

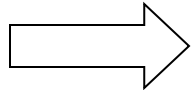
# ECE 598HH: Special Topics in Wireless Networks and Mobile Systems

## Lecture 22: Network Coding Haitham Hassanieh



\*These slides are courtesy of Sachin Katti

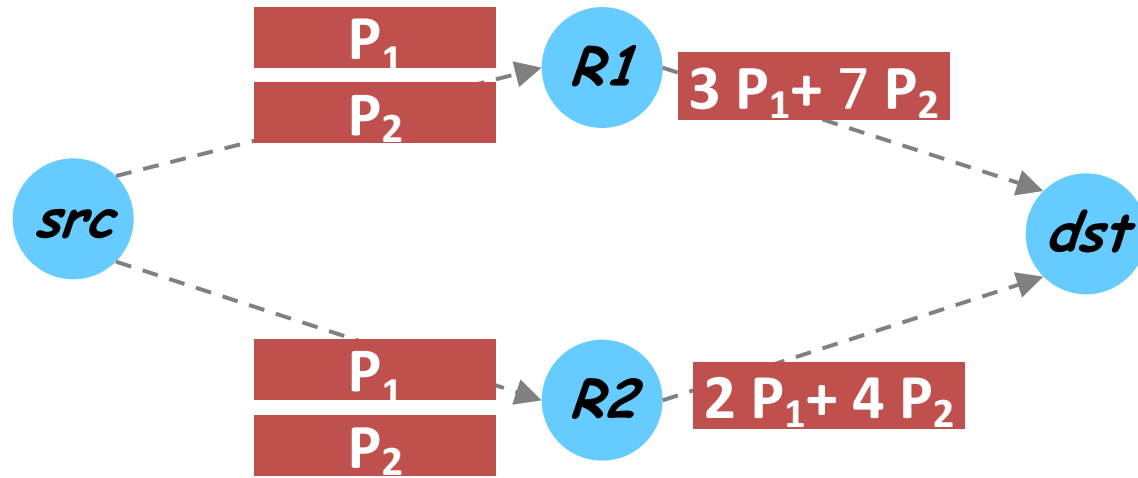
# Lecture Outline



- Intra-Flow Network Coding with MORE
- Inter-Flow Network Coding with Cope
- Analog Networking Coding

# Random Network Coding

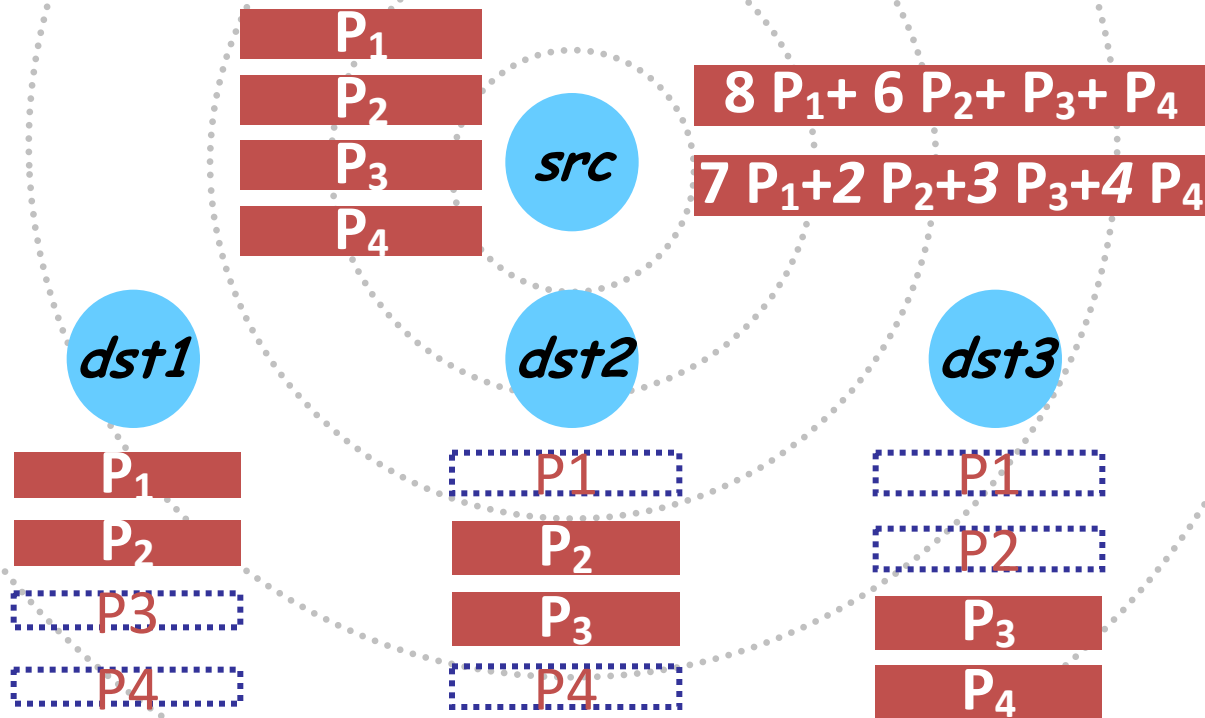
Each router forwards **random combinations** of packets



Randomness prevents duplicates

No need to know who received what  
Can exploit spatial reuse

# Network Coding Also Benefits Multicast

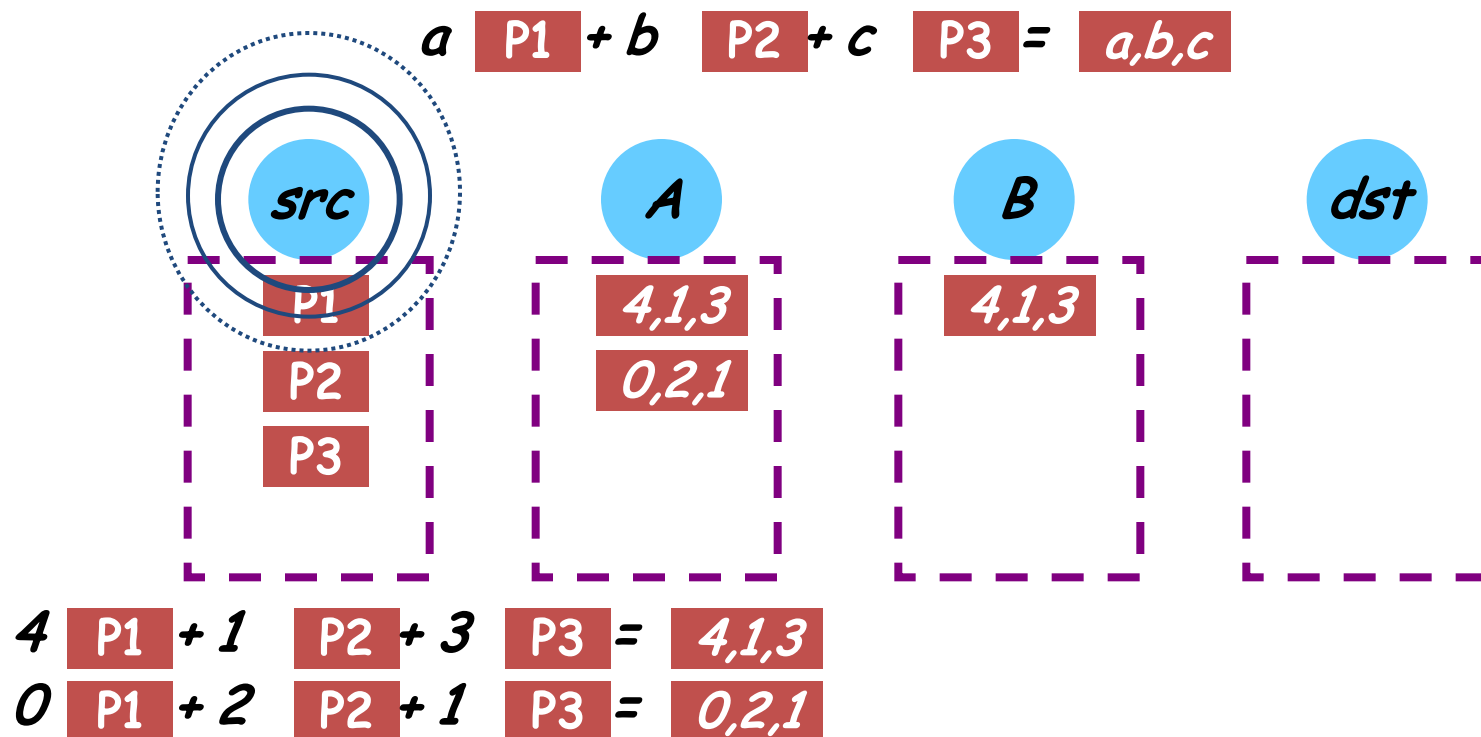


Without coding  $\rightarrow$  source has to retransmit all 4 packets

With network coding  $\rightarrow$  2 packets are sufficient

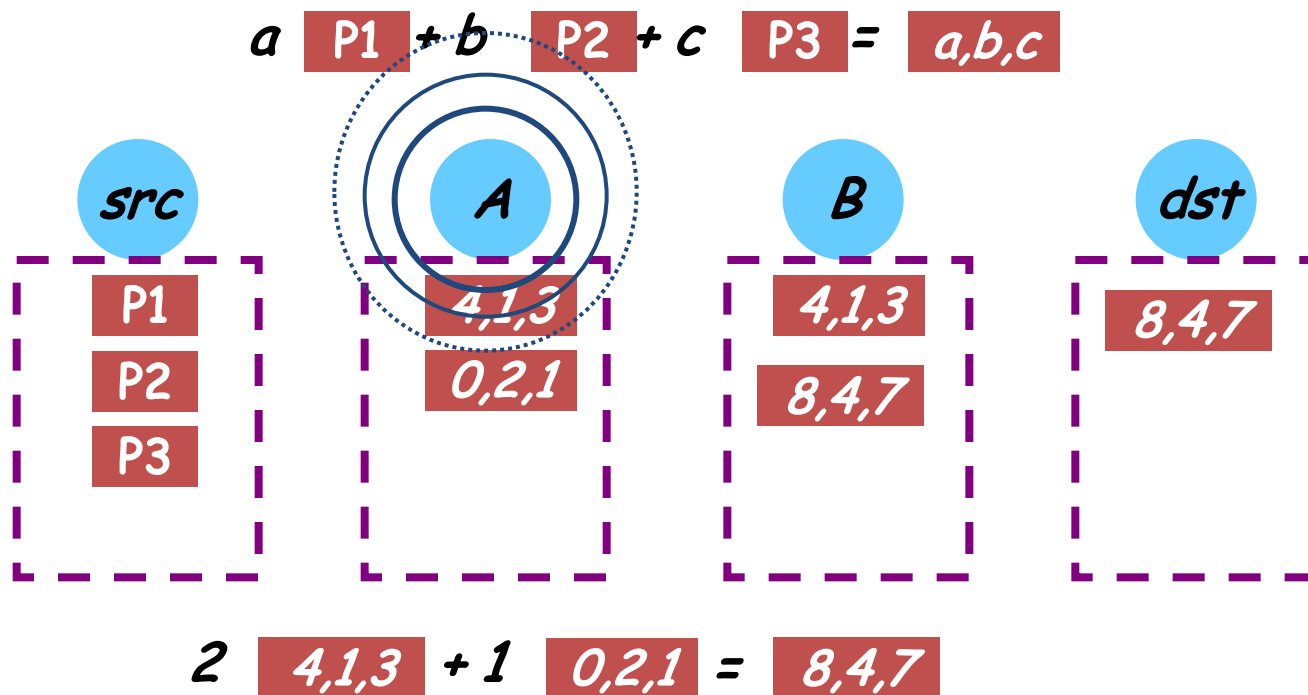
# How Does MORE Work?

- Source sends packets in batches
- Forwarders keep all heard (innovative) packets in a buffer
- Nodes transmit linear combinations of buffered packets



# How Does MORE Work?

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# Network Coding

- Requires less coordination
  - No scheduler
- More flexibility
  - One framework for unicast and multicast
- More throughput
  - 22% more than ExOR and 95% more than current shortest path routing

# Two Types of Network Coding

## Intra-flow

- Codes packets within a connection
- Robustness to packet loss
- Unicast and Multicast
- E.g., MORE

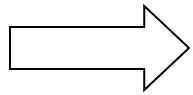
## Inter-flow

- Codes packets across connections
- Higher throughput
- Mainly Unicast
- E.g., COPE



# Lecture Outline

- Intra-Flow Network Coding with MORE



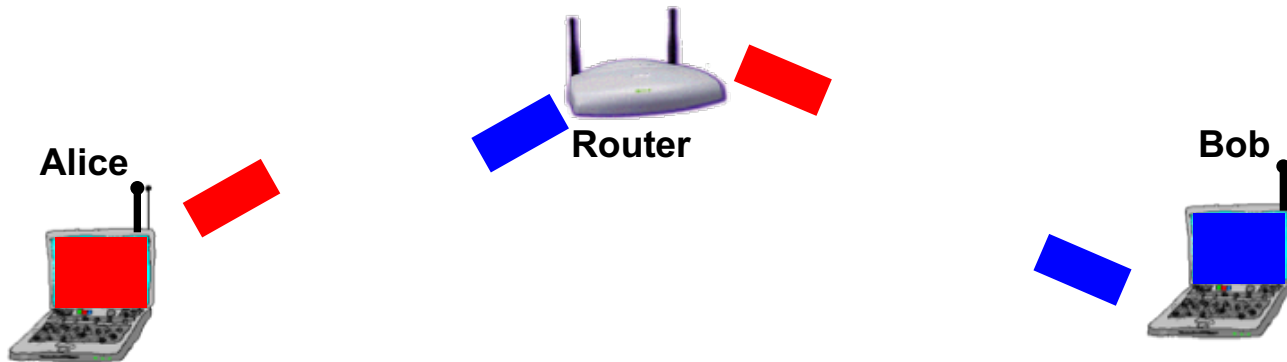
- Inter-Flow Network Coding with Cope

- Analog Networking Coding

# COPE

An Example of Inter-flow Network Coding

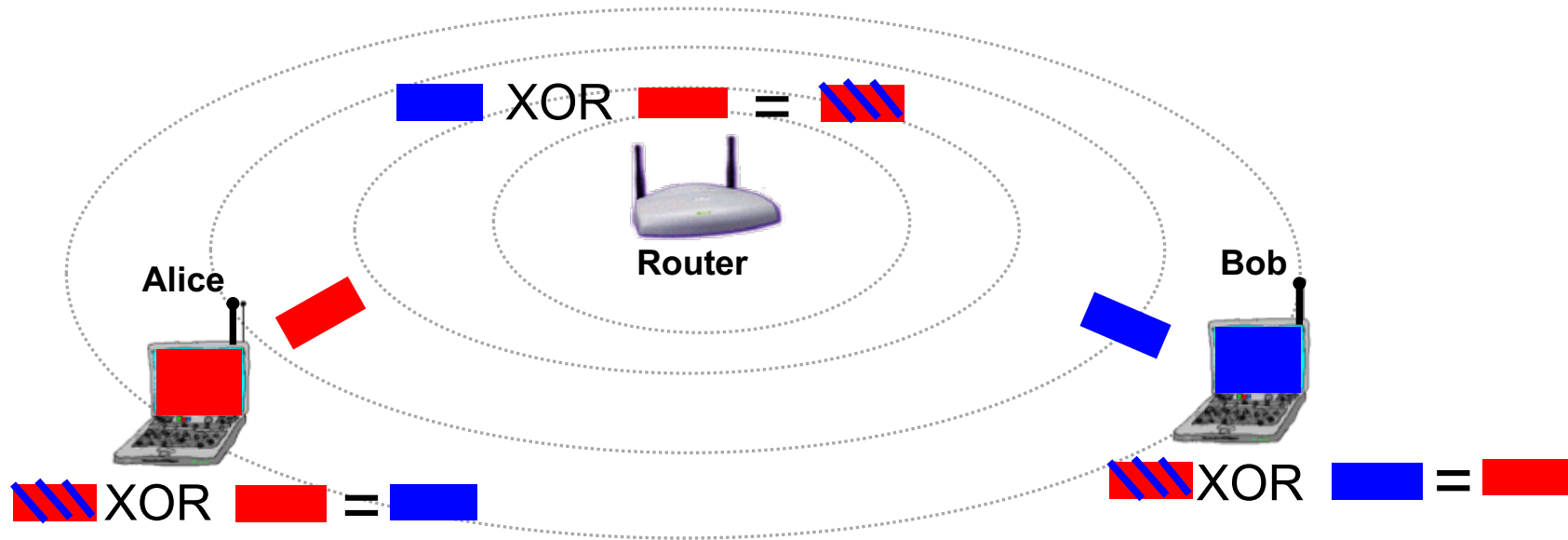
# Traditional Approach



Requires 4 transmissions

- Alice to router; Router to Bob; Bob to router; Router to Alice
- Can we exploit broadcast to do better?

# COPE

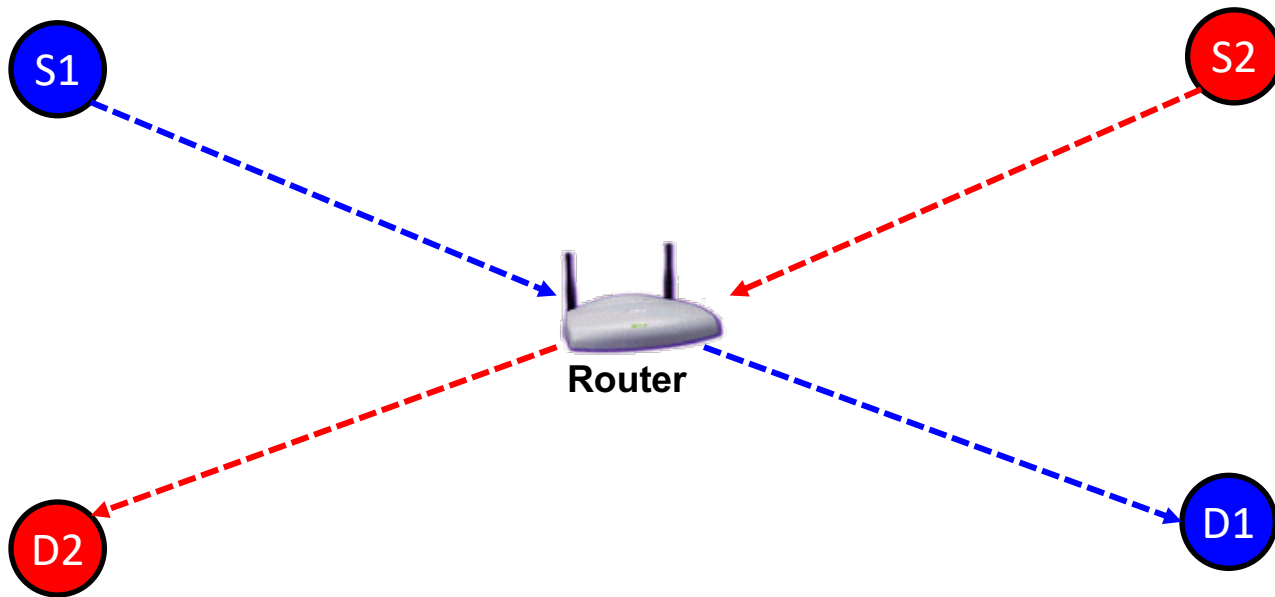


Requires 3 transmissions instead of 4

- Alice to router; Bob to router; and router to both Alice and Bob

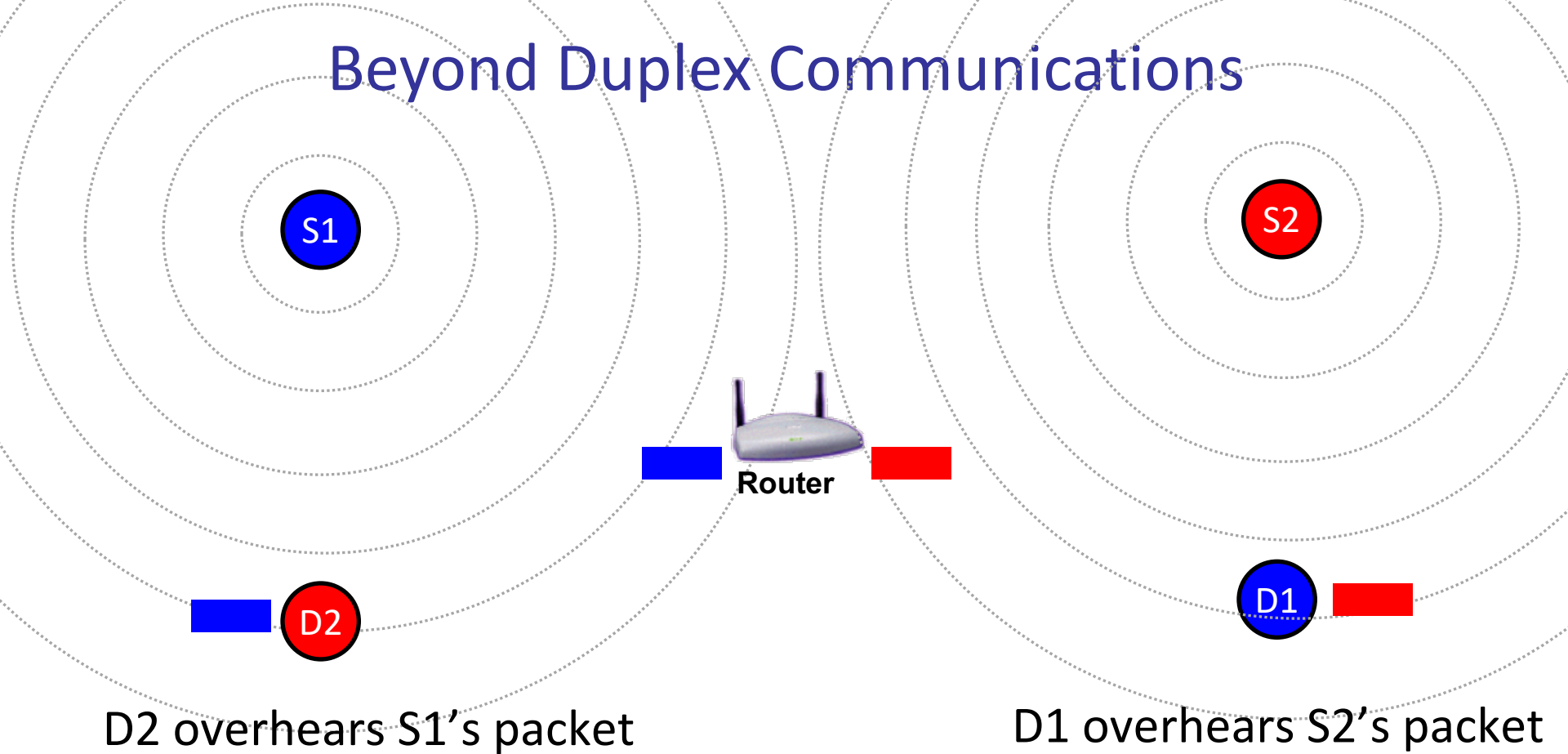
Network Coding  $\rightarrow$  3 Transmissions instead of 4  
 $\rightarrow$  Increases Throughput

