Your Comments

The Law of Malus? Seriously, that's the scariest sounding physics concept I've ever heard. Can't wait for Transformers 5: The Law of Malus

My only issue is that I thought the speed of light must be constant, now we're saying it can be slowed down with a little piece of plastic? Hmm....

Holy crap. I don't understand any of this. I really hope the lecture clears some of this up. (time spent on prelecture = 00:25)

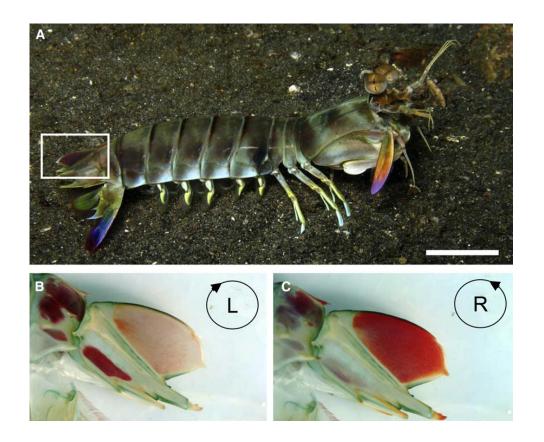
I've tried all semester to get onto the projector during class and I never get it, please put this comment up at the beginning of lecture. Yayy!!

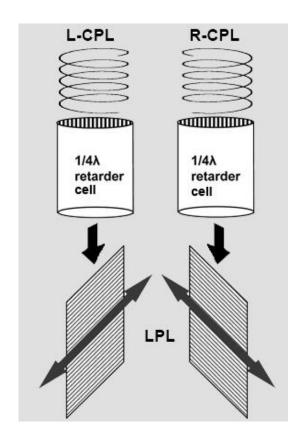
I feel good with the overall concept of polarizers. BUT the specifics of Birefringence materials and the Quarter-Wave plates is still confusing to me. Can we go over this in more detail or go over an example?

One thing the prelecture didn't cover very well is this: how does circularly polarizing light change it? Does its intensity change? Its color? What about it is significant?

Yeah so I'm really looking forward to the humbling experience of the homework for this lecture. It'll be great. Im feeling great. Everything is so great.

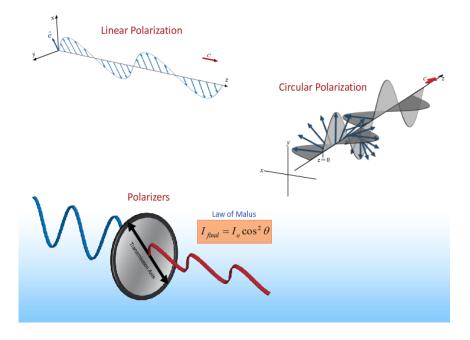
The Mantis Shrimp





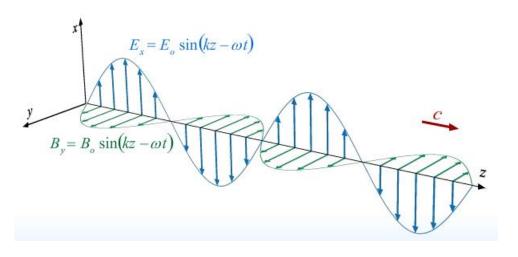
- Circularly polarized light (CPL) is very rare in nature.
- The Mantis shrimp has structures on its tail that converts the reflected ambient light to CPL.
- Structures in its eye can perceive CPL by converting it into LPL--the receptors are sensitive to LPL.
- The production and detection of CPL may be useful for "stealth" communication between Mantis shrimp.

Physics 212 Lecture 24



Linearly Polarized Light

So far we have considered plane waves that look like this:



