

Kinematics and mechanics:

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$v = v_0 + at$$

$$v^2 = v_0^2 + 2a\Delta x$$

$$F = ma$$

$$a_c = \frac{v^2}{r}$$

$$E_{tot} = K.E. + P.E.$$

$$K.E. = \frac{1}{2} m v^2 = \frac{p^2}{2m}$$

$$p = mv$$

$$W_F = Fd \cos \theta$$

Electrostatics:

$$F_{12} = \frac{kq_1 q_2}{r^2}$$

$$E \equiv \frac{F}{q_0}$$

$$U_{12} = \frac{kq_1 q_2}{r}$$

$$V \equiv \frac{U}{q_0}$$

$$W_E = -\Delta U = -W_{you}$$

Point charge:

$$E = \frac{kq}{r^2}$$

$$V = \frac{kq}{r}$$

Electric dipole:

$$p \equiv qd$$

$$\tau_{dip} = pE \sin \theta$$

$$U_{dip} = -pE \cos \theta$$

Resistance:

$$R \equiv \frac{V}{I}$$

$$I = \frac{\Delta q}{\Delta t}$$

Physical resistance: $R = \rho \frac{L}{A}$

$$P = IV = I^2 R = \frac{V^2}{R}$$

$$R_S = R_1 + R_2 + \dots$$

$$\frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

Capacitance:

$$C \equiv \frac{Q}{V}$$

Parallel plate capacitor: $C = \frac{\kappa \epsilon_0 A}{d}$, $E = \frac{Q}{\epsilon_0 A}$, $V = Ed$

$$U_C = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C}$$

$$C_P = C_1 + C_2 + \dots$$

$$\frac{1}{C_S} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

Circuits:

$$\sum \Delta V = 0$$

$$\sum I_{in} = \sum I_{out}$$

$$q(t) = q_\infty (1 - e^{-t/\tau})$$

$$q(t) = q_0 e^{-t/\tau}$$

$$I(t) = I_0 e^{-t/\tau}$$

$$\tau = RC$$

Magnetism:

$$F = qvB \sin \theta$$

$$r = \frac{mv}{qB}$$

$$F_{wire} = ILB \sin \theta$$

$$\tau_{loop} = NIAB \sin \phi$$

Magnetic dipole:

$$\mu \equiv NIA$$

$$\tau_{dip} = \mu B \sin \phi$$

$$U_{dip} = -\mu B \cos \phi$$

$$B_{wire} = \frac{\mu_0 I}{2\pi r}$$

$$B_{sol} = \mu_0 nI$$

Electromagnetic induction:

$$\varepsilon = -N \frac{\Delta\Phi}{\Delta t}$$

$$|\varepsilon_{bar}| = BLv$$

$$V_{rms} = \frac{V_{max}}{\sqrt{2}}$$

$$\Phi = BA \cos \varphi$$

$$\varepsilon_{gen} = \varepsilon_{max} \sin \omega t = \omega NAB \sin \omega t$$

$$I_{rms} = \frac{I_{max}}{\sqrt{2}}$$

$$\omega = 2\pi f$$

$$\frac{V_p}{V_s} = \frac{I_s}{I_p} = \frac{N_p}{N_s}$$

Electromagnetic waves:

$$\lambda = \frac{c}{f}$$

$$E = cB$$

$$u_E = \frac{1}{2} \varepsilon_0 E^2 \quad u_B = \frac{1}{2\mu_0} B^2$$

$$\bar{u} = \frac{1}{2} \varepsilon_0 E_{rms}^2 + \frac{1}{2\mu_0} B_{rms}^2 = \varepsilon_0 E_{rms}^2 = \frac{B_{rms}^2}{\mu_0}$$

$$S = I = \bar{u}c = \frac{P}{A}$$

$$f_o = f_e \sqrt{\frac{1+v_{rel}/c}{1-v_{rel}/c}} \approx f_e \left(1 + \frac{v_{rel}}{c}\right)$$

$$I = I_0 \cos^2 \theta$$

Reflection and refraction:

$$\theta_r = \theta_i$$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$f = \pm \frac{R}{2}$$

$$m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$v = \frac{c}{n}$$

$$\sin \theta_c = \frac{n_2}{n_1}$$

$$M = \frac{\theta'}{\theta} \approx \frac{d_{near}}{f}$$

Compound microscope:

$$m_{obj} = -\frac{L_{tube}}{f_{obj}}$$

$$M_{eye} = \frac{d_{near}}{f_{eye}}$$

$$M_{tot} = M_{eye} m_{obj}$$

Interference and diffraction:

Double slit interference:

$$d \sin \theta = m\lambda$$

$$d \sin \theta = (m + \frac{1}{2})\lambda$$

$$m = 0, \pm 1, \pm 2 \dots$$

Single-slit diffraction:

$$a \sin \theta = m\lambda$$

$$m = \pm 1, \pm 2 \dots$$

Circular aperture:

$$a \sin \theta \approx 1.22\lambda$$

Quantum mechanics:

$$E = hf = \frac{hc}{\lambda}$$

$$\lambda = \frac{h}{p}$$

$$\Delta p_x \Delta x \geq \frac{\hbar}{2}$$

$$\hbar \equiv \frac{h}{2\pi}$$

$$\text{Bohr atom: } 2\pi r_n = n\lambda \quad n = 1, 2, 3 \dots$$

$$L_n = m_e v_n r_n = n\hbar$$

$$r_n = \left(\frac{\hbar^2}{m_e k e^2} \right) \frac{n^2}{Z} \approx (5.29 \times 10^{-11} \text{ m}) \frac{n^2}{Z}$$

$$E_n = - \left(\frac{m_e k^2 e^4}{2\hbar^2} \right) \frac{Z^2}{n^2} \approx -(13.6 \text{ eV}) \frac{Z^2}{n^2}$$

$$\frac{1}{\lambda} \approx (1.097 \times 10^7 \text{ m}^{-1}) Z^2 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

$$\text{Quantum atom: } L = \sqrt{\ell(\ell+1)}\hbar$$

$$L_z = m_\ell \hbar$$

$$S_z = m_s \hbar$$

$$\text{Atomic magnetism: } \mu_{e,z} = -\frac{e}{2m_e} L_z$$

$$\mu_{s,z} = -\frac{ge}{2m_e} S_z, \quad g \approx 2$$

$$\mu_B \equiv \frac{e\hbar}{2m_e} \approx 5.8 \times 10^{-5} \text{ eV/T}$$

Nuclear physics and radioactive decay:

$$A = Z + N$$

$$r \approx (1.2 \times 10^{-15} \text{ m}) A^{1/3}$$

$$E_0 = mc^2$$

$$m_{\text{nucleus}} = Zm_{\text{proton}} + Nm_{\text{neutron}} - \frac{|E_{\text{bind}}|}{c^2}$$

$$\frac{\Delta N}{\Delta t} = -\lambda N$$

$$N(t) = N_0 e^{-\lambda t} = N_0 2^{-t/T_{1/2}}$$

$$T_{1/2} \equiv \frac{\ln 2}{\lambda} \approx \frac{0.693}{\lambda}$$

Constants and unit conversions:

$$g = 9.8 \text{ m/s}^2$$

$$e = 1.60 \times 10^{-19} \text{ C}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$$

$$k \equiv \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = 3 \times 10^8 \text{ m/s}$$

$$h = 6.626 \times 10^{-34} \text{ J} \cdot \text{s}$$

$$hc = 1240 \text{ eV} \cdot \text{nm}$$

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$

$$m_{\text{electron}} = 9.11 \times 10^{-31} \text{ kg} = 511 \text{ keV}/c^2$$

$$m_{\text{proton}} = 1.673 \times 10^{-27} \text{ kg} = 938.3 \text{ MeV}/c^2$$

$$m_{\text{neutron}} = 1.675 \times 10^{-27} \text{ kg} = 939.5 \text{ MeV}/c^2$$

| SI Prefixes | | |
|-------------|--------|--------|
| Power | Prefix | Symbol |
| 10^9 | giga | G |
| 10^6 | mega | M |
| 10^3 | kilo | k |
| 10^0 | — | — |
| 10^{-3} | milli | m |
| 10^{-6} | micro | μ |
| 10^{-9} | nano | n |
| 10^{-12} | pico | p |