## Problem 1 (10 points)

- (a)  $3^{1/p}$
- (b) Any solution such that  $\frac{1}{\sigma_1^2} > \frac{1}{\sigma_2^2} + \frac{1}{\sigma_3^2}$

## Problem 2 (10 points)

- (a) The sketch should show an ellipse with axes parallel to the main axes, passing through the points  $(\frac{5}{2},0)$ ,  $(-\frac{1}{2},0)$ , (1,1), and (1,-1).
- (b)  $(\Phi(0) \Phi(-\frac{2}{3}))(\Phi(\frac{1}{2}) \Phi(-\frac{1}{2}))$

## Problem 3 (10 points)

- (a) The sketch should show the line  $x_1 + x_2 = 3\sqrt{2}$ .
- (b) 8

## Problem 4 (10 points)

- (a) The sketch should show the square  $\max(|x_1|, |x_2|) = 1.5$ .
- (b)  $\eta = \frac{1}{2}e^{9/16}$