



Phys 102 – Lecture 14

Faraday's law of induction

Today we will...

- Continue our discussion of electromagnetic induction unifying electricity & magnetism

Last time: Lenz' law for EMF direction

Today: Faraday's law for EMF magnitude

- Apply these concepts

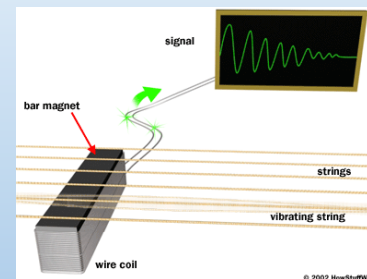
Lenz' & Faraday's law are basis for electrical generators & transformers, and much more



Power plant



Credit card reader



Guitar pickup

Faraday's law of induction

Change in flux Φ through a loop induces an EMF ε

$$\varepsilon = - \frac{\Delta\Phi}{\Delta t}$$

Induced EMF ε Rate of change of flux Φ

Magnitude

Induced EMF ε = rate of change of flux Φ

$$|\varepsilon| = \left| \frac{\Delta\Phi}{\Delta t} \right|$$

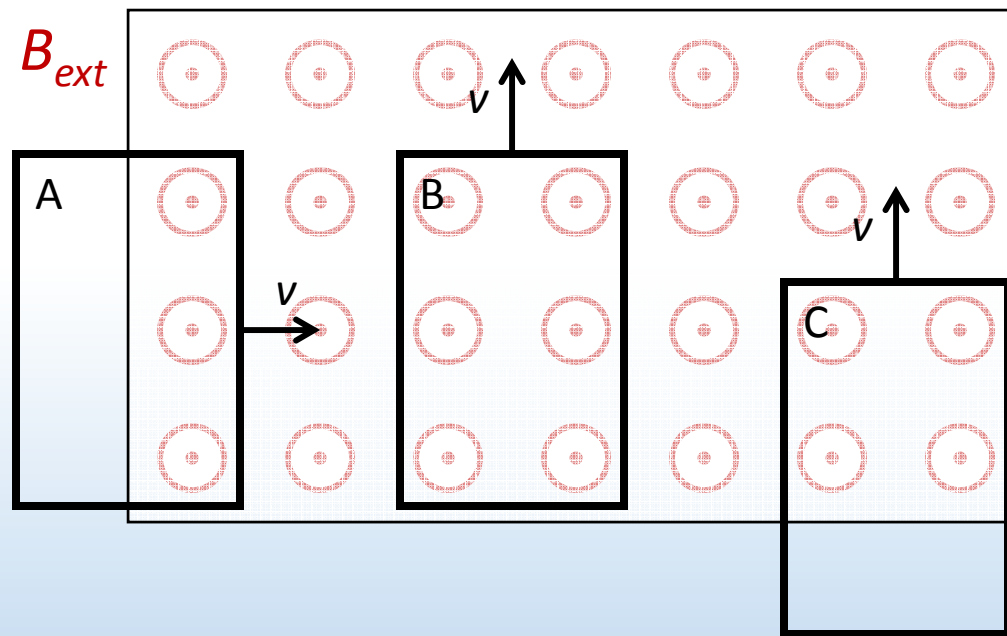
Direction

Lenz' law: EMF ε opposes change in flux Φ



ACT: moving loops

Three loops are moving at the same speed v in a region containing a uniform B field. The field is zero everywhere outside.



In which loop is $|\epsilon|$ greatest at the instant shown?

A. Loop A

B. Loop B

C. Loop C

Faraday's Law of Induction

“Induced EMF” = rate of change of magnetic flux

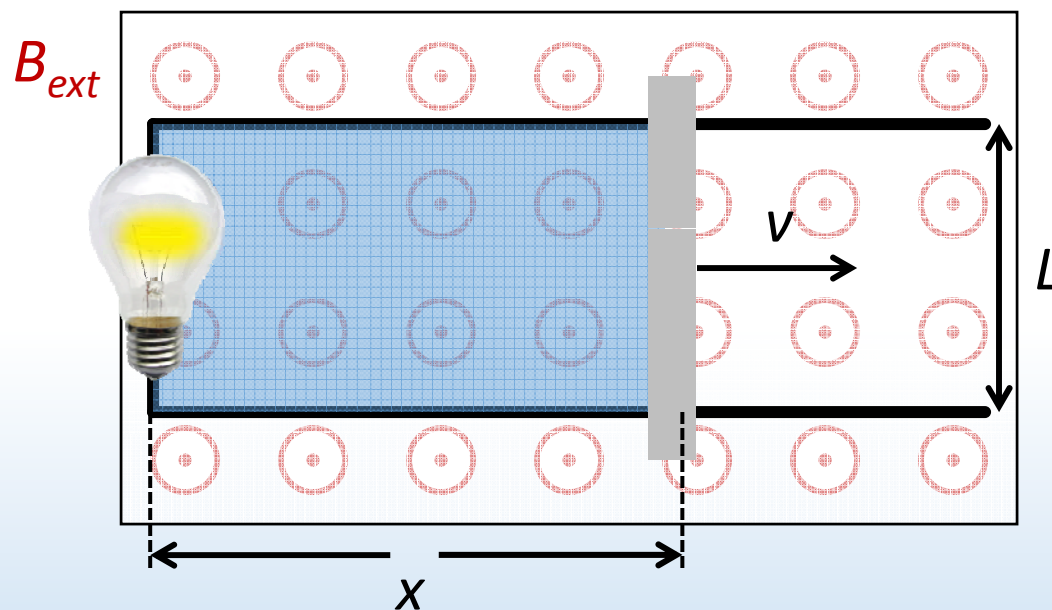
$$\varepsilon = -\frac{\Delta\Phi}{\Delta t}$$

