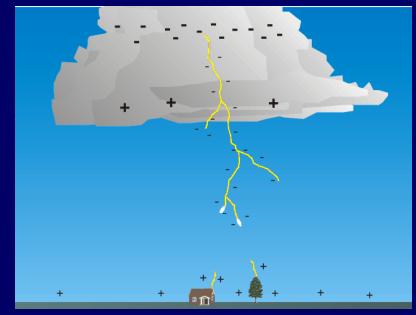
Physics 102: Lecture 04

Capacitors

(& batteries)





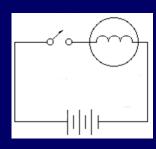
Physics 102 so far

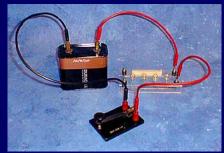
Basic principles of electricity

- Lecture 1 electric charge & electric force
- Lecture 2 electric field
- Lecture 3 electric potential energy and electric potential

Applications of electricity – circuits

- Lecture 4 capacitance
- Lecture 5 resistance
- Lecture 6 Kirchhoff's rules
- Lecture 7 RC circuits
- Lecture 12 & 13 AC circuits





Recall from last lecture.... Electric Fields, Electric Potential

Comparison:

Electric Potential Energy vs. Electric Potential



 ΔV_{AB} : the difference in electric potential between points B and A

 ΔU_{AB} : the change in <u>electric potential energy</u> of a charge q when moved from A to B

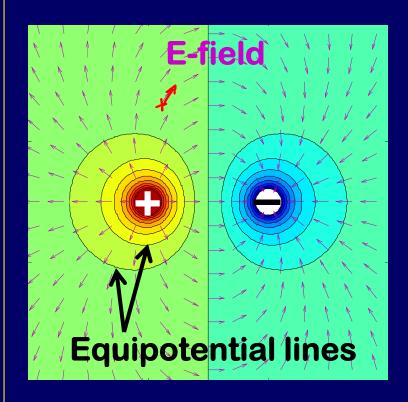
$$\Delta U_{AB} = q \Delta V_{AB}$$

Electric Potential: Summary

- E field lines point from higher to lower potential
- For positive charges, going from higher to lower potential is "downhill"

Positive charges tend to go "downhill", from + to -

Negative charges go in the opposite direction, from – to +



$$\Delta U_{AB} = q \Delta V_{AB}$$

Uniform Electric Field: Important Special Case

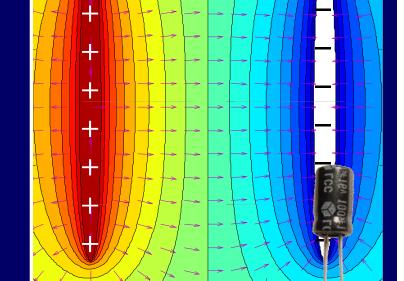
Two large parallel conducting plates of area A

- +Q on one plate
- −Q on other plate

Then E is

- uniform between the two plates: $E=4\pi kQ/A$
- zero everywhere else
- This result is independent of plate separation

 Only brucy large plates



This is called a parallel plate capacitor

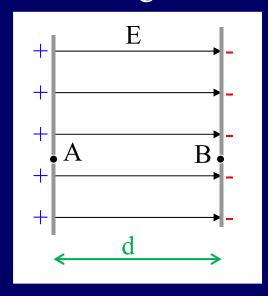


Parallel Plate Capacitor: Potential Difference

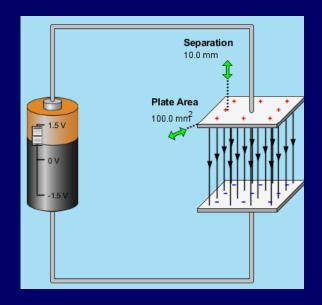
Charge Q on plates

$$V = V_A - V_B = +E d$$
 (like $W = qEd = \Delta U$; $\Delta V = \Delta U/q$)
= $4 \pi k Q d / A$ $\sqrt{\alpha} Q$

Voltage is proportional to the charge!