# Beyond Duplex Communications



Two communication flows that intersect at a router

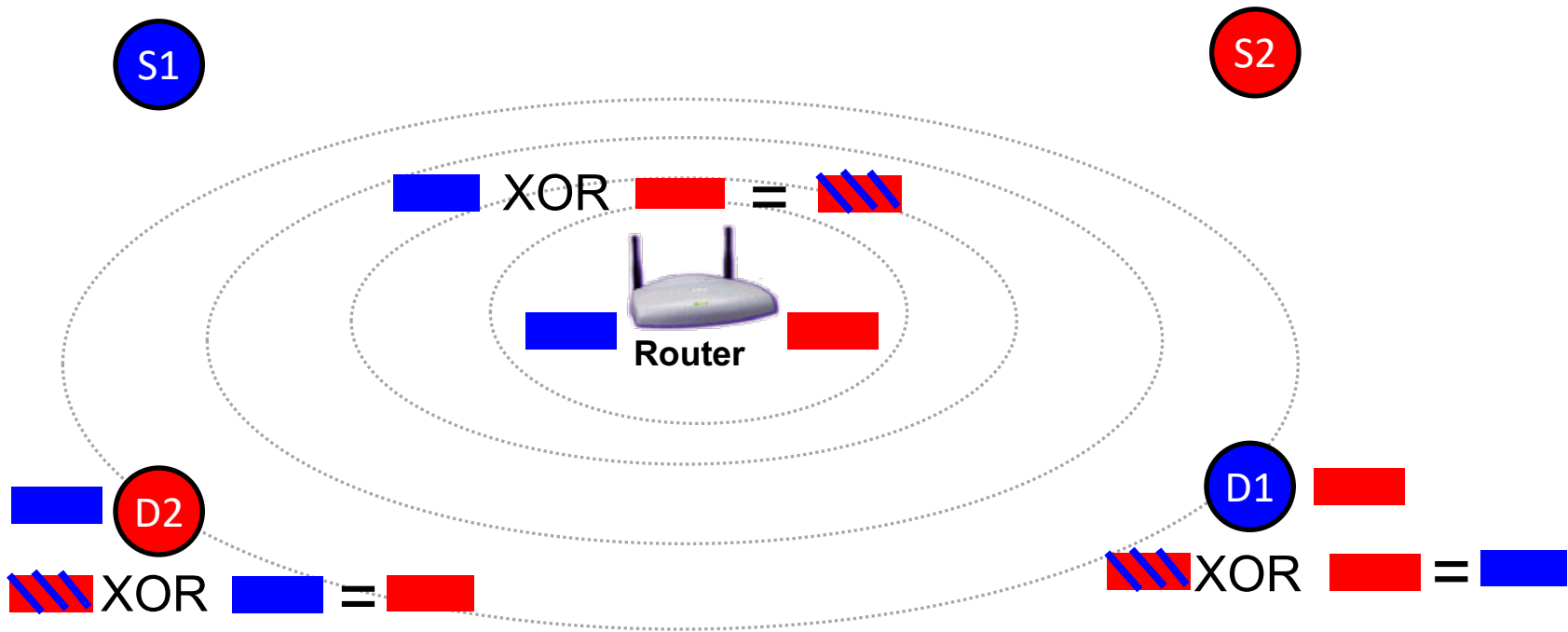
# Beyond Duplex Communications



D2 overhears S1's packet

D1 overhears S2's packet

# Beyond Duplex Communications



3 transmissions instead of 4 → Higher Throughput

# COPE

- Opportunistic Listening
- Opportunistic Coding

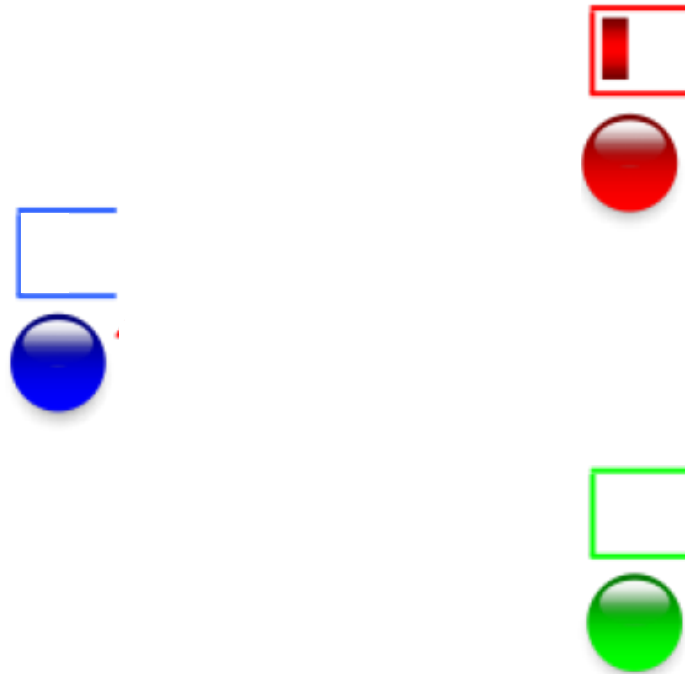


# Opportunistic Listening

- Exploit wireless broadcast
- Every node snoops on all packets
- A node stores all heard packets for a limited time

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# Opportunistic Listening

- Exploit wireless broadcast
- Every node snoops on all packets
- A node stores all heard packets for a limited time
  
- Node sends **Reception Reports** to tell its neighbors what packets it heard
  - Reports are piggybacked on packets
  - If no packets to send, periodically send reports

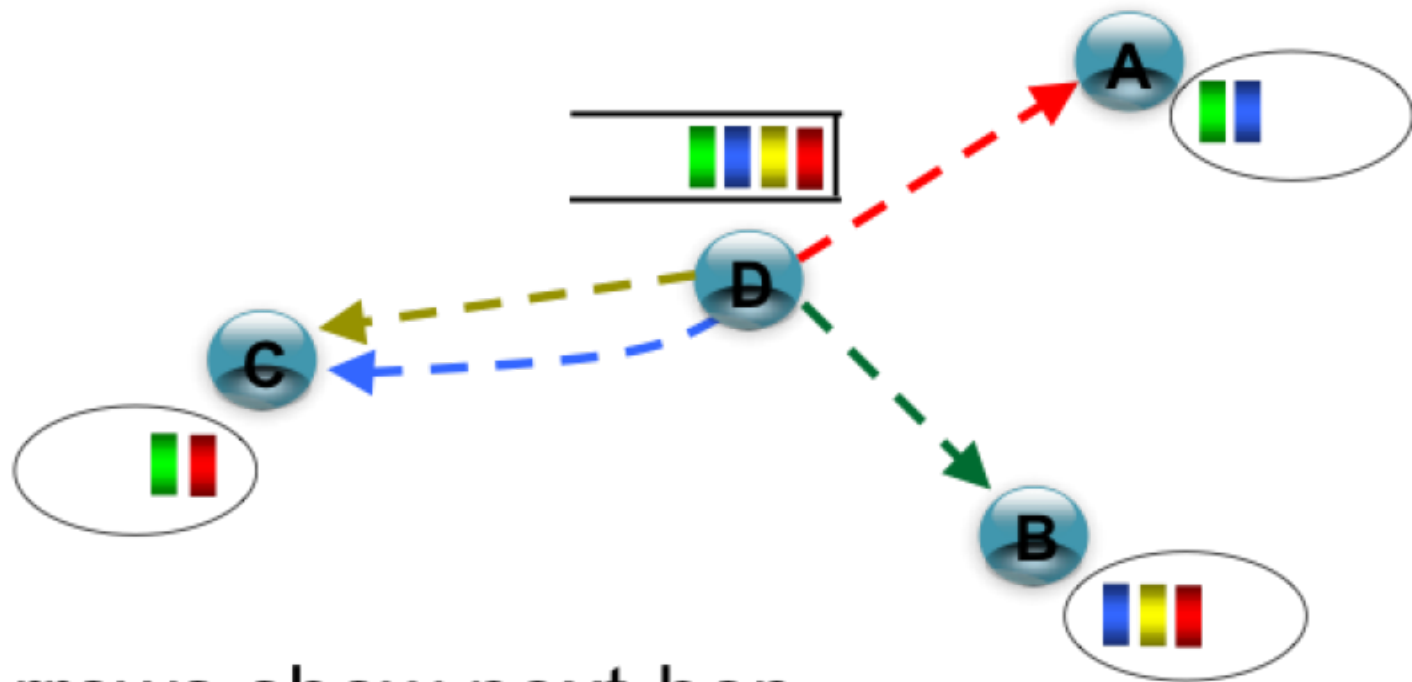
# Opportunistic Coding

- To send packet  $p$  to neighbor  $A$ , XOR  $p$  with packets already known to  $A$ 
  - Thus,  $A$  can decode

# Which Packets to Code Together?

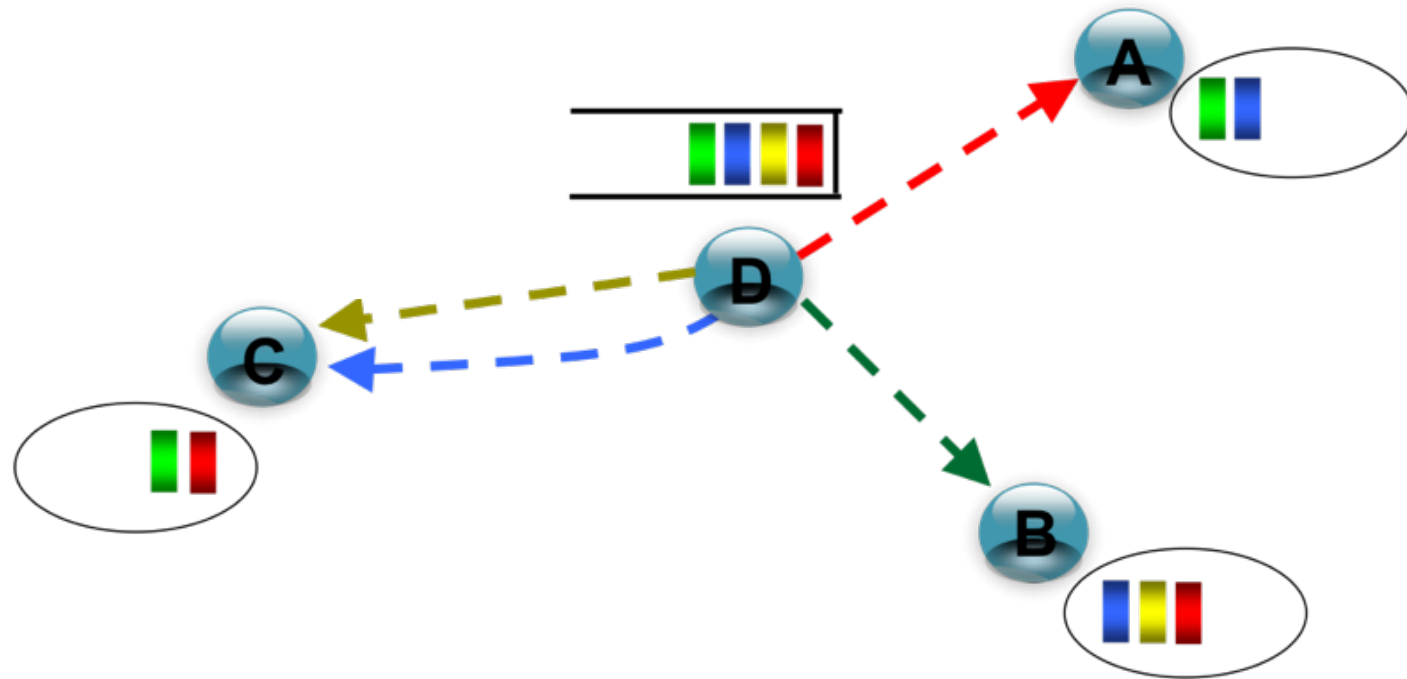


# Which Packets to Code Together?

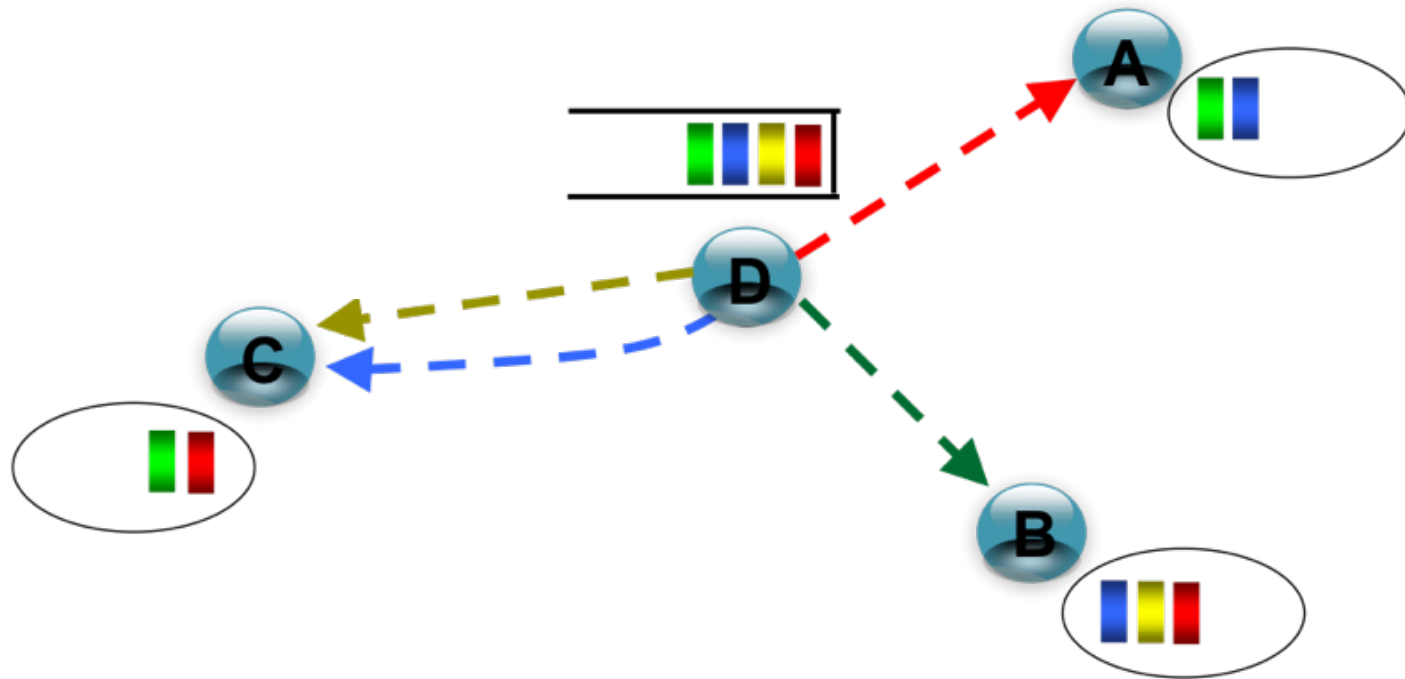


Arrows show next-hop

# Which Packets to Code Together?

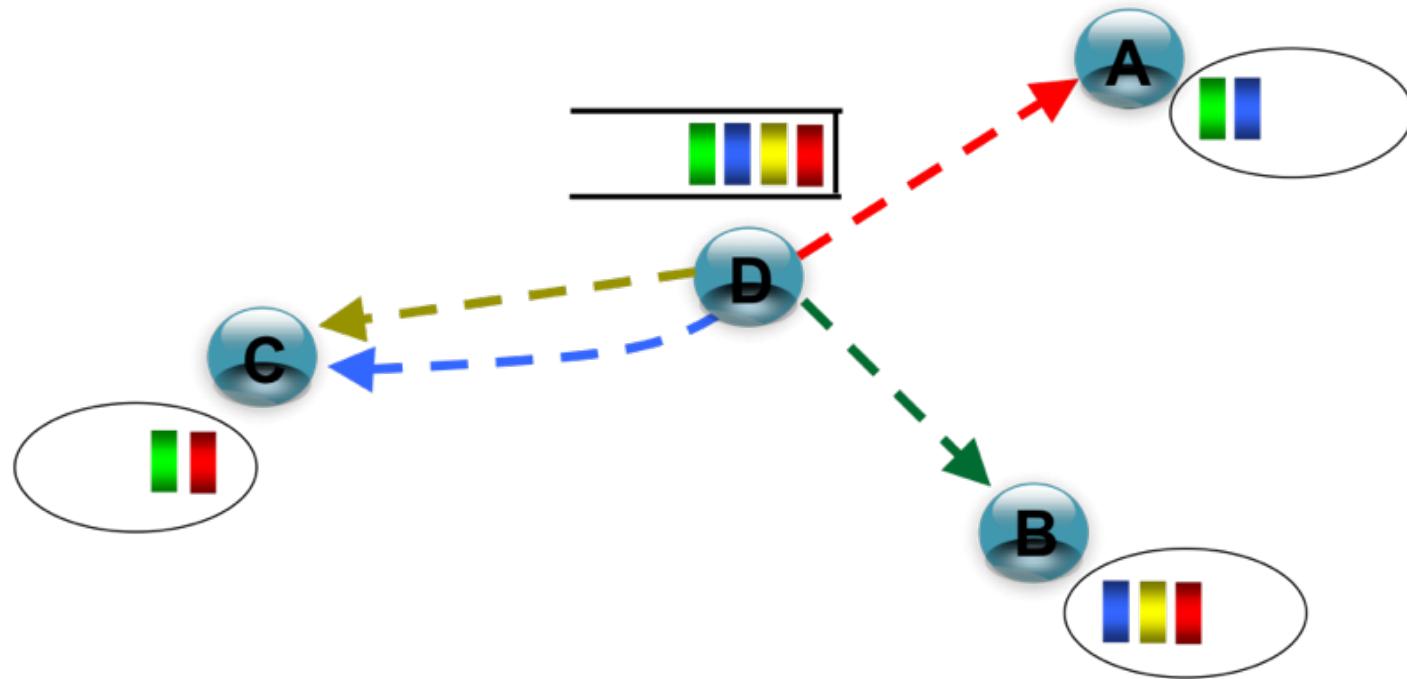


# Which Packets to Code Together?

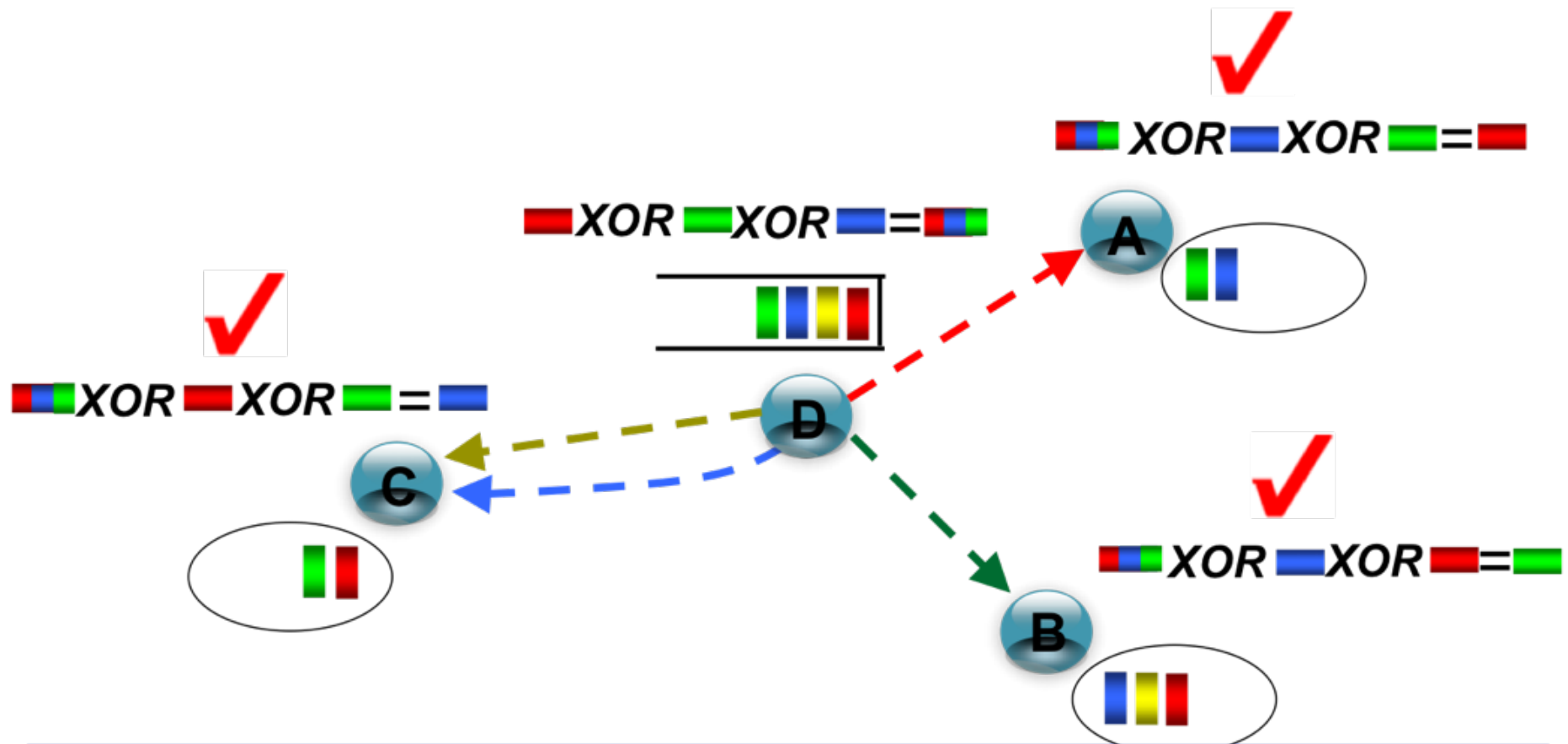




# Which Packets to Code Together?



# Which Packets to Code Together?



*XOR*  $n$  packets together iff the next hop of each packet already has the other  $n-1$  packets apart from the one it wants

# But, to decode a node needs to know which packets are XOR-ed

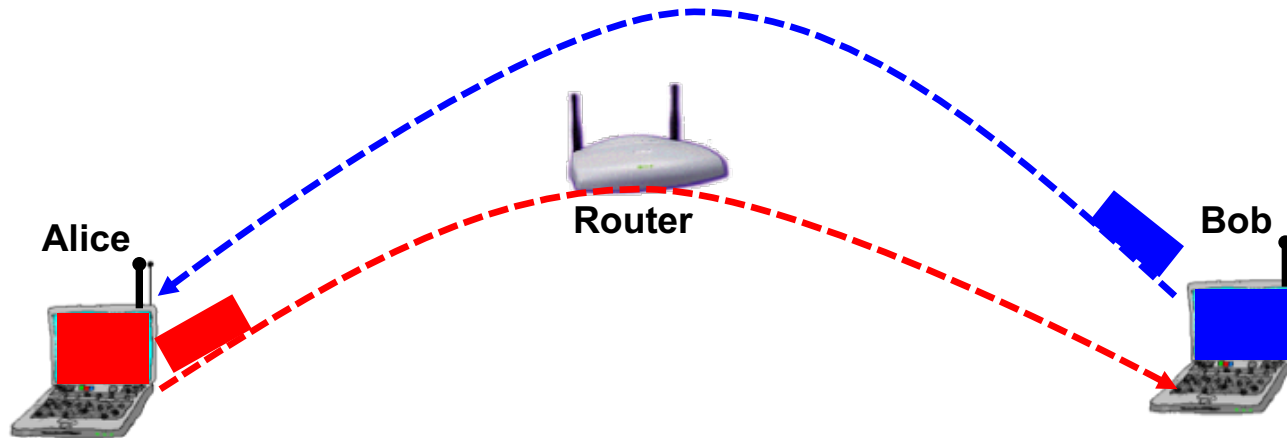
- Put that information in the header of the coded packet
- E.g.,  $P = P1 + P2 \rightarrow P$ 's header will say P1,P2

# COPE' s Characteristics

- COPE is a **forwarding mechanism**
  - It sits transparently between IP and MAC
  - Routing is unmodified (i.e., shortest path)
- **Opportunistic** → Code packets if possible, if not forward without coding
- Does not delay packets

