

# Physics 101: Lecture 29

## Thermodynamics II: Engines & refrigerators

# Recap:

→ 1st Law of Thermodynamics

→ energy conservation

$$Q = \Delta U + W$$

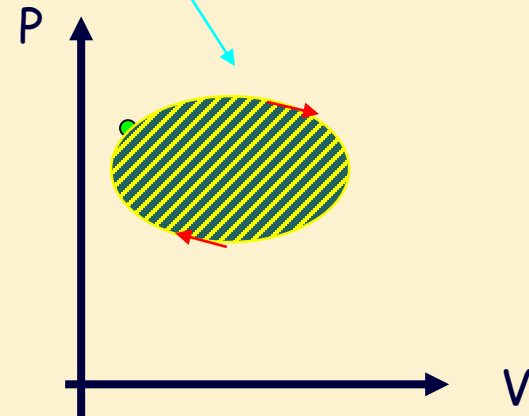
Heat flow  
into system

Change in internal  
energy of system

Work done by system

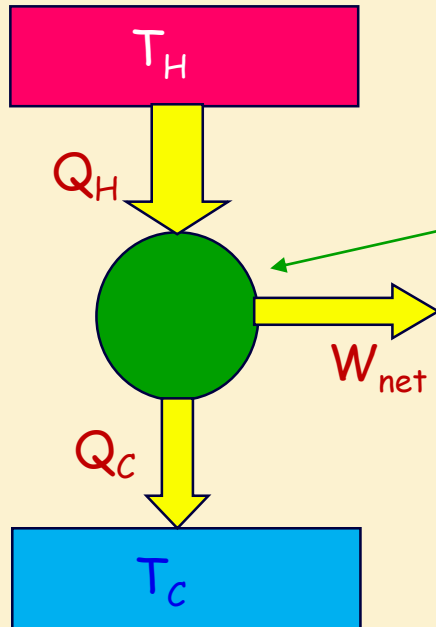
- $U$  depends only on  $T$  ( $U = 3nRT/2 = 3PV/2$ )
- point on  $p$ - $V$  plot completely specifies state of system ( $PV = nRT$ )
- work done is area under curve
- for a complete cycle

$$\Delta U = 0 \Rightarrow Q = W$$

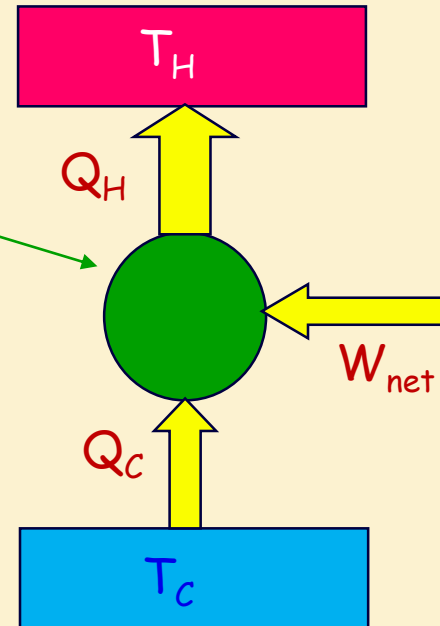


# Engines and Refrigerators

"HEAT ENGINE"



REFRIGERATOR



- system taken in closed cycle  $\Rightarrow \Delta U_{\text{system}} = 0$
- therefore, net heat absorbed = work done by system

$$Q_H = Q_C + W_{\text{net}} \quad (\text{Engine})$$

$$Q_C + W_{\text{net}} = Q_H \quad (\text{Refrigerator})$$

energy into green blob = energy leaving green blob

# Heat Engine: Efficiency

The objective: turn heat from hot reservoir into work

The cost: "waste heat"

1st Law:  $Q_H - Q_C = W$

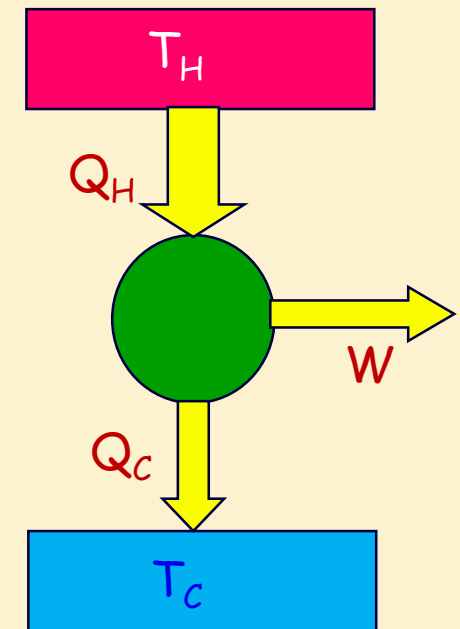
efficiency definition:  $e \equiv W/Q_H$

