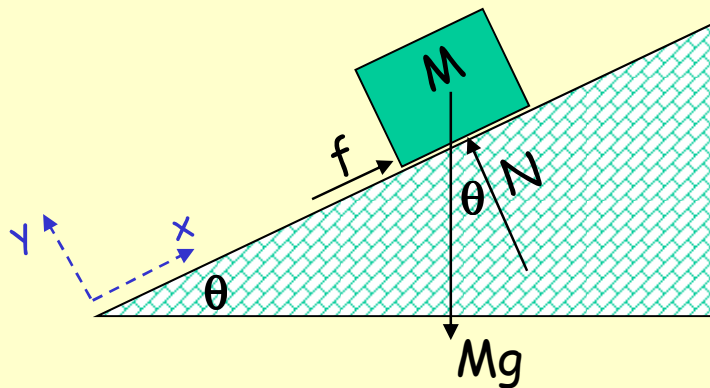


# PHYS 100: Lecture 7

## FRICTION



Static:

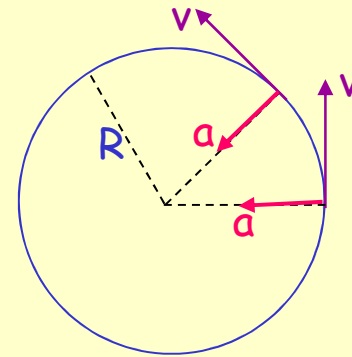
$$f \leq \mu_S N$$

Kinetic:

$$f = \mu_K N$$

and

## UNIFORM CIRCULAR MOTION

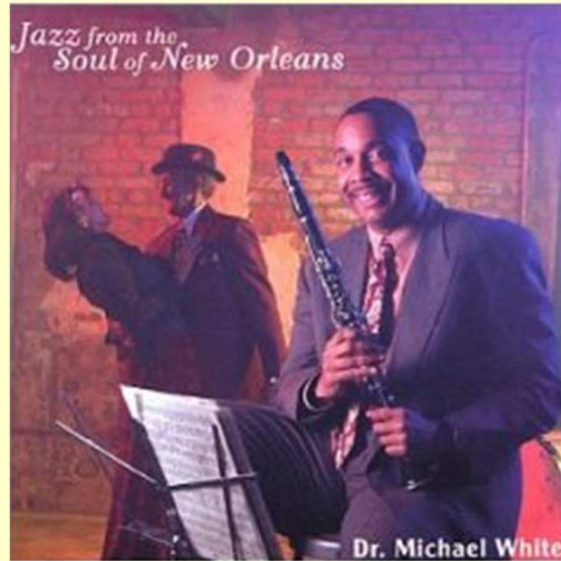


$$a = \frac{v^2}{R}$$

# Music

Who is the Artist?

- A) Pete Fountain
- B) Dr. Michael White
- C) Al Hirt
- D) George Lewis
- E) Dr. John



Why??

FOUR DAYS TO MARDI GRAS

Master of traditional New Orleans jazz !!

Catch the Traditional Jazz Orchestra (Jeff Helgesen et al) at the Iron Post from 5pm -7pm on Fat Tuesday !



BB

# Midterm Exam

Next FRIDAY (Mar 11):

Review Lecture  
257 Loomis

Following Tuesday (10/19)

Midterm Exam  
7pm in 136 Loomis

any conflicts???



# WHAT DID YOU FIND DIFFICULT?

Real forces in centripetal acceleration.

VERY IMPORTANT DISTINCTION HERE.

Newton's Second Law :

$$\vec{a} = \frac{\vec{F}_{net}}{m}$$

 Kinematics (description)       Dynamics (cause)

Newton's Second Law works in **INERTIAL FRAMES**

A Rotating Body is **NOT** an **INERTIAL FRAME**

The only **FORCES** that should appear on a **FREE BODY DIAGRAM** are **REAL FORCES**

As of now, you know about: **weight, normal, tension, friction and "applied"**

EVERYTHINGGGGG!!!!!!