Performance

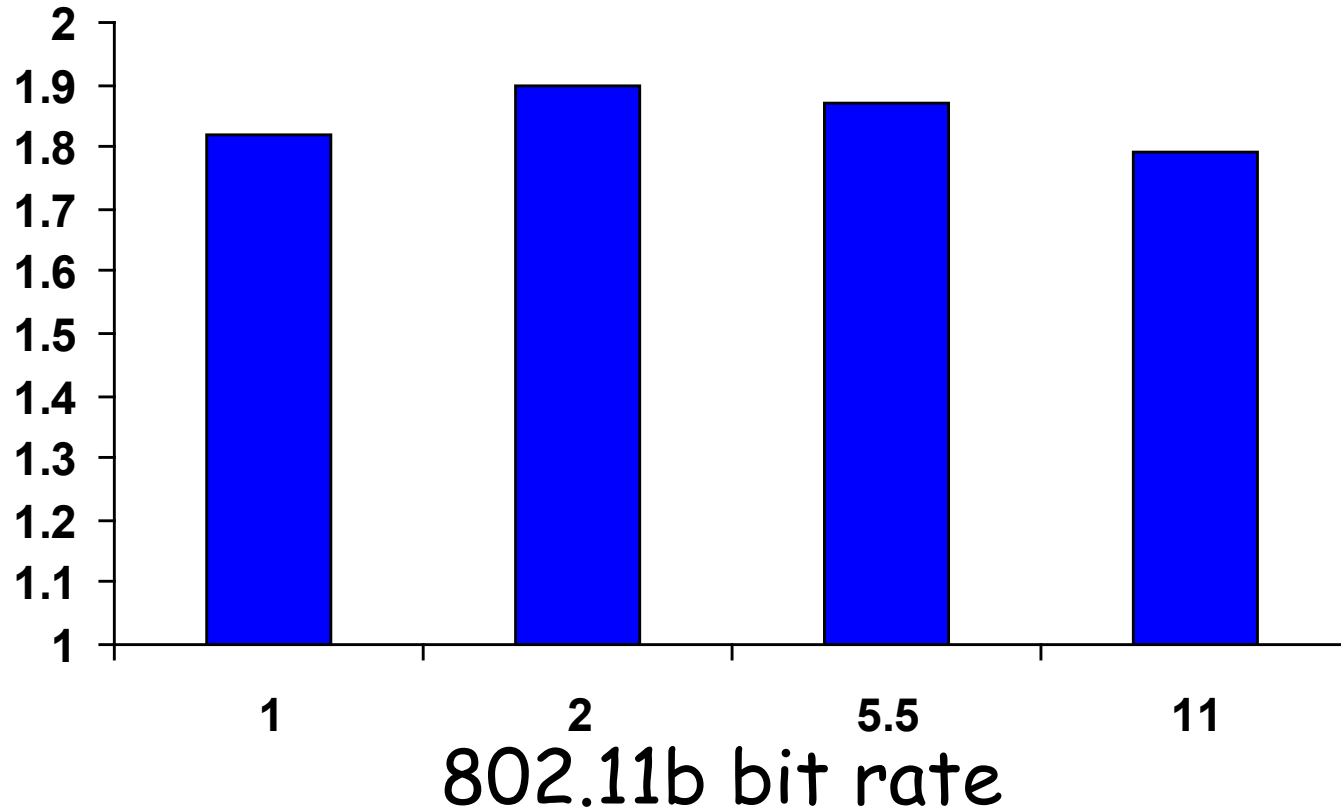
# Alice and Bob Experiment



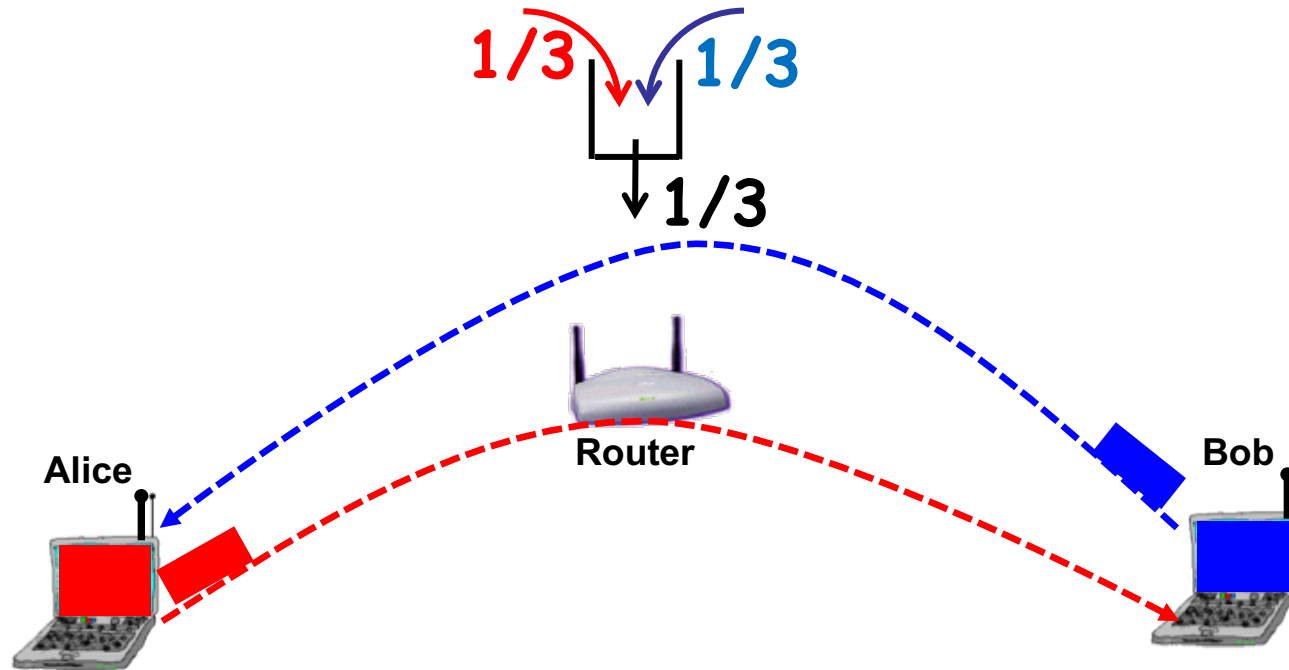
3 transmissions instead of 4  
→ Throughput Gain =  $4/3 = 1.3333$

# Results of the Alice-and-Bob

Ratio of Throughput with COPE to Current Approach



# Why the Gain is more than 1.33 ?



802.11 is fair  $\rightarrow$  Each node transmits  $1/3$

- Without COPE: Router needs to transmit twice as much
- With COPE: All nodes need equal rate.

COPE alleviates the mismatch between MAC's allocation and the congestion at a node



## Coding Gain

Reduction in #Transmissions

In Alice-and-Bob scenario,  
Coding Gain is  $4/3 = 1.33$

Nodes **not** backlogged

## Coding+MAC Gain

Improvement of Draining Rate  
at Bottlenecks

In Alice-and-Bob scenario,  
Coding+MAC Gain is 2

Nodes **backlogged**

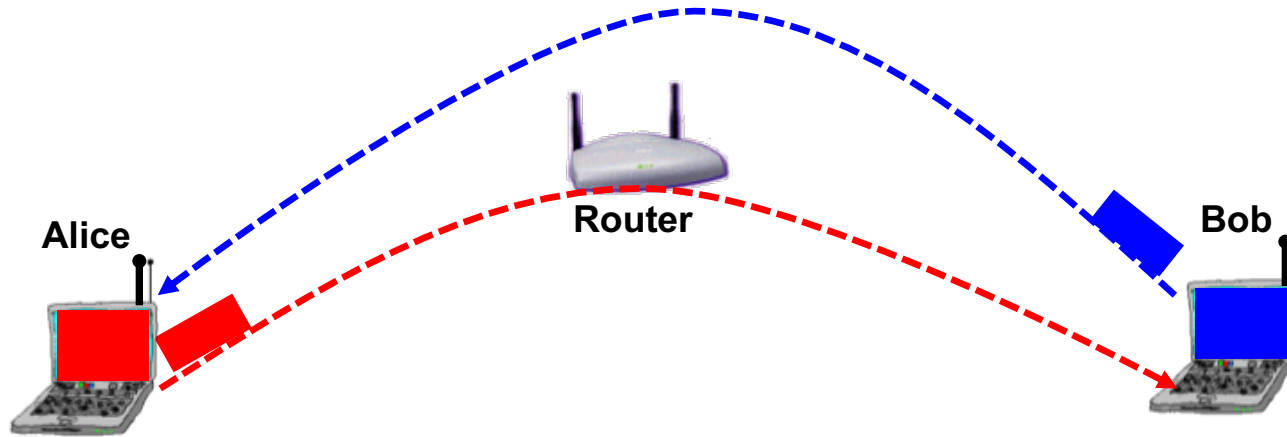
*Can show that, in a plane*

Coding gain is bounded by 2

Coding+MAC gain can be infinite

# Limitations of COPE

- Like other protocols that exploit broadcast (e.g., ExOR, MORE), it assigns the same bit rate to all transmitters
  - Need new ideas for bit rate adaptation
- Applicable only in multi-hop networks, i.e., doesn't apply to WLANs
- The benefit of coding decreases if the traffic in the forward and reverse direction is not balanced



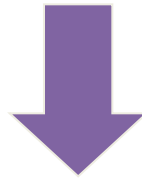
Traditional Approach: requires 4 transmissions

COPE: requires 3 transmissions

Can we do it in 2 transmissions?

Instead of router mixing packets...

Exploit that the wireless *channel naturally mixes signals*



Analog Network Coding (ANC)

# Lecture Outline

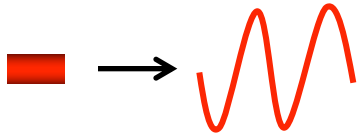
- Intra-Flow Network Coding with MORE
- Inter-Flow Network Coding with Cope
- ➔ ■ Analog Networking Coding

# Analog Network Coding

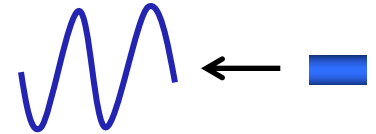


Router

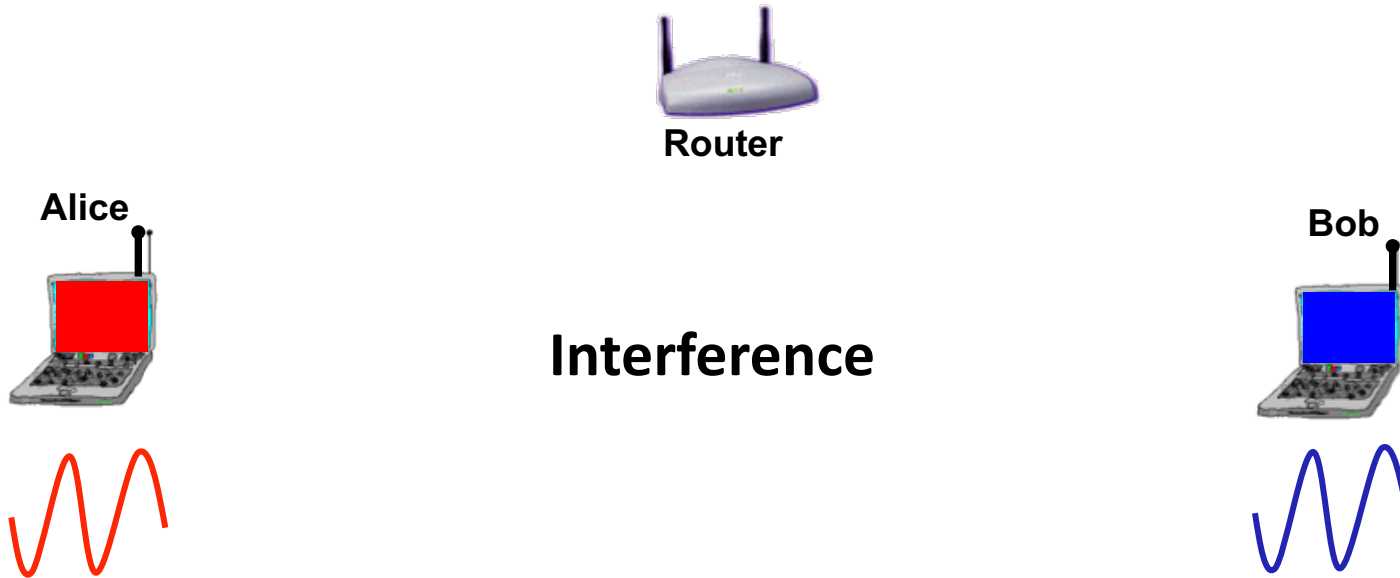
Alice



Bob

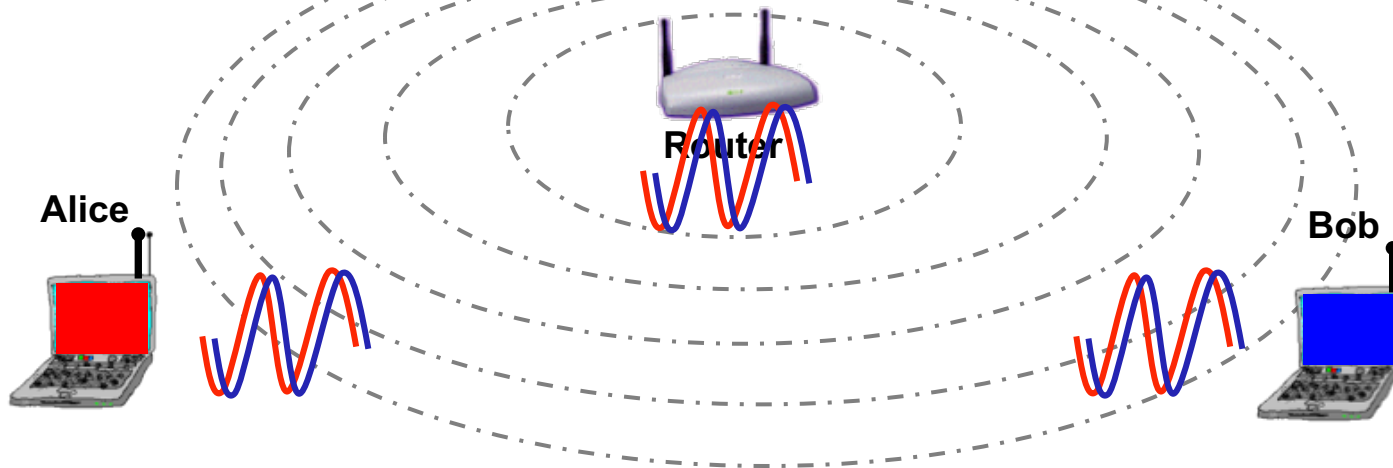


# Analog Network Coding



1) Alice and Bob transmit simultaneously

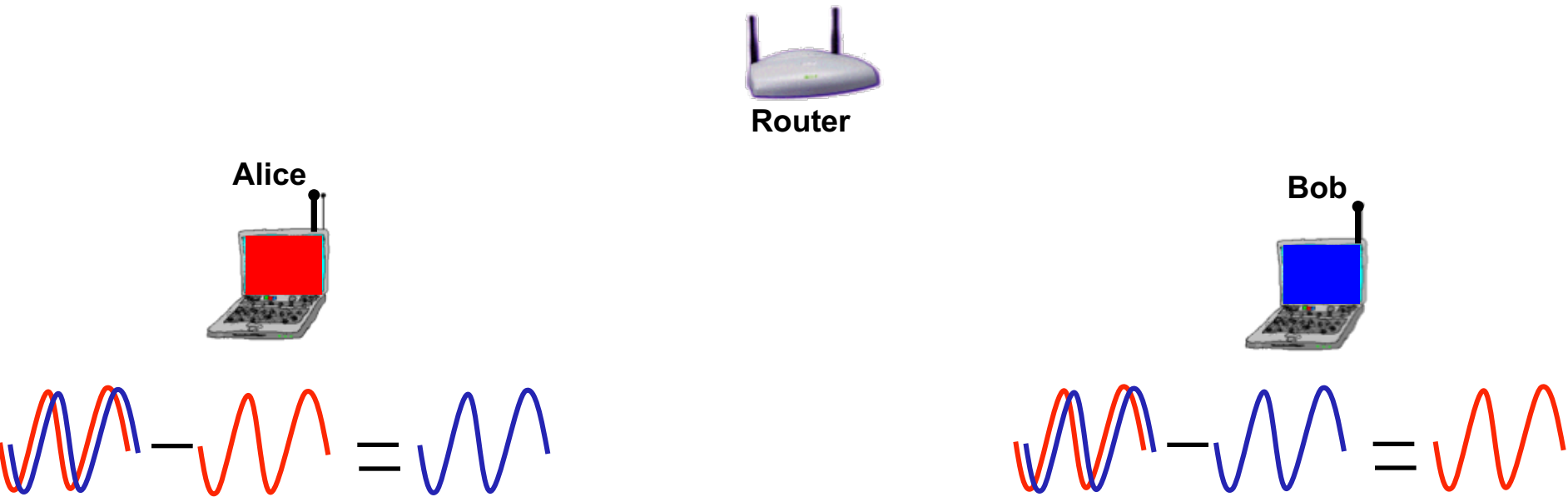
# Analog Network Coding



- 1) Alice and Bob transmit simultaneously
- 2) Router amplifies and broadcasts interfered signal

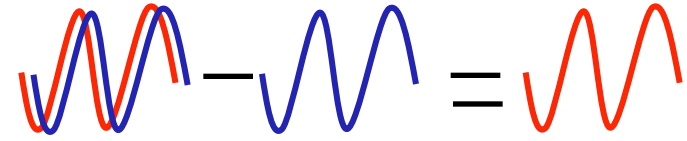
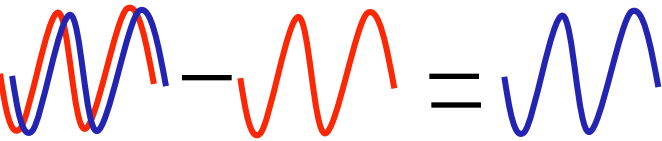


# Analog Network Coding



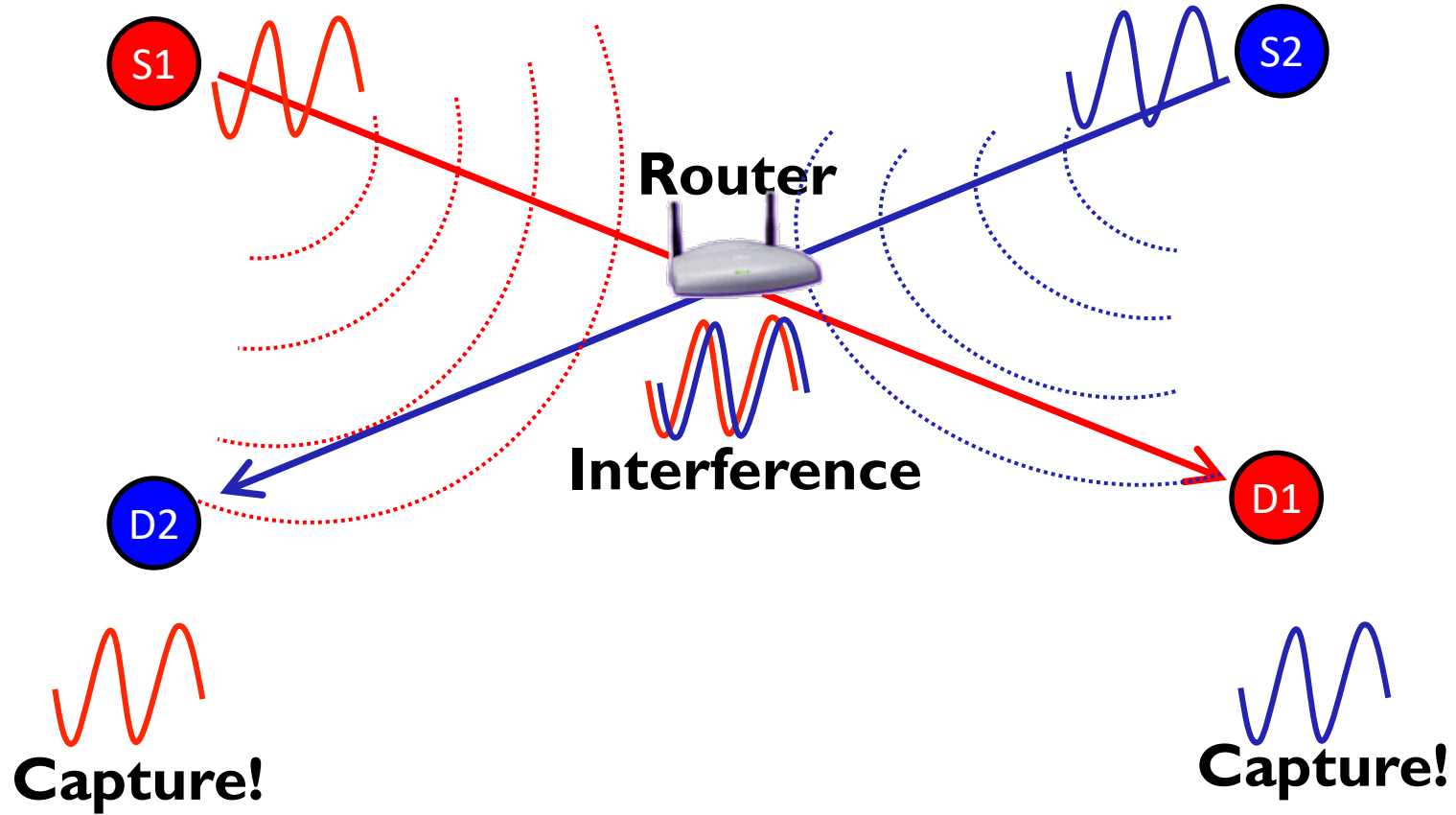
- 1) Alice and Bob transmit simultaneously
- 2) Router amplifies and broadcasts interfered signal
- 3) Alice subtracts known signal from interfered signal

# Analog Network Coding

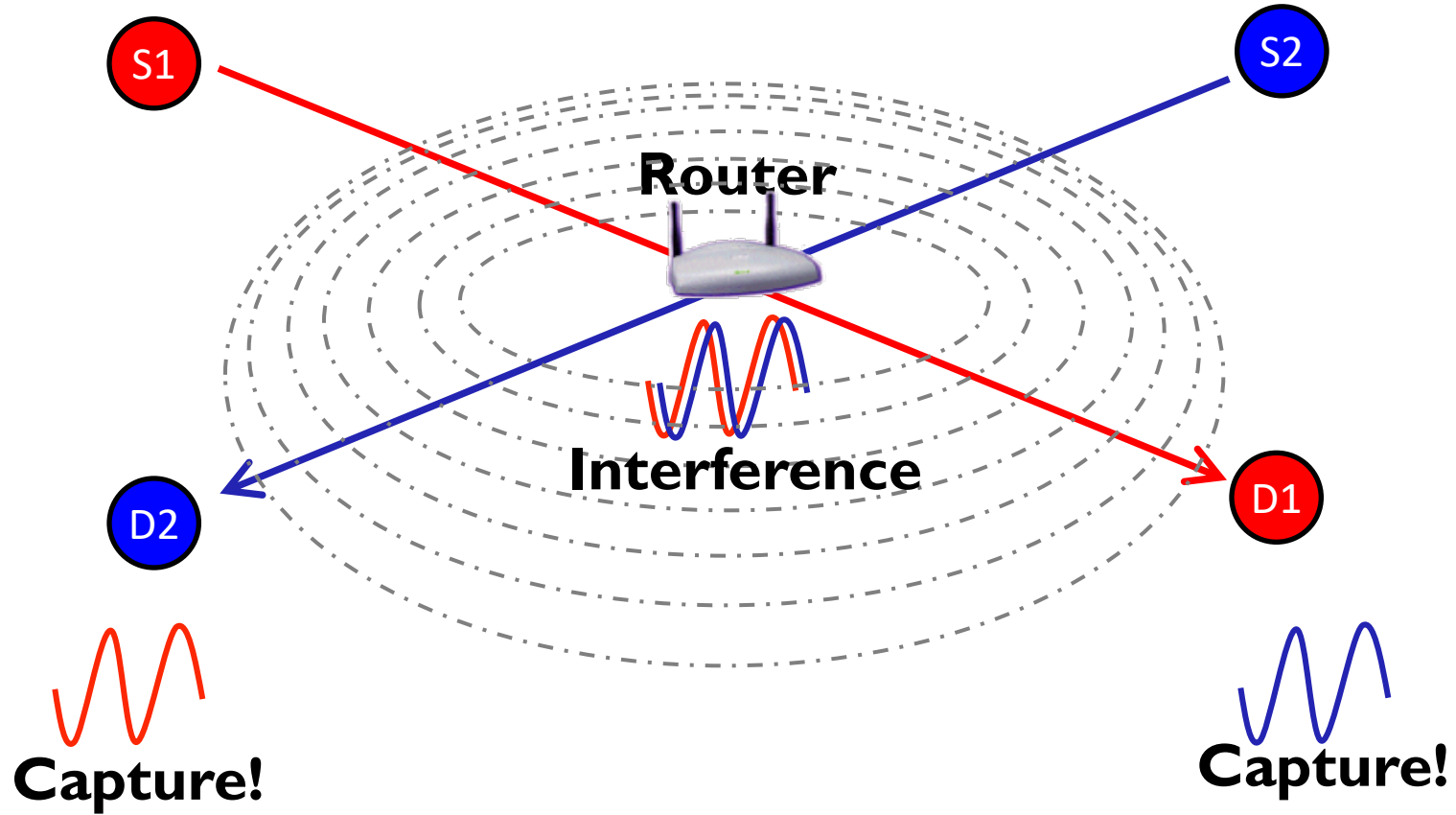


**Analog Network Coding requires 2 time slots  
→ Higher throughput**

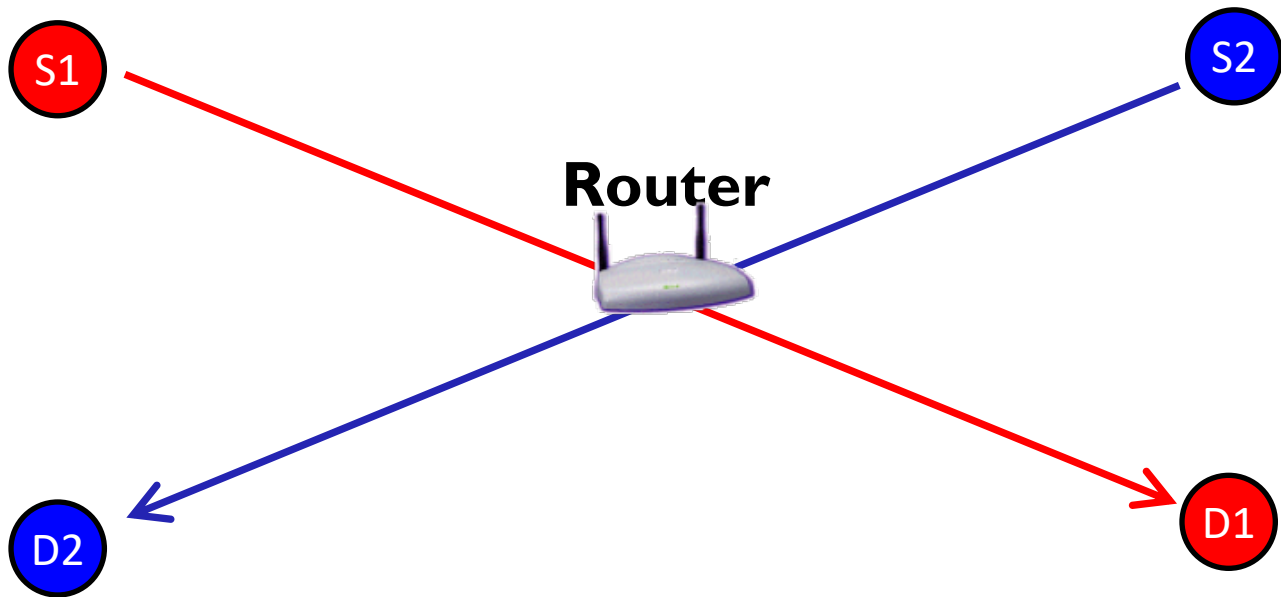
# X topology



# X topology



# X topology



A waveform diagram illustrating signal cancellation. It shows a blue sine wave and a red sine wave in phase, followed by a minus sign and another red sine wave in phase. This is followed by an equals sign and a blue sine wave, representing the result of subtracting the red signal from the sum of the blue and red signals.

