ECE 598HH: Advanced Wireless Networks and Sensing Systems

Lecture 9: MIMO Part 2 Haitham Hassanieh



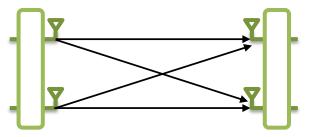


*Some of the slides in this lecture are courtesy of on Kate Lin, Hariharan Rahul, & Omid Abari

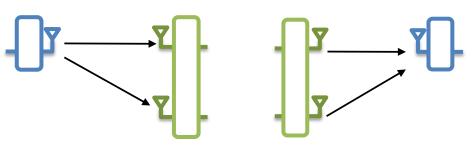
Last Lecture

This Lecture

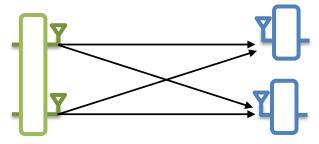
MIMO Multiplexing Gain



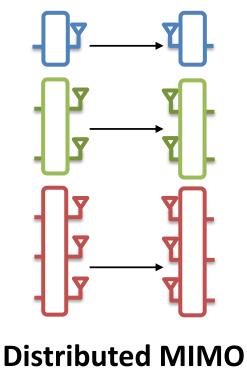
MIMO TX/RX Diversity Gain

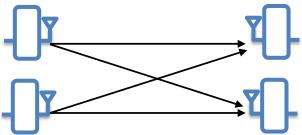


MU-MIMO Beamforming



Heterogeneous # of antennas (Interference Nulling/Alignment)















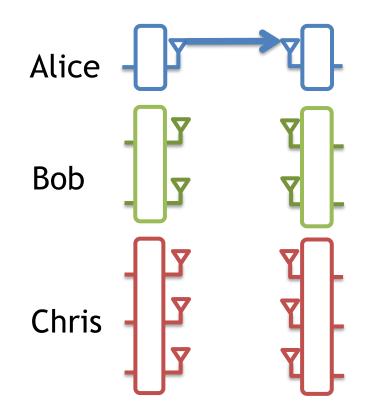
1-antenna devices

2-antenna devices

3-antenna devices

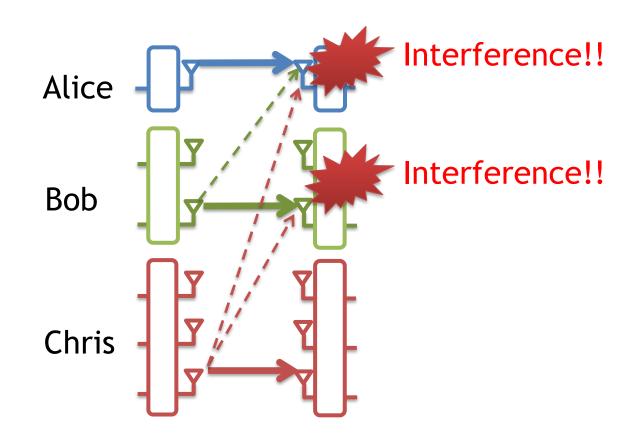
Wireless nodes increasingly have heterogeneous numbers of antennas

Consider a scenario with Tx-Rx pairs that have a different number of antennas



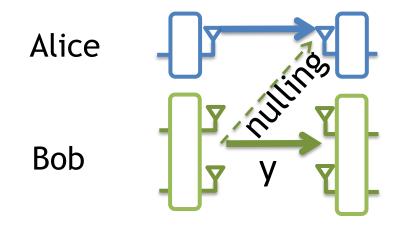
When a single-antenna node transmits, multi-antenna nodes refrain from transmitting But, MIMO Nodes Can Receive Multiple **Concurrent Streams** Alice Bob Chris

It's Not That Simple



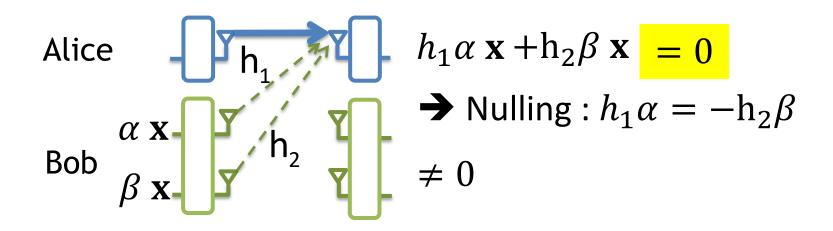
But, how do we transmit without interfering at receivers with fewer antennas?

Interference Nulling



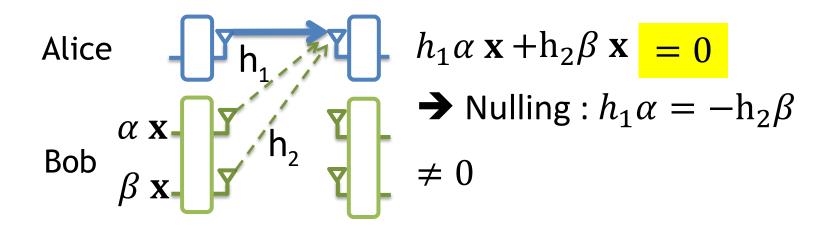
• Signals cancel each other at Alice's receiver

Interference Nulling



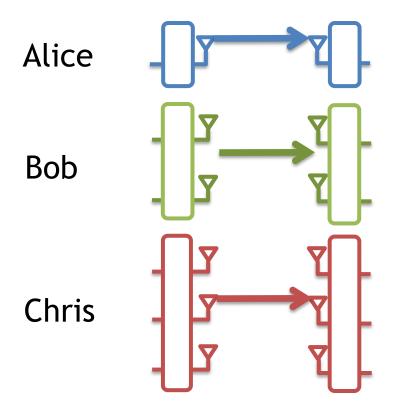
- Signals cancel each other at Alice's receiver
- Signals don't cancel each other at Bob's receiver
 - Because channels are different
- Bob's sender learns channels either by feedback from Alice's receiver or via reciprocity

Interference Nulling

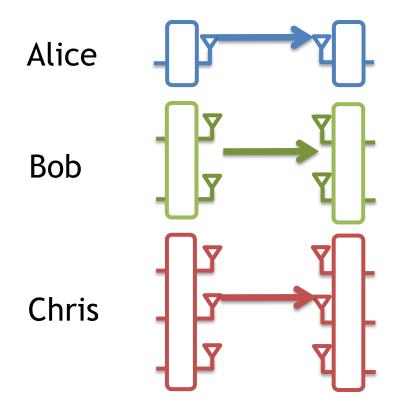


Q: How to transmit without interfering with receivers with fewer antennas?

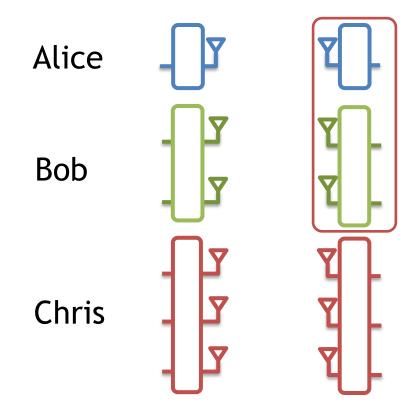
A: Nulling



Is Nulling Alone Enough?



Is Nulling Alone Enough?

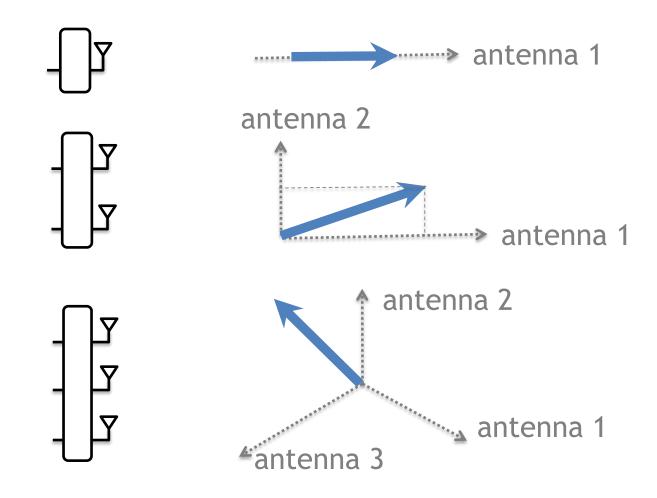


Chris needs to null at three antennas

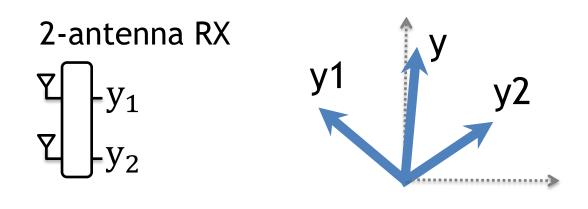
Is Nulling Alone Enough? NO! null $(h_{11}\alpha + h_{21}\beta + h_{31}\gamma)z = 0$ Alice $(h_{12}\alpha + h_{22}\beta + h_{32}\gamma)z = 0$ Bob $(h_{13}\alpha + h_{23}\beta + h_{33}\gamma)z = 0$ αz Only Solution: $\alpha = \beta = \gamma = 0$ Chris β_z Ζ Transmit Nothing!!!

Are we doomed?