Since $\Phi = BA \cos \varphi$, 3 things can change Φ

1. Area of loop covered by flux
2. Magnetic field B
3. Angle φ between normal and B

Calculation: changing area

A bar slides with speed v on a conducting track in a uniform B field

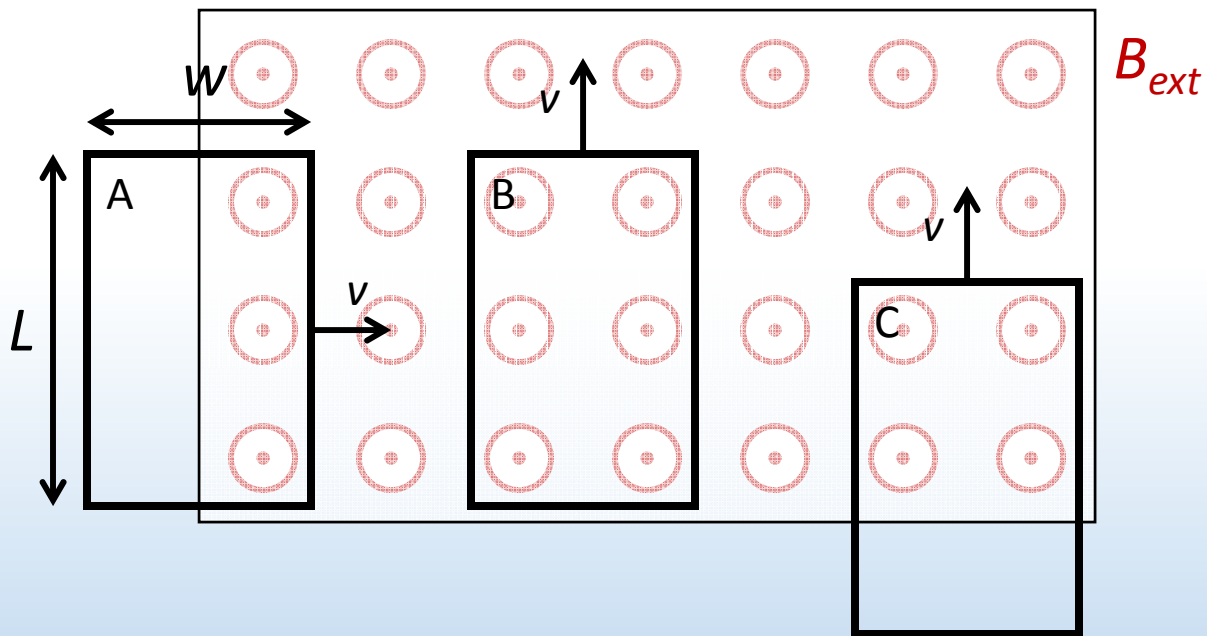


What is the magnitude of the EMF induced in the circuit?

$$|\varepsilon| = \left| \frac{\Delta\Phi}{\Delta t} \right| \quad \Phi = B_{ext}Lx \quad \text{and only } x \text{ is changing}$$
$$= \frac{\Delta(B_{ext}Lx)}{\Delta t} = B_{ext}L \frac{\Delta x}{\Delta t} = B_{ext}Lv$$

Moving loops revisited

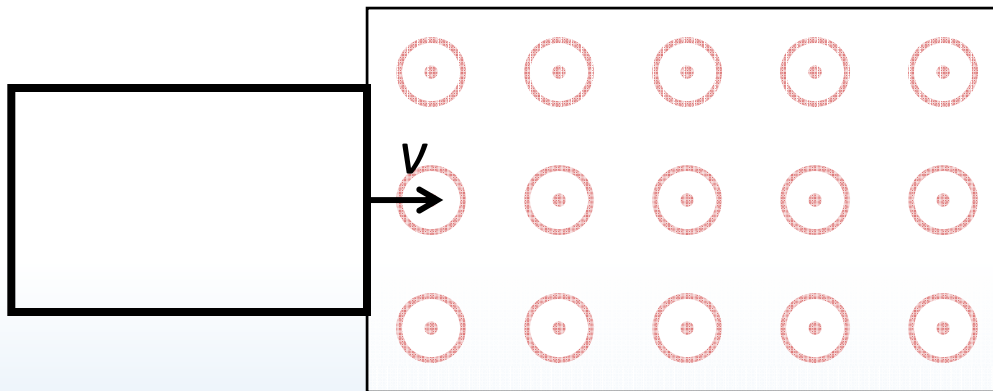
Three loops are moving at the same speed v in a region containing a uniform B field. The field is zero everywhere outside.