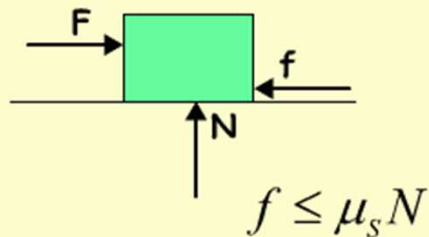
# THE BIG IDEAS

NOTE: THE BIG IDEAS ARE ALWAYS GIVEN IN THE LAST SLIDE

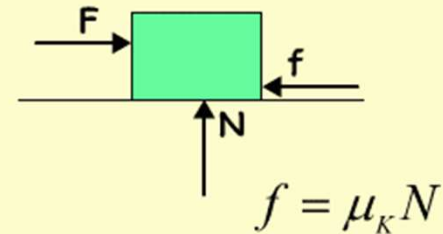
## Main Points

New Force: Friction

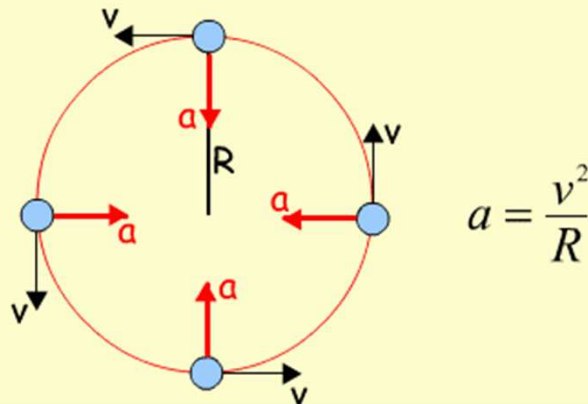
Static: No Relative Motion



Kinetic: Relative Motion



New Motion: Uniform Circular Motion



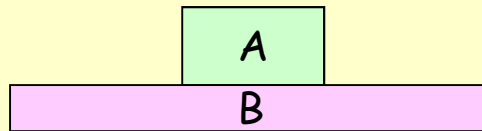
1. Frictional forces oppose relative motion:
2. Static (use  $\Sigma F_i = 0$ ) & Kinetic (use  $f = \mu_k N$ ) are different
3. Uniform circular motion has centripetal acceleration  $= v^2/R$

# Direction of Frictional Forces



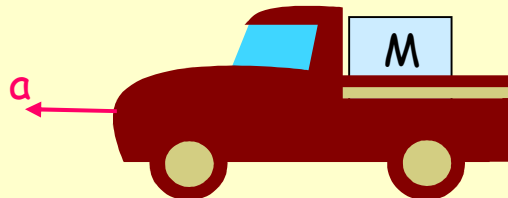
BB

Two ways to determine  $f_{B \text{ on } A}$ :



- Friction forces oppose relative motion (A relative to B)
- Draw freebody diagram and use Newton's Second Law

A block of mass  $M$  rests on the bed of a truck that is accelerating to the left



What is the direction of the frictional force that the bed of the truck exerts on the block?

(A) To left ←

(B) To right →

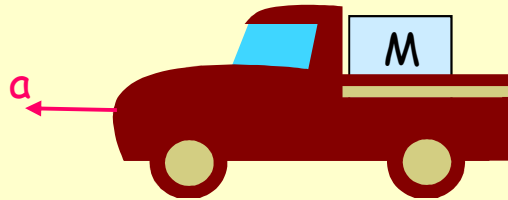
(C)  $f = 0$

# Direction of Frictional Forces



Suppose bed of truck were frictionless. What would be the motion of  $M$  relative to the truck?

BB



(A) Slide forward



(B) Slide backward



(C) Remain at rest

WHY??

Think of it from the reference frame of the ground (inertial)

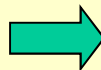
Are there any horizontal forces on  $M$ ?

