)</i>
<i>PVs</i>	4.20/ <i>W</i> (<i>DC</i>)
<i>inverter</i>	1.20/ <i>W</i> (<i>DC</i>)
<i>tracker</i>	400 + 100/ <i>m</i> ²
<i>installation</i>	3,800

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

- We assume the *PVs* have a 12 % efficiency and the inverter efficiency is 75 %
- We use the solar insolation tables in *Appendix G* to obtain the average daily insolation for a fixed array
- We compare the costs of a fixed array with a -15° tilt angle and those with a *single – axis* tracker

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

- The solar insolation tables in *Appendix G* indicate the average daily insolation in Boulder for a fixed array to be $5.4 \text{ kWh/m}^2 - d$
- We interpret the insolation as 5.4 h/d of 1 *sun*
- We compute

$$P_{DC, stc} = \frac{4,000}{(0.75)(5.4)(365)} = 2.71 \text{ kW}_p$$

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

- The costs of the *PVs* and the inverters are

$$\text{costs of } PVs = 4.20 \times 2,710 = \$ 11,365$$

$$\text{costs of inverters} = 1.20 \times 2,710 = \$ 3,247$$

- Given the 12 % efficiency of the *PVs*, the array

area required is

$$\text{area} = \frac{P_{DC, stc}}{(1 \text{ kW} / m^2) \eta} = \frac{2.71}{1 \times 0.12} = 22.6 \text{ m}^2$$

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

- We next consider the average daily insolation in

Boulder with a *single-axis* tracker of $7.2 \text{ kWh/m}^2 - d$,

i.e., $7.2 \text{ h/d of full sun}$ – as given in *Appendix G*

- We compute

$$P_{DC, stc} = \frac{4,000}{(0.75)(7.2)(365)} = 2.03 \text{ kW}_p$$

- The costs of the *PVs* and the inverters are

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

$$\text{costs of PVs} = 4.20 \times 2,030 = \$8,524$$

$$\text{costs of inverters} = 1.20 \times 2,030 = \$2,436$$

□ Thus the area for the system is

$$\text{area} = \frac{P_{DC, stc}}{(1 \text{ kW} / \text{m}^2) \eta} = \frac{2.03}{1 \times 0.12} = 16.9 \text{ m}^2$$

□ The tracker costs are

$$\text{costs of trackers} = 400 + 16.9 \times 100 = \$2,090$$

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

<i>element</i>	<i>fixed tilt array</i>	<i>single-axis tracker</i>
<i>PVs</i>	\$ 11,365	\$ 8,524
<i>inverter</i>	\$ 3,247	\$ 2,436
<i>tracker</i>	—	\$ 2,090
<i>installation</i>	\$ 3,800	\$ 3,800
<i>total</i>	\$ 18,412	\$ 16,850

EXAMPLE: BOULDER HOUSE *PV* SYSTEM

- ❑ The installation of the trackers increases the average daily insolation received at the *PV* panels and decreases the area required for the system
- ❑ While the trackers add \$ 2,090 to the fixed costs of the *PV* system, the *PV* system investment costs with the trackers are nevertheless markedly below those of the fixed panels

REVIEW OF THE *c.r.f.*

- The *capital recovery factor* is the scheme we use to determine the financing costs of a *PV* project
- A loan of P at interest rate i may be recovered over n years through fixed annual payments of

$$A = P \left(\frac{i}{1 - (\beta)^n} \right)$$

interest rate → i

c.r.f. → $\frac{i}{1 - (\beta)^n}$

$\beta \triangleq \frac{1}{1 + i}$

EXAMPLE: *LCOE* FOR THE *PV* SYSTEMS

□ We illustrate the determination of the *LCOE* with a *PV* system example with the following features:

○ installation costs: \$ 7 million

○ annual *O&M* costs: \$ 35,000

○ annual land lease fee: \$ 40,000

○ annual energy production: 4 *GWh*

○ 9 %, 20 – year loan

□ The *c.r.f.* is computed to be

EXAMPLE: *LCOE* FOR THE *PV* SYSTEMS

$$c.r.f.(9\%, 20y) = \frac{(0.09)(1 + 0.09)^{20}}{(1 + 0.09)^{20} - 1} = 0.1095 y^{-1}$$

- The *c.r.f.* results in the annual amortized fixed costs of

$$7,000,000 \times 0.1095 = \$ 766,500$$

- Then we can evaluate the *LCOE* using

$$\frac{766,500 + 35,000 + 40,000}{4,000,000} = 0.21 \frac{\$}{kWh}$$

FINANCIAL INCENTIVES FOR SOLAR

- ❑ A significant factor that was ignored in the cost calculation in the previous example is the impacts of the financial and tax incentives
- ❑ Many solar installations are eligible for federal and state tax incentives for the purchase and implementation of *PV* systems

FEDERAL BUSINESS ENERGY INVESTMENT TAX CREDIT (*ITC*)

State:	Federal
Incentive Type:	Corporate Tax Credit
Administrator:	U.S. Internal Revenue Service
Expiration Date:	Varies by technology, see below
Eligible Renewable/Other Technologies:	Solar Water Heat, Solar Space Heat, Geothermal Electric, Solar Thermal Electric, Solar Thermal Process Heat, Solar Photovoltaics, Wind (All), Geothermal Heat Pumps, Municipal Solid Waste, Combined Heat & Power, Fuel Cells using Non-Renewable Fuels, Tidal, Wind (Small), Geothermal Direct-Use, Fuel Cells using Renewable Fuels, Microturbines
Applicable Sectors:	Commercial, Industrial, Investor-Owned Utility, Cooperative Utilities, Agricultural
Incentive Amount:	30% for solar, fuel cells, small wind* 10% for geothermal, microturbines and CHP
Maximum Incentive:	Fuel cells: \$1,500 per 0.5 kW Microturbines: \$200 per kW Small wind turbines placed in service 10/4/08 - 12/31/08: \$4,000 Small wind turbines placed in service after 12/31/08: no limit All other eligible technologies: no limit

Source: <http://programs.dsireusa.org/system/program/detail/658>

TAX INCENTIVES FOR SOLAR

- ❑ The *ITC* originally enacted in the *Energy Policy Act* of 2005 for solar has been renewed numerous times and is currently set at 30 % of the initial investment
- ❑ The *ITC* supports electricity generated by solar systems on residential and commercial properties

EXAMPLE: TAX INCENTIVES FOR SOLAR

- We illustrate the *ITC* impacts on the *LCOE* in the previous *PV* system example
- With the *ITC* , the initial investment tax savings amount to $0.3 \times 7,000,000 = \$ 2,100,000$
- The resulting annual amortized fixed costs are $(1 - 0.3) \times 7,000,000 \times 0.1095 = \$ 536,550$

EXAMPLE: TAX INCENTIVES FOR SOLAR

- Then we can evaluate the *LCOE* using

$$\frac{536,550 + 35,000 + 40,000}{4,000,000} = 0.15 \frac{\$}{kWh}$$

- We observe that the introduction of the *ITC*

results in a 6 ¢/*kWh* reduction in the *LCOE*

- This corresponds to a 27 % reduction in the

LCOE

TAX BENEFITS FOR SOLAR

□ The use of a home loan to finance the installation

of a *PV* system has an important impact on the

PV electricity price in light of the income tax

benefits, which depend on the homeowner

marginal tax bracket (MTB)

TAX BENEFIT FOR SOLAR

- ❑ For a loan over several years, almost all of the first year payments constitute the interest due, with a very small contribution to the reduction of the loan principal, while the opposite allocation occurs towards the end of the loan life
- ❑ In the first year, interest is owed on the entire amount of the loan and the tax benefits are

$$i \times loan \times MTB$$

EXAMPLE: TAX BENEFIT FOR SOLAR

□ Consider a 30 – *year* 4.5 % loan to install a residential 3.36 – kW_p PV system in Chicago, with the annual energy of 4,942 kWh