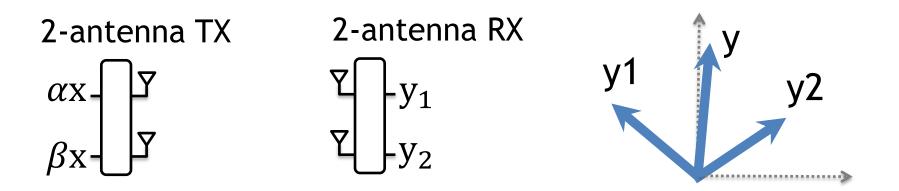
1. N-antenna node receives in N-dimensional space



- 1. N-antenna node receives in N-dimensional space
- 2. N-antenna receiver can decode N signals

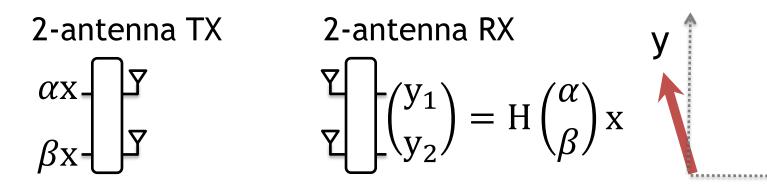


- 1. N-antenna node receives in N-dimensional space
- 2. N-antenna receiver can decode N signals
- 3. Transmitter can rotate the received signal



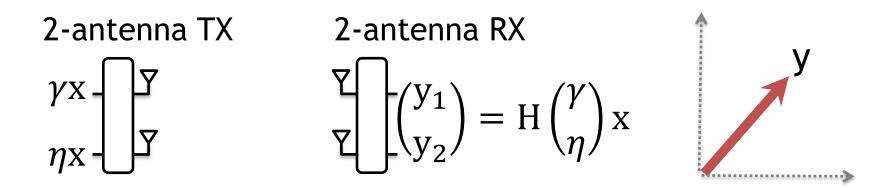
x is the sender's symbol, (y1,y2) is the received symbol, (α , β) is the pre-coding vector, and H is the channel matrix

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- 2. N-antenna receiver can decode N signals
- 3. Transmitter can rotate the received signal



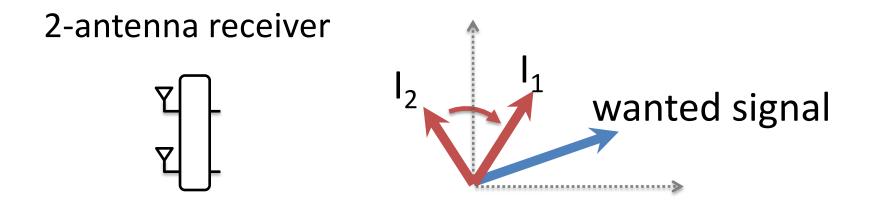
x is the sender's symbol, (y1,y2) is the received symbol, (α , β) is the pre-coding vector, and H is the channel matrix

- 1. N-antenna node receives in N-dimensional space
- 2. N-antenna receiver can decode N signals
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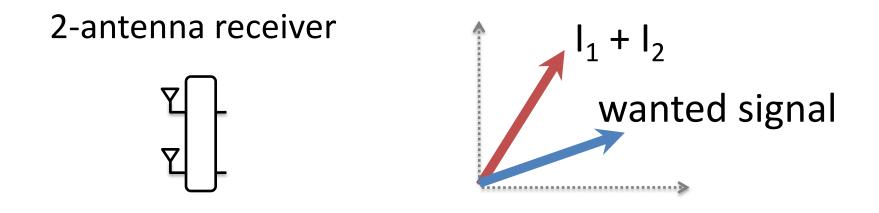
Sender can rotate the received symbol by multiplying with a different pre-coding vector; However to align along a particular direction, sender needs to know H

Interference Alignment

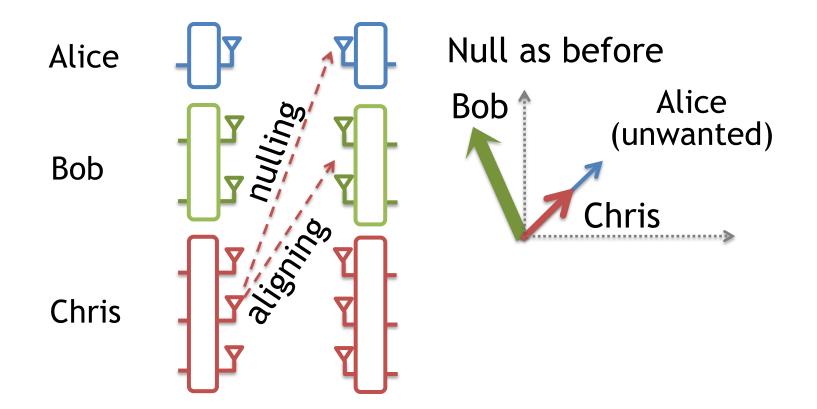


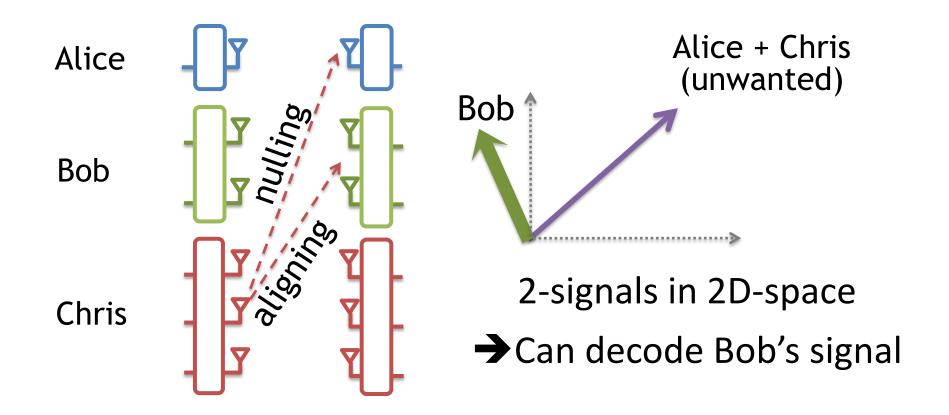
If I_1 and I_2 are aligned,

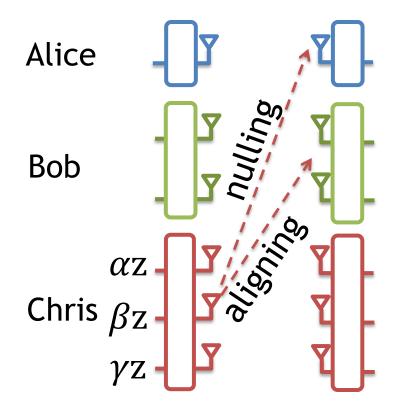
Interference Alignment



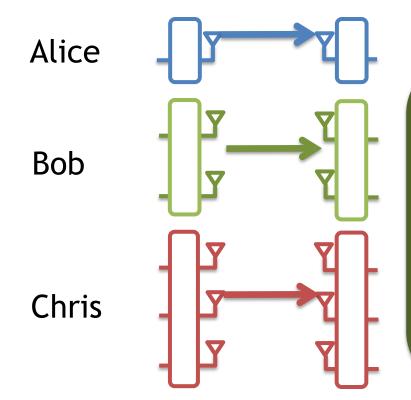
- If I_1 and I_2 are aligned,
- \rightarrow appear as one interferer
- \rightarrow 2-antenna receiver can decode the wanted signal





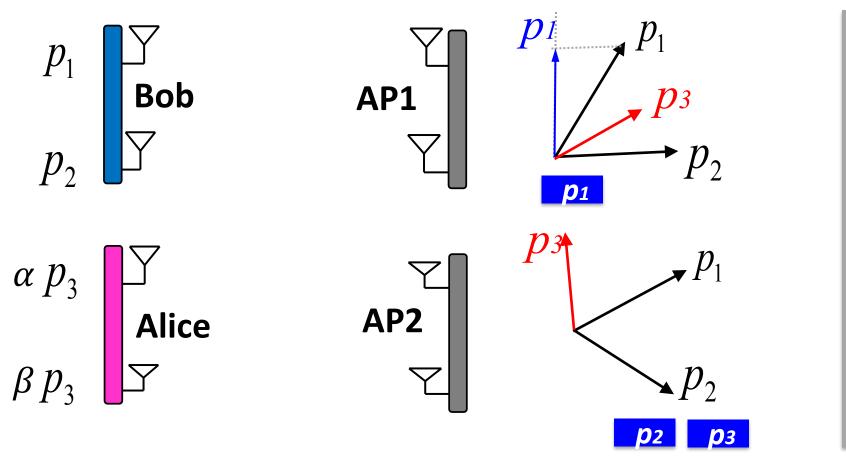


$$(h_{11}\alpha + h_{21}\beta + h_{31}\gamma)z = 0$$
$$\binom{h_{12}\alpha + h_{22}\beta + h_{32}\gamma}{h_{13}\alpha + h_{23}\beta + h_{33}\gamma} \propto \binom{h_{a1}}{h_{a2}}$$



3 packets though receivers have fewer than 3 antennas

Interference Alignment and Cancellation (IAC)



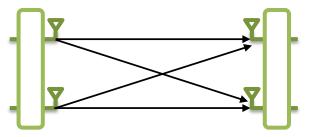
Ethernet

- Align P3 with P2 at AP1 \rightarrow AP1 decodes P1 to its bits
- AP1 broadcasts P1 on Ethernet
- AP2 subtracts/cancels P1→ decodes P2, P3

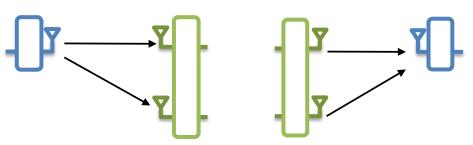
Last Lecture

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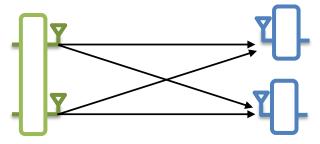
MIMO Multiplexing Gain



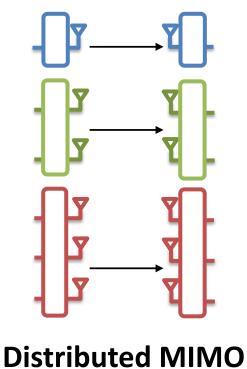
MIMO TX/RX Diversity Gain

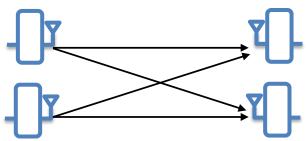


MU-MIMO Beamforming



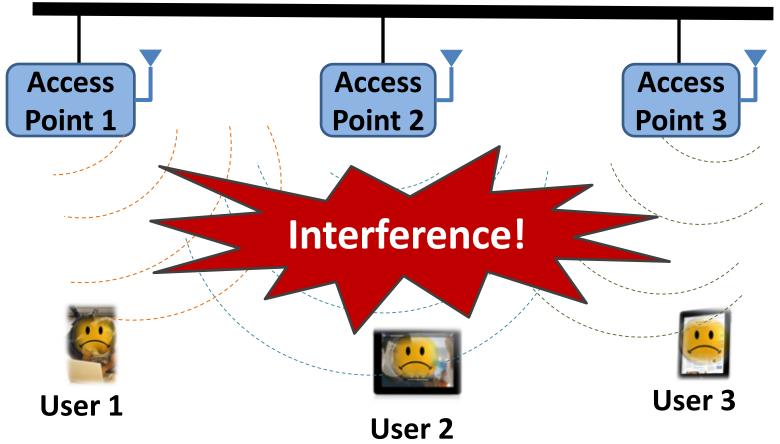
Heterogeneous # of antennas (Interference Nulling/Alignment)