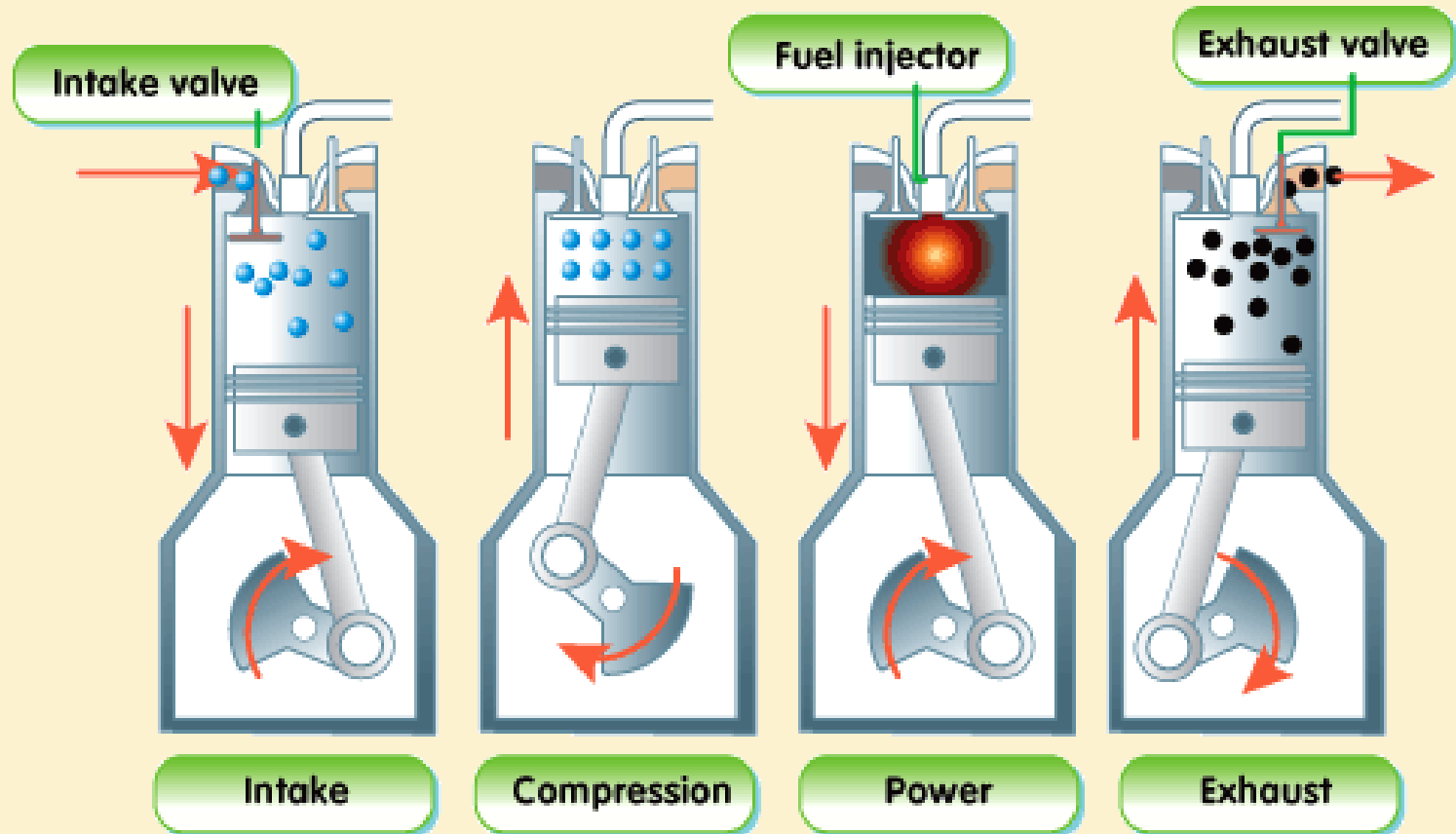
$$= W/Q_H$$

$$= (Q_H - Q_C)/Q_H$$

$$= 1 - Q_C/Q_H$$

HEAT ENGINE





# Heat Engine Clicker Q

- Can you get “work” out of a heat engine, if the hottest thing you have is at room temperature?