NO! The block would remain at rest relative to the ground ( $a = 0$ )

Since truck moves to the left,  $M$  would move to the right RELATIVE to the TRUCK

NOTE:

The Truck is NOT an INERTIAL FRAME



Newton's Second Law is NOT TRUE  
in TRUCK FRAME

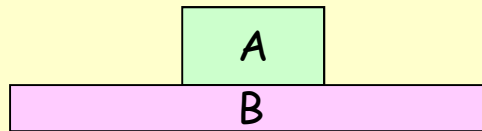
$$a \neq 0 \quad \text{BUT} \quad F_{\text{net}} = 0$$

# Direction of Frictional Forces



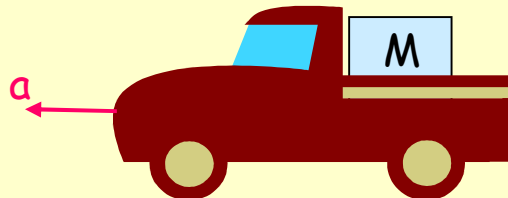
BB

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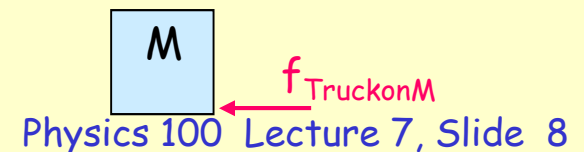
(A) To left ←

(B) To right →

(C)  $f = 0$

Since, in absence of friction,  $M$  would slide back (to right), the friction force on  $M$  must **OPPOSE** this motion and point forward (to left)

We can get this result from Newton's Second Law **ALSO**, knowing that the acceleration is to the **LEFT**!



Physics 100 Lecture 7, Slide 8

# Preflight 1

A constant force  $F$  is applied to block  $m$  and both blocks are observed to move together with constant acceleration.

What is the frictional force  $f$  that  $m$  exerts on  $M$ ?

(A)  $f < F$  :  $f$  points to left

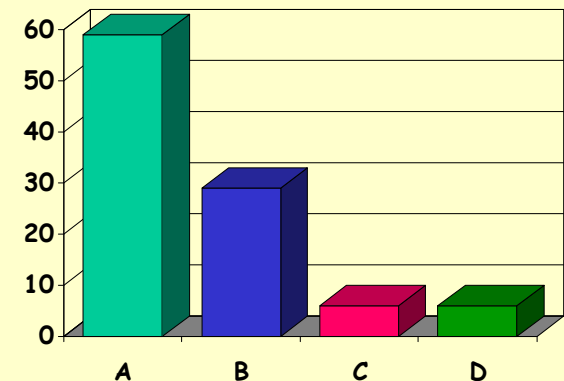
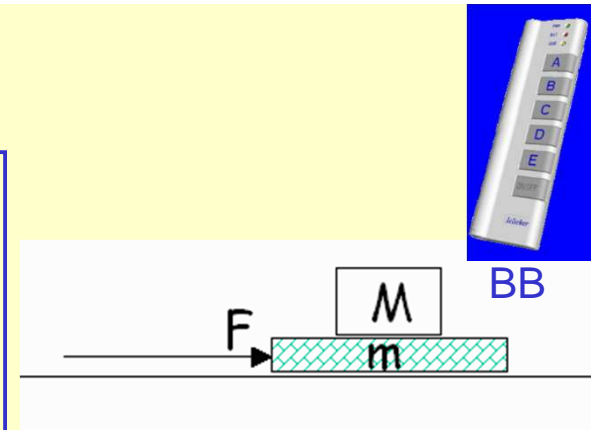
(B)  $f < F$  :  $f$  points to right

(C)  $f > F$  :  $f$  points to left

(D)  $f > F$  :  $f$  points to right

You said:

- Since they both move to the right, then  $F$  has to be greater than  $f$  so that it is able to overcome friction and move.  $f$  points to the left because it has to oppose the motion of  $m$ .
- For starters,  $f$  must point to the right. If the frictional force was not great enough to allow the blocks to move together than  $M$  would slide off  $m$  on the left side of the block. To counter that  $f$  points to the right to allow them to move together. Also,  $f$  does not have to be large than  $F$  because block  $M$  has mass, and the force of  $Mg$  will contribute to the staying on the block  $m$ .  $f$  only has to be what it is to do the job it does.