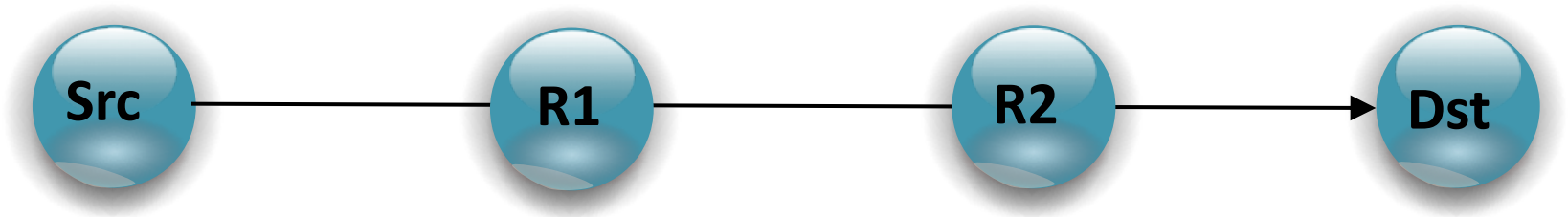
A waveform diagram illustrating signal cancellation. It shows a blue sine wave and a red sine wave in phase, followed by a minus sign and another blue sine wave in phase. This is followed by an equals sign and a red sine wave, representing the result of subtracting the blue signal from the sum of the blue and red signals.

**ANC decodes interference using overheard signals**

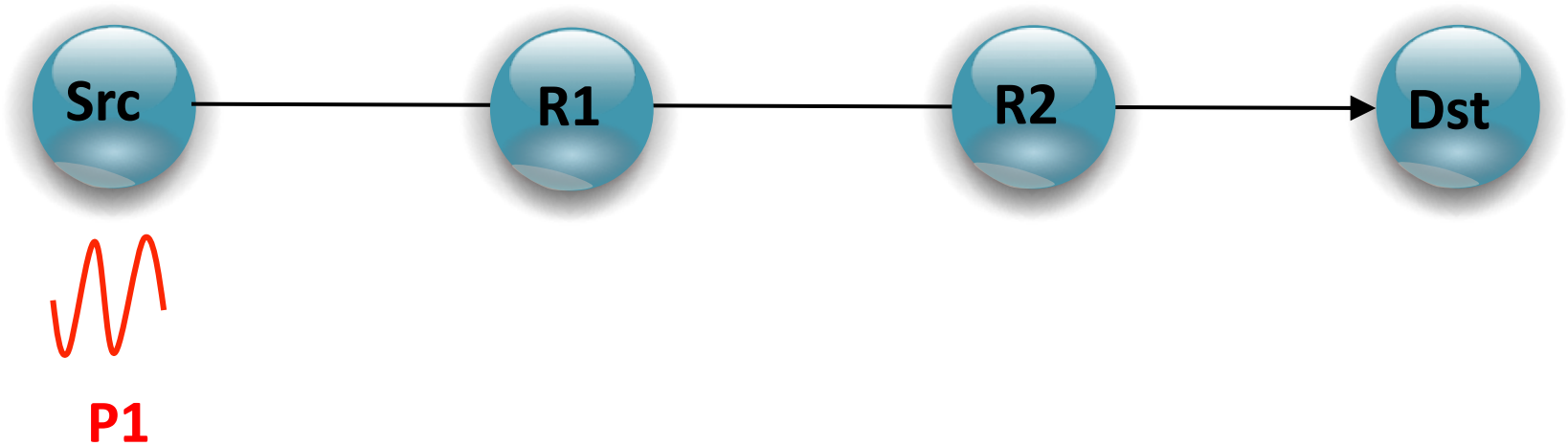
# It Is More Than Going From 3 To 2!

- Philosophical shift in **dealing with interference**
  - Strategically exploit interference instead of avoiding it
- Promises new ways of **dealing with hidden terminals**

# Hidden Terminal Scenario

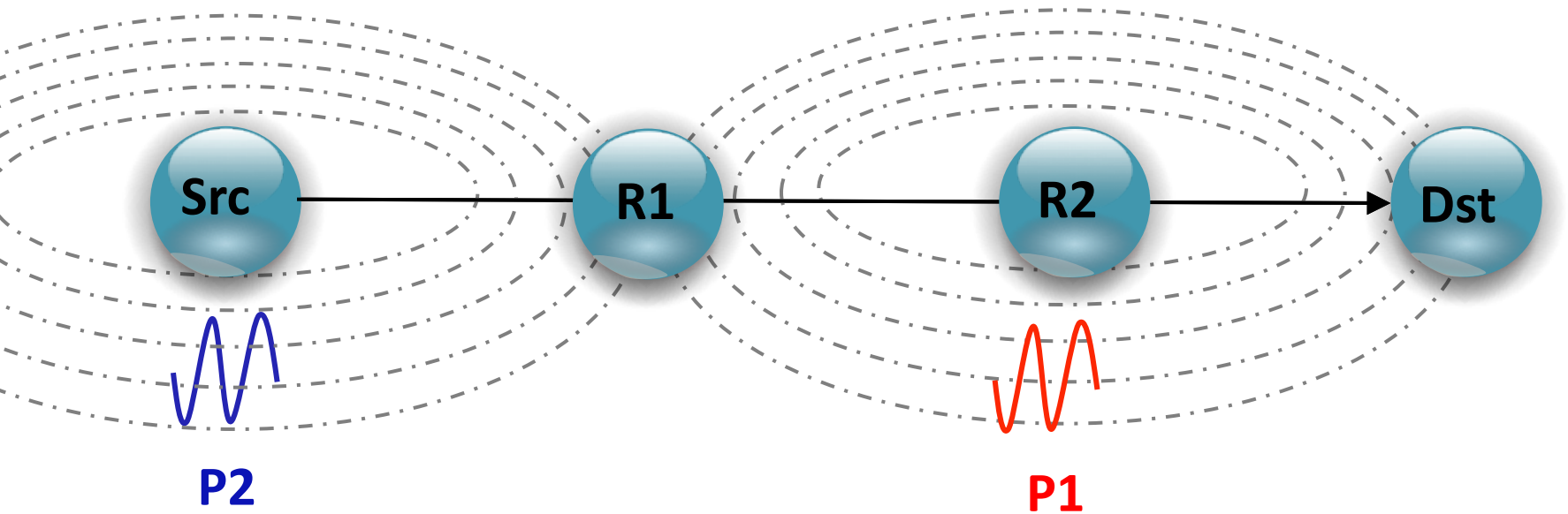


# Hidden Terminal Scenario



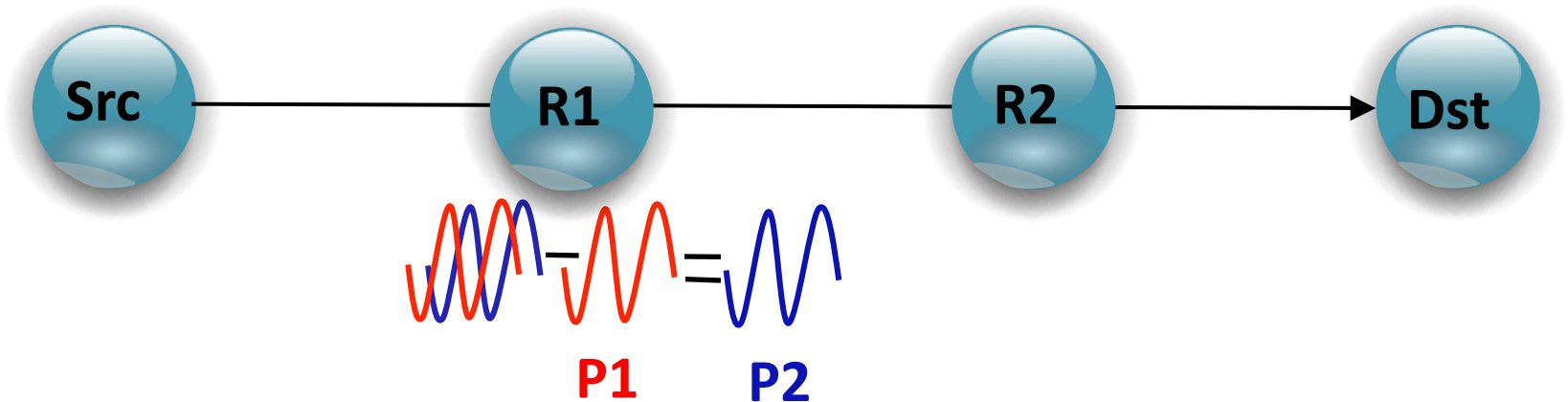


# Hidden Terminal Scenario



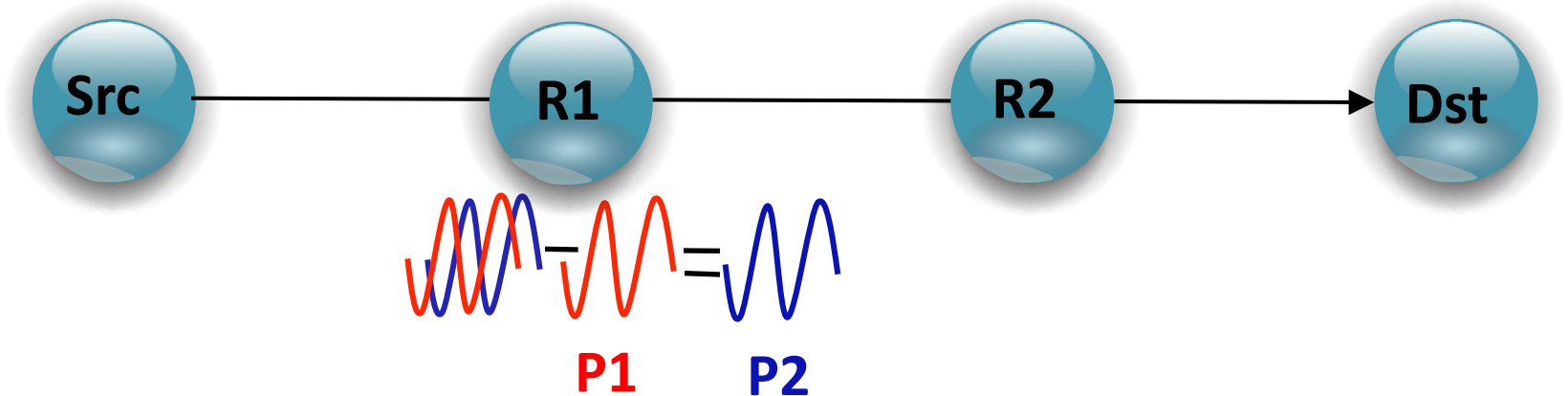
- 1) Src and R2 transmit simultaneously

# Hidden Terminal Scenario



- 1) Src and R2 transmit simultaneously
- 2) R1 subtracts P1, which he relayed earlier to recover P2 that he wants

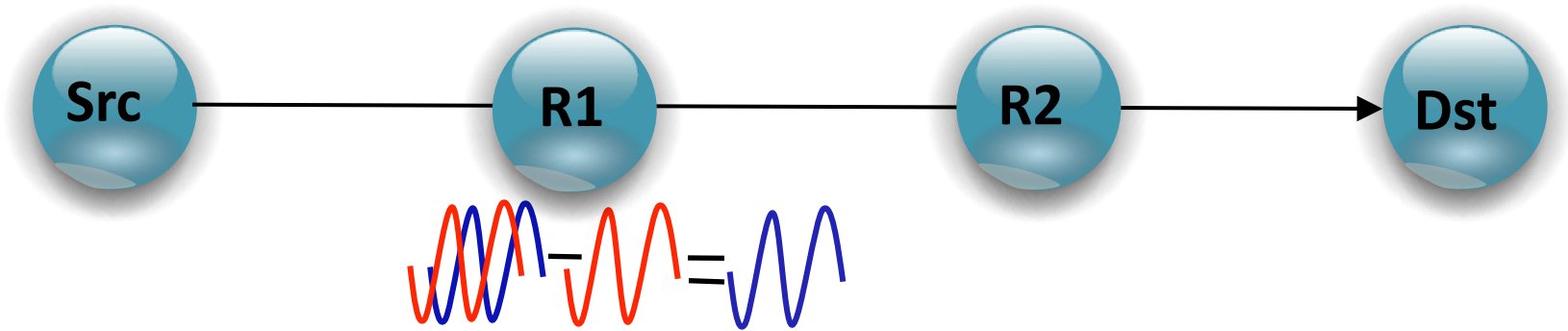
# Hidden Terminal Scenario



R2 and Src are hidden terminals

- Today : Simultaneous transmission → Collision
- ANC : Simultaneous transmission → Success!

# Hidden Terminal Scenario



## Other Benefits of ANC:

- First step toward addressing hidden terminals
- ANC extends network coding to new scenarios

How do we make it work?

# Practical Challenges

- Interfered signal is not exactly the sum

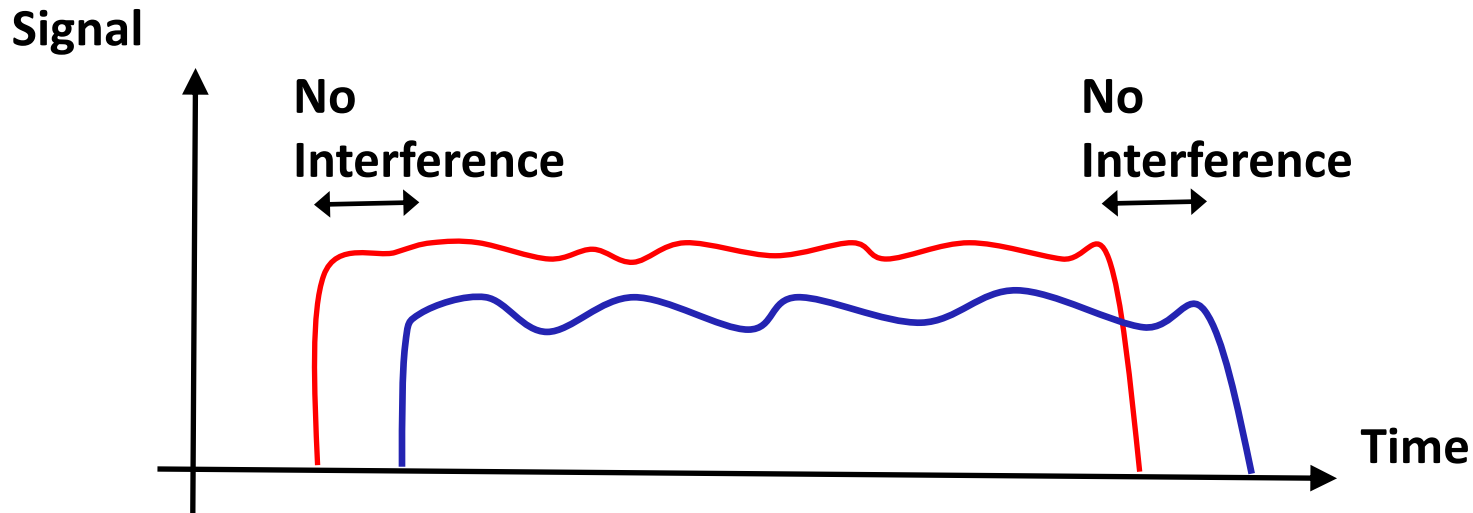
- Channel distorts signals

- Two signals are never synchronized

- It is not  $s_A(t) + s_B(t)$   
but  $f_1(s_A(t)) + f_2(s_B(t - T))$

Key Idea: Exploit Asynchrony!

# Key Idea: Exploit Asynchrony!



- Alice uses interference-free parts to estimate channel and timing
- Alice compensates for her interfering signal

**Exploit asynchrony to make it practical**



# Protocol

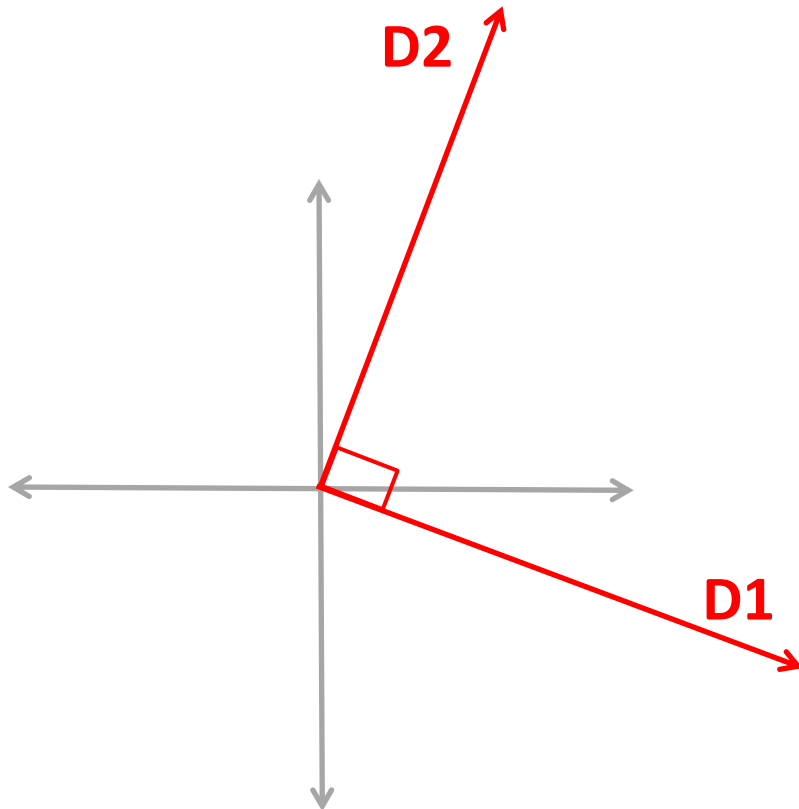
- Router senses idle medium and broadcasts a trigger to Alice and Bob
- Alice and Bob jitter their start times randomly and transmit
- Router amplifies and forwards interfered signal
- Alice and Bob receive and decode

**How do they decode?**

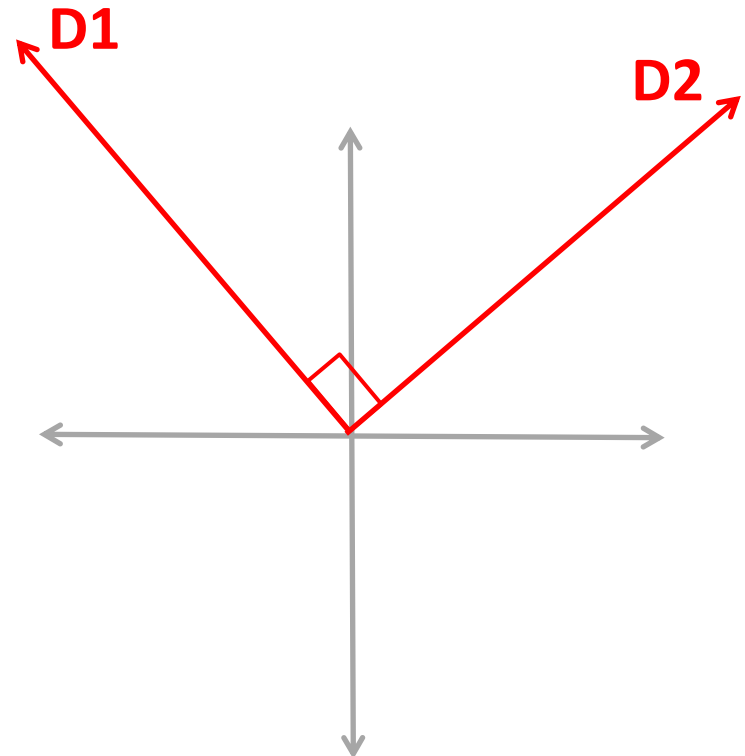
# Minimum Shift Keying

- Nodes transmit vectors on channel
- Focus on MSK (Minimum Shift Keying) modulation