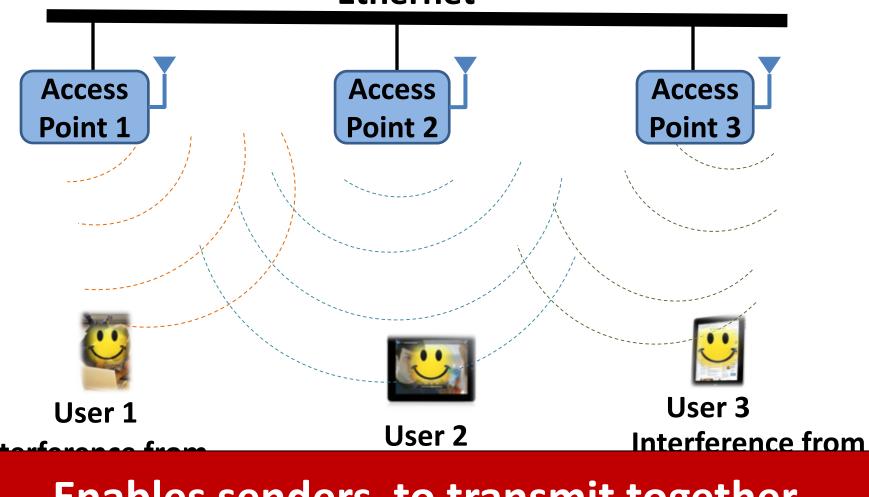
MegaMIMO: Scaling Wireless Throughput with the Number of Users

Today's Wireless Networks Ethernet



Access Points Can't Transmit Together in the Same Channel

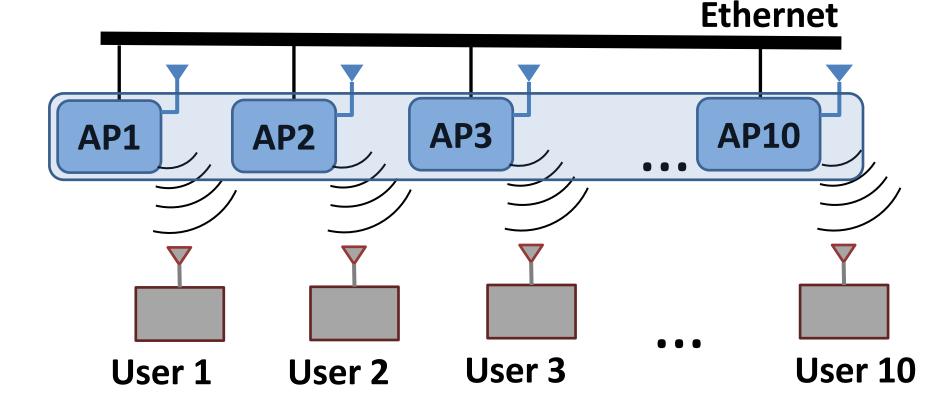
MegaMIMO Ethernet



Enables senders to transmit together without interference

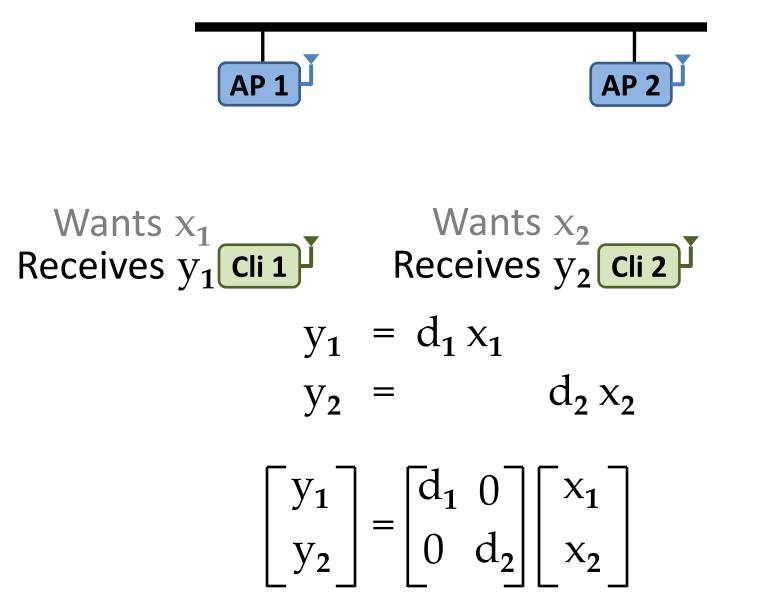
MegaMIMO = Distributed MIMO

Distributed protocol for APs to act as a huge MIMO transmitter with sum of antennas

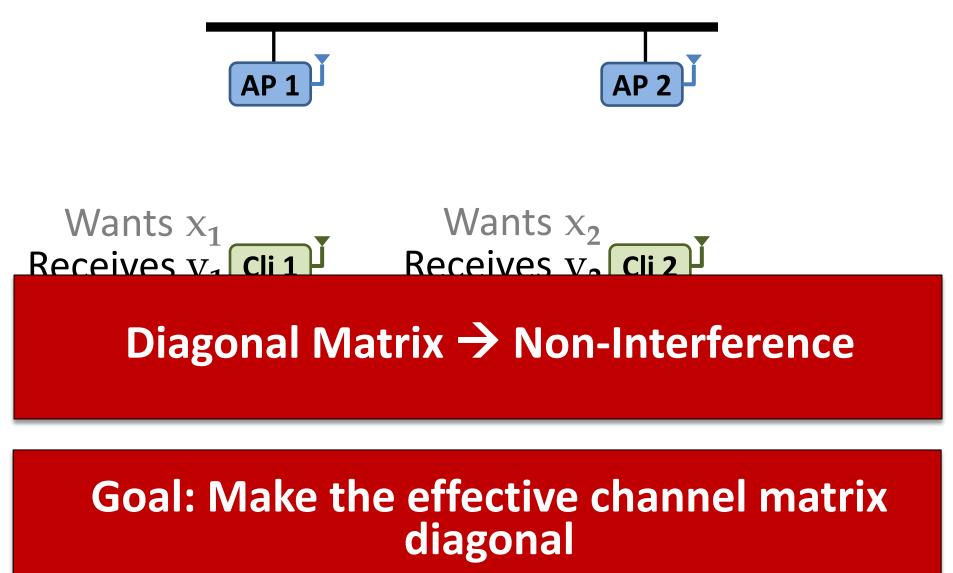


10 APs \rightarrow 10x higher throughput

Transmitting Without Interference



Transmitting Without Interference

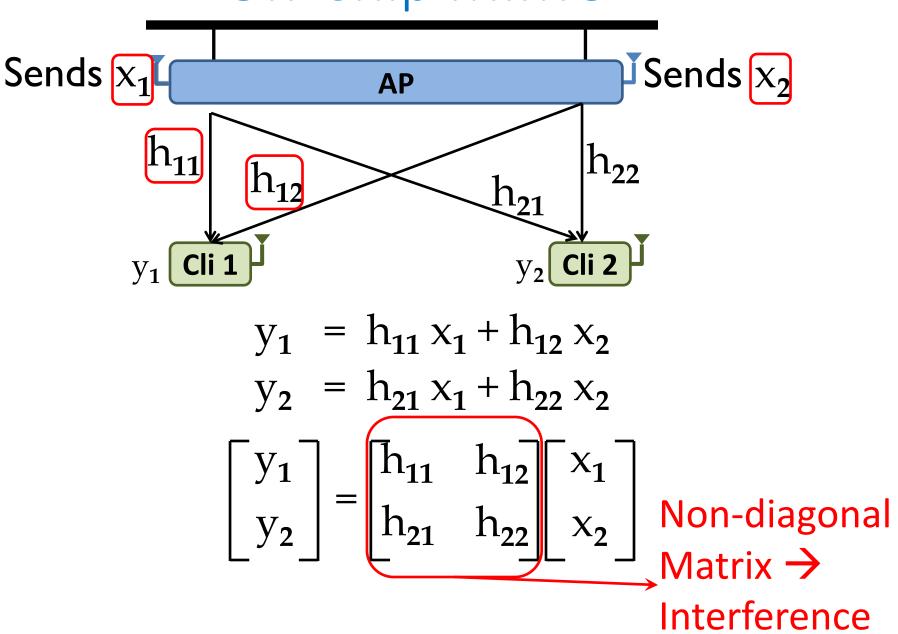


On-Chip MIMO

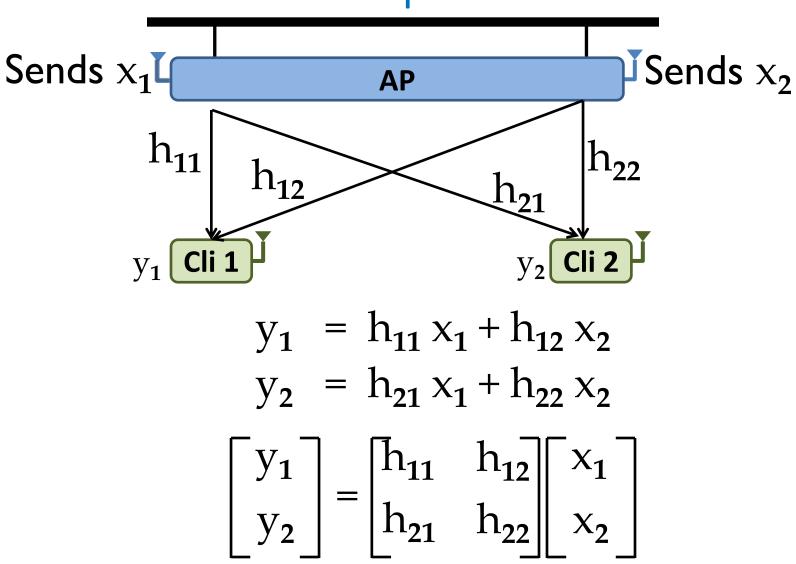
 All antennas on the MIMO sender are synchronized in time to within nanoseconds of each other.