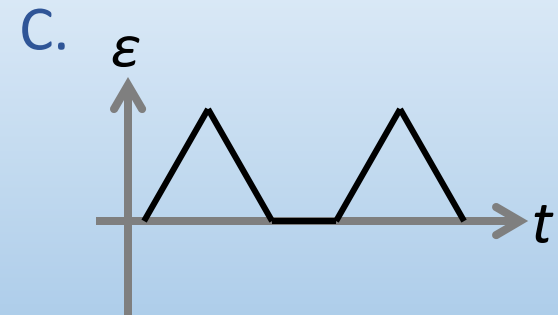
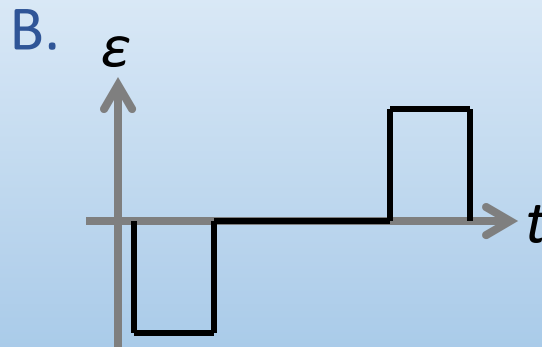
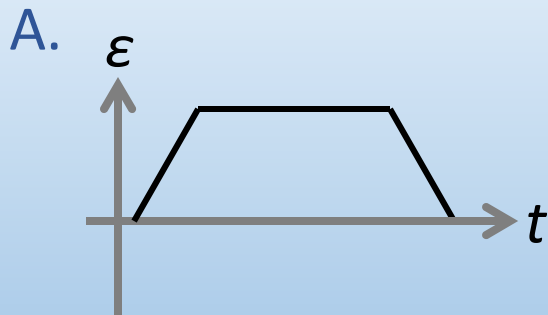


ACT: Moving loop

A loop moves through a region with a uniform B field at a constant speed v . The field is zero outside.



Which diagram best represents the EMF ϵ in the loop vs. time?



Calculation: solenoid cannon

A loop of radius $r_{loop} = 11$ cm is placed around a long solenoid. The solenoid has a radius $r_{sol} = 4.8$ cm and $n = 10,000$ turns/m of wire. The current I through solenoid increases at a rate of 1.5 A/s.

EXAM 2, FA13

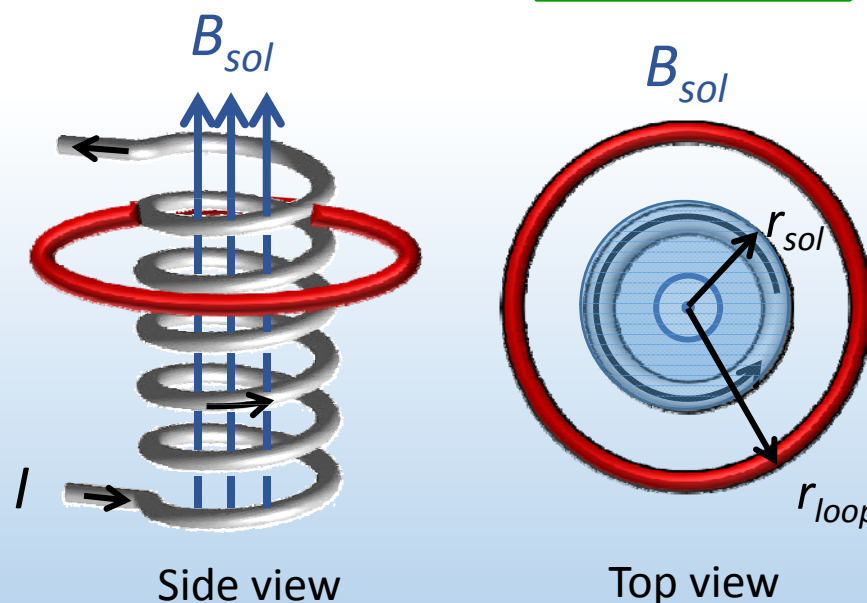
What is the EMF $|\varepsilon|$ in the loop?

$$|\varepsilon| = \left| \frac{\Delta\Phi}{\Delta t} \right| \quad \Phi = B_{sol} A_{sol} \cos \varphi$$