**D2** leads **D1** by 90 degrees  
→ Bit "1"

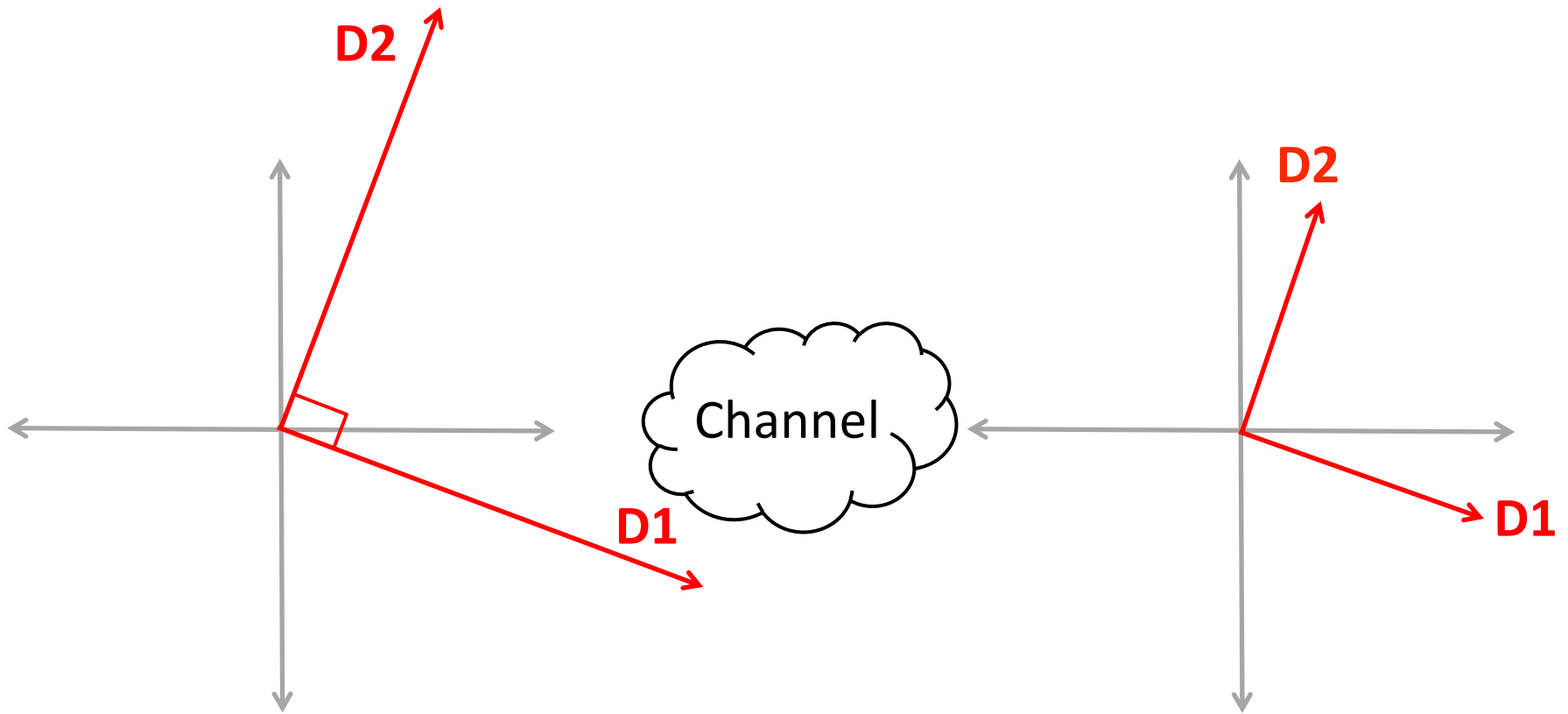


**D2** lags **D1** by 90 degrees  
→ Bit "0"



# Channel Effects

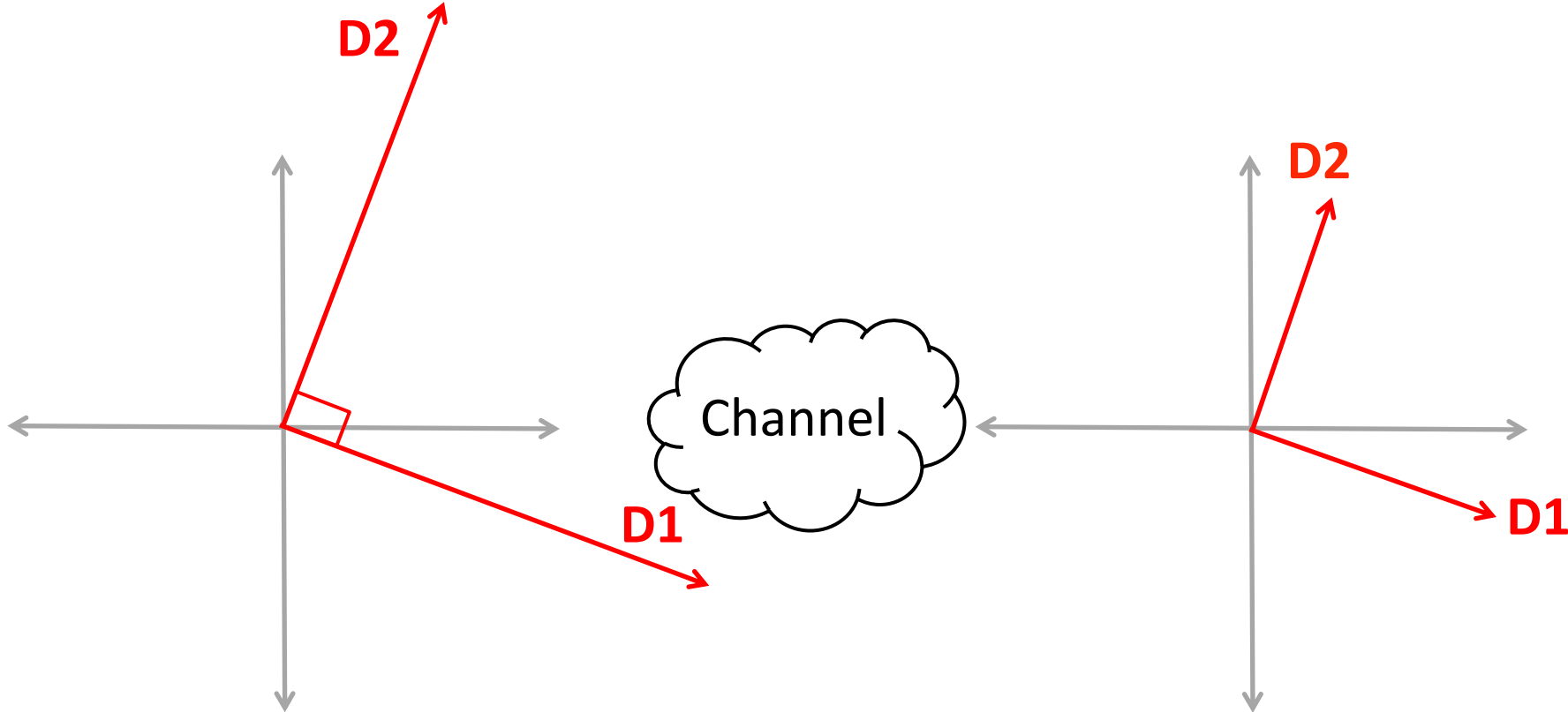
- Attenuation



**D2** and **D1** are attenuated by the same amount

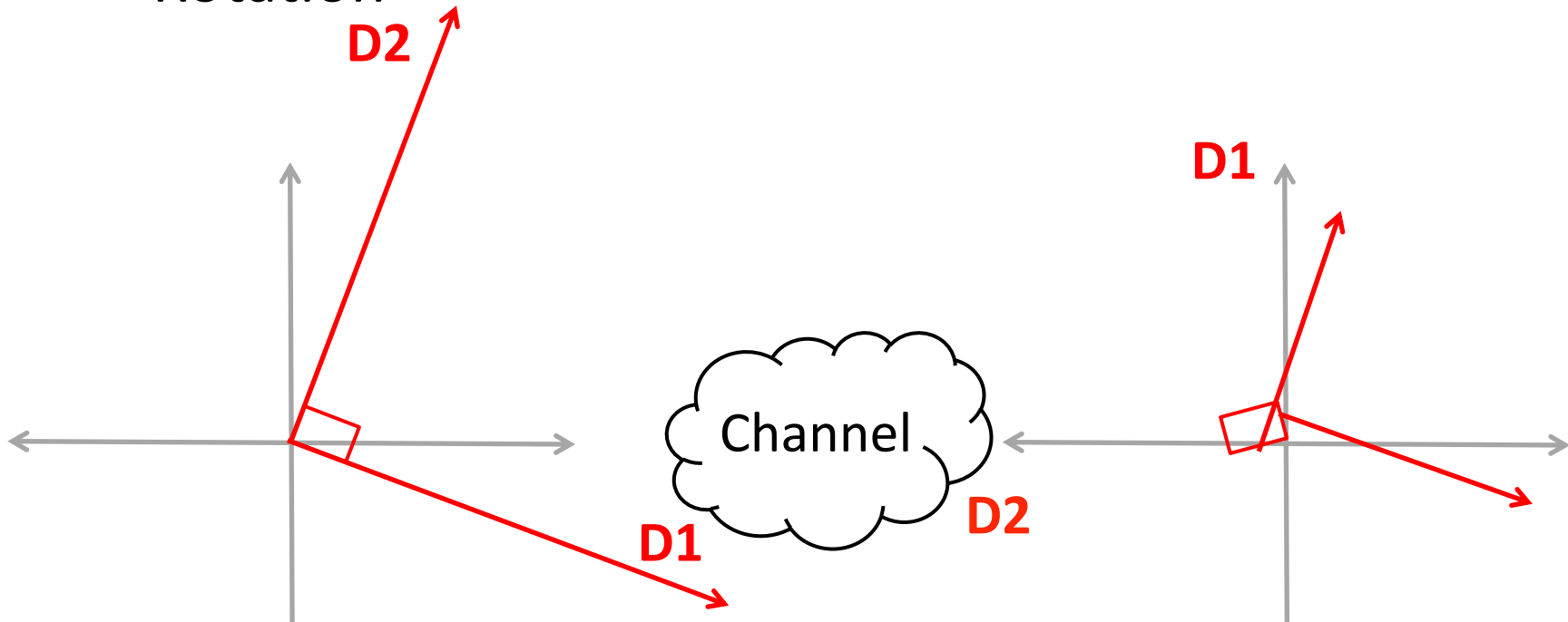
# Channel Effects

- Attenuation
- Rotation



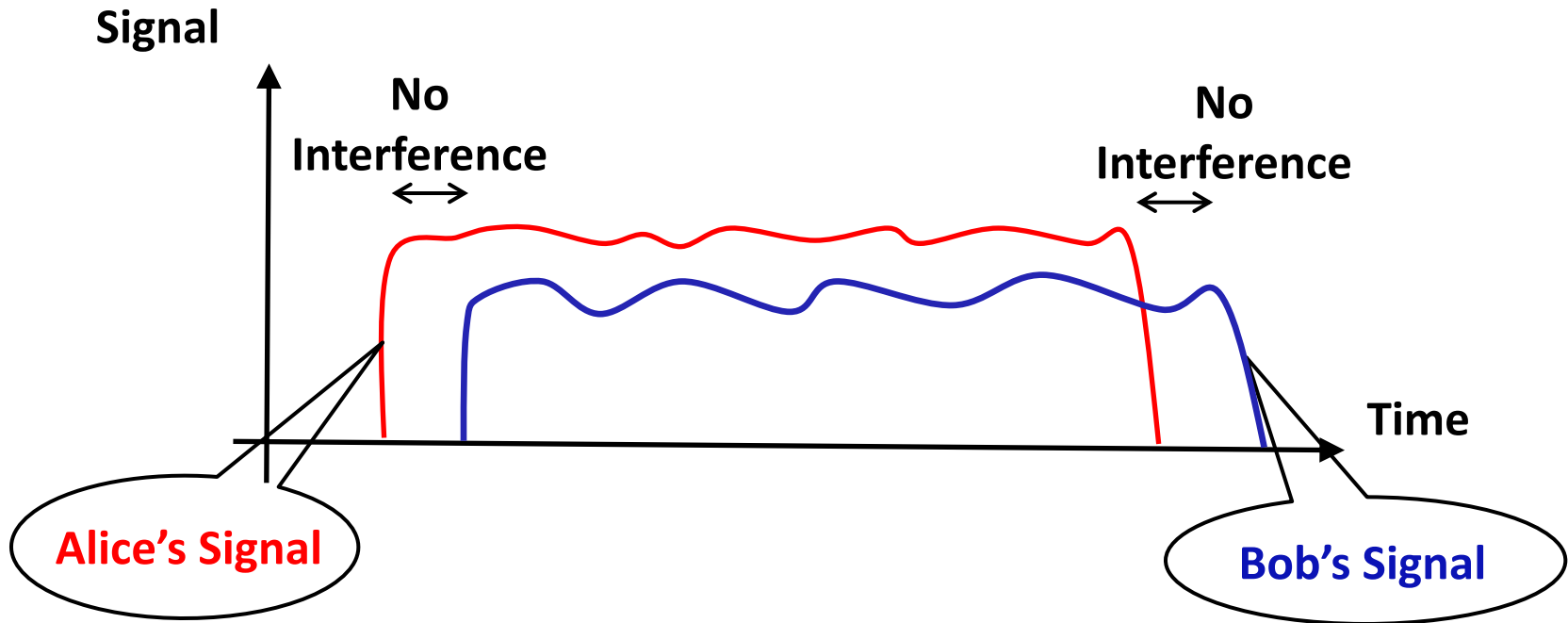
# Channel Effects

- Attenuation
- Rotation

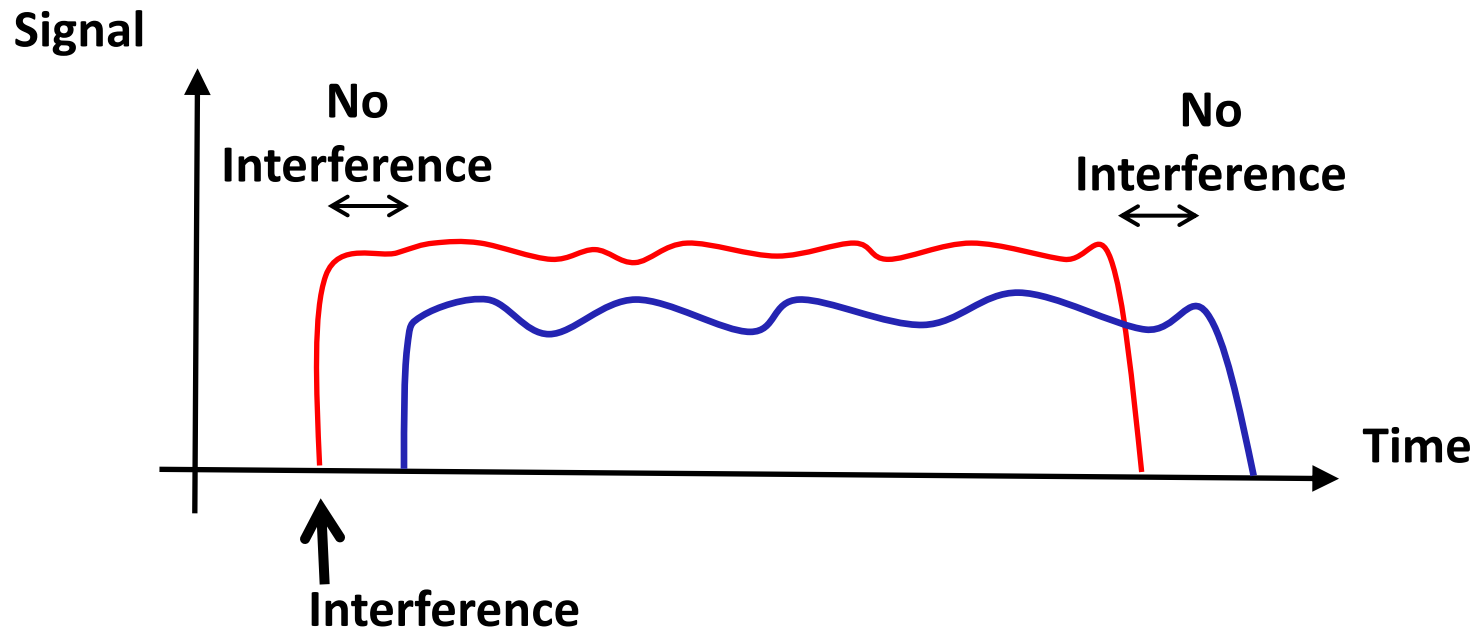


To decode, receiver computes angle between received vectors  
**Angle (D2, D1) = 90 degrees** → Bit "1" was transmitted

# So, How Does Alice Decode?

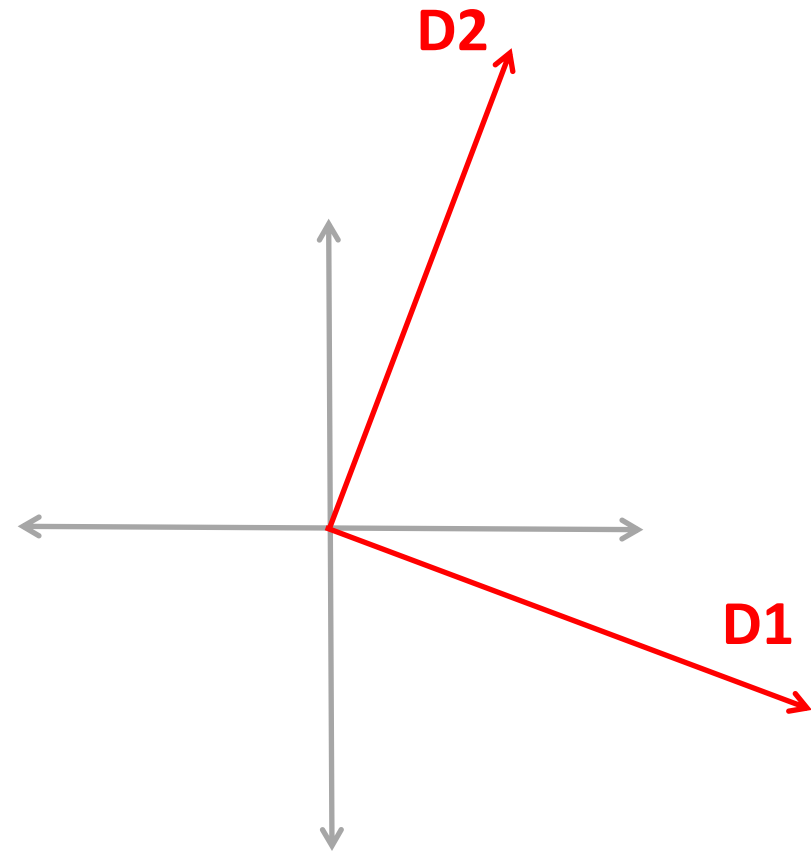


# So, How Does Dina Decode?



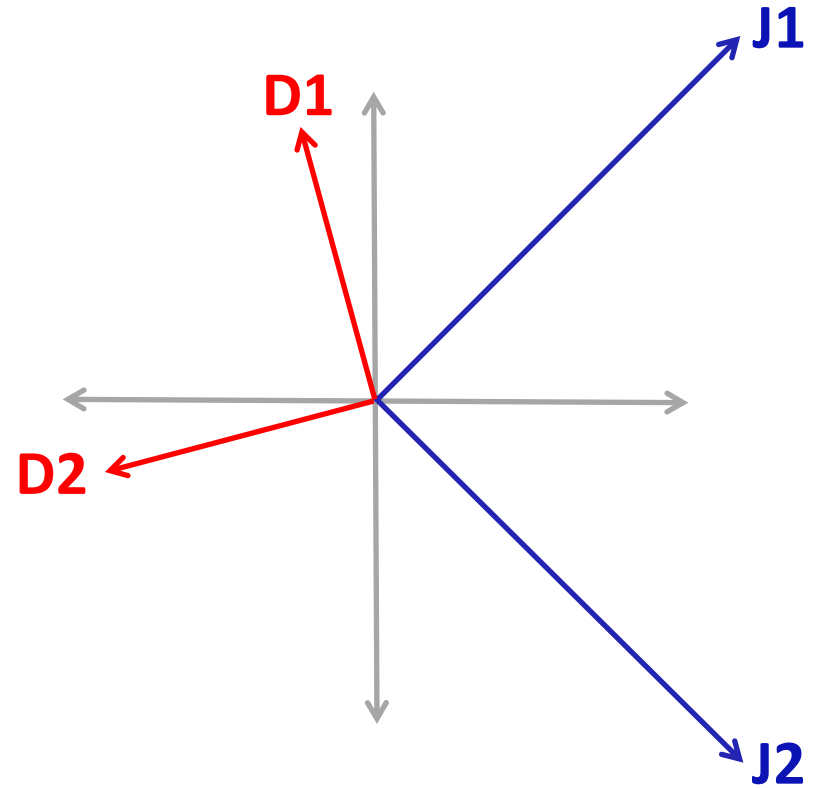
- Small uninterfered part at the start
- Decodes uninterfered part via standard MSK demodulation
- Once interference starts, Alice changes decoding algorithm

● What did Alice send?

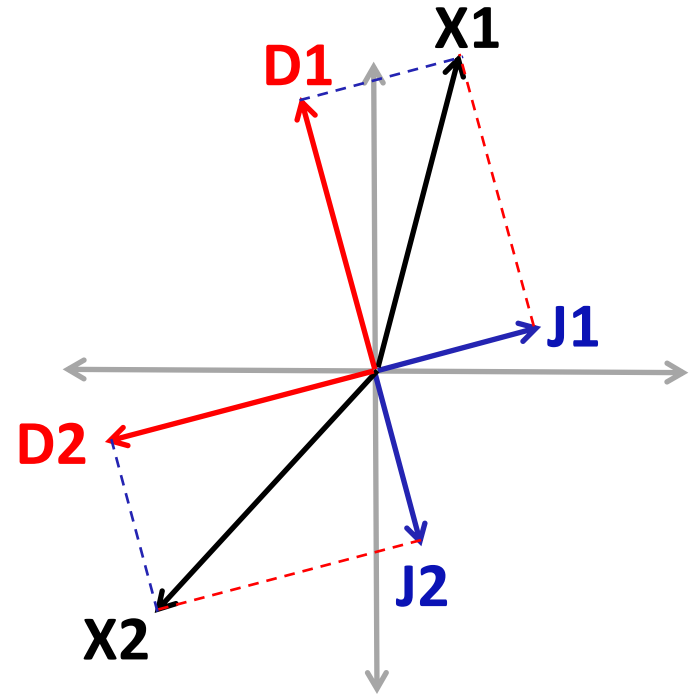




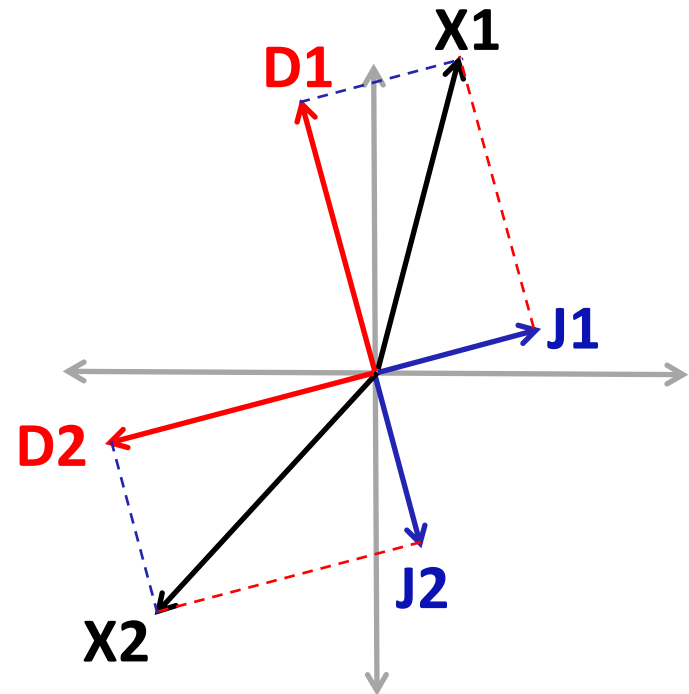
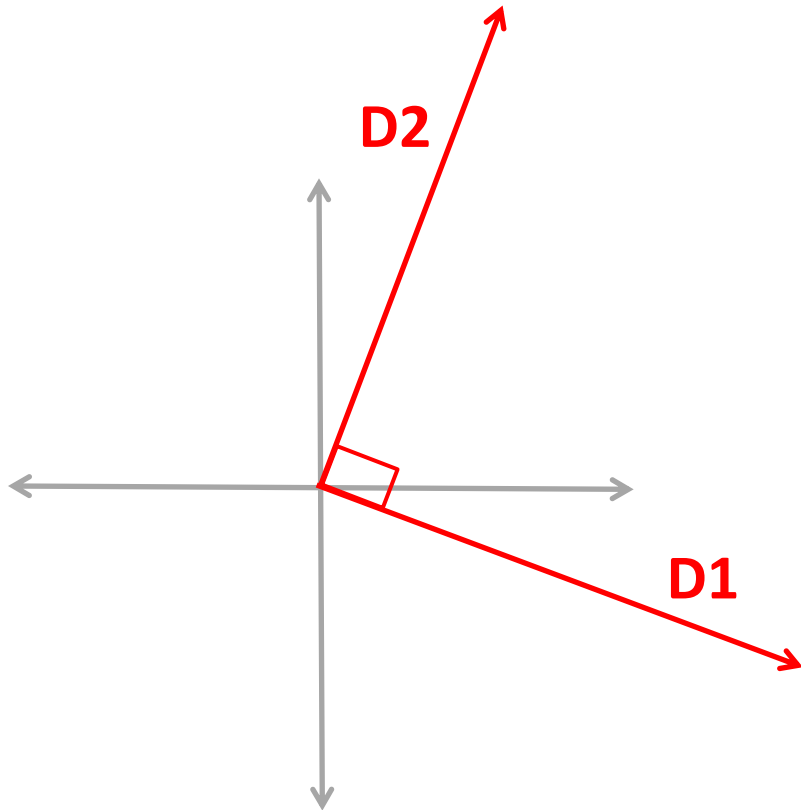
- What did Alice send?
- What did Bob send?