# Preflight 1: Direction

A constant force  $F$  is applied to block  $m$  and both blocks are observed to move together with constant acceleration.

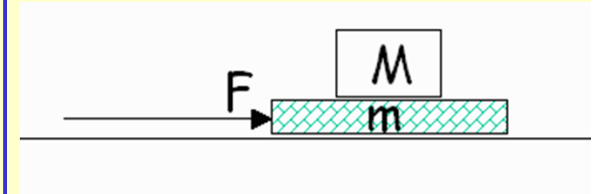
What is the frictional force  $f$  that  $m$  exerts on  $M$ ?

(A)  $f < F$  :  $f$  points to left

(B)  $f < F$  :  $f$  points to right

(C)  $f > F$  :  $f$  points to left

(D)  $f > F$  :  $f$  points to right



Two ways

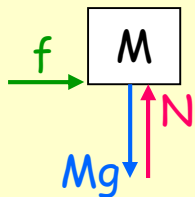
In absence of friction, there would be **NO** horizontal force on  $M$

Therefore  $M$  would **NOT** accelerate, but  $m$  would **ACCELERATE to RIGHT**

Therefore, **RELATIVE to  $m$** ,  $M$  would be moving to the **LEFT**.

The force  $m$  exerts on  $M$  then would **OPPOSE** this motion and point to the **RIGHT**

Free Body Diagram:



The acceleration of  $M$  is to the right (as measured in **INERTIAL FRAME**)

Newton's Second Law demands  $f$  to point to right since it is the **ONLY** horizontal force and must be the **CAUSE** of the acceleration of  $M$ .

# Preflight 1: Magnitude

A constant force  $F$  is applied to block  $m$  and both blocks are observed to move together with constant acceleration.

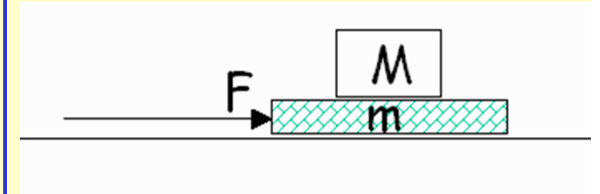
What is the frictional force  $f$  that  $m$  exerts on  $M$ ?

(A)  $f < F$ :  $f$  points to left

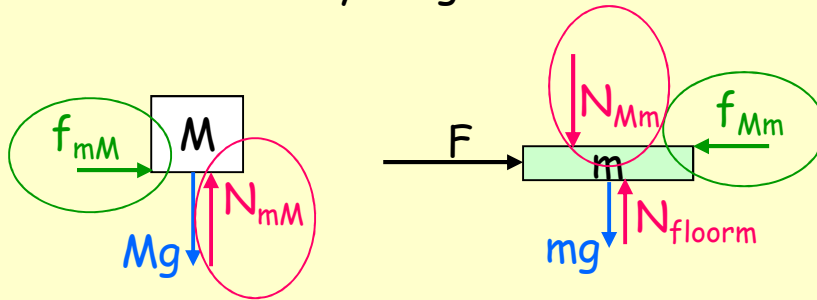
(B)  $f < F$ :  $f$  points to right

(C)  $f > F$ :  $f$  points to left

(D)  $f > F$ :  $f$  points to right



Free Body Diagrams:



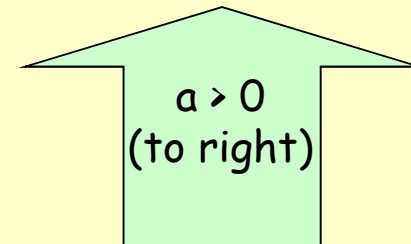
NOTE the Action-Reaction Pairs

$$\vec{F}_{m \text{ on } M} = -\vec{F}_{M \text{ on } m}$$

We used this info to draw  $f_{Mm}$  in the opposite direction to  $f_{mM}$

Free Body  
for m

$$f_{Mm} < F$$



$$F - f_{Mm} = ma$$

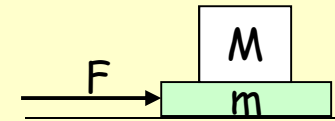
# Follow Up

A constant force  $F$  is applied to block  $m$  in Case I and to block  $M$  in Case II and in both cases, both blocks are observed to move together with constant acceleration. ( $M > m$ )

Compare the magnitude of the force  $f$  that  $m$  exerts on  $M$ .