1) Yes

2) No

# Rate of Heat Exhaustion

An engine operating at 25% efficiency produces work at a rate of 0.10 MW. At what rate is heat exhausted into the surrounding?

$$\text{Efficiency } e = W_{\text{net}}/Q_{\text{H}} \Rightarrow Q_{\text{H}} = W_{\text{net}}/e$$

The question is asking for  $Q_{\text{C}}/\Delta t$  .

$$Q_{\text{H}}/t = (W_{\text{net}}/t)/e = 0.10 \text{ MW}/0.25 = 0.40 \text{ MW}$$

From 1<sup>st</sup> Law of Thermo:  $W_{\text{net}} = Q_{\text{H}} - Q_{\text{C}}$ ; divide by  $\Delta t$ :

$$W_{\text{net}}/\Delta t = (Q_{\text{H}} - Q_{\text{C}})/\Delta t$$

$$0.10 \text{ MW} = 0.40 \text{ MW} - Q_{\text{C}}/\Delta t$$

$$Q_{\text{C}}/\Delta t = 0.40 \text{ MW} - 0.10 \text{ MW} = 0.3 \text{ MW}$$

# Refrigerator: Coefficient of Performance

The objective: remove heat from cold reservoir

The cost: work

1st Law:  $Q_H = W + Q_C$

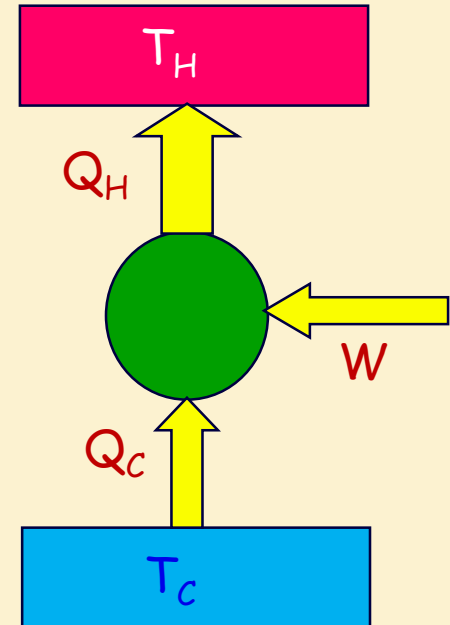
coefficient of performance

$$\begin{aligned} CP &\equiv Q_C / W \\ &= Q_C / (Q_H - Q_C) \end{aligned}$$

Best CP you can have is Carnot coeff. of performance (more on Carnot in 4 slides):

$$CP_{\text{Carnot}} = T_C / (T_H - T_C)$$

REFRIGERATOR





# Entropy (S)

- A measure of “disorder” (more entropy means more disorder)
- A property of a system (just like P, V, T, U)
  - related to number of number of different possible “states” of system
- Examples of increasing entropy:
  - ice cube melts
  - gases expand into vacuum (recall demo of vacuum cannon)
- Change in entropy:
  - $\Delta S = Q/T$ 
    - »  $> 0$  if heat flows into system ( $Q > 0$ )
    - »  $< 0$  if heat flows out of system ( $Q < 0$ )

# Clicker Questions

A hot (98 C) slab of metal is placed in a cool (5C) bucket of water.

$$\Delta S = Q/T$$

What happens to the entropy of the metal?

- A) Increases      B) Same      C) Decreases

What happens to the entropy of the water?

- A) Increases      B) Same      C) Decreases

What happens to the total entropy (water+metal)?

- A) Increases      B) Same      C) Decreases

# A word on the Checkpoint Q on mixing yellow and blue water

- Process is irreversible—the mixing creates a batch of green water that we cannot separate back into two batches of blue and yellow water, so entropy increases.
- Another way to look at it. Big batch of water has more space for molecules to move around than the two smaller batches so it is more disordered.
- Answers to Checkpoint: 1. A 2. D 3. A
- (To answer 3, use last equation is slide 8: “refrigerators” from the last prelecture, or last eqn on slide 8 in this lecture, to compare impact of raising  $T_C$  by 10 or lowering  $T_H$  by 10)