B field is changing, area is constant

$$B_{sol}(t) = \mu_0 n I(t)$$

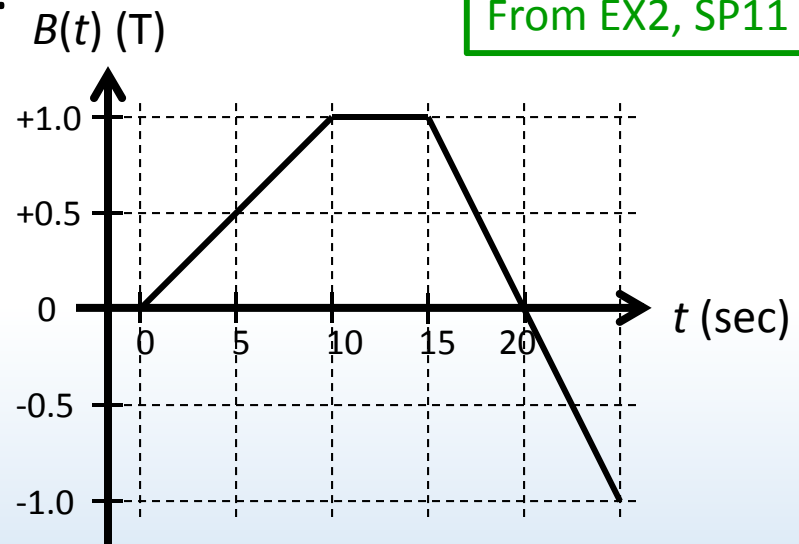
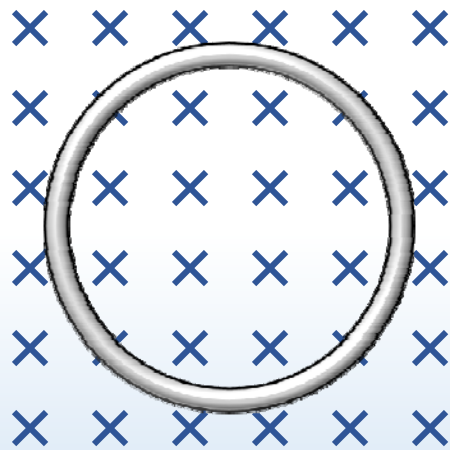
$$|\varepsilon| = \frac{\Delta B_{sol}}{\Delta t} A_{sol} = \mu_0 n \frac{\Delta I}{\Delta t} A_{sol}$$





ACT: time-varying B field

A circular loop is placed in a uniform B field that varies in time according to the plot on the right.

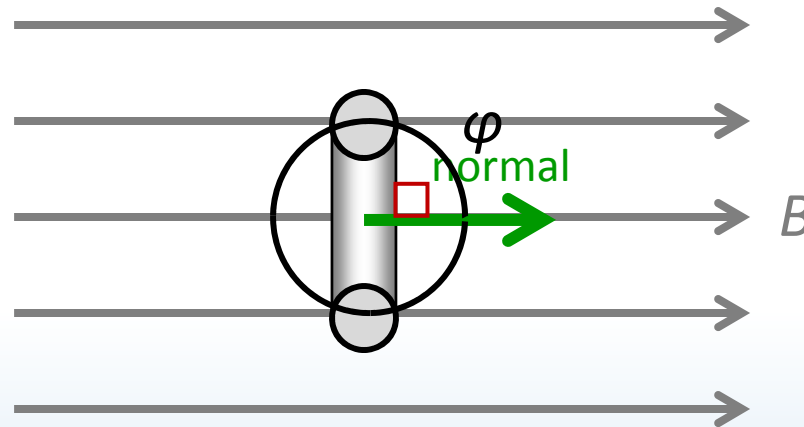


At which time is the EMF magnitude $|\varepsilon|$ in the loop largest?

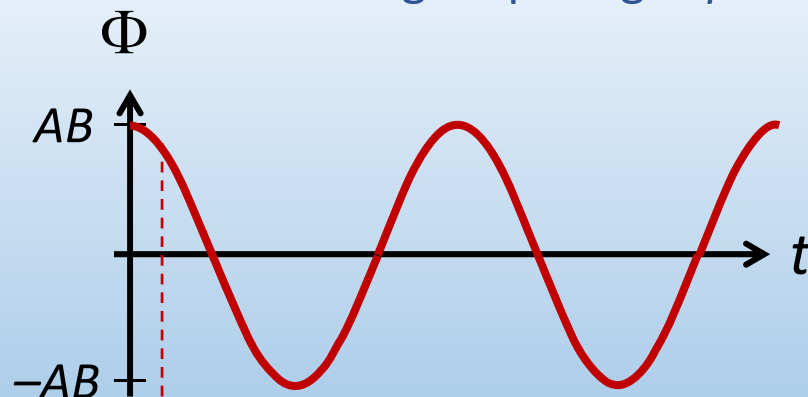
- A. $t = 5 \text{ s}$
- B. $t = 12 \text{ s}$
- C. $t = 20 \text{ s}$

Changing φ

EMF can be induced by changing angle φ between loop normal and B field



Rotating loop: Angle φ increases at a rate ω (in rad/s)