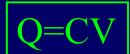


PhET Simulation



Capacitance: The ability to store separated charge C≡Q/V

- Any pair conductors separated by a small distance. (e.g. two metal plates)
- Capacitor stores <u>separated charge</u>



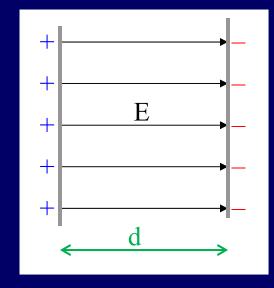
- Positive Q on one conductor, negative Q on other
- Net charge is zero

• Stores Energy $U_c = (\frac{1}{2}) Q V$ $U_c = \frac{1}{2} C V = \frac{1}{2} Q V$

Units:

1 Coulomb/Volt

= 1 Farad (F)



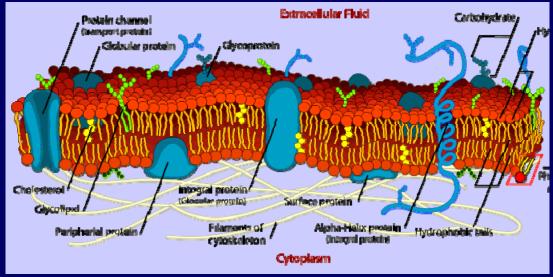
Why Separate Charge?

A way to store and release energy!

- Camera Flash
- Defibrillator
- AC \rightarrow DC
- Tuners / resonant circuits
 - Radio
 - Cell phones
- Cell membranes









Capacitance of Parallel Plate Capacitor

 $V = Ed \quad E=4\pi kQ/A$

(Between two large plates)

So: $V = 4\pi kQd/A$

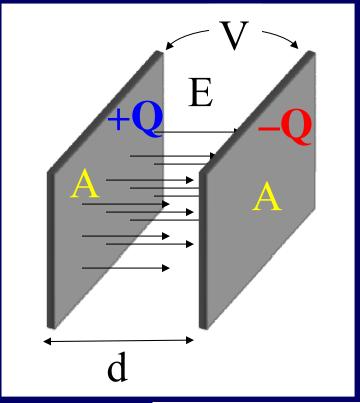
Recall: C≡Q/V

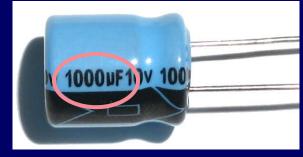
So: $C = A/(4\pi kd)$

Recall: Leex. 1

 $\varepsilon_0 = 1/(4\pi k) = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

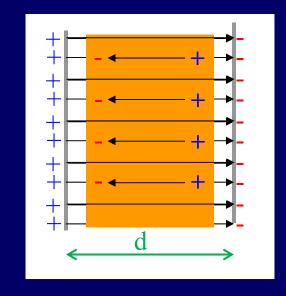
 $C = \varepsilon_0 A/d$ Parallel plate capacitor

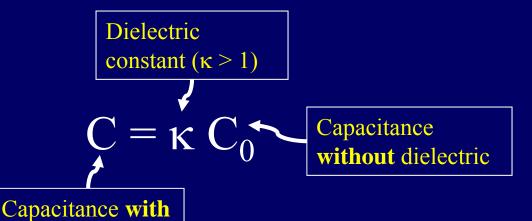




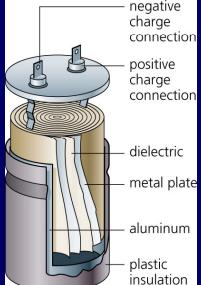
Dielectric

• Placing a dielectric (insulator) between the plates increases the capacitance.