□ The *c.r.f.* for the loan is

$$\frac{(0.045)(1 + 0.045)^{30}}{(1 + 0.045)^{30} - 1} = 0.06139 \text{ y}^{-1}$$

EXAMPLE: TAX BENEFIT FOR SOLAR

- The residential *PV* system costs \$ 19,186 and the annual loan payment is

$$19,186 \times 0.06139 = \$1,178$$

- Thus the cost of *PV* electricity in the first year is

$$\frac{1,178}{4,932} = 0.239 \frac{\$}{kWh}$$

- During the first year, the owner pays the annual interest on the \$ 19,186 loan in the amount of

EXAMPLE: TAX BENEFIT FOR SOLAR

$$\textit{first year interest} = 19,186 \times 0.045 = \$863$$

□ We assume the homeowner is in the 25 % *MTB*

and determine the first year tax savings to be

$$863 \times 0.25 = \$216$$

which reduce the cost of *PV* electricity to

$$\frac{1,178 - 216}{4,932} = 0.192 \frac{\$}{kWh}$$

REBATES

- ❑ Many states and certain jurisdictions have introduced rebate programs to promote investments in solar systems
- ❑ A rebate reduces the total investment required by, in effect, returning some of the costs of the *PV* system installation to the investor:

$$\textit{reduced costs} = \textit{original costs} - \textit{rebate}$$

ILLINOIS SOLAR AND WIND ENERGY REBATE PROGRAM

Budget:	\$2.5 million
Start Date:	12/16/1997
Expiration Date:	10/10/2014 (current applications)
Eligible Renewable/Other Technologies:	Solar Water Heat, Solar Photovoltaics, Wind (All), Solar Pool Heating, Wind (Small)
Applicable Sectors:	Commercial, Industrial, Local Government, Nonprofit, Residential, Schools, State Government, Federal Government
Incentive Amount:	<p>Residential PV: \$1.50/watt or 25% of project costs</p> <p>Commercial PV: \$1.25/watt or 25% of project costs</p> <p>Nonprofits and Public Sector PV: \$2.50/watt or 40% of project costs</p> <p>Residential and Commercial Wind (SWCC certified): \$1.75/watt or 30% of project costs</p> <p>Nonprofits and Public Sector Wind (SWCC certified): \$2.60/watt or 40% of project costs</p> <p>Wind energy systems that are not SWCC certified: \$1.00/watt</p> <p>Residential and Commercial Solar Thermal: 30% of eligible project costs</p> <p>Nonprofits and Public Sector Solar Thermal: 40% of eligible project costs</p>
Maximum Incentive:	<p>Residential: \$10,000</p> <p>Commercial: \$20,000</p> <p>Nonprofits and Public Sector: \$30,000</p>
Eligible System Size:	<p>PV systems: Rated design capacity of at least 1 kW;</p> <p>Solar thermal systems: Designed to produce at least 0.5 therms or 50,000 Btus per day or contain at least 60 sq. ft. of collectors</p> <p>Wind: Name-plate capacity 1-100 kW</p>

Source: <http://programs.dsireusa.org/system/program/detail/585>

EXAMPLE: REBATES

- For instance, if the total investment costs in the previous example are reduced by the 25 % rebate under the Illinois solar and wind energy program, we can determine the reduced annual payment

$$19,186 \times (1 - 0.25) \times 0.06139 = \$883$$

- Then the first year interest reduces to

EXAMPLE: REBATES

$$19,186 \times (1 - 0.25) \times 0.045 = \$648$$

- Therefore the first year tax savings are given by

$$648 \times 0.25 = \$162$$

- Consequently the cost of *PV* electricity in the first year reduces to

$$\frac{883 - 162}{4,932} = 0.146 \frac{\$}{kWh}$$