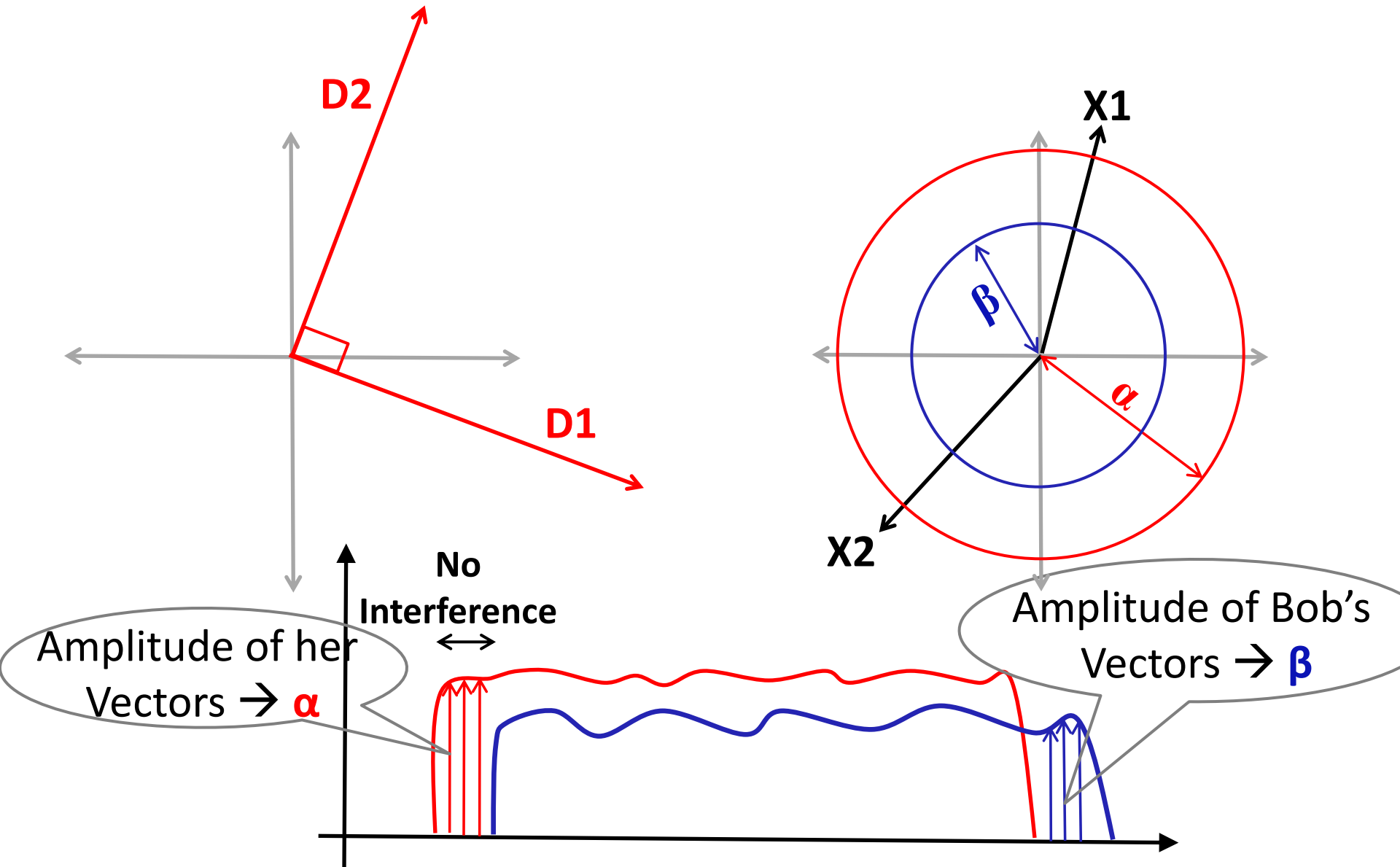
# ● What is Interference → Vector addition



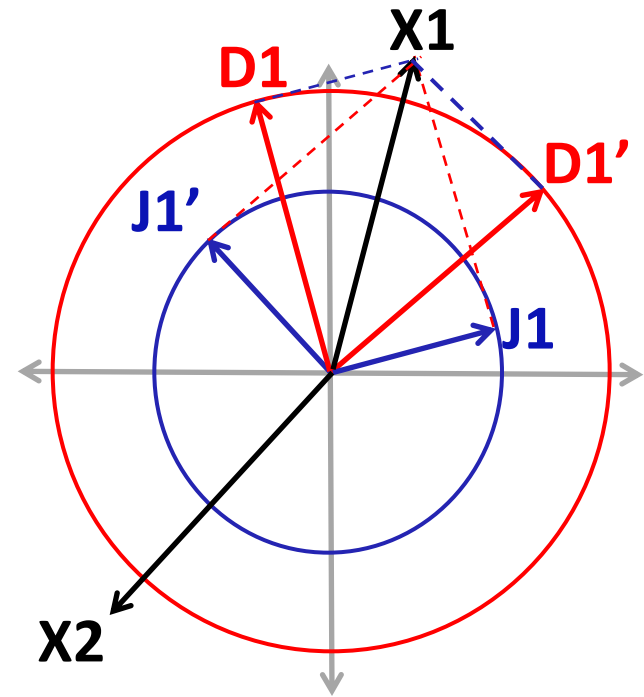
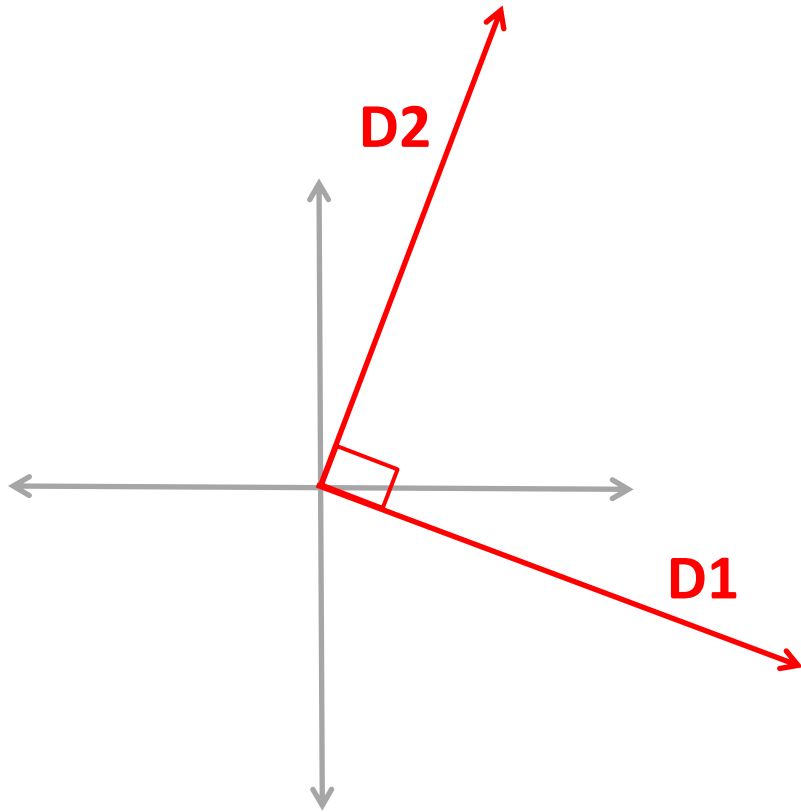
● What does Alice know?



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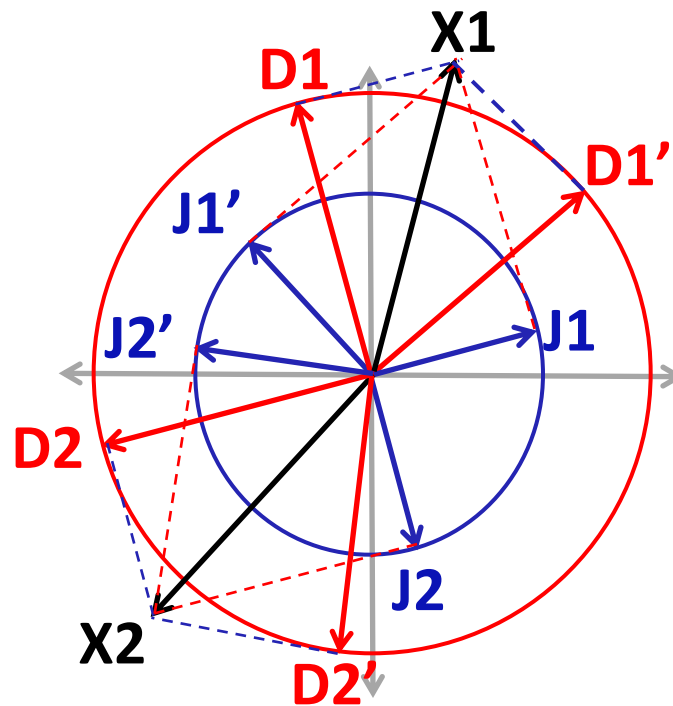
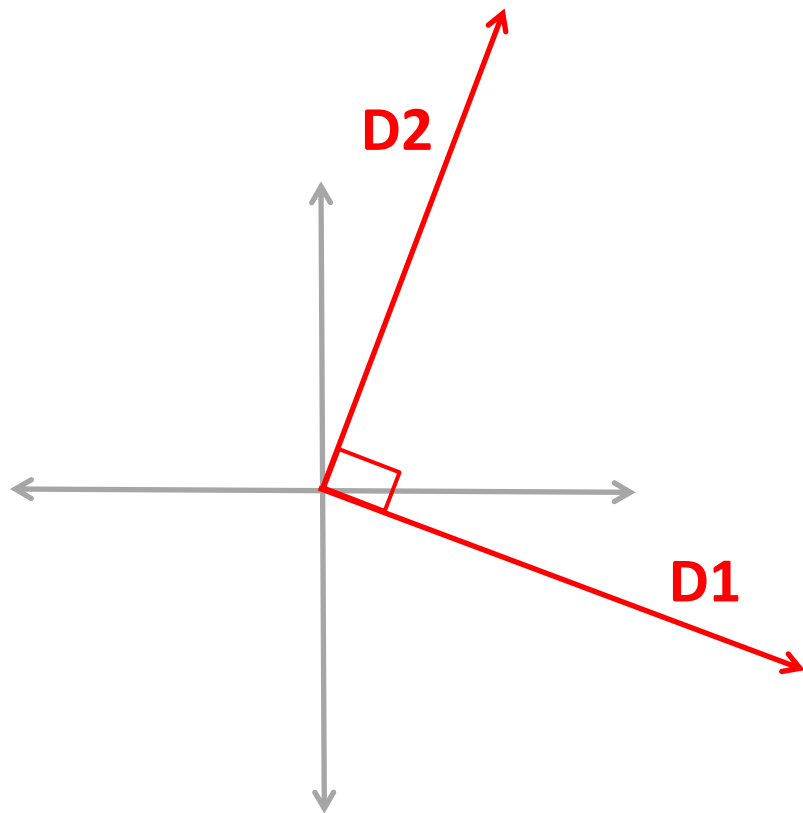


● What does Alice know?



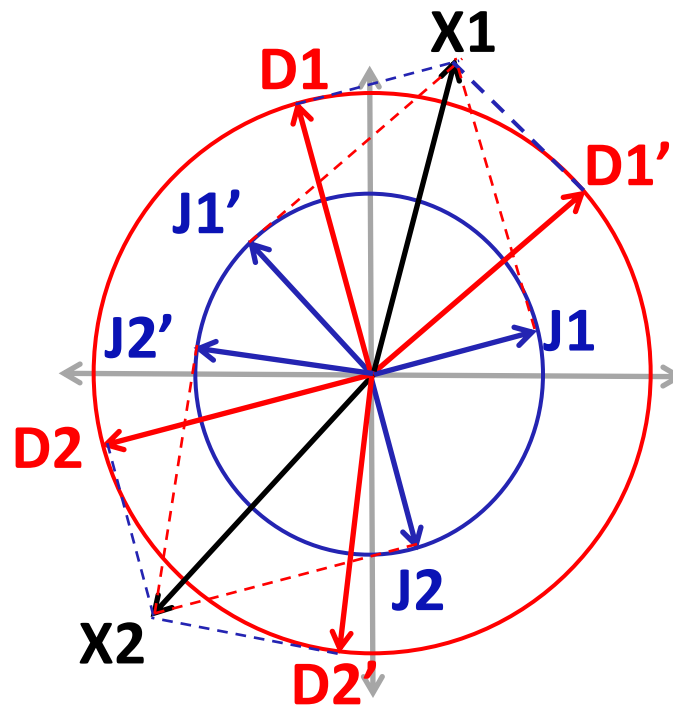
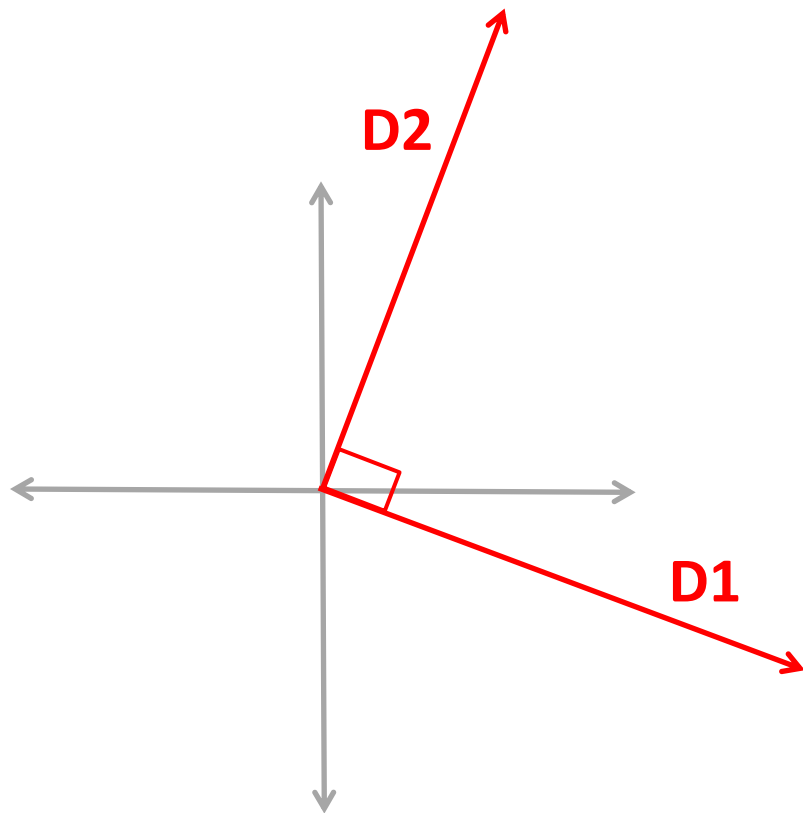
● Alice finds solutions for  $X1$  and  $X2$

● What does Alice know?



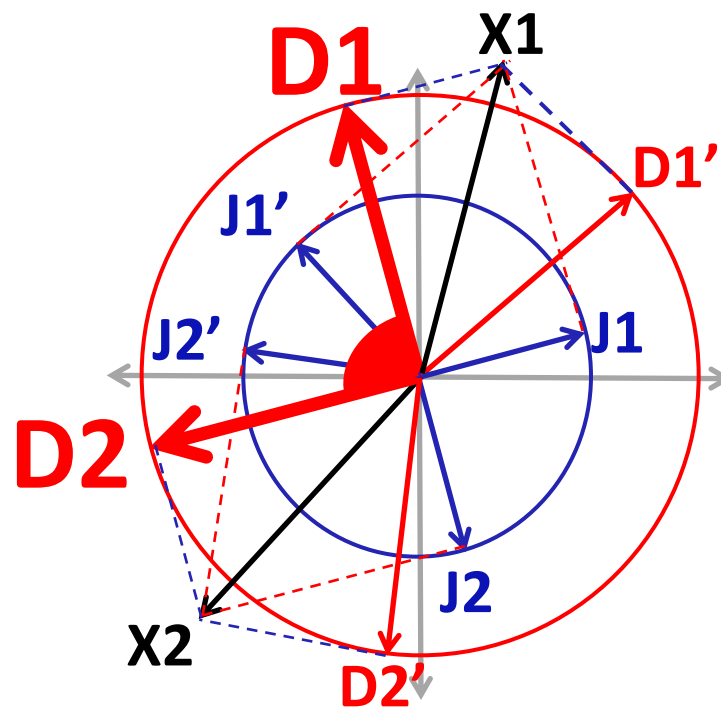
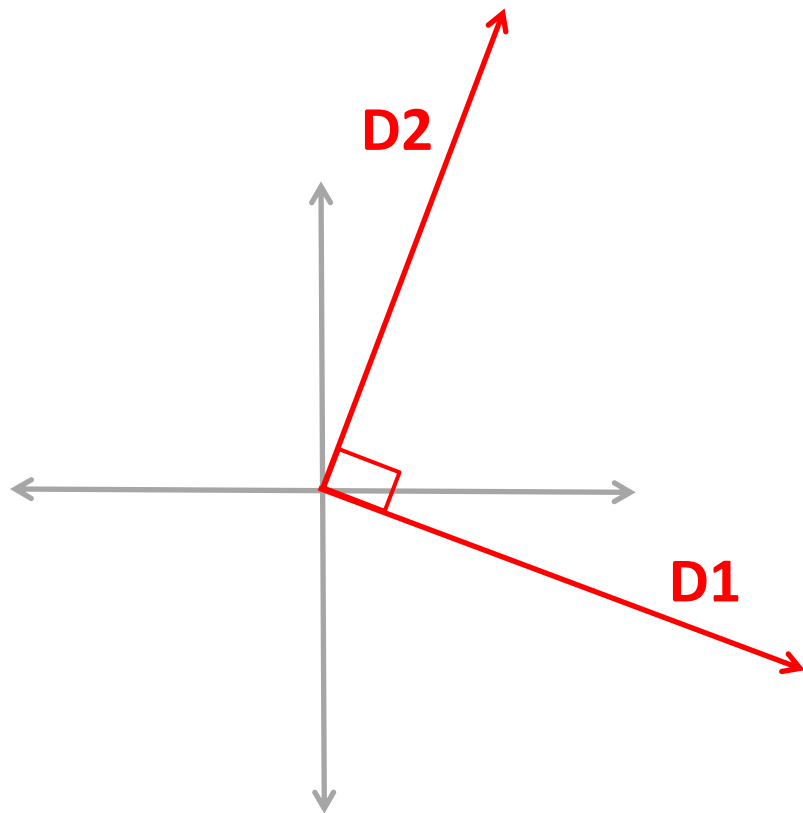
**Two solutions for each interfered vector!**

● What does Alice know?



**Four possible angles!**

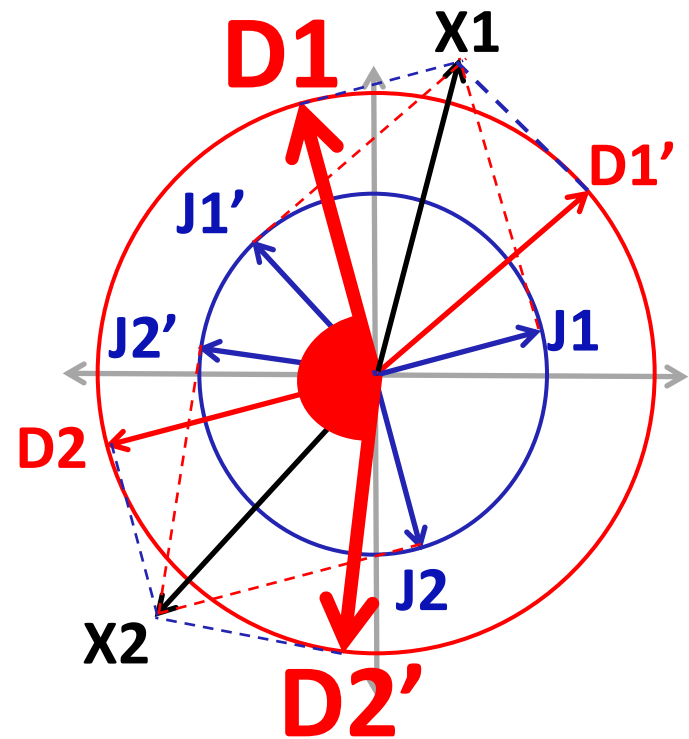
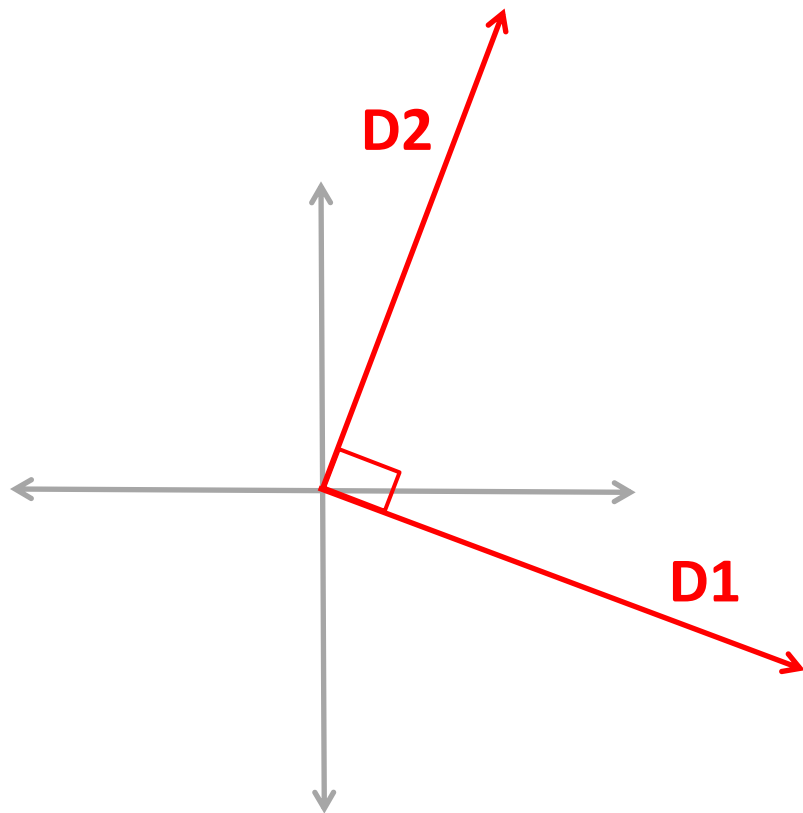
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Four possible angles!

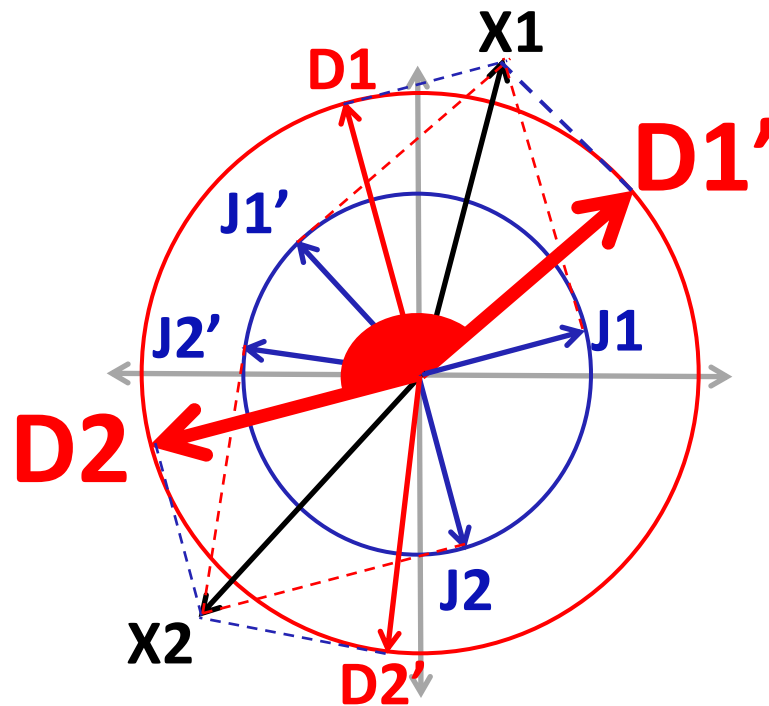
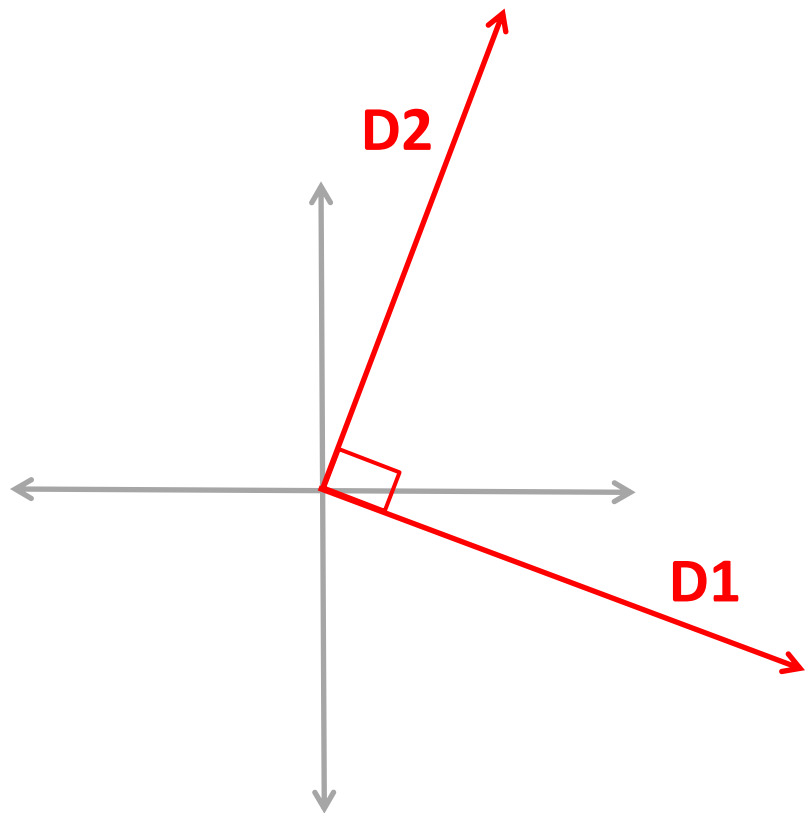


● What does Alice know?