• All antennas on a MIMO sender have exactly the same oscillator, i.e., no frequency offset.

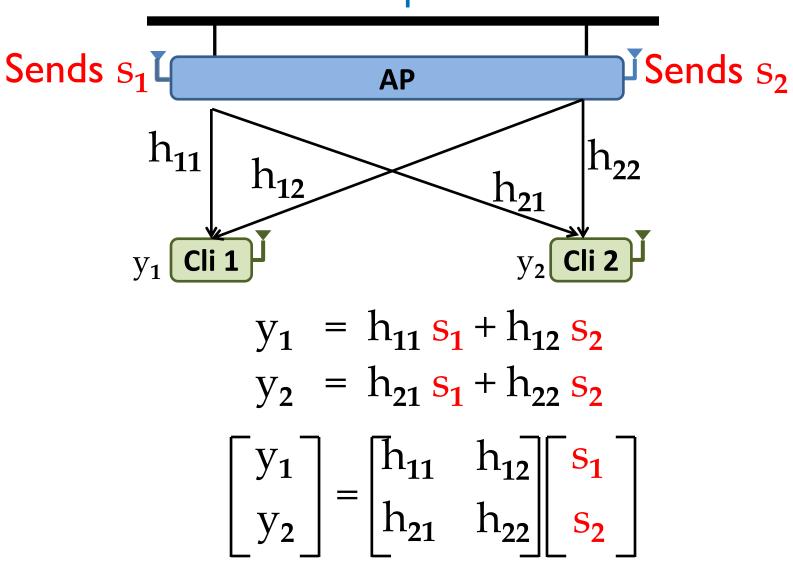
On-Chip MIMO



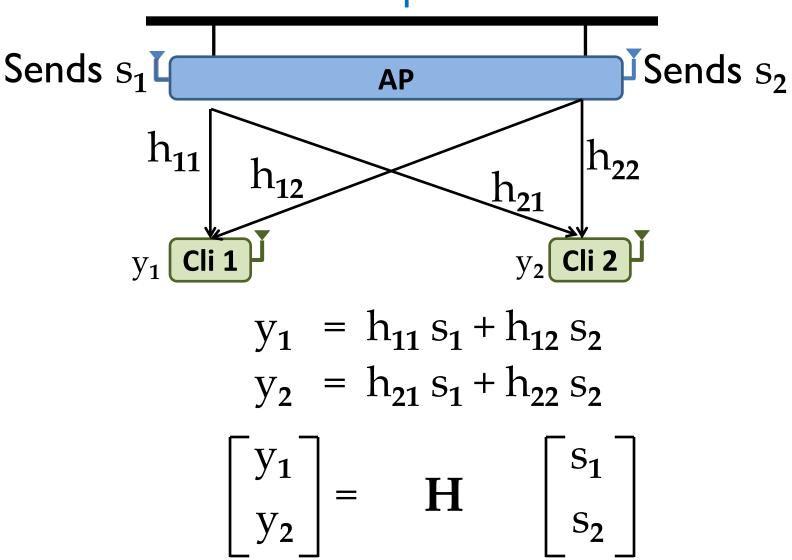
On-Chip MIMO



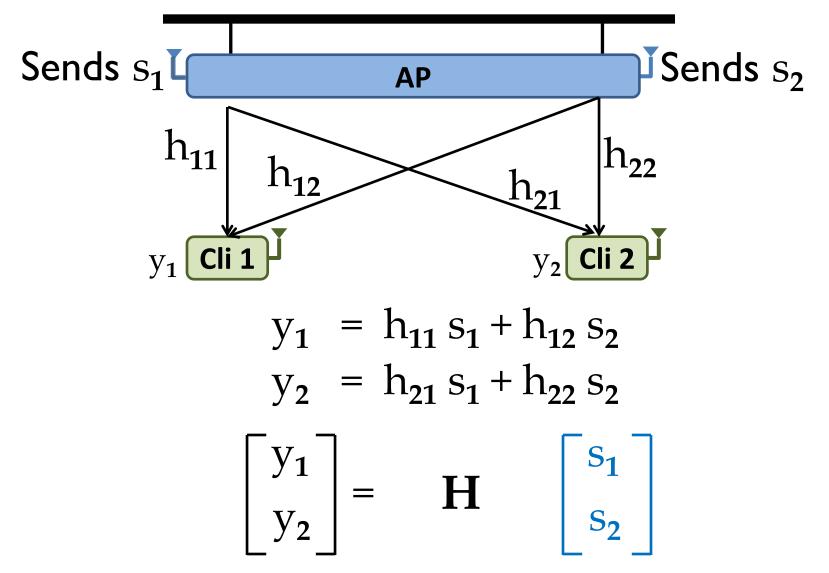
On-Chip MIMO



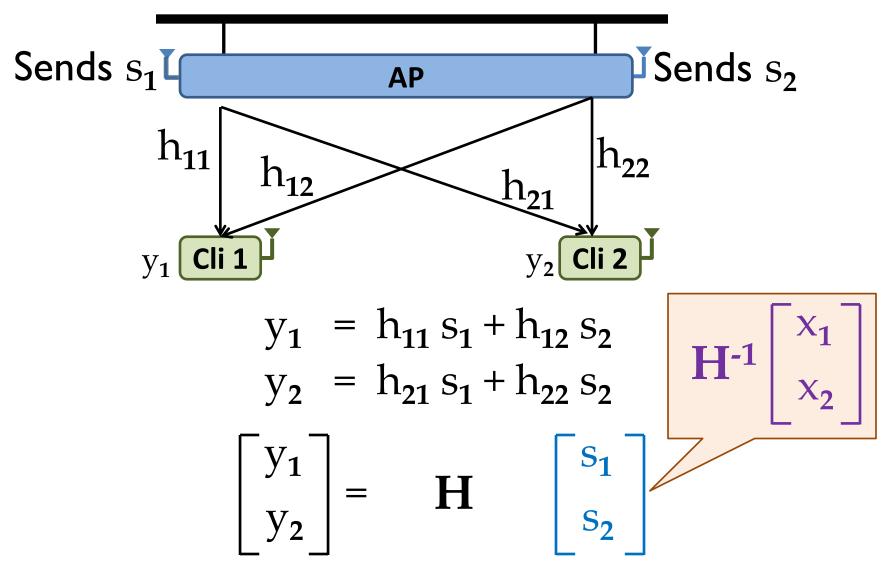
On-Chip MIMO



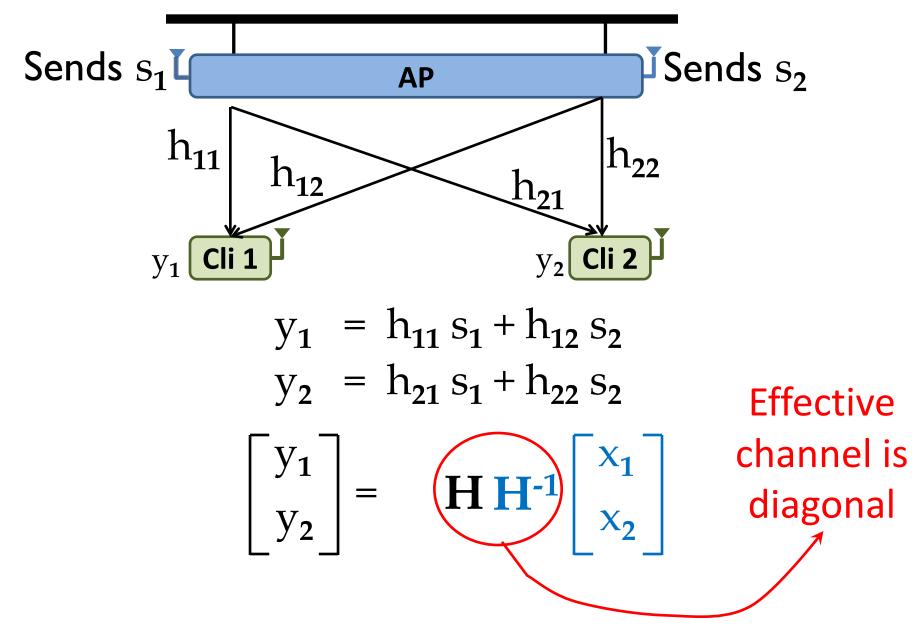
Making Effective Channel Matrix Diagonal



Making Effective Channel Matrix Diagonal



Making Effective Channel Matrix Diagonal



Beamforming System Description

Channel Measurement:

- Measure channels from sending antennas to clients
- Clients report measured channels back to APs

Data Transmission:

- MIMO sender computes its beamformed signal s_i using the equation $\vec{s} = H^{-1} \vec{x}$
- Clients 1 and 2 decode x₁ and x₂ independently

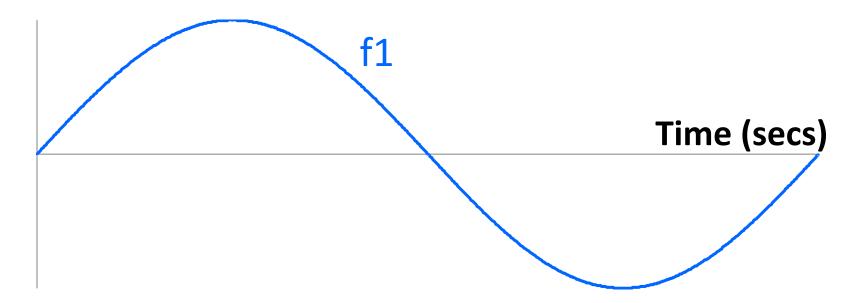
Distributed Transmitters Are Different

- Nodes are not synchronized in time.
 - We use SourceSync to synchronize senders within 10s of ns
 - Works for OFDM based systems like Wi-Fi, LTE etc.
- Oscillators are not synchronized and have frequency offsets relative to each other.