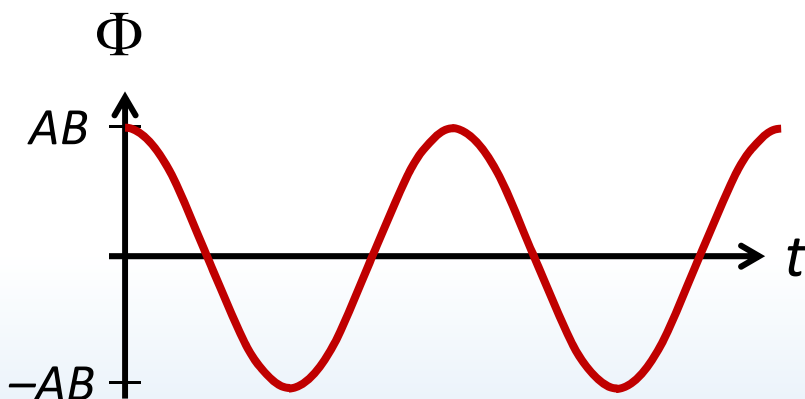


$$\Phi(t) = BA \cos \omega t$$

$\varphi = 30^\circ$ (**CheckPoint 1.1**)

Calculation: EMF from changing φ

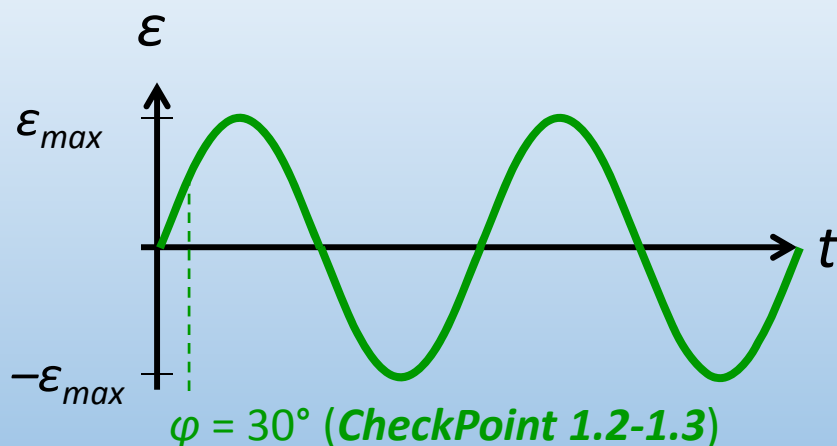
What is the EMF induced by changing angle φ between loop normal and B field?



$$\Phi(t) = BA \cos \omega t$$

$$\varepsilon = -\frac{\Delta\Phi}{\Delta t}$$

$\Delta\Phi/\Delta t$ represents rate of change or *slope* of Φ vs. t at that particular time



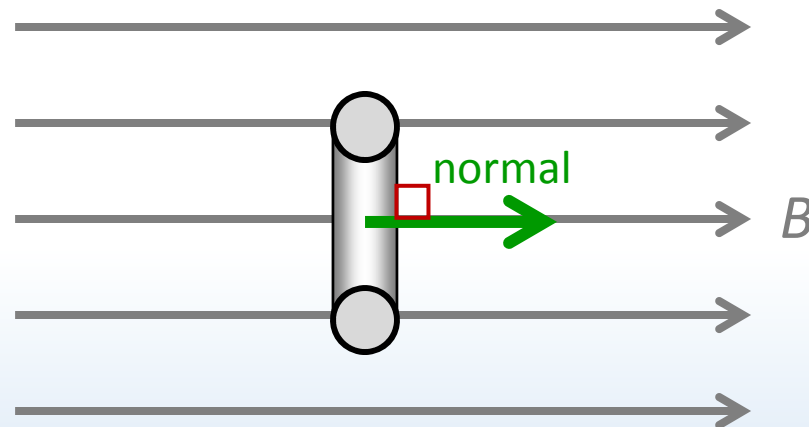
$$\varepsilon(t) = \varepsilon_{\max} \sin \omega t$$

EMF is a sine wave!



ACT: Rotating loop

The loop below rotates in a uniform B field. Which of the following factors can increase the EMF in the loop?