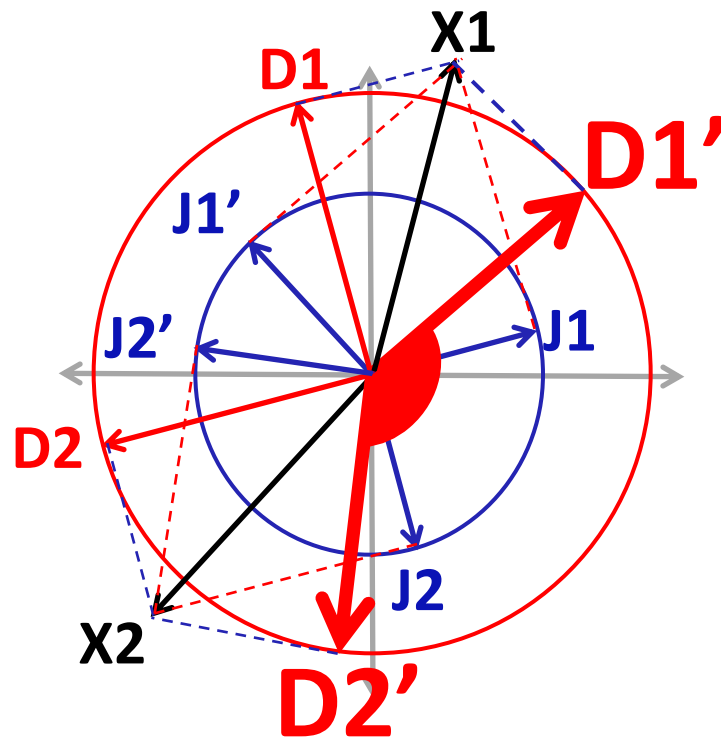
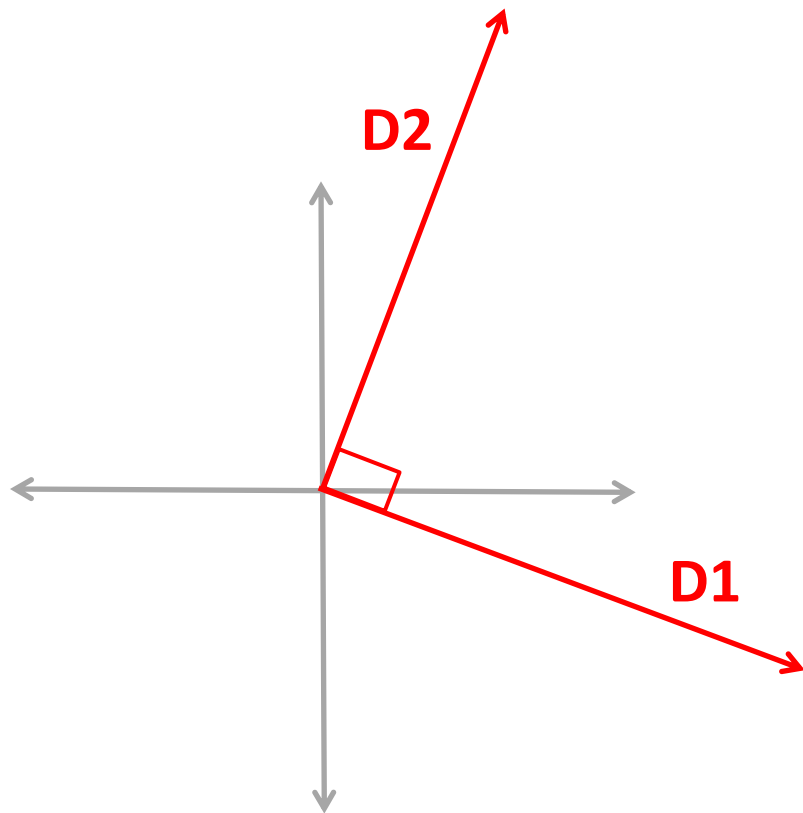
Four possible angles!

● What does Alice know?



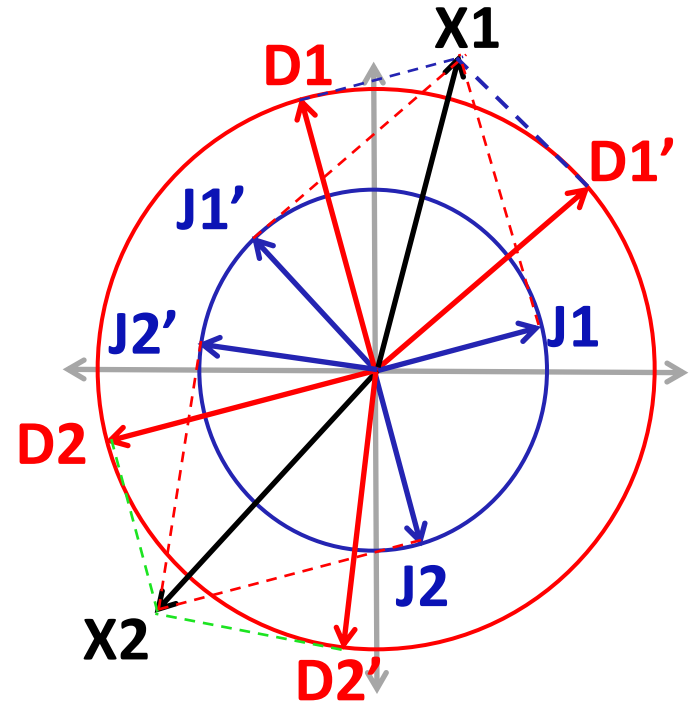
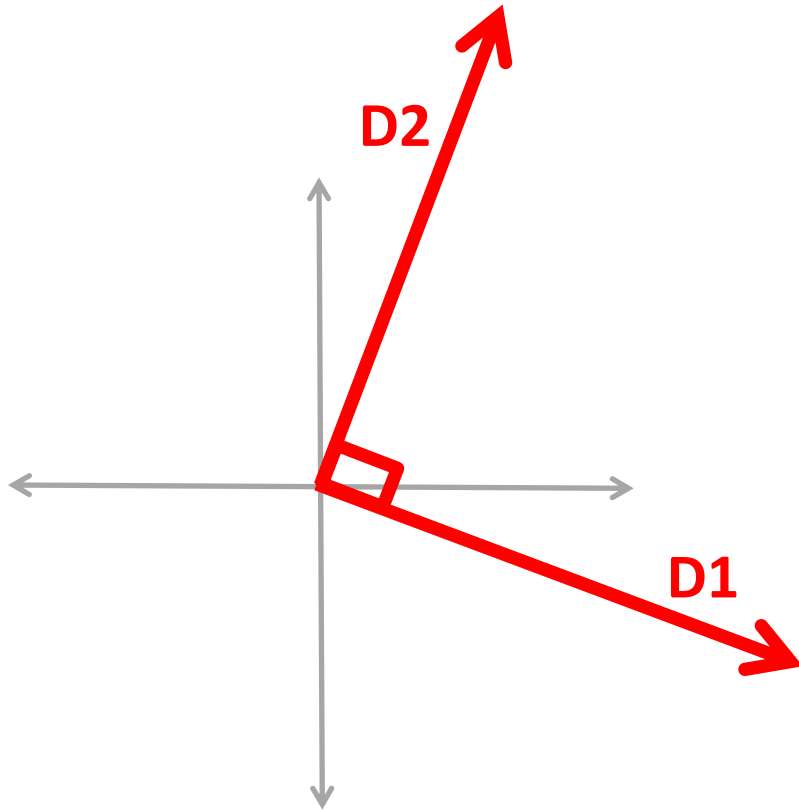
**Four possible angles!**

● What does Alice know?



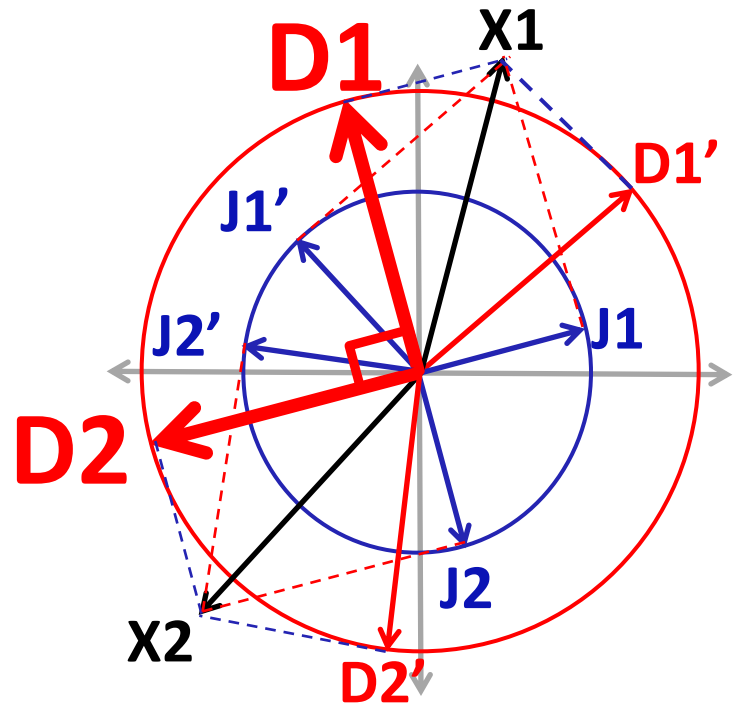
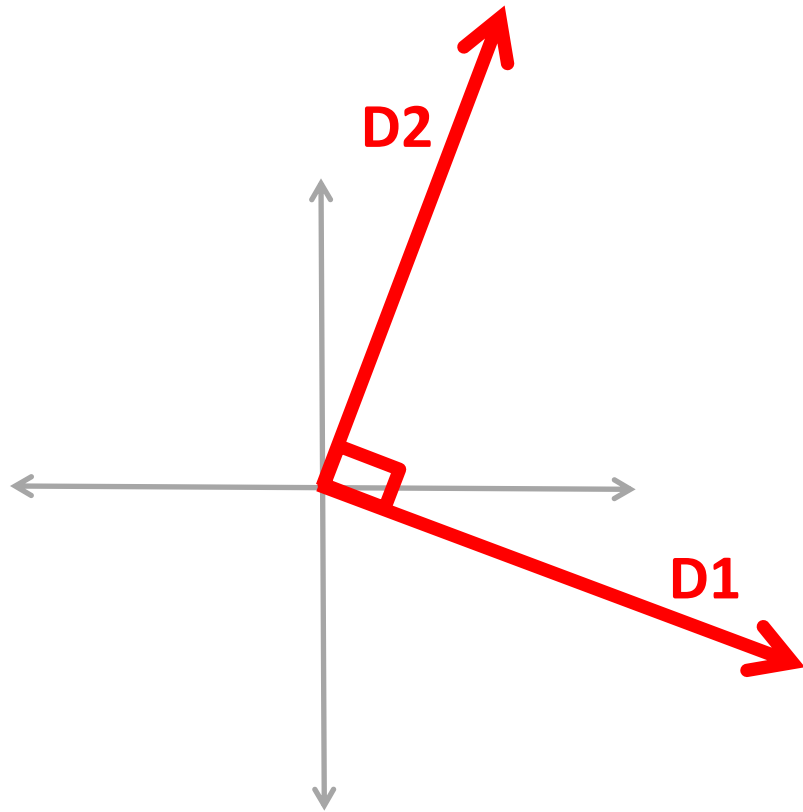
Four possible angles!

● What does Alice know?



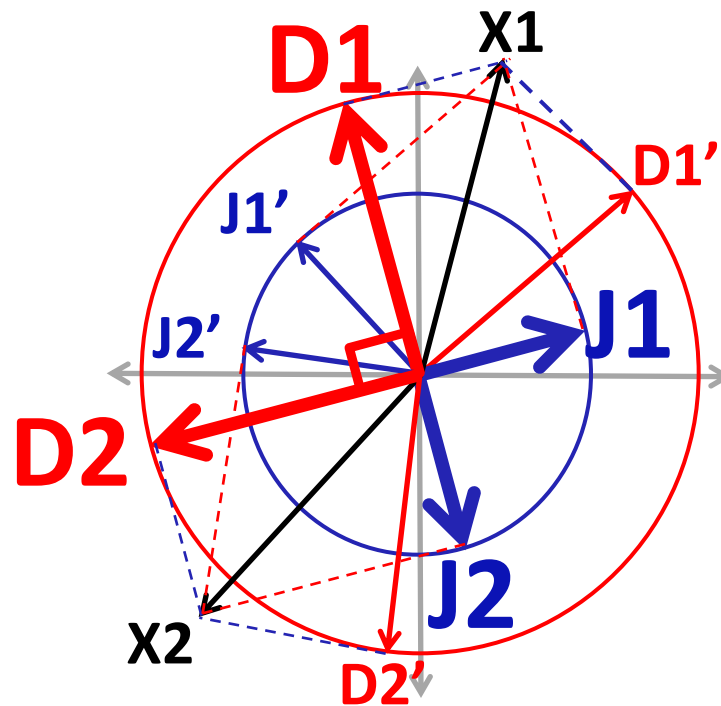
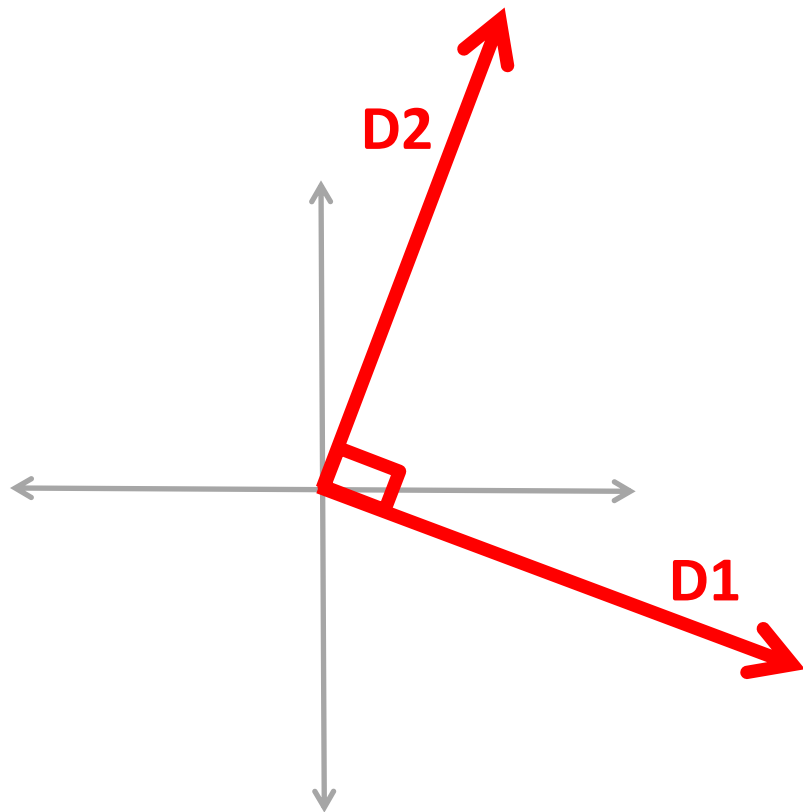
Pick the correct angle  $\rightarrow$  90 degrees

● What does Alice know?



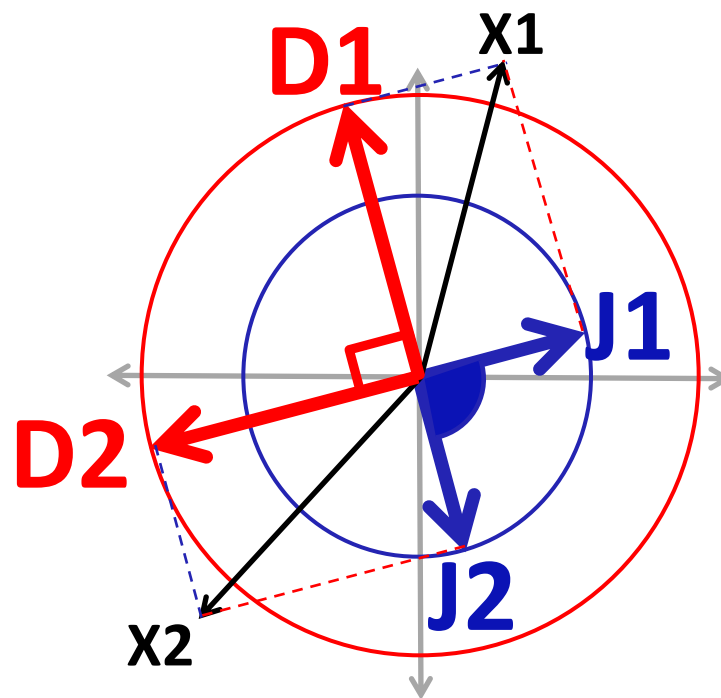
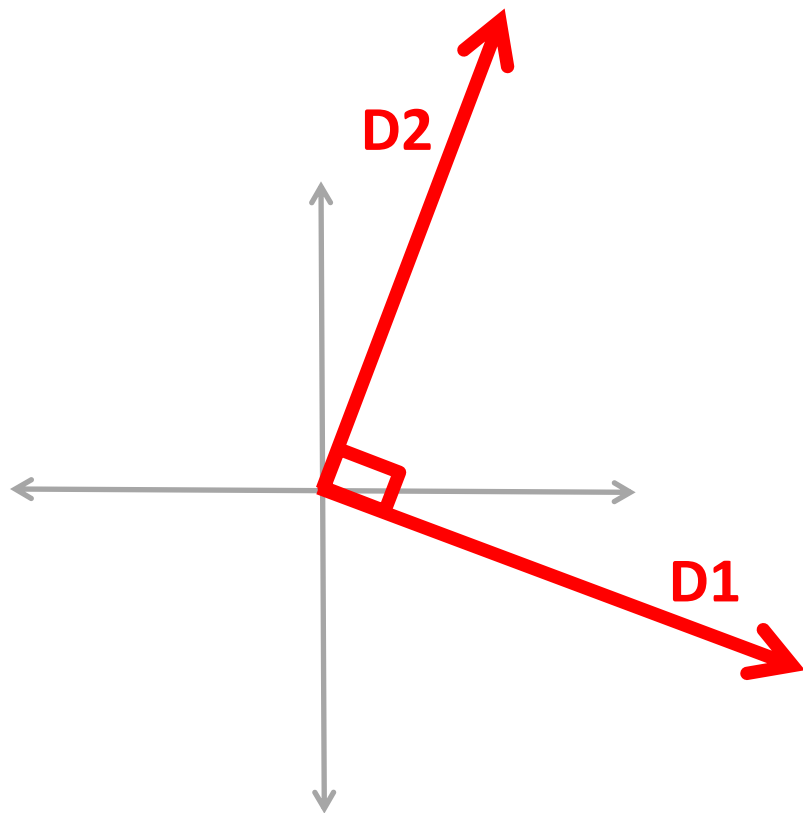
Pick the correct angle  $\rightarrow$  +90 degrees

● What does Alice know?



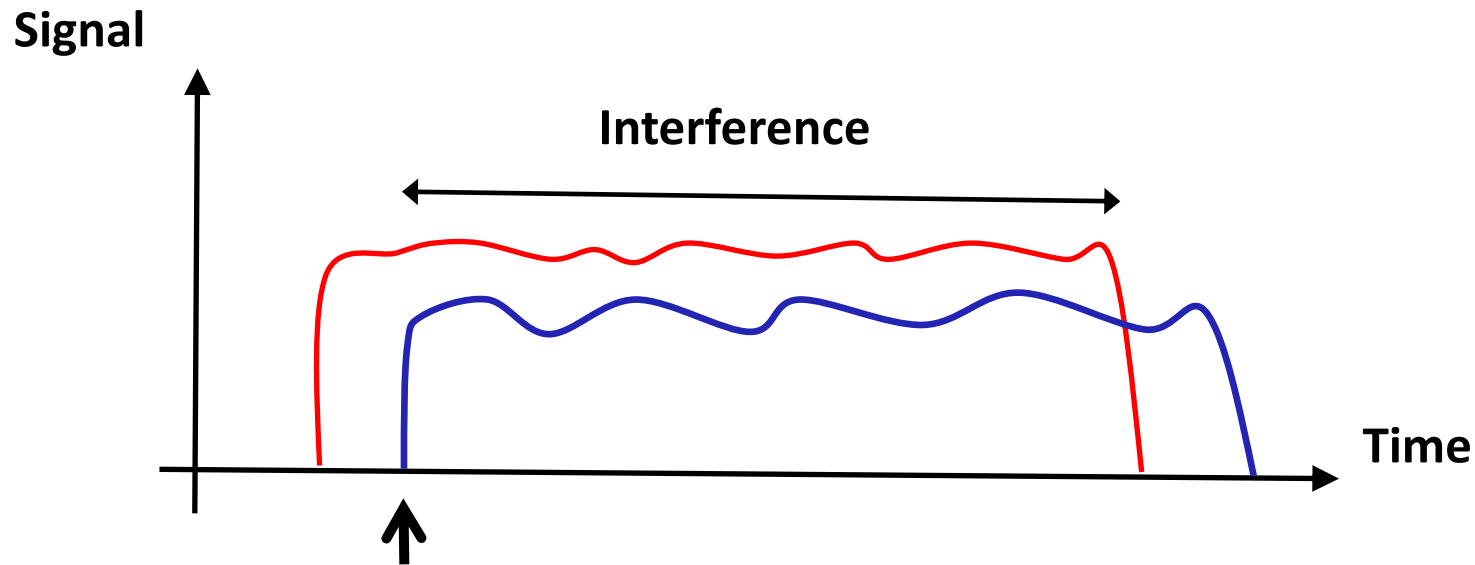
Dictates solution for Bob's vectors!

● What does Alice know?