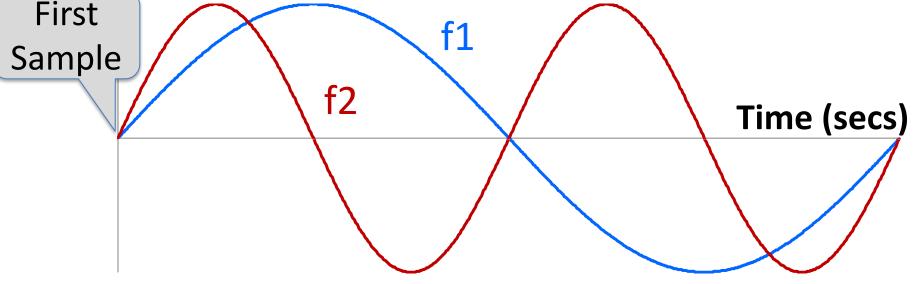
Synchronize Time Across APs

- Lead AP starts transmitting; Follower APs use the packet detection time to synchronize
- Challenge: Follower APs do not detect the packet at exactly the same time (difference in propagation delay, etc.)
- Solution: Each follower AP estimates the delay between its detection of the packet and the time the lead AP sent the first symbol in the packet... but How?

OFDM transmits signal over multiple frequencies

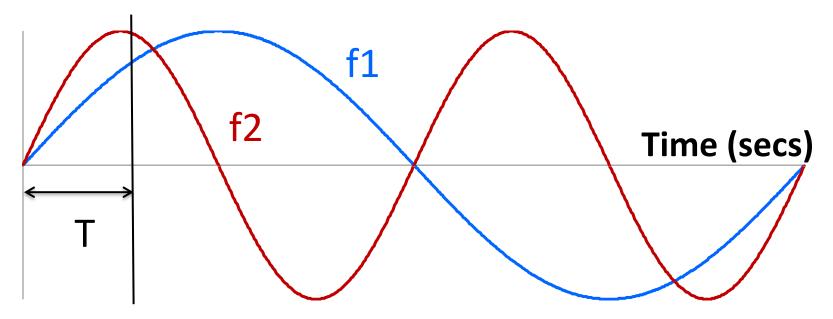


Estimating Packet Detection Delay in SourceSync OFDM transmits signal over multiple frequencies



Detect on first sample \rightarrow Same phase

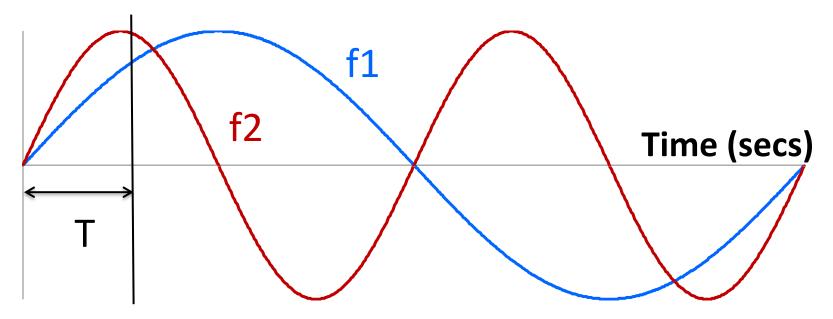
OFDM transmits signal over multiple frequencies



Detect after T

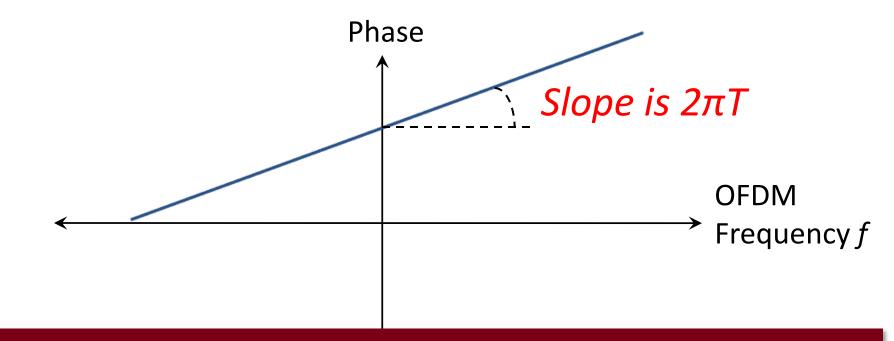
Frequencies rotate at different speeds

OFDM transmits signal over multiple frequencies



Detect after T

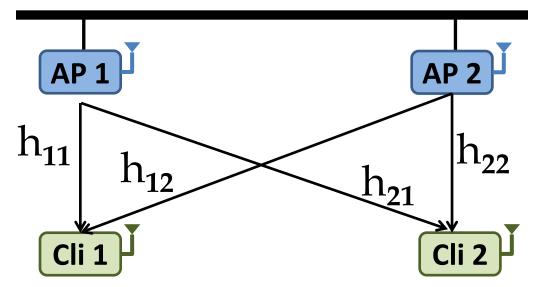
Different frequencies exhibit different phases $Phase = 2\pi fT$

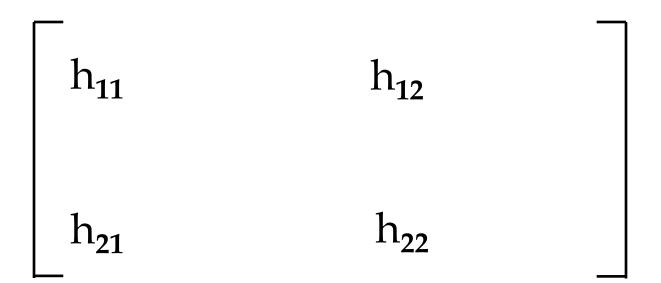


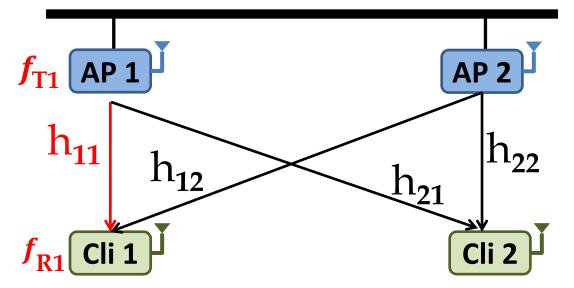
- Each AP estimates packet detection delay
- Estimate uses every symbol in packet \rightarrow Robust to noise

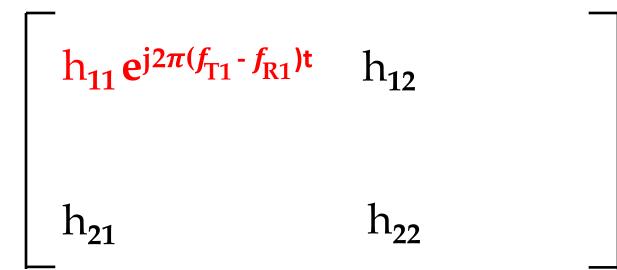
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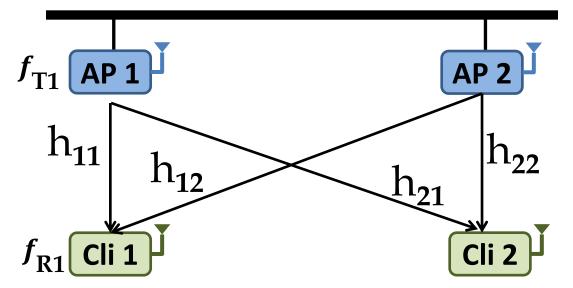
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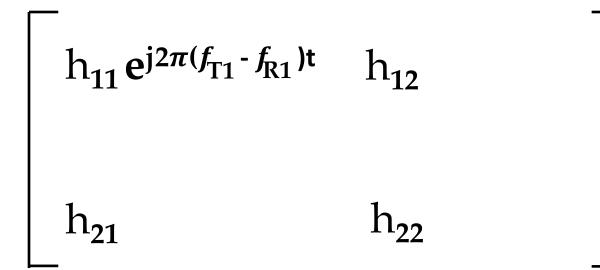