# Second Law of Thermodynamics

- The entropy change ( $Q/T$ ) of the system+**environment**  $\geq 0$ 
  - never  $< 0$
  - order to disorder
- Consequences
  - A “disordered” state cannot spontaneously transform into an “ordered” state
  - No engine operating between two reservoirs can be more efficient than one that produces 0 change in entropy. This is called a “Carnot engine”

# Carnot Cycle

- Idealized Heat Engine

- No Friction

- $\Delta S = Q/T = 0$

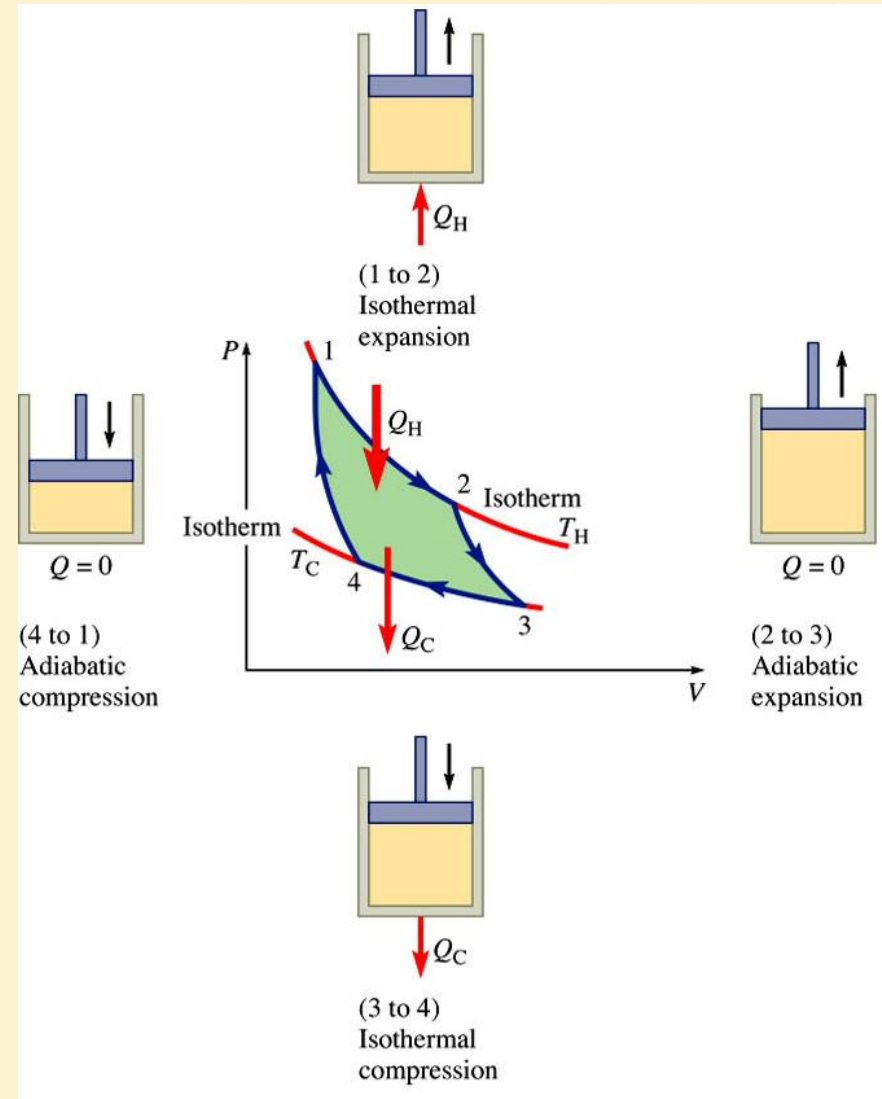
- Reversible Process

- » Isothermal Expansion

- » Adiabatic Expansion

- » Isothermal Compression

- » Adiabatic Compression



# Engines and the 2nd Law

The objective: turn heat from hot reservoir into work

The cost: "waste heat"