For same charge Q, E (and V) is reduced so C = Q/V increases

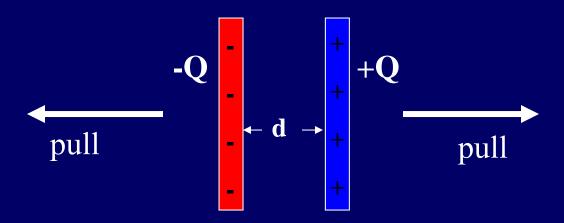


Physics 102: Lecture 4, Slide 11

dielectric



ACT: Parallel Plates



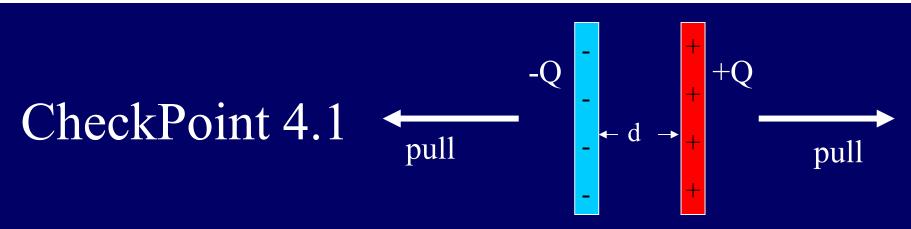
A parallel plate capacitor given a charge Q. The plates are then pulled a small distance further apart. What happens to the charge Q on each plate of the capacitor?

A) Increases



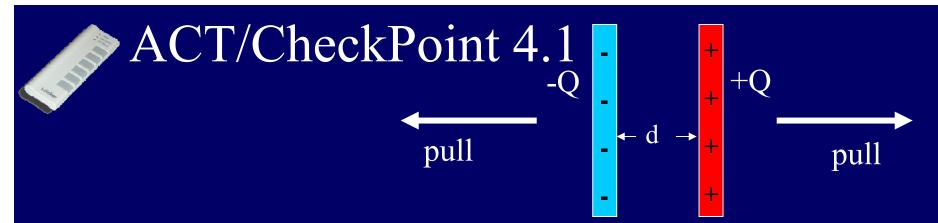
C) Decreases

Remember charge is real/physical. There is no place for the charges to go.



A parallel plate capacitor given a charge Q. The plates are then pulled a small distance further apart. Which of the following apply to the situation after the plates have been moved?





A parallel plate capacitor given a charge Q. The plates are then pulled a small distance further apart. Which of the following apply to the situation after the plates have been moved?

The energy stored in the capacitor



B) constant

C) decreases

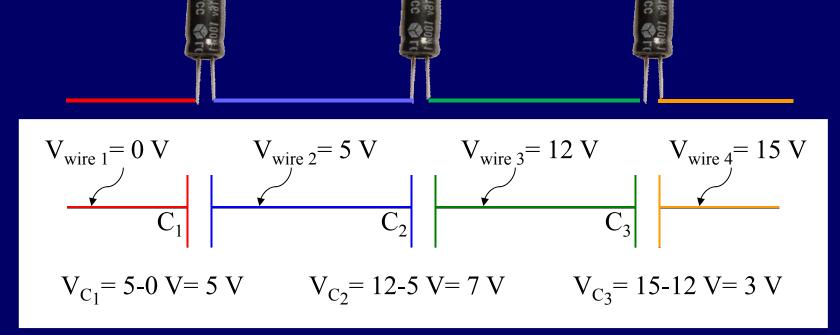
U= ½ QV Q constant, V increased

Plates are attracted to each other, you must pull them apart, so the potential energy of the plates increases.

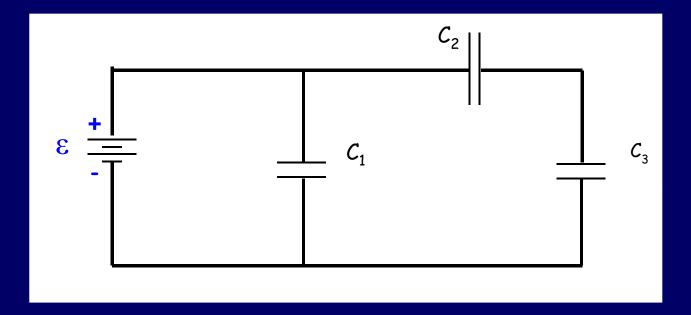
Capacitors are used in circuits!