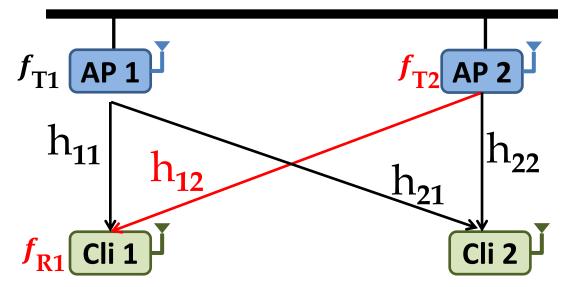


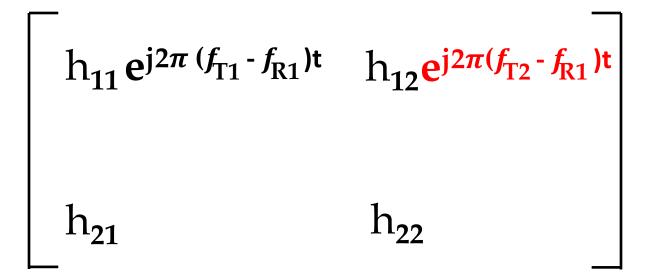


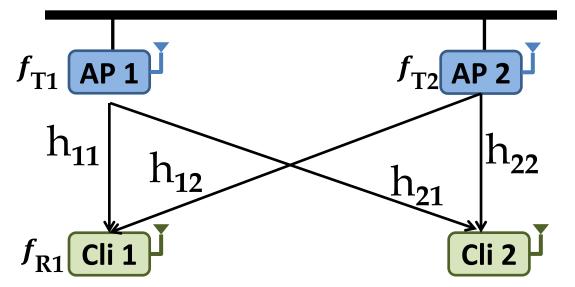


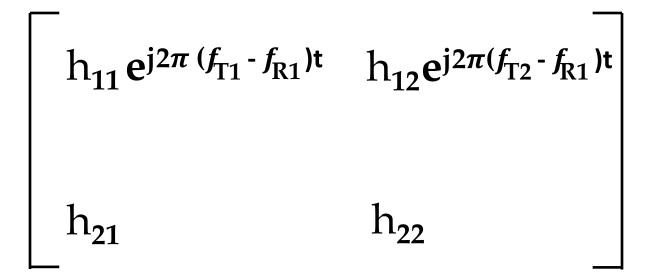


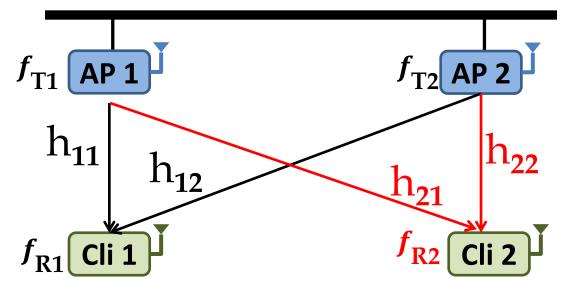






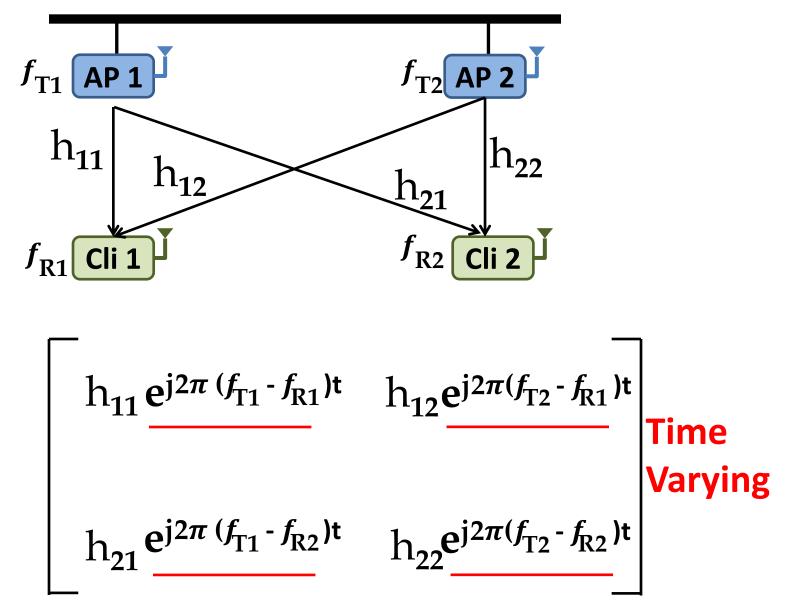




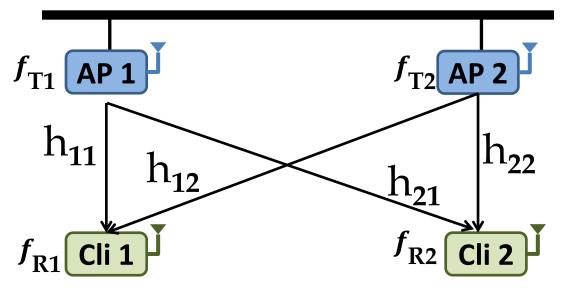


$$h_{11} e^{j2\pi (f_{T1} - f_{R1})t} \quad h_{12} e^{j2\pi (f_{T2} - f_{R1})t}$$

$$h_{21} e^{j2\pi (f_{T1} - f_{R2})t} \quad h_{22} e^{j2\pi (f_{T2} - f_{R2})t}$$

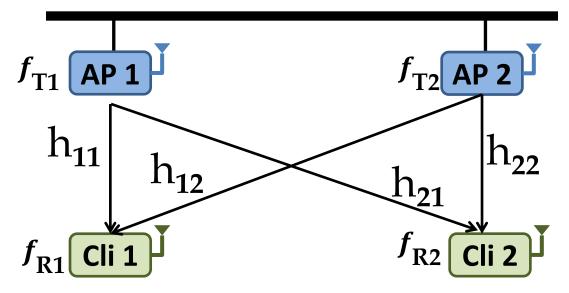


Channel is Time Varying



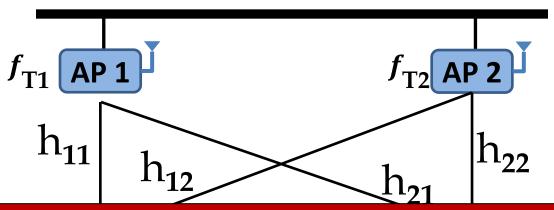
H(t)

Does Traditional Beamforming Still Work?



 $\begin{vmatrix} y_1(t) \\ y_2(t) \end{vmatrix} = \mathbf{H(t)} \begin{bmatrix} s_1(t) \\ s_2(t) \end{bmatrix}$

Does Traditional Beamforming Still Work?



Beamforming does not work

$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \underbrace{\mathbf{H(t)H^{-1}} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}}_{\text{Not}} \underbrace{\text{Not}}_{\text{Diagonal}}$$



Channel is Rapidly Time Varying

Relative Channel Phases of Transmitted Signals Changes Rapidly With Time

Prevents Beamforming

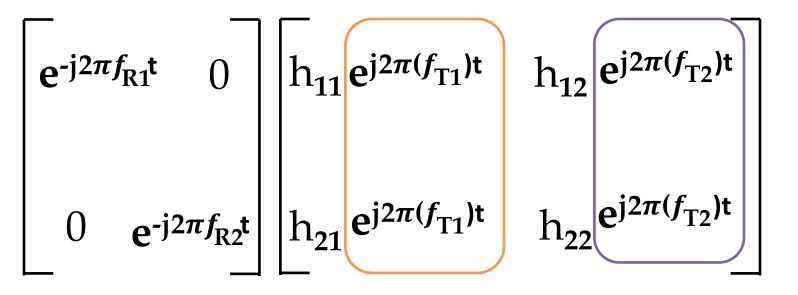
Distributed Phase Synchronization

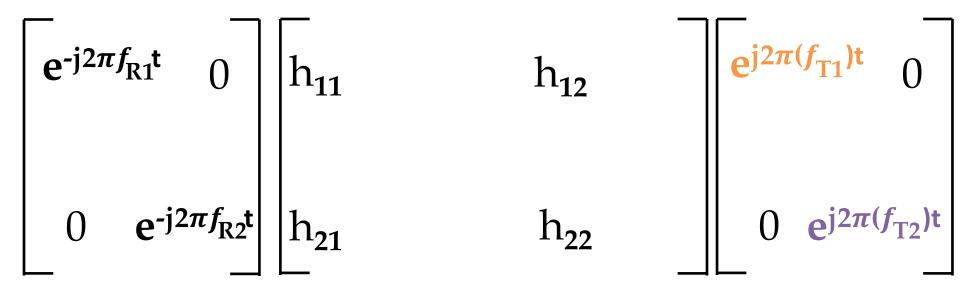
High Level Intuition:

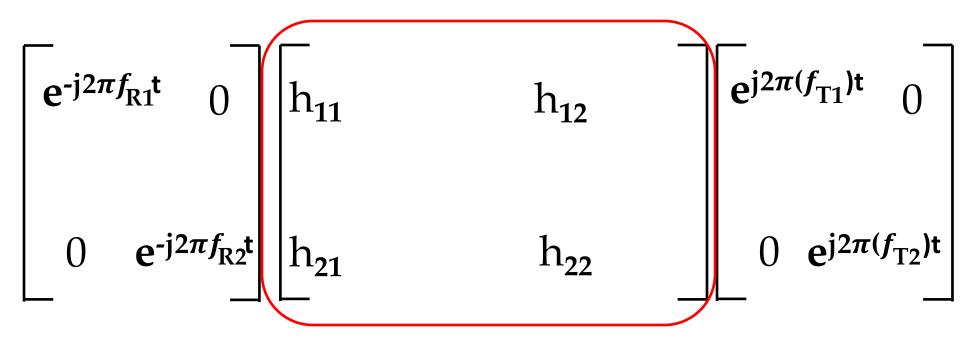
- Pick one AP as the lead
- All other APs are followers

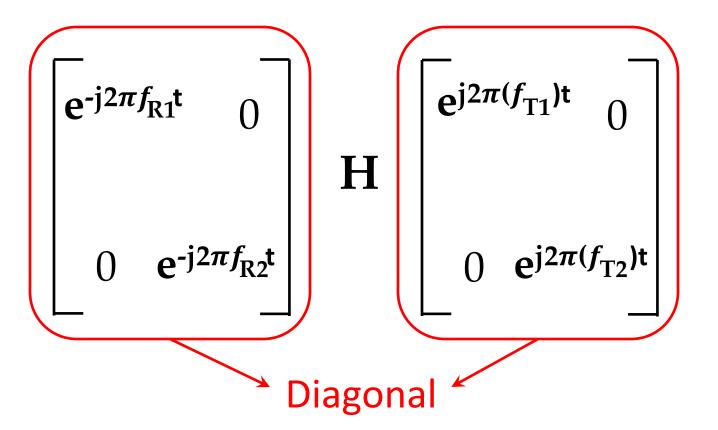
 Imitate the behavior of the lead AP by fixing the rotation of their oscillator relative to the lead.

$$\begin{array}{c} \textbf{Decomposing H(t)} \\ \begin{bmatrix} h_{11}e^{j2\pi}(f_{T1} \cdot f_{R1})t & h_{12}e^{j2\pi}(f_{T2} \cdot f_{R1})t \\ h_{21}e^{j2\pi}(f_{T1} \cdot f_{R2})t & h_{22}e^{j2\pi}(f_{T2} \cdot f_{R2})t \end{bmatrix} \\ \hline e^{-j2\pi}f_{R1}t & 0 \\ \hline 0 & e^{-j2\pi}f_{R2}t \end{bmatrix} \begin{bmatrix} h_{11}e^{j2\pi}(f_{T1})t & h_{12}e^{j2\pi}(f_{T2})t \\ h_{21}e^{j2\pi}(f_{T1})t & h_{22}e^{j2\pi}(f_{T2})t \end{bmatrix}$$