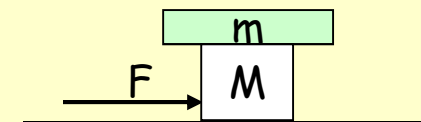
- (A)  $f(I) < f(II)$       (B)  $f(I) = f(II)$       (C)  $f(I) > f(II)$

Case I

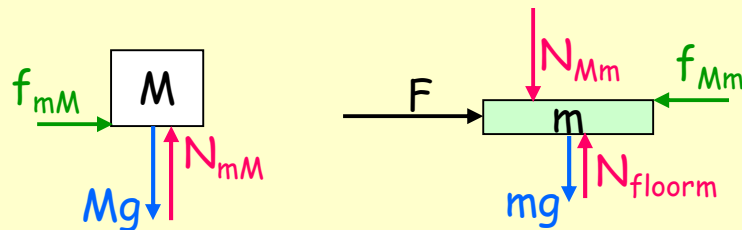


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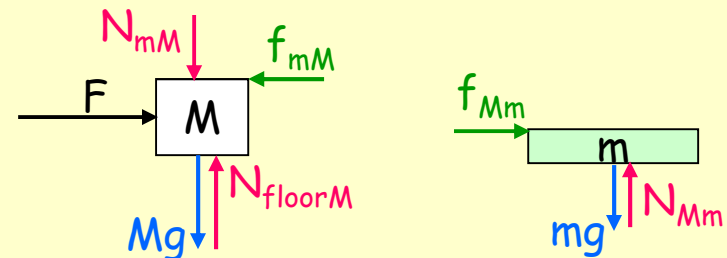
Case II



Free Body Diagrams  
Case I



Free Body Diagrams  
Case II



Newton's  
Second Law

$$f_{mM}^I = Ma$$

$$M > m \Rightarrow f_{mM}^I > f_{Mm}^{II}$$

NOTE: These are real friction forces (**NOT** "ma" forces). They simply have the value =  $ma$ .

Newton's  
Second Law

$$f_{Mm}^{II} = ma$$

# Static Friction

A block of mass  $M$  rests on a horizontal floor. The coefficient of static friction between the block and the floor is equal to  $\mu_s$ .

What is  $f$ , the frictional force that the floor exerts on  $M$ ?

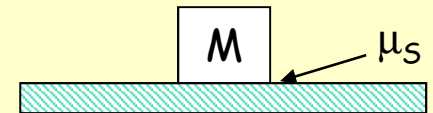
(A)  $f = \mu_s Mg$

(B)  $0 < f < \mu_s Mg$

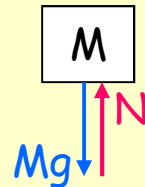
(C)  $f = 0$



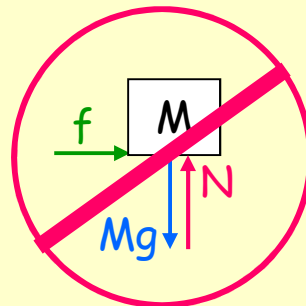
BB



Free Body Diagram



There is no force for the friction force to oppose !!



$M$  would accelerate !!

# Static Friction

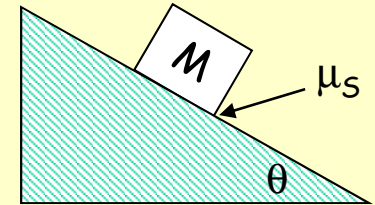
A block of mass  $M$  rests on an incline of angle  $\theta$ , as shown.  
The coefficient of static friction between the block and the floor is equal to  $\mu_s$ .

What is  $f$ , the frictional force that the plane exerts on  $M$ ?

