

Phys 102 – Lecture 21

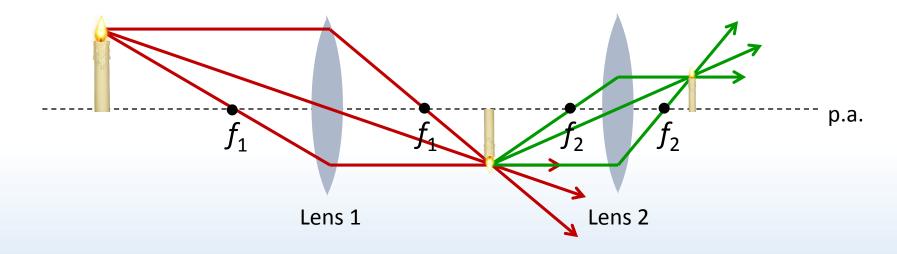
Optical instruments

Today we will...

- Learn how combinations of lenses form images
 Thin lens equation & magnification
- Learn about the compound microscope
 Eyepiece & objective
 Total magnification
- Learn about limits to resolution
 Spherical & chromatic aberrations
 Dispersion

CheckPoint 1.1–1.2: multiple lenses

Image of first lens becomes object for second lens, etc...



Lens 1 creates a real, inverted and reduced image of the object 65%

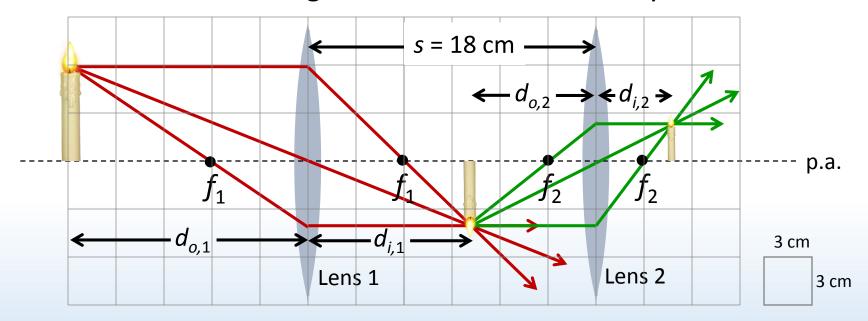
Lens 2 creates a real, inverted and reduced image of the image from lens 1

The combination gives a real, upright, reduced image of the object 52%



Calculation: final image location

Determine the final image location for the 2-lens system



$$\frac{1}{d_{i,1}} = \frac{1}{f_1} - \frac{1}{d_{o,1}} = \frac{1}{6} - \frac{1}{15} = \frac{1}{10}$$

$$\frac{1}{d_{i,2}} = \frac{1}{f_2} - \frac{1}{d_{o,2}} = \frac{1}{3} - \frac{1}{8} = \frac{1}{4.8}$$

$$d_{i,1} + d_{o,2} = s$$

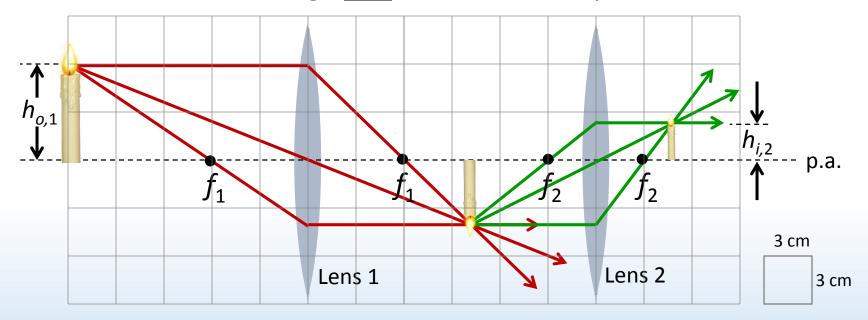
$$d_{i,1} + d_{o,2} = s$$
 $d_{o,2} = 18 - 10 = 8 \text{ cm}$

$$d_{i,2} \neq 4.8$$
 m

Diagram should agree!