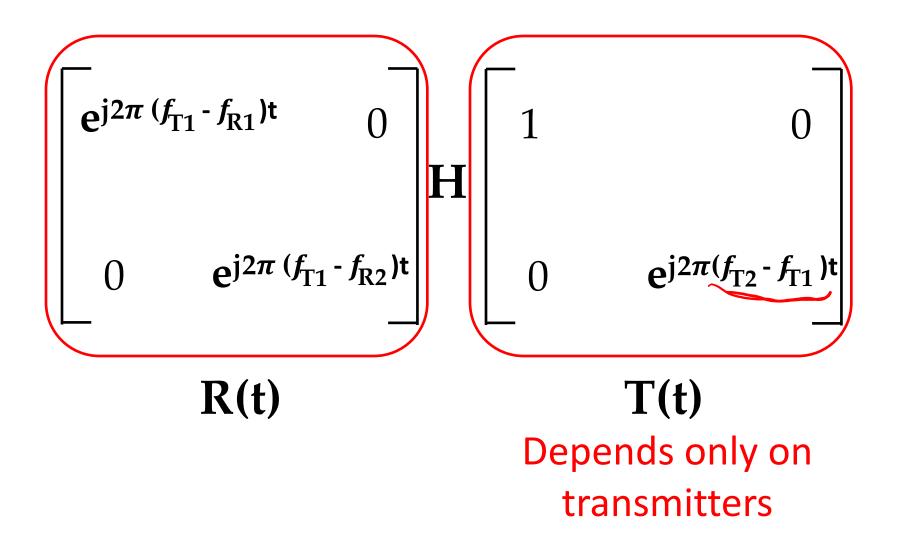


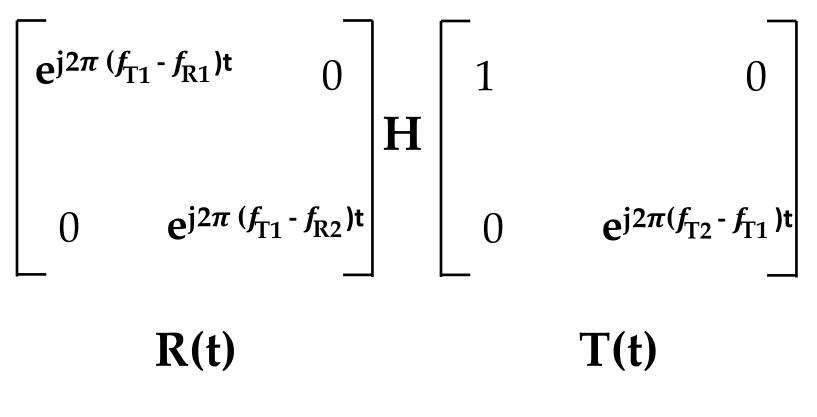




Devices cannot track their own oscillator phases...

$$\mathbf{e}^{j2\pi(f_{T1})t}\begin{bmatrix}\mathbf{e}^{-j2\pi f_{R1}t} & 0\\ & & \\ 0 & \mathbf{e}^{-j2\pi f_{R2}t}\end{bmatrix} \mathbf{H} \begin{bmatrix}\mathbf{e}^{j2\pi(f_{T1})t} & 0\\ & & \\ 0 & \mathbf{e}^{-j2\pi(f_{T1})t}\\ 0 & \mathbf{e}^{j2\pi(f_{T2})t}\end{bmatrix} \mathbf{e}^{-j2\pi(f_{T1})t}$$





H(t) = R(t).H.T(t)

Beamforming with Different Oscillators

$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \mathbf{R(t).H.T(t)} \begin{bmatrix} s_1(t) \\ s_2(t) \end{bmatrix}$$

$$\begin{bmatrix} s_1(t) \\ s_2(t) \end{bmatrix} = \mathbf{T}(t)^{-1}\mathbf{H}^{-1}\begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

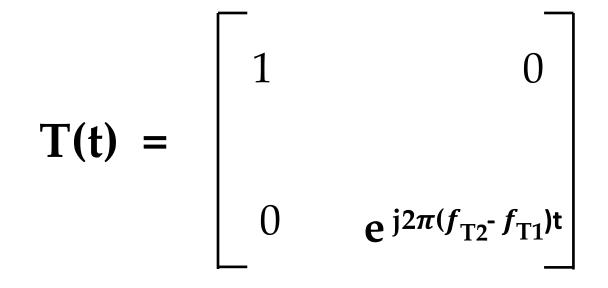
Beamforming with Different Oscillators

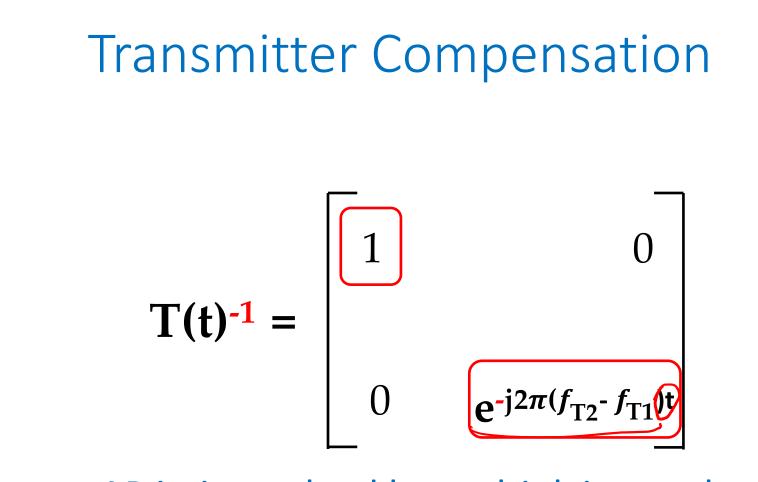
$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \mathbf{R(t)} \cdot \mathbf{H} \cdot \mathbf{T(t)} \cdot \mathbf{T(t)}^{-1} \mathbf{H}^{-1} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

Diagonal

$$\begin{bmatrix} s_1(t) \\ s_2(t) \end{bmatrix} = \mathbf{T}(t)^{-1}\mathbf{H}^{-1}\begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

Transmitter Compensation





Follower AP imitates lead by multiplying each sample by oscillator rotation relative to lead

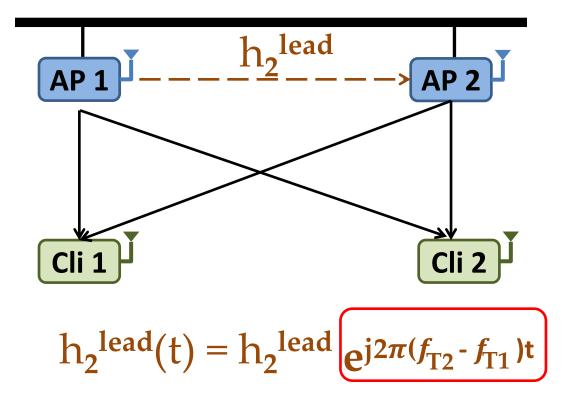
Requires only local information \rightarrow Fully distributed

Measuring Phase Offset

- Multiply frequency offset by elapsed time
- Requires very accurate estimation of frequency offset
 - Error of 25 Hz (10 parts per BILLION) changes complete alignment to complete misalignment in 20 ms.

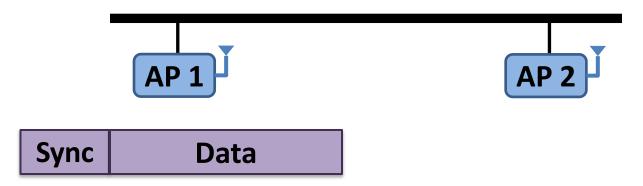
Need to keep resynchronizing to avoid error accumulation

Resynchronization



Directly compute phase at each follower AP by measuring channel from lead

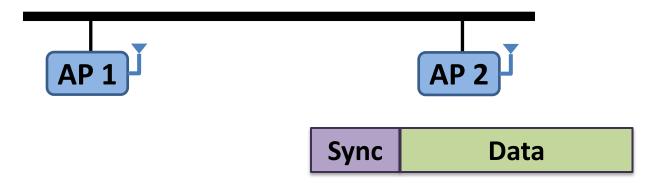
Resynchronization



Lead AP:

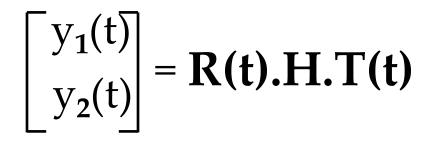
 Prefixes data transmission with synchronization header

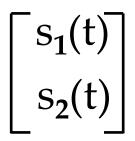
Resynchronization



Follower AP:

- Receives Synchronization Header
- Corrects for change in channel phase from lead
- Transmits data





$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \mathbf{R}(t) \cdot \mathbf{H} \cdot \mathbf{T}(t) \cdot \mathbf{T}(t)^{-1} \cdot \mathbf{H}^{-1} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

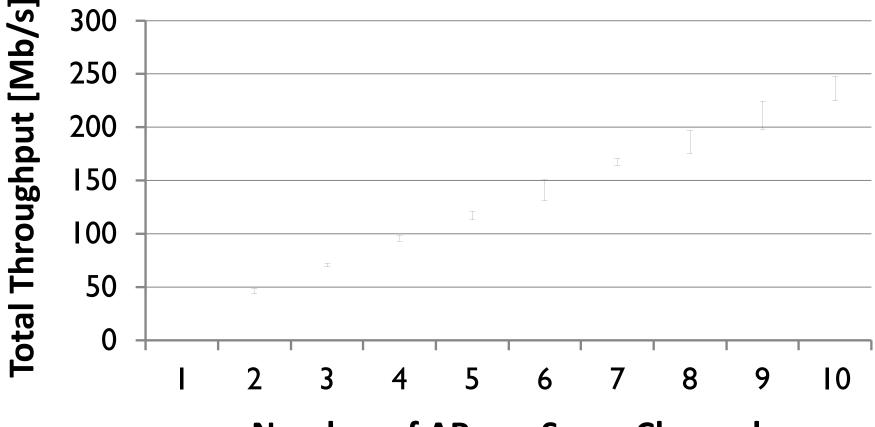
$$\begin{bmatrix} y_1(t) \\ y_2(t) \end{bmatrix} = \mathbf{R(t)^{-1}} \mathbf{R(t)} \begin{bmatrix} x_1(t) \\ x_2(t) \end{bmatrix}$$

$$\mathbf{R(t)} = \begin{bmatrix} e^{j2\pi (f_{T1} - f_{R1})t} & 0 \\ 0 & e^{j2\pi (f_{T1} - f_{R2})t} \end{bmatrix}$$

$$\mathbf{R(t)^{-1}} = \begin{bmatrix} e^{-j2\pi (f_{T1} - f_{R1})t} & 0 \\ 0 & e^{-j2\pi (f_{T1} - f_{R2})t} \end{bmatrix}$$

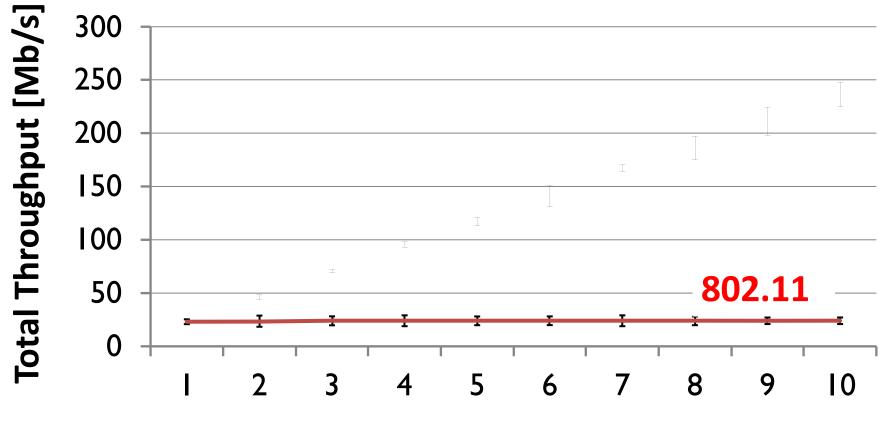
Receiver does what it does today – correct for oscillator offset from lead

Does MegaMIMO Scale Throughput with the Number of Users?