- (A)  $f = \mu_s M g \cos \theta$       (B)  $f = \mu_s M g \sin \theta$       (C)  $f = 0$   
(D)  $f = M g \cos \theta$       (E)  $f = M g \sin \theta$



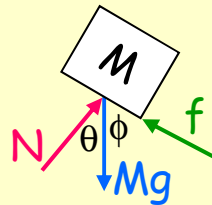
BB



Free Body Diagram

Perpendicular to the plane:

$$N - M g \cos \theta = 0$$



Parallel to the plane:

$$f - M g \cos \phi = 0$$



$$f = M g \cos \phi$$

$$\phi = 90^\circ - \theta$$

$$f = M g \sin \theta$$

$$f < f_{\max} = \mu_s N = \mu_s M g \cos \theta$$

$$M g \sin \theta < \mu_s M g \cos \theta$$

$$\sin \theta < \mu_s \cos \theta$$

$$\tan \theta < \mu_s$$

# Preflight 3

In both cases a block of mass  $m$  is at rest on the surface which has a coefficient of static friction  $\mu_s$ .

Compare  $f_I$  to  $f_{II}$ , the frictional forces on the blocks in I & II

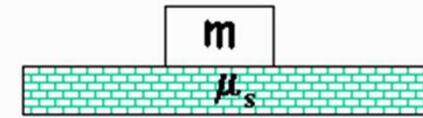
(A)  $f_I < f_{II}$

(B)  $f_I = f_{II}$

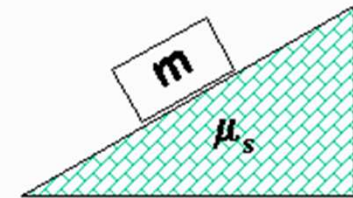
(C)  $f_I > f_{II}$

You said:

- Case one has no static friction added so case II would have a greater frictional force
- The force of friction would be the same because the block has the same mass.
- The frictional force depends on the Normal Force. The Normal force =  $mg$  in Case I, but it only equals  $Mg\cos(\theta)$  in case II. Therefore, the frictional force of Case I is greater than Case II.



Case I

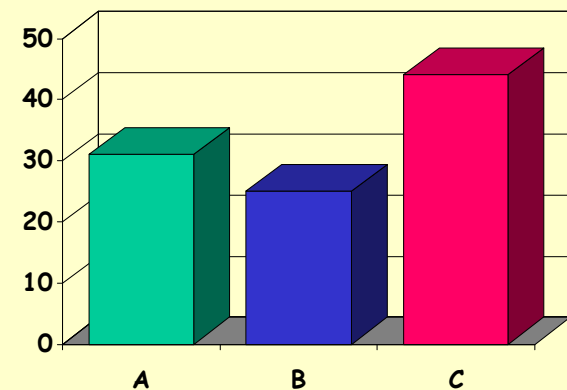


Case II



BB

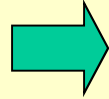
$f_I$  is ZERO !!



# Uniform Circular Motion

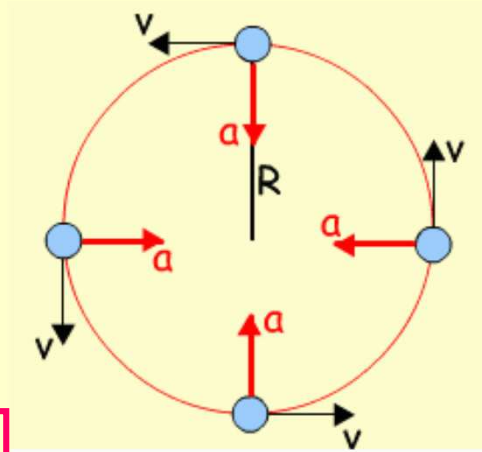
KINEMATICS ONLY !!  
MOTION HAS BEEN SPECIFIED

$$\vec{a} \equiv \frac{d\vec{v}}{dt}$$



$$a = \frac{v^2}{R}$$

This is **TRUE** whenever you have uniform circular motion, no matter what kind of force causes it !!