Calculation: final magnification

Determine the final image <u>size</u> for the 2-lens system



$$m_{tot} = m_1 m_2 = \frac{h_{i,1}}{h_{o,1}} \frac{h_{i,2}}{h_{o,2}} = \frac{h_{i,2}}{h_{o,1}}$$
 $h_{i,2} = m_{tot} h_{o,2} = +0.4 \cdot 6 +2.4 \text{ cm}$ Upright, reduced image

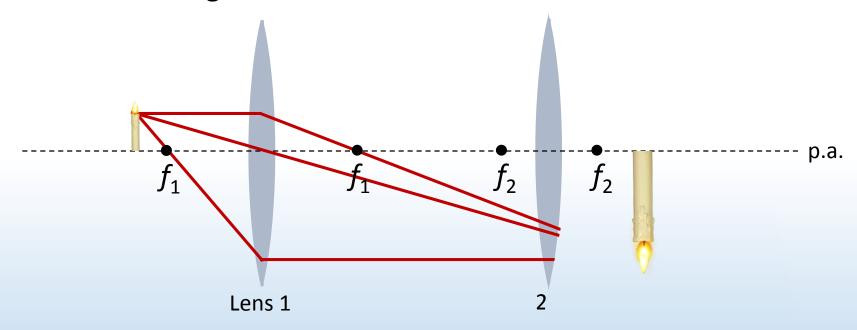
$$= \left(-\frac{d_{i,1}}{d_{o,1}}\right) \left(-\frac{d_{i,2}}{d_{o,2}}\right) = \left(-\frac{10}{15}\right) \left(-\frac{4.8}{8}\right) = +0.4$$

oprignt, reduced image



ACT: CheckPoint 1.3

Now, the second converging lens is placed to the left of the first lens' image.



Which statement is true?

30% A. Lens 2 has no object

38% B. Lens 2 has a real object

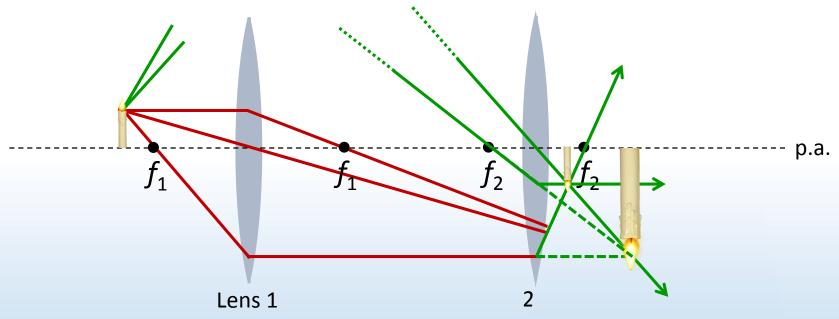
32% C. Lens 2 has a virtual object

Object after lens 2 is virtual: $d_{o,2} < 0$ Image still forms but rays seem to originate from point after lens 2



ACT: CheckPoint 1.4

Now, the second converging lens is placed to the left of the first lens' image.



What is the image formed from lens 2?

33% A. There is no image

36% **B.** Real

31% C. Virtual

$$\frac{1}{d_{i,2}} = \frac{1}{f_2} - \frac{1}{d_{o,2}}$$

$$d_{o,2} < 0$$
, so $d_{i,2} > 0$

Lens combination: summary

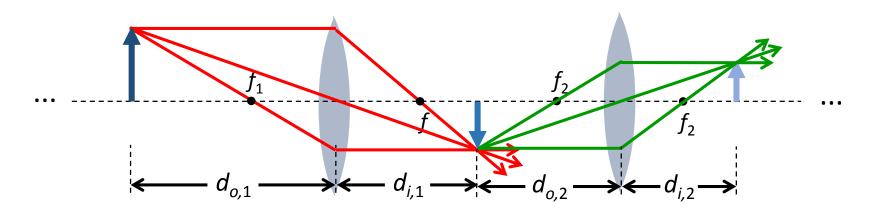


Image of first lens becomes object of second lens, ...

$$m_{tot} = m_1 m_2 m_3 \dots$$

- d_0 = distance object is from lens:
 - > 0: <u>real</u> object (<u>before</u> lens)
 - < 0: virtual object (after lens)

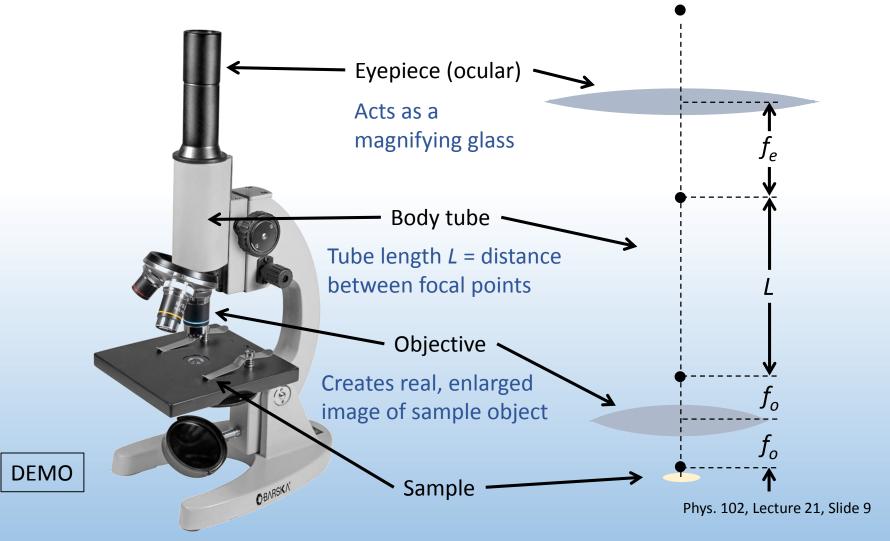
- d_i = distance image is from lens:
 - > 0: real image (after lens)
 - < 0: virtual image (before lens)