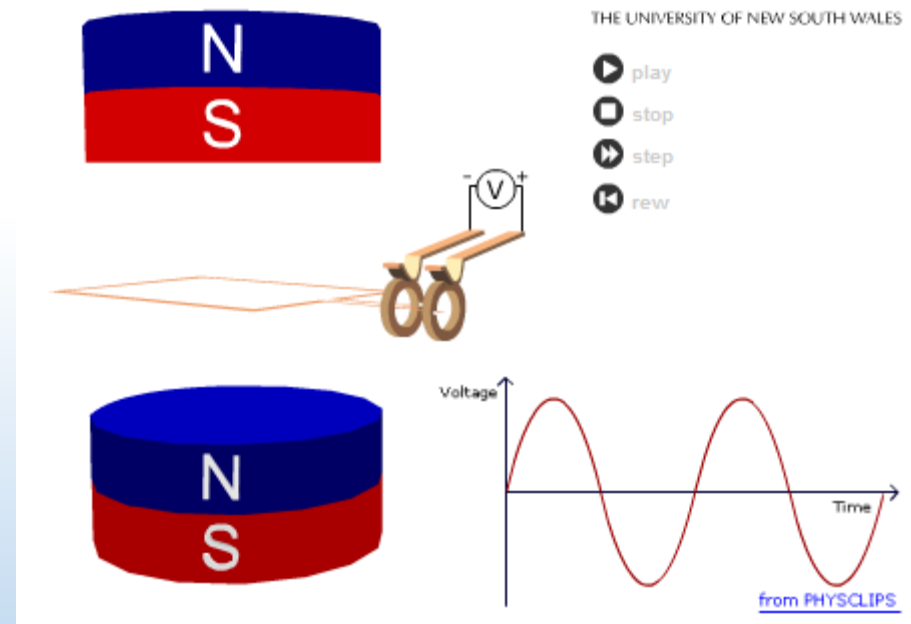
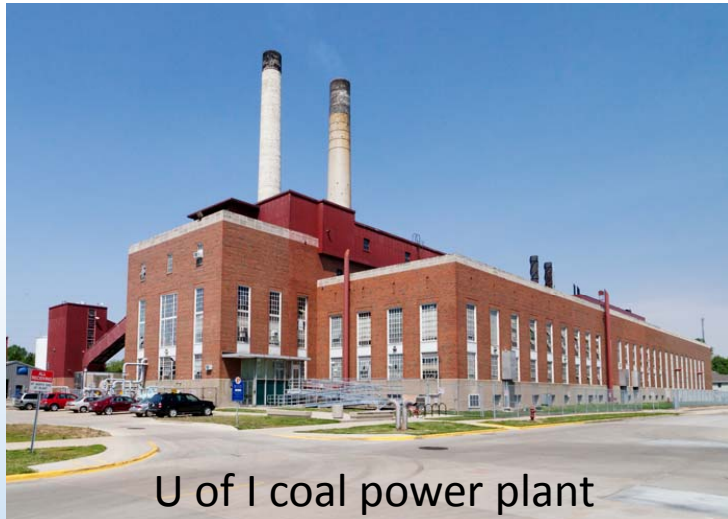


DEMO

- A. Increasing the rotation rate ω
- B. Wrapping more turns of wire around the loop
- C. Increasing the B field
- D. All of the above

Application: generators

Electrical generators use external energy source (gas, steam, water, wind, nuclear, etc) to spin loop in B field



Why electrical current from outlets is alternating current (AC)
In US, current oscillates at a frequency of 60 Hz (cycles/s)

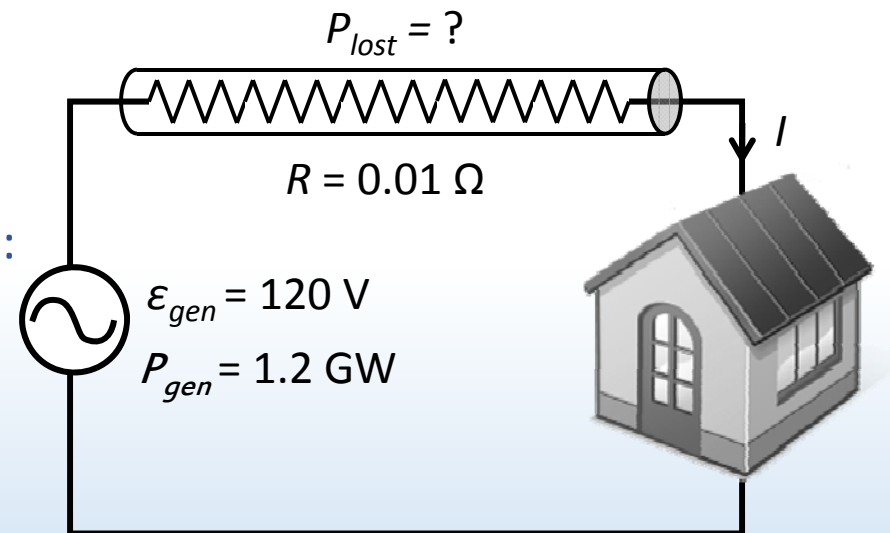
Calculation: CheckPoint 2

A generator produces 1.2 Giga Watts of power, which it transmits to a town through power lines with total resistance 0.01Ω .

How much power is lost in the lines if it is transmitted at 120 V?