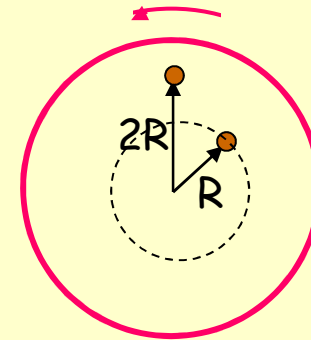


BB

A block of mass  $M$  rests on a turntable. The turntable makes one complete revolution in  $P$  seconds. Two pennies are at rest relative to the turntable and are located at distances  $R$  and  $2R$  from the center,

We want to determine the accelerations of the pennies.  
First step: What is the speed of the penny at  $R$ ?

(A)  $v = RP$       (B)  $v = 2\pi RP$       (C)  $v = \frac{R}{P}$       (D)  $v = \frac{2\pi R}{P}$



Distance =  $2\pi R$   
Time =  $P$

$P$  is called the PERIOD

# Uniform Circular Motion



A block of mass  $M$  rests on a turntable. The turntable makes one complete revolution in  $P$  seconds. Two pennies are at rest relative to the turntable and are located at distances  $R$  and  $2R$  from the center.

Compare the accelerations of the pennies at  $R$  and  $2R$ .

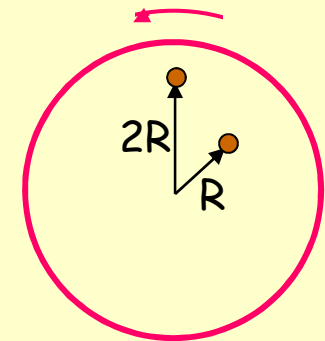
(A)  $a(R) = \frac{1}{4}a(2R)$

(B)  $a(R) = \frac{1}{2}a(2R)$

(C)  $a(R) = a(2R)$

(D)  $a(R) = 2a(2R)$

(E)  $a(R) = 4a(2R)$



$v = \frac{2\pi R}{P}$  at  $R$

Acceleration at  $R$ :  $a_R = \frac{v^2}{R} \Rightarrow a_R = \frac{1}{R} \left( \frac{4\pi R^2}{P^2} \right) = \frac{4\pi}{P^2} R$

Acceleration at  $2R$ :  $v_{2R} = \frac{2\pi(2R)}{P} \Rightarrow a_{2R} = \frac{1}{2R} \left( \frac{16\pi R^2}{P^2} \right) = \frac{8\pi}{P^2} R$

$a_R = \frac{1}{2} a_{2R}$

General:  $a = \omega^2 R$

$\omega$  is Angular Velocity (radians/sec):  $\omega \equiv \frac{v}{R}$

# Uniform Circular Motion



A block of mass  $M$  rests on a turntable. The turntable makes one complete revolution in  $P$  seconds. Two pennies are at rest relative to the turntable and are located at distances  $R$  and  $2R$  from the center.

Compare the net forces on the pennies at  $R$  and  $2R$ .

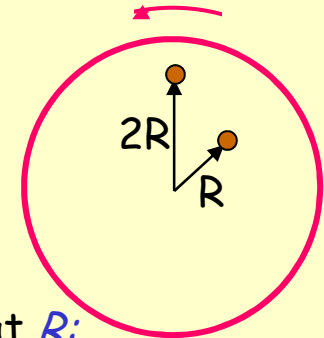
(A)  $F(R) = \frac{1}{4} F(2R)$

(B)  $F(R) = \frac{1}{2} F(2R)$

(C)  $F(R) = F(2R)$

(D)  $F(R) = 2F(2R)$

(E)  $F(R) = 4F(2R)$



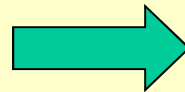
at  $R$ :

$$v = \frac{2\pi R}{P} \quad a = \omega^2 R$$

$$\omega \equiv \frac{v}{R} = \frac{2\pi}{P}$$

$$F_{net} = ma$$

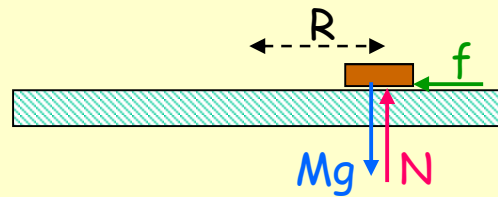
$$a = \omega^2 R$$



$$F_{net} = m\omega^2 R$$

WHAT IS THIS FORCE ??