- *f* = focal length lens:
 - > 0: converging lens
 - < 0: diverging lens

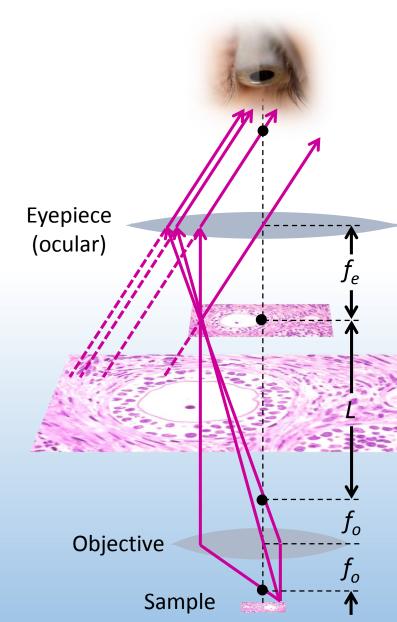
Watch your signs!

Compound microscope

A compound microscope is made up of two converging lenses



Microscope ray diagram



Total image magnification:

$$M_{tot} = M_e m_o = -\frac{d_{near}}{f_e} \frac{L}{f_o}$$

Eyepiece creates virtual, upright image at ∞

$$M_e = \frac{d_{near}}{f_e}$$
 Recall Lect. 20

Object just past objective focal pt. creates real, inverted image at eyepiece focal pt.

$$\frac{1}{d_{i}} = \frac{d_{i}^{1}}{f_{bo}} \frac{d_{i}^{1}}{dd_{o}} = \frac{L + f_{o}}{f_{o}} + m_{o}$$

$$m_{o} = -\frac{d_{i}}{d_{o}} = -\frac{L}{f_{o}}$$



ACT: Microscope eyepiece

The magnification written on a microscope eyepiece assumes the user has "normal" adult vision



 $10 \times \text{means } M_{\rho} = 10$

$$M_e = \frac{d_{near}}{f_e}$$

In normal vision $d_{near} = 25$ cm

$$f_e = \frac{d_{near}}{M_e} = \frac{25}{10} = 2.5 \,\text{cm}$$

What is the focal length of a 10× eyepiece?

A.
$$f_e = 2.5 \text{ cm}$$

B.
$$f_e = 10 \text{ cm}$$

C.
$$f_e = 25 \text{ cm}$$



ACT: Microscope objective

A standard biological microscope has a 160 mm tube length and is equipped with a 40× objective



$$40 \times \text{ means } m_o = -40$$

$$m_o = -\frac{L}{f_o}$$

$$f_o = -\frac{160}{-40} = 4 \text{mm}$$

What is the focal length of the objective?

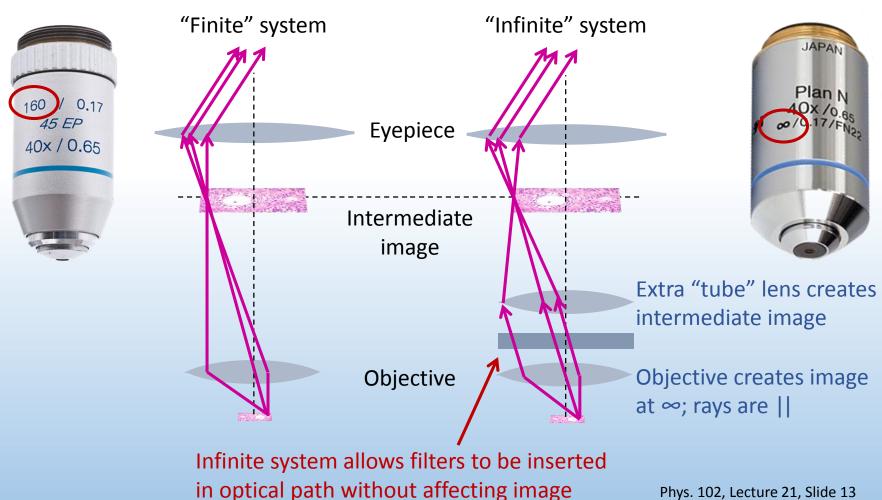
A.
$$f_o = 4 \text{ mm}$$

B.
$$f_0 = 8 \text{ mm}$$

C.
$$f_0 = 16 \text{ mm}$$

Modern microscope objectives

Most modern objectives are "infinity corrected"