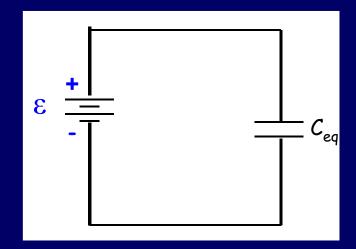
- In circuits, elements are connected by wires.
- Any connected region of wire has the same potential.
- The potential difference across an element is the *element's* "voltage."



To understand complex circuits...

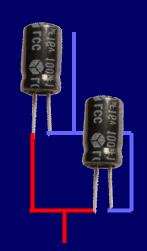


...treat capacitors in series and parallel as a fictitious equivalent capacitor!

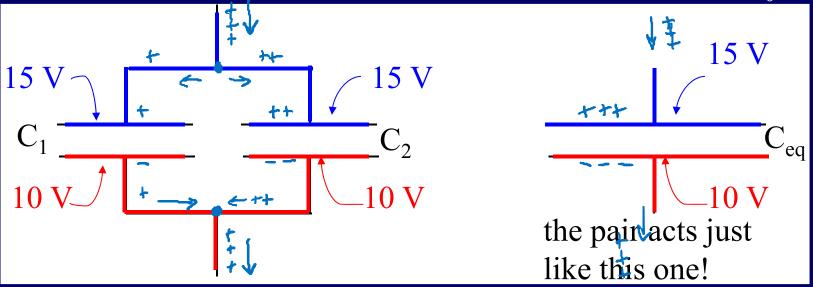


Capacitors in Parallel

- Both ends connected together by wire
- Same voltage: $V_1 = V_2 = V_{eq}$
- Share Charge: $Q_{eg} = Q_{1} + Q_{2}/J_{2}$ Equivalent C: $C_{eg} = C_{1} + C_{2}$
- Equivalent C: C_{eq}



Add areas – remember $C=\varepsilon_0 A/d$



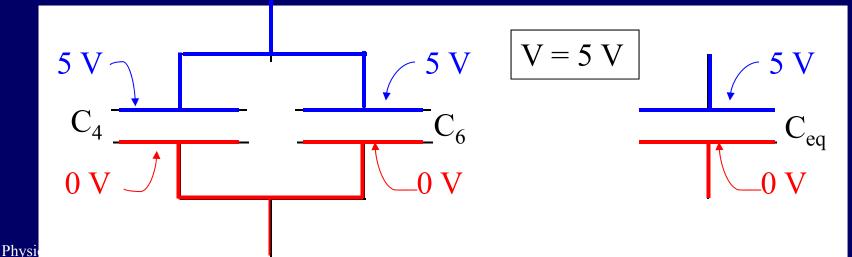




Parallel Practice

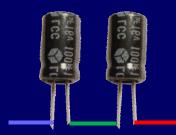
A 4 μF capacitor and 6 μF capacitor are connected in parallel and charged to 5 volts. Calculate C_{eq} , and the charge on each capacitor.

$$\begin{split} &C_{eq} = C_4 + C_6 = 4 \ \mu F + 6 \ \mu F = 10 \ \mu F \\ &Q_4 = C_4 \ V_4 = (4 \ \mu F)(5 \ V) = 20 \ \mu C \\ &Q_6 = C_6 \ V_6 = (6 \ \mu F)(5 \ V) = 30 \ \mu C \\ &Q_{eq} = C_{eq} \ V_{eq} = (10 \ \mu F)(5 \ V) = 50 \ \mu C = Q_4 + Q_6 \end{split}$$