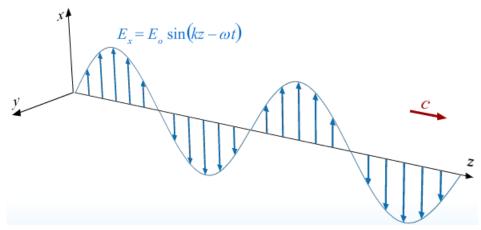
$$\omega = kc$$

$$E_o = cB_o$$

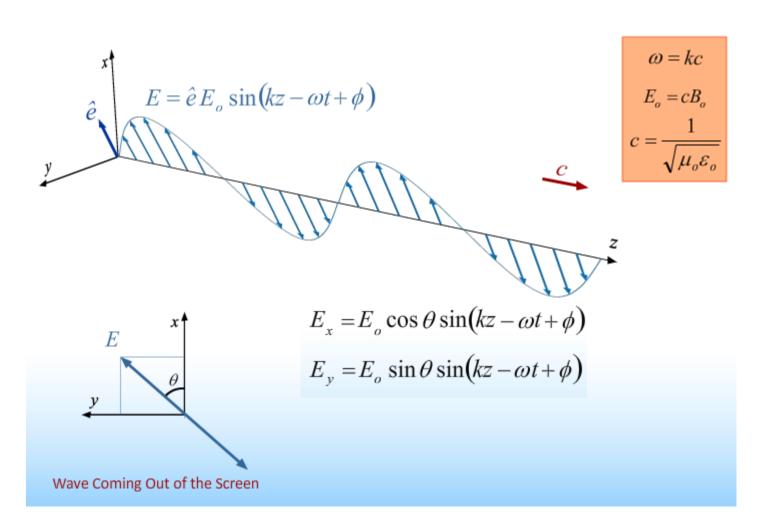
$$c = \frac{1}{\sqrt{\mu_o \varepsilon_o}}$$

From now on just draw E and remember that B is still there:

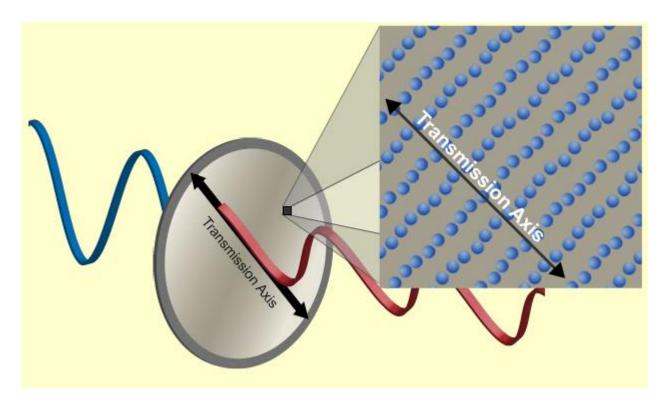
$$ec{E}$$
 Field determines Polarization



Linear Polarization



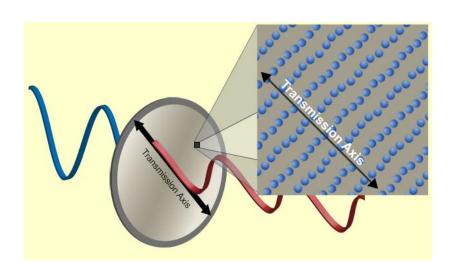
Polarizer



The molecular structure of a polarizer causes the component of the \boldsymbol{E} field perpendicular to the Transmission Axis to be absorbed.

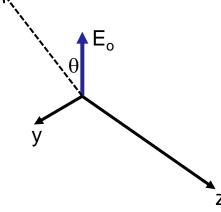
Clicker Question





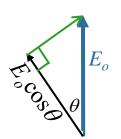
The molecular structure of a polarizer causes the component of the *E* field perpendicular to the Transmission Axis to be absorbed.

Suppose we have a beam traveling in the +z – direction. At t=0 and z=0, the electric field is aligned along the positive x – axis and has a magnitude equal to E_o

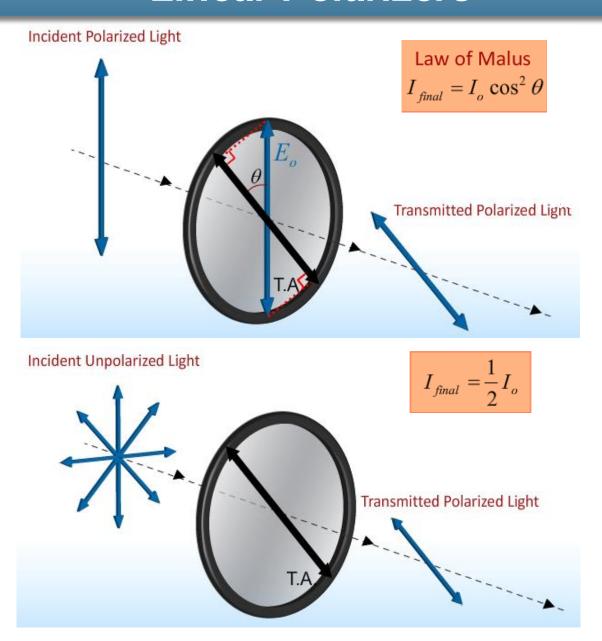


What is the component of E_o along a direction in the x-y plane that makes an angle of θ with respect to the x-x axis?