Phys. 102, Lecture 21, Slide 13

Calculation: Angular size

A microscope has a $10 \times$ eyepiece and a $60 \times$ objective. How much larger does the microscope image appear to our eyes?

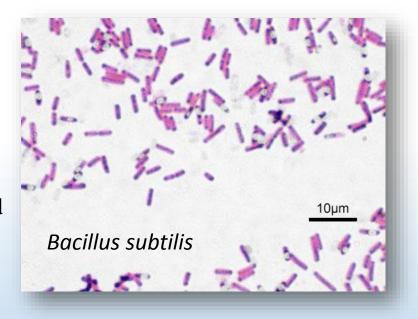
$$M_{tot} = M_e m_o = \frac{\theta_{mic}}{\theta_{unaided}}$$
$$= -600$$

At a near pt. of 25 cm, a 2-μm bacterium has angular size to an unaided eye of:

$$\theta_{unaided} \approx \frac{h_o}{d_{near}} = \frac{2 \times 10^{-6}}{0.25} = 8 \times 10^{-6} \text{ rad}$$

In the microscope the angular size is:

$$|\theta_{mic}| = 600 \cdot 8 \times 10^{-6} = 4.8 \times 10^{-3} \text{ rad}$$



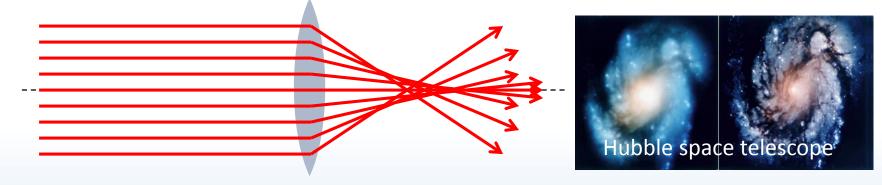
Equivalent to a $600 \times 2 \mu m = 1.2 mm$ object at 25 cm

What limits the resolution of a light microscope?

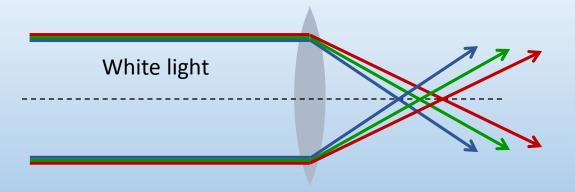
Aberrations

Aberrations are imperfections relative to ideal lens

Spherical: rays hitting lens at different points focus differently



Chromatic: rays of different color focus differently



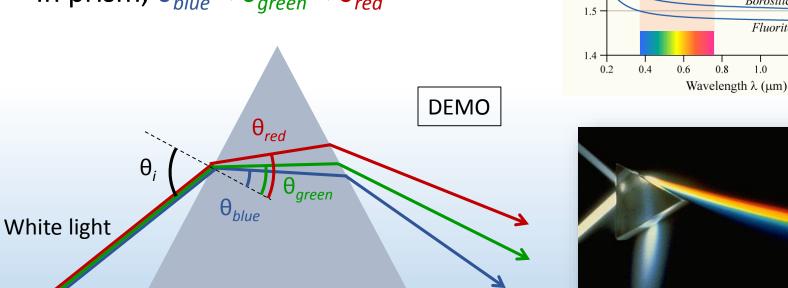


Dispersion

The index of refraction n depends on λ

In glass,
$$n_{blue} > n_{green} > n_{red}$$

In prism,
$$\theta_{blue} < \theta_{green} < \theta_{red}$$



Blue light gets deflected more

1.8

1.7

Refractive index n

 $n_i \sin \theta_i = n_{blue} \sin \theta_{blue} = n_{green} \sin \theta_{green} = n_{red} \sin \theta_{red}$