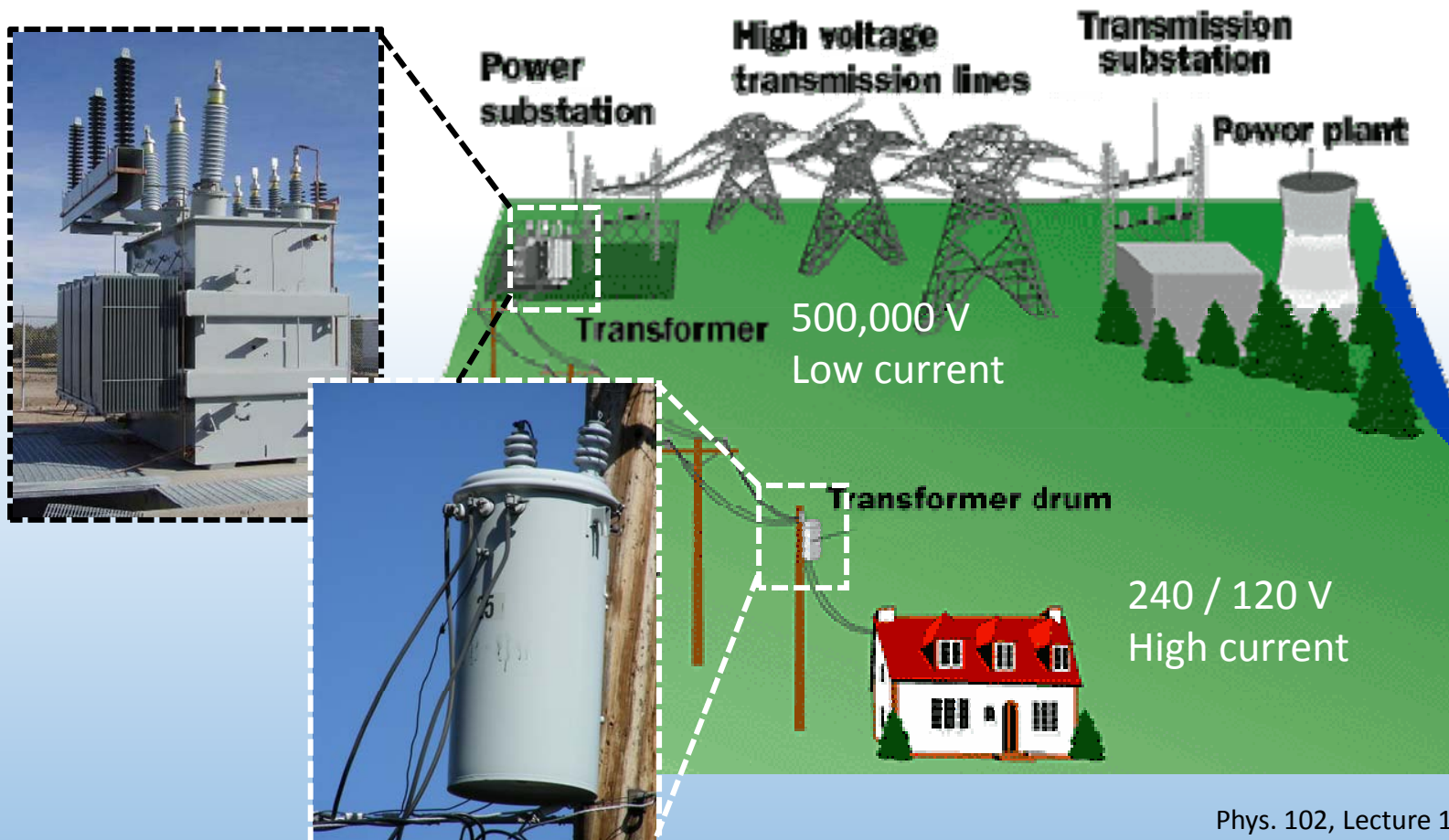
Power delivered by generator through lines:

Power lost in lines:



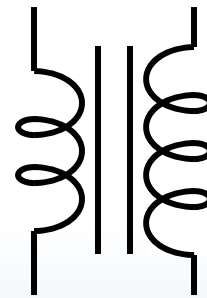
Electrical power distribution

Transformers make it possible to distribute electrical power at high voltage and “step-down” to low voltage at your house.



Transformers

Transformers are made of two coils wound around a common iron core



- Key to modern electrical system
- Transform between high and low voltages
- Very efficient

Principles of transformers

Transformers work by Faraday's law. Changing current in "primary" creates changing flux in primary and "secondary"

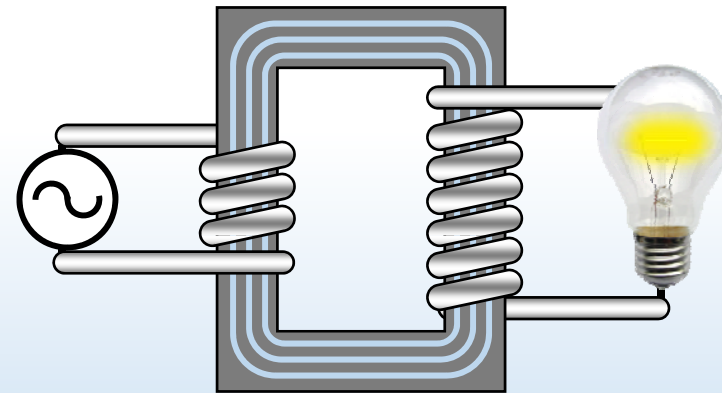
$$V_p = -N_p \frac{\Delta\Phi}{\Delta t} \quad V_s = -N_s \frac{\Delta\Phi}{\Delta t}$$

