

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN  
Department of Electrical and Computer Engineering

ECE 498MH PRINCIPLES OF SIGNAL ANALYSIS  
Fall 2013

**MIDTERM EXAM SOLUTIONS**

Wednesday, October 1, 2013

**Problem 1 (20 points)**

$$x = \frac{3}{2}, \quad y = \frac{\sqrt{3}}{2}$$

**Problem 2 (20 points)**

$$z(t) = \cos(2\pi 2000t)$$

**Problem 3 (20 points)**

$$X_k = \begin{cases} -\frac{1}{2} & k = 0 \\ \frac{1}{2} & k = 1, 2, 3 \end{cases}$$

**Problem 4 (20 points)**

For example, suppose  $x_1[n] = \cos \pi n$ ; then  $y_1[n] = \cos(\pi n) \cos(\omega_0 n)$ . Let  $x_2[n] = \cos \pi(n - 1)$ ; then  $y_2[n] = \cos(\pi(n - 1)) \cos(\omega_0 n) \neq y_1[n - 1]$ .

**Problem 5 (20 points)**

$$y[n] = \begin{cases} 1 & n = 0 \\ -1 & n = 10 \\ 0 & \text{otherwise} \end{cases}$$