Prism

Lanthanum dense flint LaSF9

Dense flint SF10

Barium crown BaK4

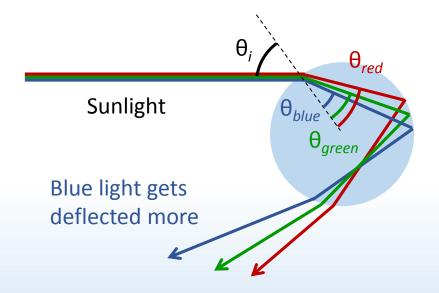
Borosilicate crown BK7

Fluorite crown FK51A

Flint F2

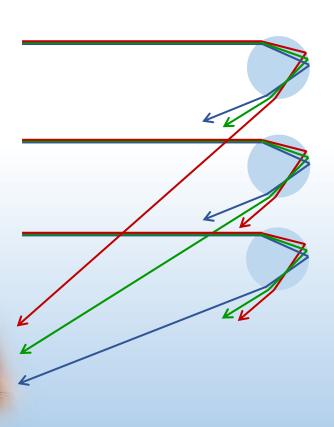
CheckPoint 2.1: Rainbows

Dispersion in water droplets create rainbows

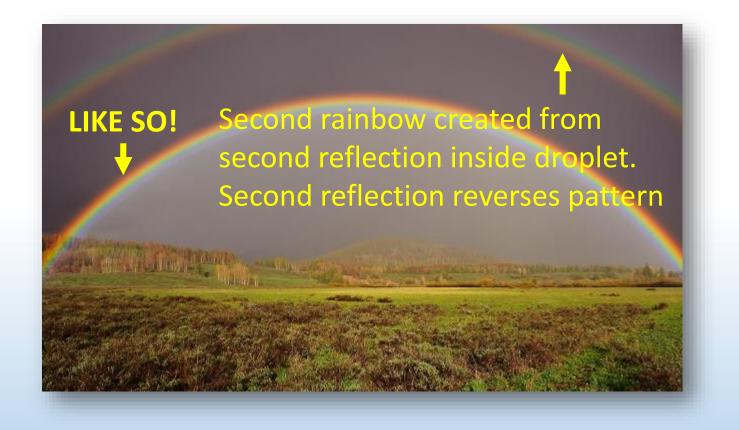


In water, $n_{blue} > n_{green} > n_{red}$

Red rays from higher droplet, blue rays from lower droplet reach eye



Double rainbow

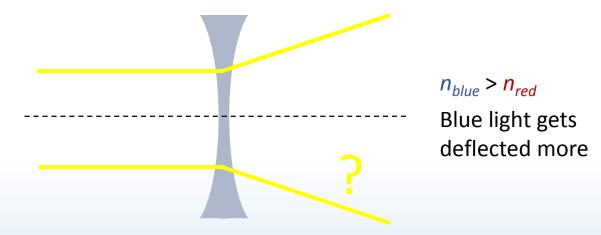


Double rainbow

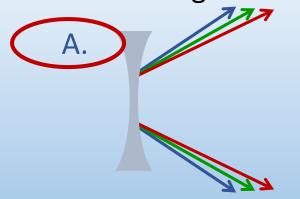


ACT: Dispersion

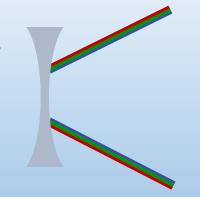
A <u>diverging</u> lens made of flint glass has $n_{red} = 1.57$, $n_{blue} = 1.59$. Parallel rays of white light are incident on the lens.

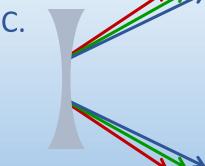


Which diagram best represents how light is transmitted?



B.





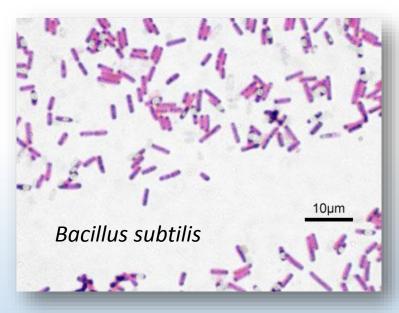
Ultimate limit of resolution

One can play clever tricks with combinations of lenses to compensate for spherical and chromatic aberrations

Ultimately, even with *ideal* lenses resolution of light microscope is limited to ~λ of light (~500 nm)

We won't understand why using ray picture of light; we have to treat light as a wave again

Next two lectures!



Ray optics works for objects $\gg \lambda$

Summary of today's lecture

Combinations of lenses:

Image of first lens is object of second lens... Watch signs!

The compound microscope

Objective forms real image at focal pt. of eyepiece Eyepiece forms virtual image at ∞

Limits to resolution

Spherical & chromatic aberrations

Dispersion

Diffraction limit – next week!