$$\frac{V_s}{V_p} = \frac{N_s}{N_p} = \frac{I_p}{I_s}$$

Energy is conserved

$$P_p = I_p V_p = I_s V_s = P_s$$

"Step-up" transformer: $N_s > N_p$



"Primary" coil
with N_p turns

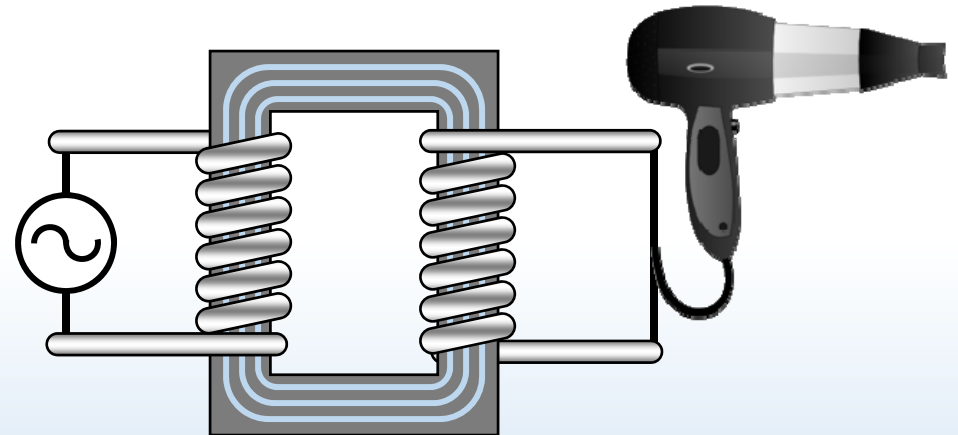
"Secondary" coil
with N_s turns

Core ensures B field of primary passes through secondary



ACT: CheckPoint 3.1

You are going on a trip to France where the outlets are 240 V. You remember from PHYS 102 that you need a transformer, so you wrap 100 turns of a *primary*.



How many turns should you wrap around the *secondary* to get 120 V out to run your hair dryer?

A. 50

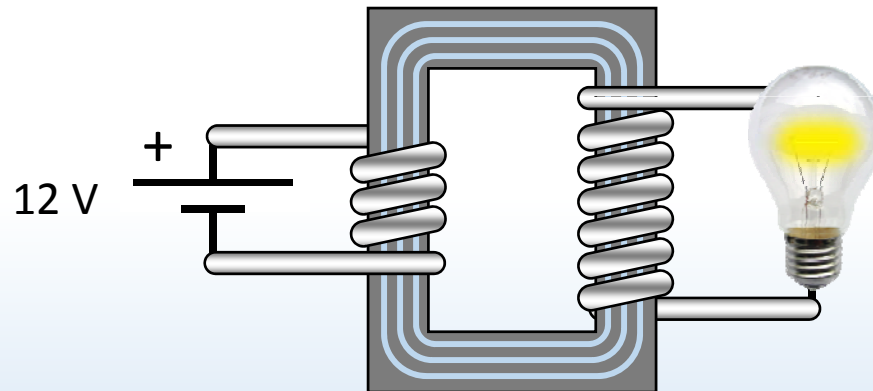
B. 100

C. 200



ACT: Transformers

A 12 V battery is connected to a transformer that has a 100 turn primary coil and 200 turn secondary coil.



What is the voltage across the secondary after the battery has been connected for a long time?

- A. $V_s = 0 \text{ V}$ B. $V_s = 6 \text{ V}$ C. $V_s = 12 \text{ V}$ D. $V_s = 24 \text{ V}$

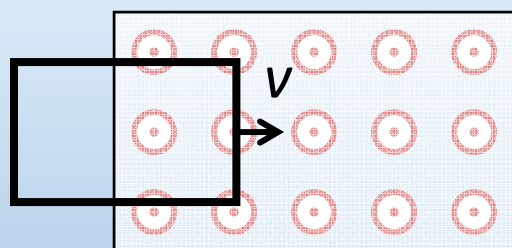
Summary of today's lecture

Faraday's law: "Induced EMF" = rate of change of magnetic flux

$$\varepsilon = -\frac{\Delta\Phi}{\Delta t}$$

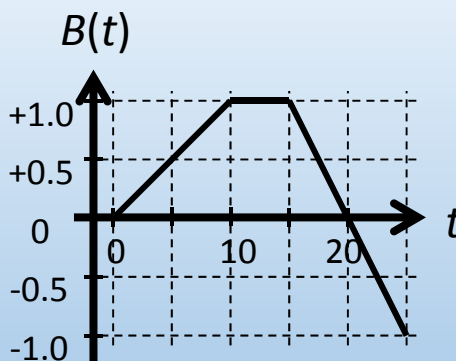
Since $\Phi = BA \cos \varphi$, 3 things can change Φ

1. Area of loop



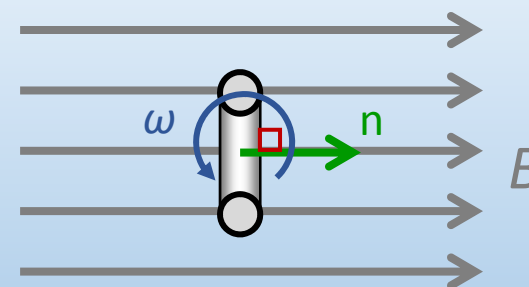
$$\varepsilon = BLv$$

2. Magnetic field B



$$\varepsilon = -\frac{\Delta B}{\Delta t} A$$

3. Angle φ



$$\varepsilon(t) = \omega NBA \sin \omega t$$