FRICTION !!



side view

Here:  $f = m\omega^2 R$

It must also be true that:

$$f \leq \mu_s Mg$$

# DEMO



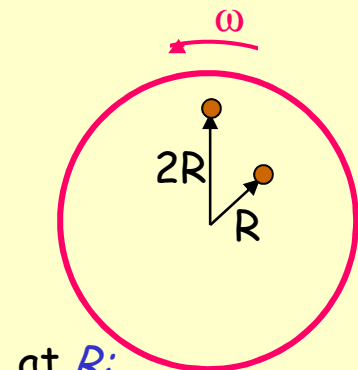
BB

Friction force responsible for penny's acceleration  
Friction force is proportional to the distance from the center

$$f = m\omega^2 R$$

As I increase the angular velocity, what will happen?

- (A) Both pennies fly off at same time
- (B) Penny at R flies off first
- (C) Penny at 2R flies off first



$$v = \frac{2\pi R}{P} \quad a = \omega^2 R$$

$$\omega \equiv \frac{v}{R} = \frac{2\pi}{P}$$

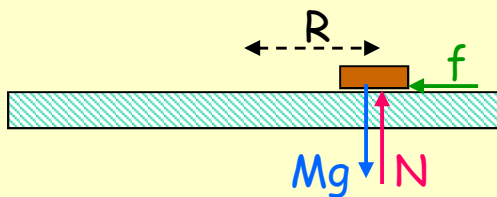
WHY !!

As  $\omega$  increases, the frictional force must increase (to provide increased acceleration)

$$f = m\omega^2 R$$

There is, however, a maximum possible frictional force:

$$f_{\max} = \mu_s Mg$$



The force at 2R is always bigger than the force at R  
The force at 2R will reach maximum before the force at R

# Preflight 5

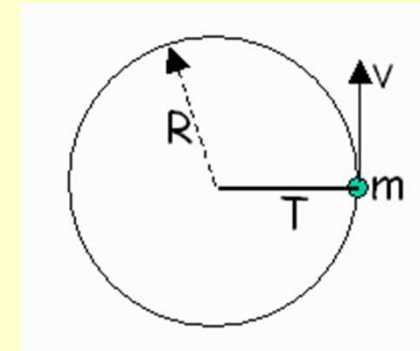
Mass  $m$  is connected to a string and moves with speed  $v$  in uniform circular motion of radius  $R$  in horizontal plane. The tension in the string is  $T$ .

If we double the radius ( $R' = 2R$ ), but keep the period of the motion the same, how is  $T'$  related to  $T$ ?

- (A)  $T' = \frac{1}{4} T$       (B)  $T' = \frac{1}{2} T$       (C)  $T' = T$   
 (D)  $T' = 2 T$       (E)  $T' = 4 T$

You said:

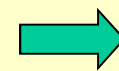
- $T = (MV^2)/R$ , so if you double the radius, the equation will be multiplied by 1/2.
- If you double the Radius you have to double the speed to keep the period the same. Since the Tension force in this case is  $mv^2/R$ , doubling the radius and velocity would result in a net change of 2 to the original Tension.
- to double the radius and keep the period the same, the ball will now travel twice as far in the same time interval. this will press the need for a greater velocity ( $v$  to  $2v$ ). in equations in relation to kinematics, the velocity is a squared term. thus, if he transition from  $v$  to  $2v$ , our force to hold this will go from  $T$  to  $4T$  (2 squared is four).



BB

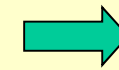
KEY

$$v = \frac{2\pi R}{P}$$



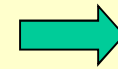
$v$  doubles  
when  
 $R$  doubles

$$a = \frac{v^2}{R}$$



$a$  doubles  
when  
 $R$  doubles

$$T = ma$$



$T$  doubles  
when  
 $R$  doubles