1st Law:  $Q_H - Q_C = W$

efficiency  $e \equiv W/Q_H = (Q_H - Q_C)/Q_H$

$$\Delta S = Q_C/T_C - Q_H/T_H \geq 0$$

$$\Delta S = 0 \text{ for Carnot}$$

Therefore,  $Q_C/Q_H \geq T_C/T_H$

$$Q_C/Q_H = T_C/T_H \text{ for Carnot}$$

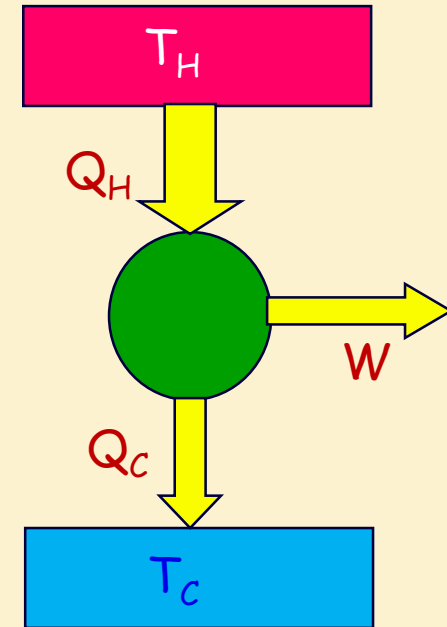
Therefore  $e = 1 - Q_C/Q_H \leq 1 - T_C/T_H$

$$e = 1 - T_C/T_H \text{ for Carnot}$$

$e = 1$  is forbidden!

$e$  largest if  $T_C \ll T_H$

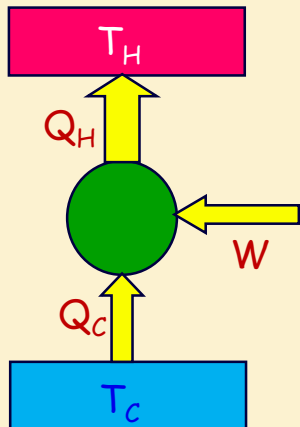
## HEAT ENGINE



# Example 1

Consider a hypothetical refrigerator that takes 1000 J of heat from a cold reservoir at 100K and ejects 1200 J of heat to a hot reservoir at 300K.

- |   |                   |
|---|-------------------|
| 1. How much work does the refrigerator do?          | Answers:<br>200 J |
| 2. What happens to the entropy of the universe?     | Decreases         |
| 3. Does this violate the 2nd law of thermodynamics? | yes               |



$$Q_C = 1000 \text{ J} \quad \text{Since } Q_C + W = Q_H, \quad W = 200 \text{ J}$$
$$Q_H = 1200 \text{ J}$$

$$\Delta S_H = Q_H / T_H = (1200 \text{ J}) / (300 \text{ K}) = 4 \text{ J/K}$$

$$\Delta S_C = -Q_C / T_C = (-1000 \text{ J}) / (100 \text{ K}) = -10 \text{ J/K}$$

$$\Delta S_{\text{TOTAL}} = \Delta S_H + \Delta S_C = -6 \text{ J/K} \rightarrow \text{decreases (violates 2nd law)}$$

# Example 2

Consider a hypothetical device that takes 1000 J of heat from a hot reservoir at 300K, ejects 200 J of heat to a cold reservoir at 100K, and produces 800 J of work.

Does this device violate the second law of thermodynamics ?

1. Yes ← correct

2. No total entropy decreases.

$$\Delta S_H = Q_H / T_H = (1000 \text{ J}) / (300 \text{ K}) = 3.33 \text{ J/K}$$

$$\Delta S_C = Q_C / T_C = (200 \text{ J}) / (100 \text{ K}) = 2 \text{ J/K}$$

$$\Delta S_{\text{TOTAL}} = \Delta S_C - \Delta S_H = -1.33 \text{ J/K} \rightarrow \text{(violates 2}^{\text{nd}} \text{ law)}$$

- $W (800) = Q_{\text{hot}} (1000) - Q_{\text{cold}} (200)$
- $\text{Efficiency} = W / Q_{\text{hot}} = 800 / 1000 = 80\%$
- $\text{Max eff} = 1 - T_c / T_h = 1 - 100 / 300 = 67\%$



# Clicker Q

Which of the following is forbidden by the second law of thermodynamics?

1. Heat flows into a gas and the temperature falls
2. The temperature of a gas rises without any heat flowing into it
3. Heat flows spontaneously from a cold to a hot reservoir
4. All of the above

# Summary

- **First Law** of thermodynamics: Energy Conservation  
→  $Q = \Delta U + W$
- Heat Engines  
→ Efficiency =  $1 - Q_C/Q_H$
- Refrigerators  
→ Coefficient of Performance =  $Q_C/(Q_H - Q_C)$
- Entropy  $\Delta S = Q/T$
- **Second Law**: Entropy always increases!
- Carnot Cycle: Reversible, Maximum Efficiency  $e = 1 - T_c/T_h$

It has been a pleasure teaching this class!