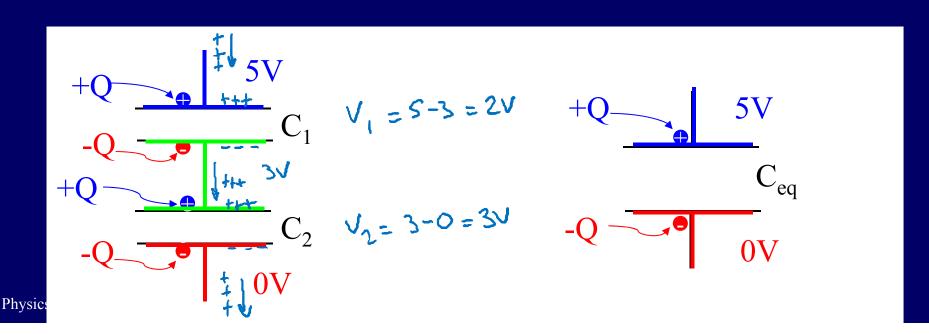


Capacitors in Series

- Connected end-to-end with NO other exits
- Same Charge: $Q_1 = Q_2 = Q_{eq}$



• Share Voltage: $V_{Q_1} + V_{Q_2} = V_{Q_1}$ • Equivalent C: $\frac{1}{c_{eq}} = \frac{1}{c_1} + \frac{1}{c_2}$ Add d – remember $C = \varepsilon_0 A/d$







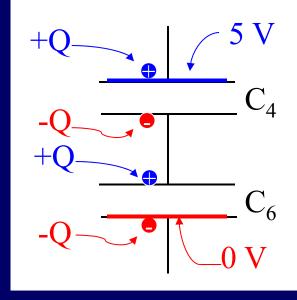
Series Practice

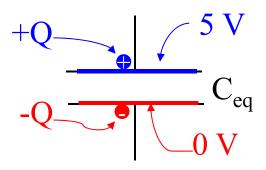
A 4 μF capacitor and 6 μF capacitor are connected in series and charged to 5 volts. Calculate C_{eq} , and the charge on the 4 μF capacitor.

$$C_{eq} = \left(\frac{1}{C_4} + \frac{1}{C_6}\right)^{-1} = \left(\frac{1}{4\mu F} + \frac{1}{6\mu F}\right)^{-1} = 2.4\mu F$$

$$Q = CV$$

$$Q_4 = Q_6 = Q_{eq} = C_{eq}V = (2.4\mu F)(5V) = 12\mu C$$





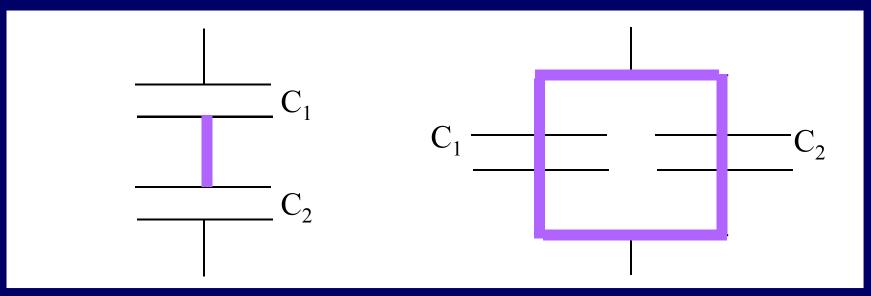
Comparison: Series vs. Parallel

Series

• Can follow a wire from one element to the other with no branches in between.

Parallel

• Can find a loop of wire containing both elements but no others (may have branches).

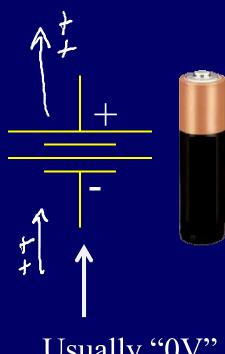


Electromotive Force

Battery

- Maintains constant potential difference V (electromotive force – emf ε)
- Does NOT produce or supply charges, just "pushes" them.

Like a pump for charge!