● Alice finds angle between  $J1$  and  $J2$  and decodes

# Decoding Algorithm – Decoding interference



- Decode rest of the interfered part using this algorithm
- Decode final uninterfered part from Jon via standard MSK demodulation



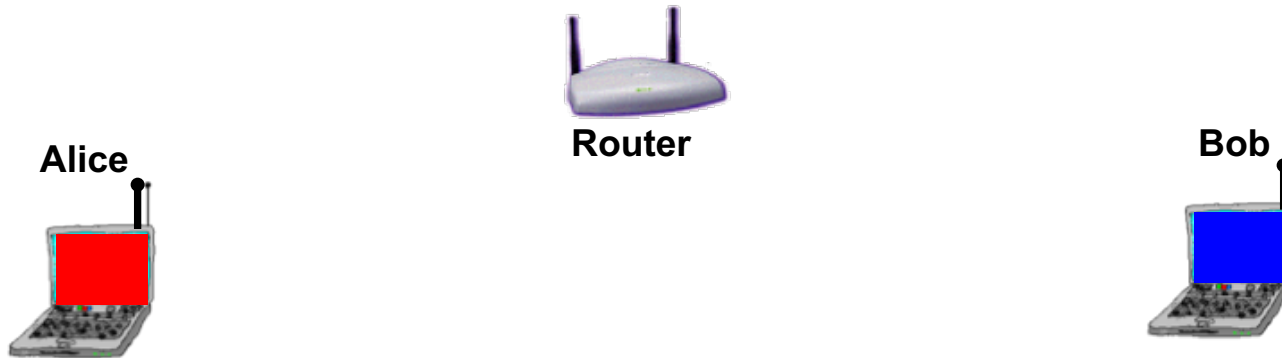
Performance

# ANC Implementation

- Software – GNURadio codebase
- Hardware – USRP frontend
- 2.4-2.48 GHz frequency range
- SNR of 20-30 dB
- Canonical topologies in mesh networks

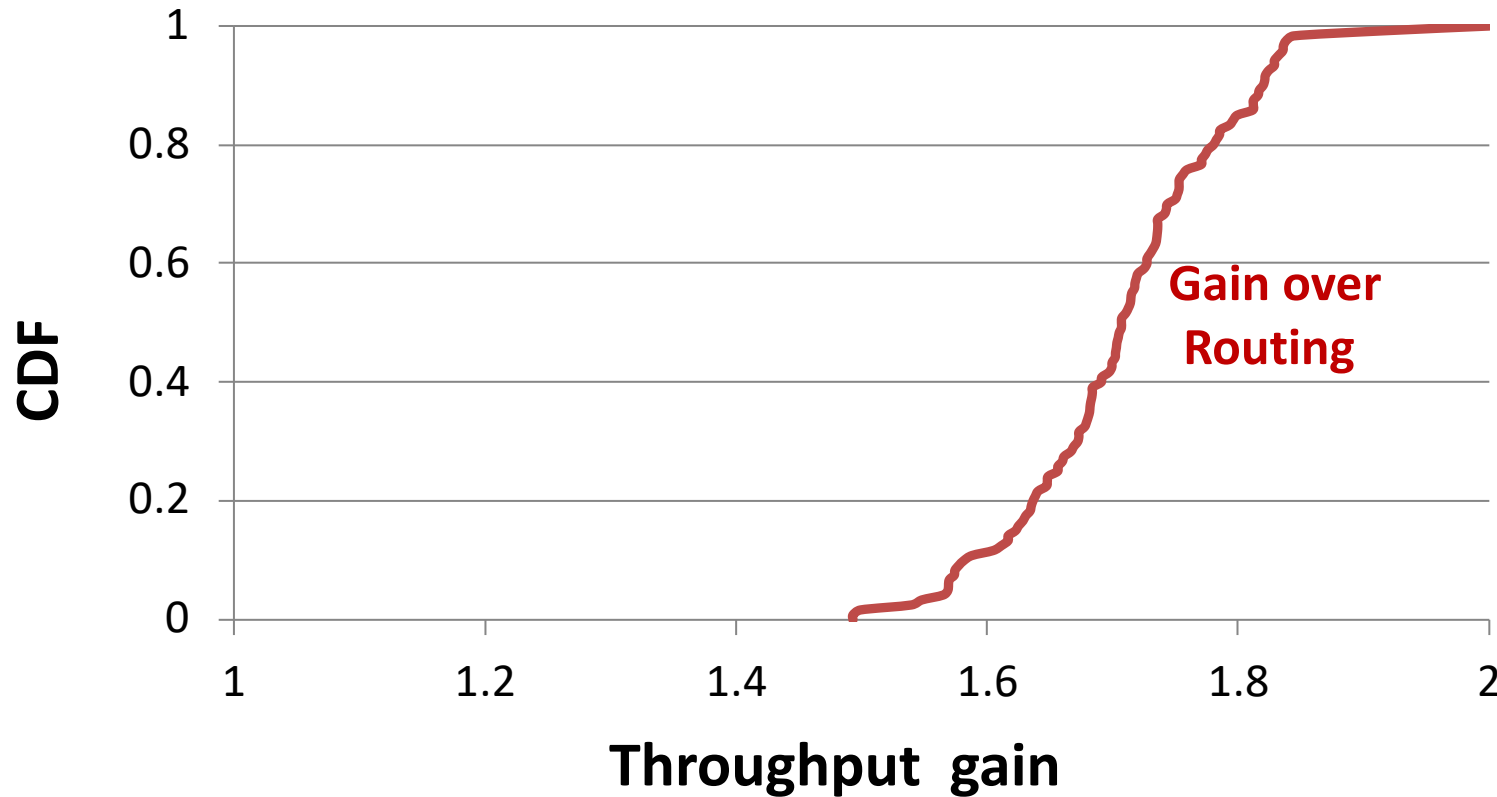


# Alice and Bob



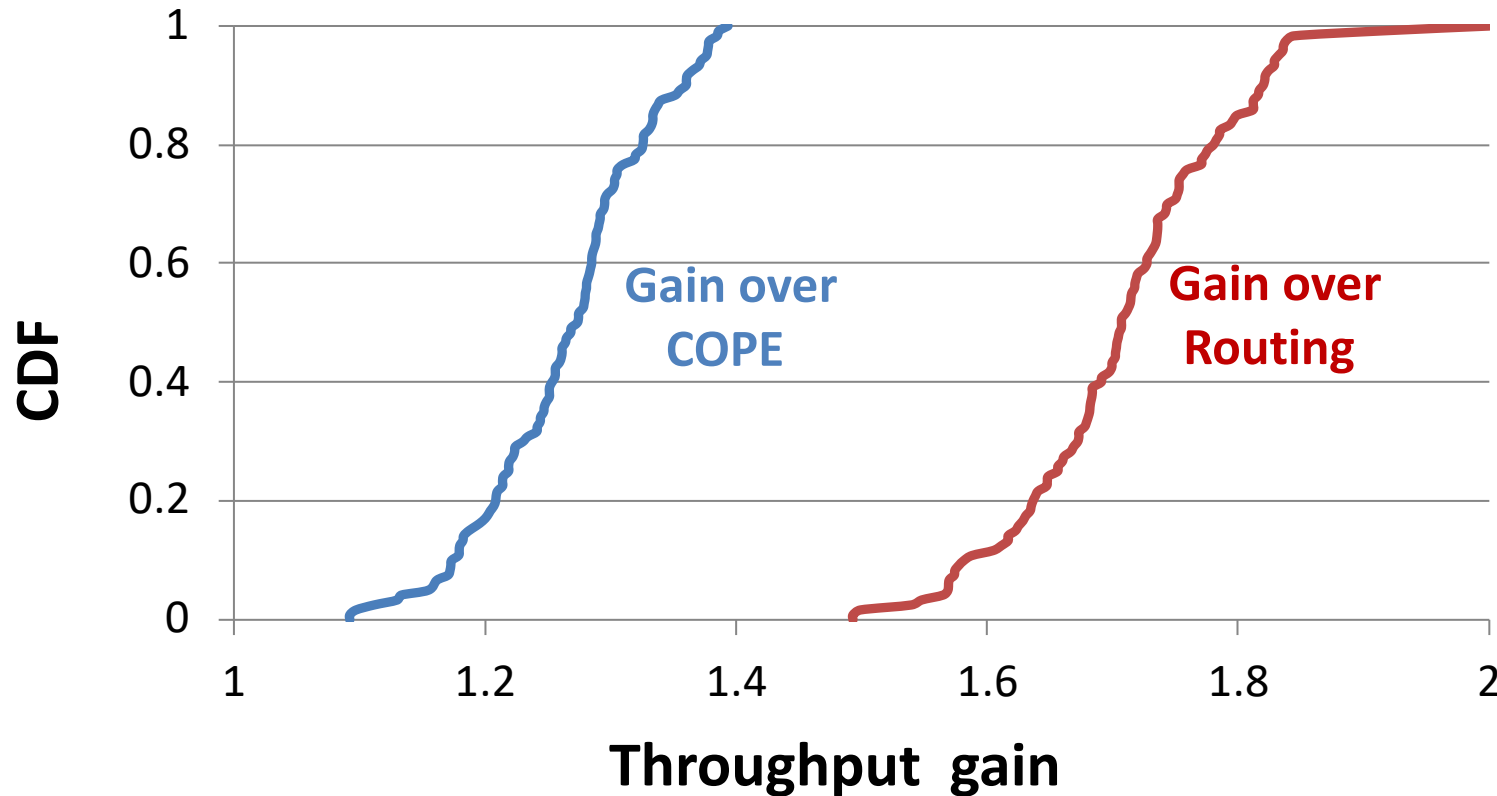
- ANC throughput gain over current  $4/2 = 2$
- ANC throughput gain over COPE  $3/2 = 1.5$

# Throughput gain for Alice & Bob scenario



**Median Gain over Routing – 70%**

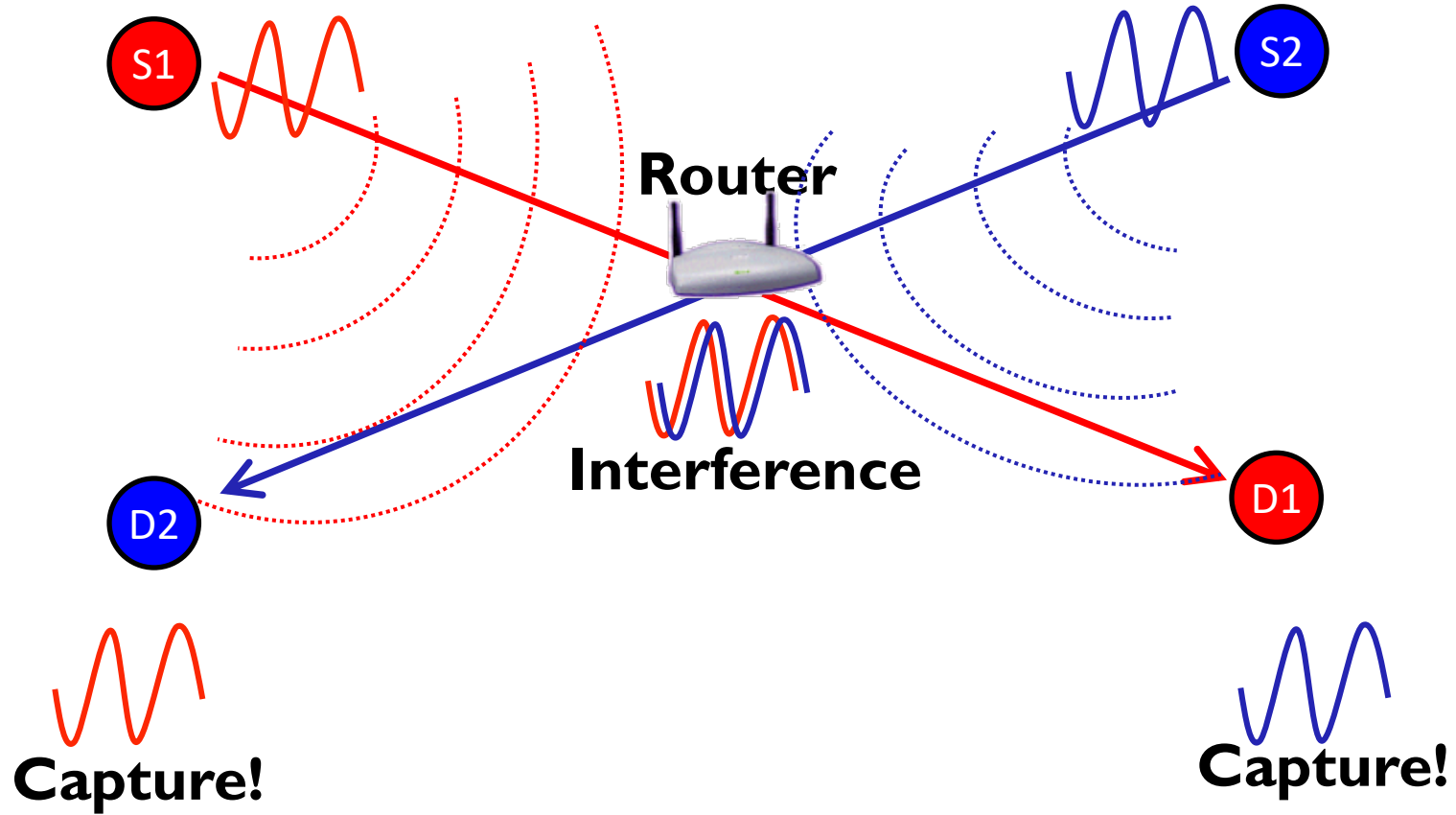
# Throughput gain for Alice & Bob scenario



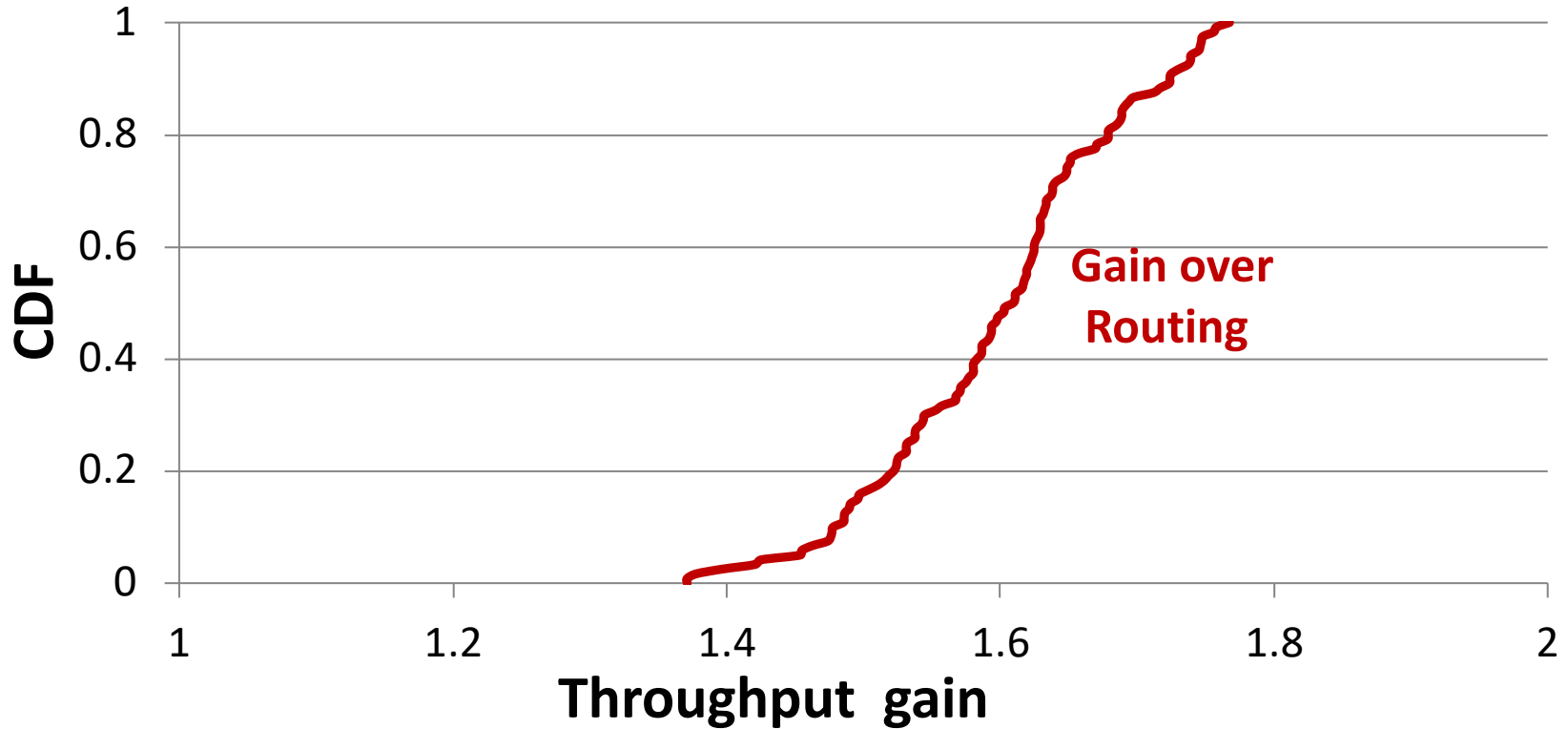
**Median Gain over Routing – 70%**

**Median Gain over COPE – 30%**

# X topology

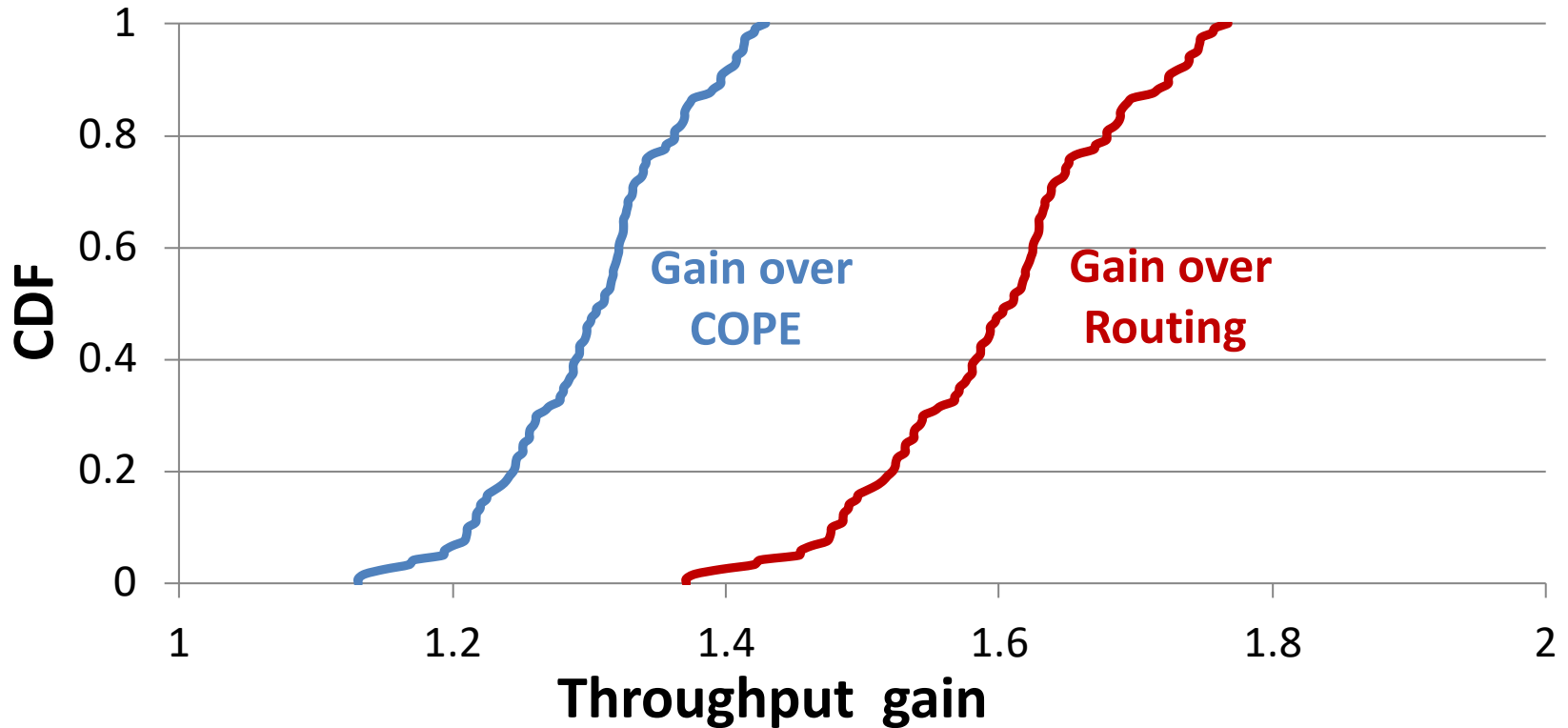


# Throughput gain – X topology



**Median Gain over Routing – 65%**

# Throughput gain – X topology

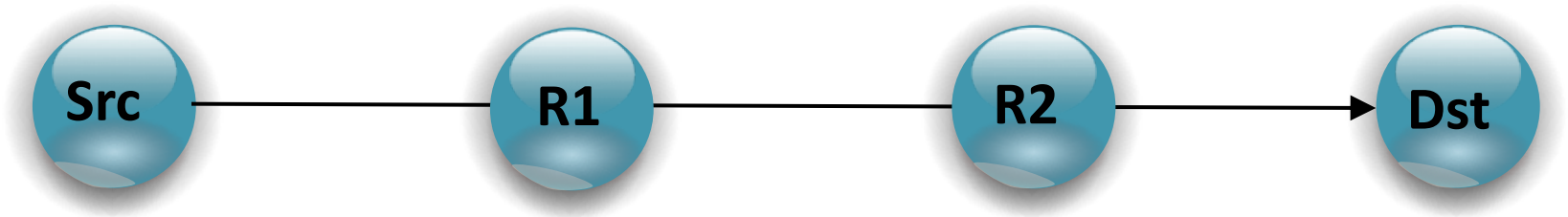


**Median Gain over Routing – 65%**

**Median Gain over COPE – 28%**

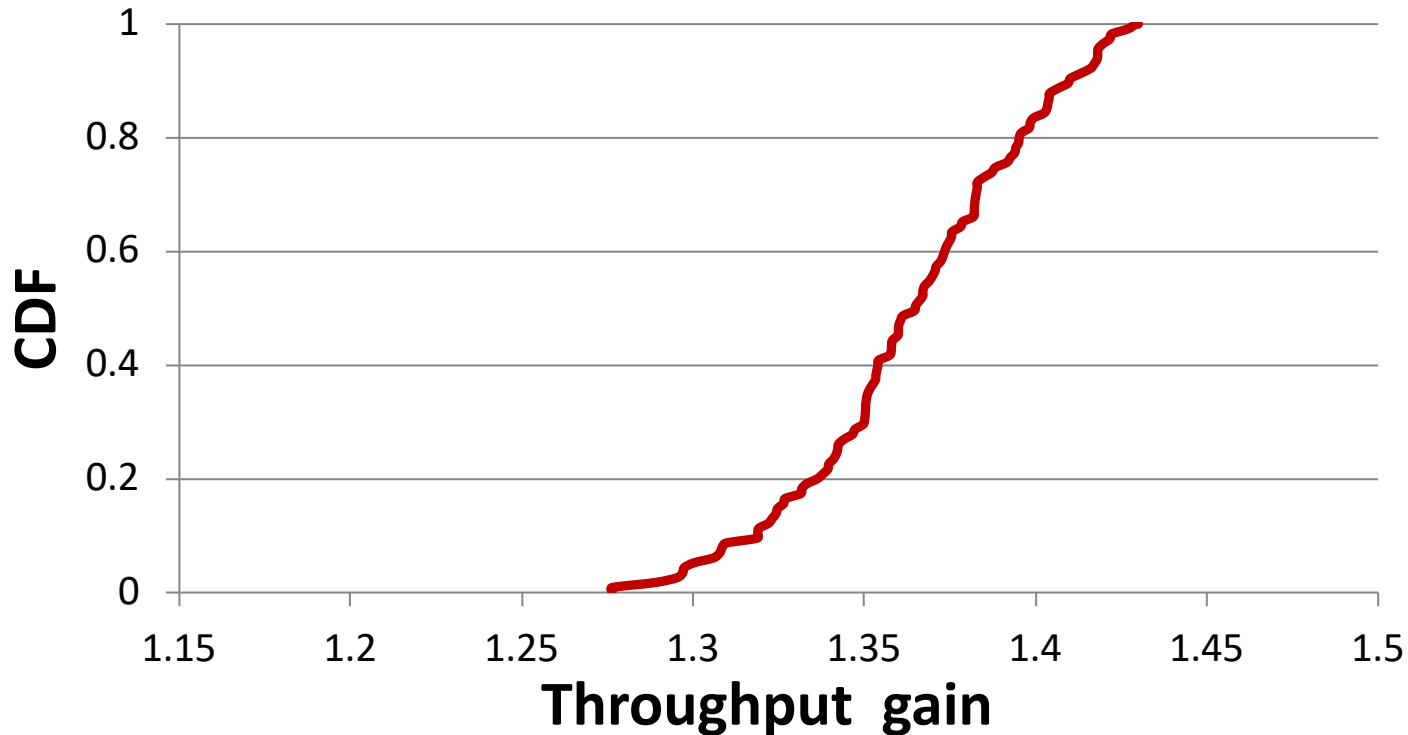


# Chain topology



- ANC throughput gain over current  $3/2 = 1.5$

# Throughput gain – Chain topology



**Median Gain over Routing – 37%**

# ANC Limitations

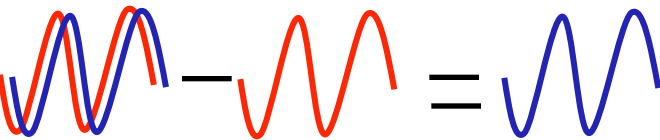
- Complexity.
- Buffering analog samples... expensive.
- Amplify noise!

# Analog Network Coding

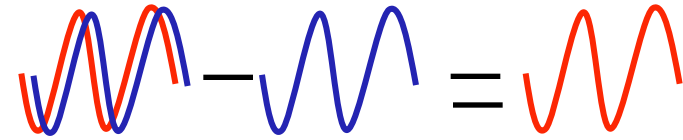


Router

Alice



Bob



**Analog Network Coding requires 2 time slots**

**Can we do it in 1 time slot?**

# Conclusion

- Network Coding :
  - Improve throughput & resilience to loss
  - Less coordination
  - Inter- & Intra- flow network coding
  - Analog coding using wireless channels
- Shifts in the design of wireless networks to recognize wireless for what it is:
  - Embrace Broadcast
  - Embrace Interference