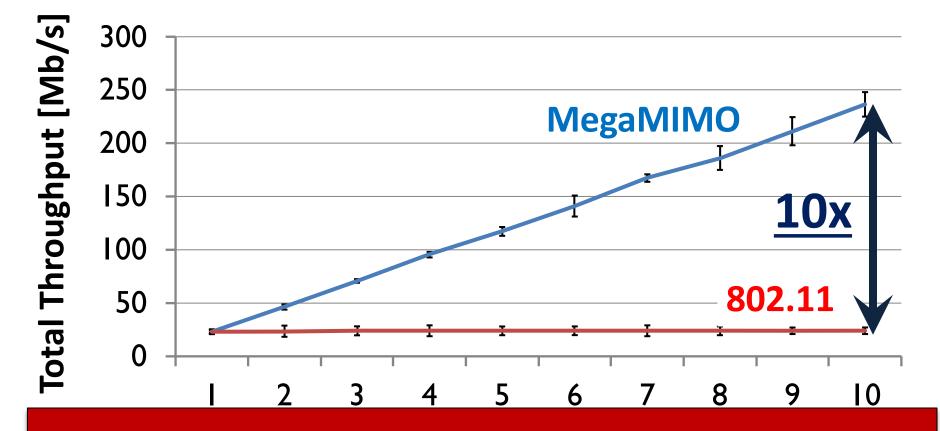
Number of APs on Same Channel

Does MegaMIMO Scale Throughput with the Number of Users?



Number of APs on Same Channel

Does MegaMIMO Scale Throughput with the Number of Users?



10x throughput gain over existing Wi-Fi

AirShare

transmits the reference clock over the air & eliminates CFO

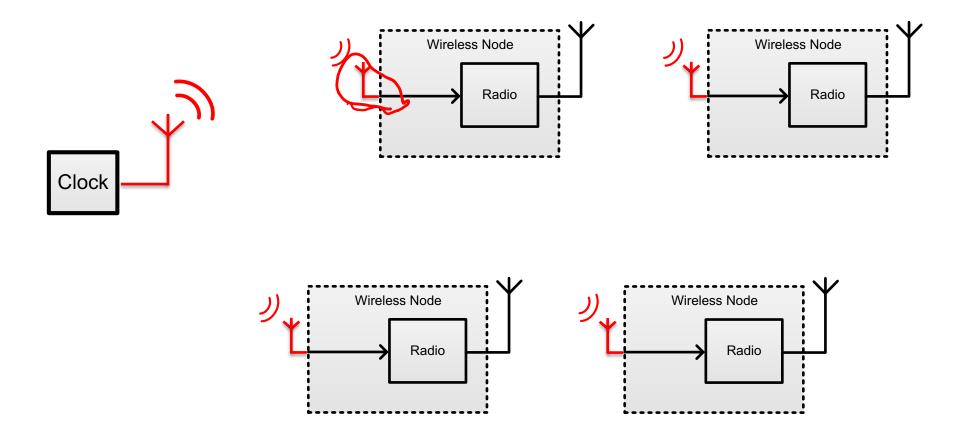
Protocol independent

Supports mobility

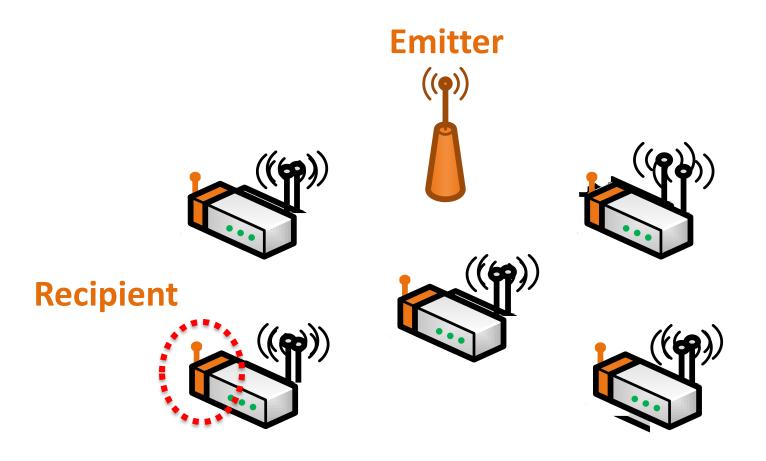
Cheap and Low-Power

Idea

Transmit a reference over-the-air



AirShare Architecture





How can emitter transmit a clock?

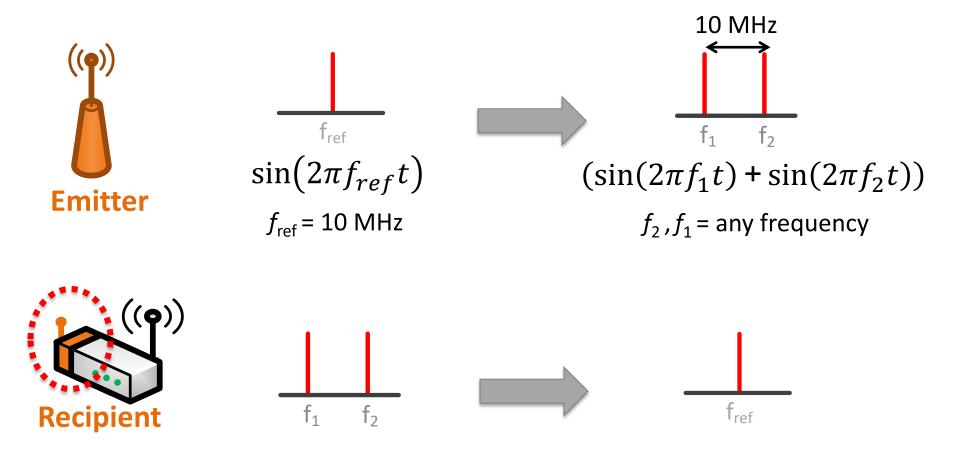
Problem: Reference clocks are typically 10-40 MHz

- FCC forbids transmitting such a low-frequency signal
- Requires large antennas

Transmit a Differential-reference

Instead of transmitting a signal at the clock frequency (10 MHz)

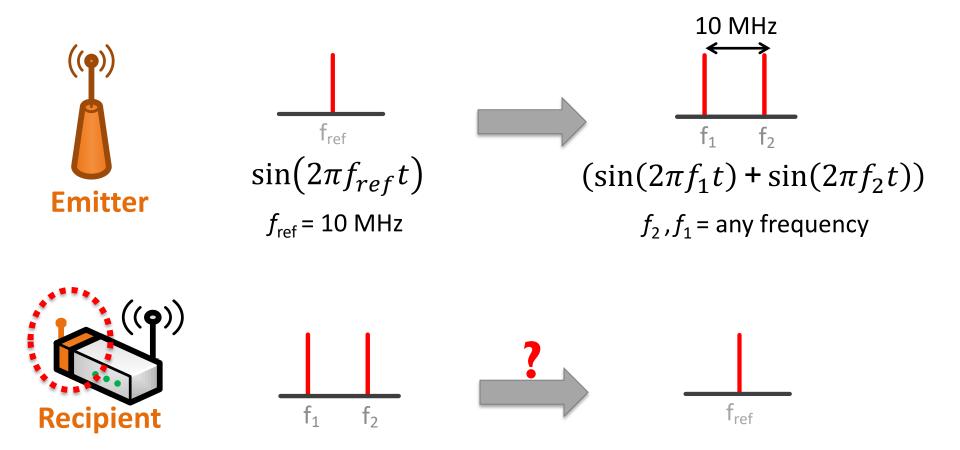
Transmits two signals separated by the clock frequency

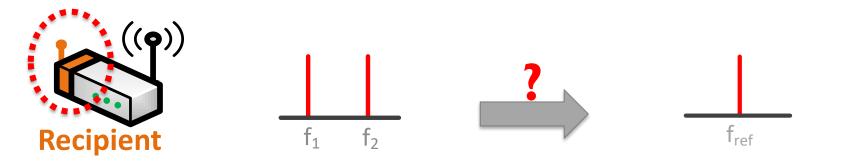


Transmit a Differential-reference

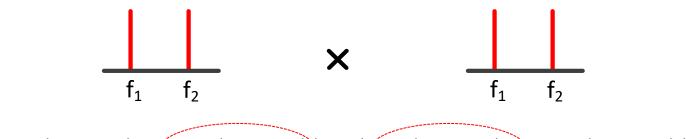
Instead of transmitting a signal at the clock frequency (10 MHz)

Transmits two signals separated by the clock frequency





receives the signal and multiplies the signal by itself



 $(\sin(2\pi f_1 t) + \sin(2\pi f_2 t)) \times (\sin(2\pi f_1 t) + \sin(2\pi f_2 t))$

Using trigonometric identities: $sin(\alpha) \times sin(\beta) = \frac{1}{2}cos(\alpha + \beta) + \frac{1}{2}cos(\alpha - \beta)$

AirShare transmits the reference clock without violating FCC regulations

Conclusion

- Learned about Interference Nulling, IA, IAC and MegaMIMO
- In IA, the gains are lower, but
 - Transmitters need not be connected to the same Ethernet and exchange the packets
 - No need for phase synchronization
- IAC can bring additional gains in comparison to IA
 - Transmitters need not be connected to the same Ethernet and exchange the packets
 - No need for phase synchronization
- In MegaMIMO, the gains are linear with the total number of users
 - Need high speed Ethernet to connect the transmitters
 - Need tight phase synchronization between transmitters
- AirShare: Distributed phase synchronization