Usually "0V" by convention

CheckPoint 4.4

A circuit consists of three initially uncharged capacitors C_1 , C_2 , and C_3 , which are then connected to a battery of emf ε . The capacitors obtain charges q_1 , q_2 , q_3 , and have voltages across their plates V_1 , V_2 , and V_3 . C_{eq} is the equivalent capacitance of the circuit. Which of these are true?

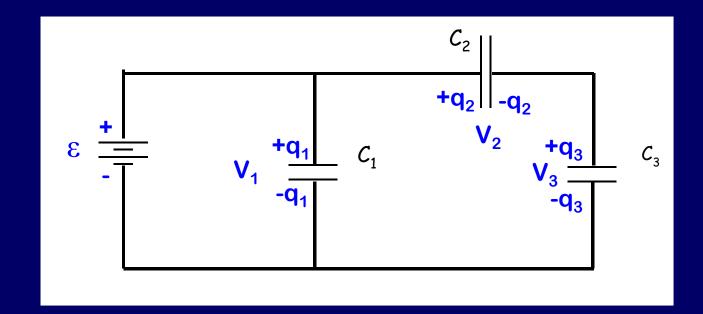
1)
$$q_1 = q_2$$

2)
$$q_2 = q_3$$

3)
$$V_2 = V_3$$

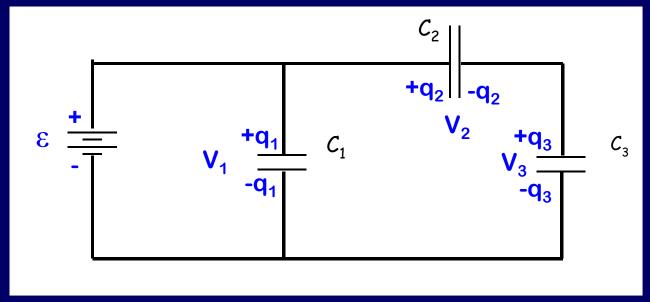
4)
$$\varepsilon = V_1$$

5)
$$V_1 < V_2$$



ACT/CheckPoint 4.4: Which is true?

A circuit consists of three initially uncharged capacitors C_1 , C_2 , and C_3 , which are then connected to a battery of emf ε . The capacitors obtain charges q_1 , q_2 , q_3 , and have voltages across their plates V_1 , V_2 , and V_3 . C_{eq} is the equivalent capacitance of the circuit.

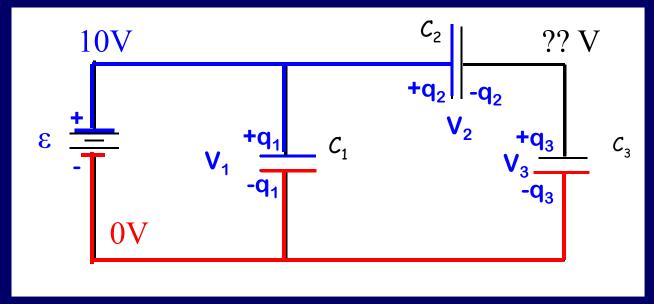


1) $q_1 = q_2$ Not necessarily. C_1 and C_2 are NOT in series.

(2)
$$q_2 = q_3$$
 Yes! C_2 and C_3 are in series.

ACT/CheckPoint 4.4: Which is true?

A circuit consists of three initially uncharged capacitors C_1 , C_2 , and C_3 , which are then connected to a battery of emf ε . The capacitors obtain charges q_1 , q_2 , q_3 , and have voltages across their plates V_1 , V_2 , and V_3 . C_{eq} is the equivalent capacitance of the circuit.



1) $V_2 = V_3$ Not necessarily, only if $C_2 = C_3$

2) $\varepsilon = V_1$ Yes! Both ends are connected by wires

Recap of Today's Lecture

- Capacitance C = Q/V
- Parallel Plate: $C = \varepsilon_0 A/d$
- Capacitors in parallel: $C_{eq} = C_1 + C_2$
- Capacitors in series: $1/C_{eq} = 1/C_1 + 1/C_2$
- Batteries provide fixed potential difference