- A) $E_o \sin \theta$
- B) $E_o \cos \theta$
- **C)** 0
- D) $E_o/\sin\theta$
- E) $E_o/\cos\theta$

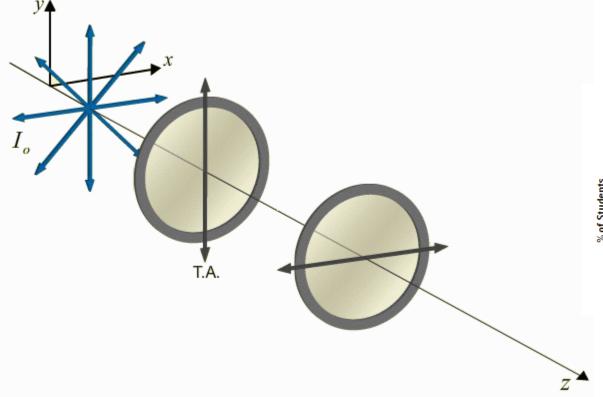


Linear Polarizers



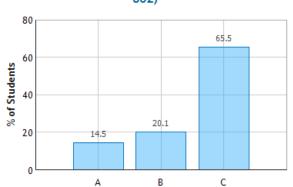
CheckPoint 1a

An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers





What percentage of the intensity gets through both polarizers?

A. 50%

B. 25%

C. 0%

C. 0%

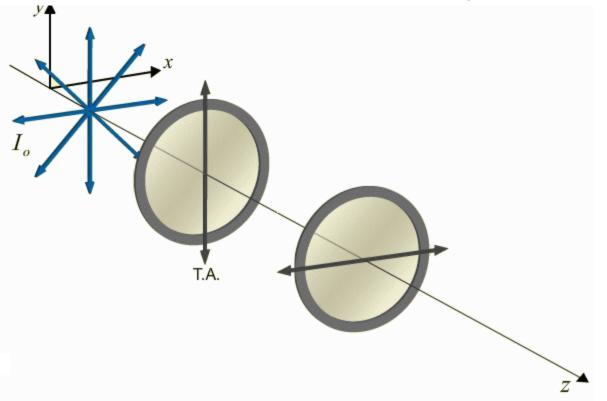
No light will come through.

 $\cos(90^{\circ}) = 0$

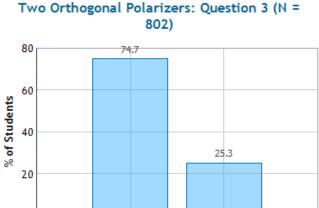


CheckPoint 1b

An unpolarized EM wave is incident on two orthogonal polarizers.



Two Polarizers



Is it possible to increase this percentage by inserting another Polarizer between the original two?

A. Yes

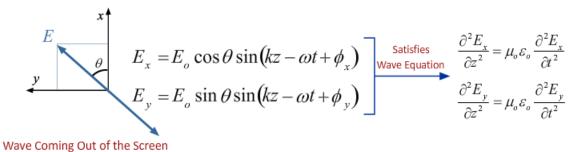
B. No

DEMO

"just like the example in the prelecture, add one at 30 degrees"

Circularly Polarized Light

There is no reason that ϕ has to be the same for E_x and E_y :



Making ϕ_x different from ϕ_y causes circular or elliptical polarization:

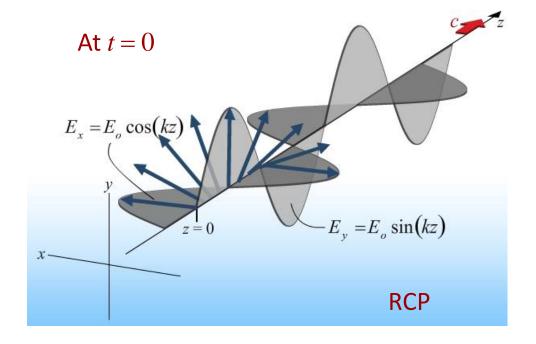
Example:

$$\phi_x - \phi_y = 90^\circ = \frac{\pi}{2}$$

$$\theta = 45^\circ = \pi/4$$

$$E_x = \frac{E_0}{\sqrt{2}}\cos(kz - \omega t)$$

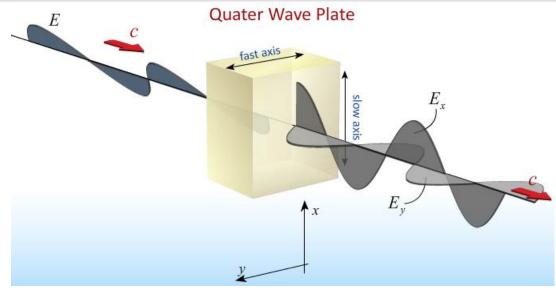
$$E_{y} = \frac{E_{0}}{\sqrt{2}}\sin\left(kz - \omega t\right)$$

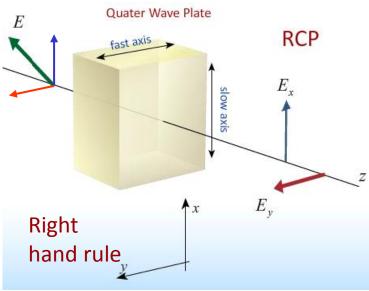


Quarter Waveplates

Q: How do we change the relative phase between E_x and E_y ?

A: Birefringence





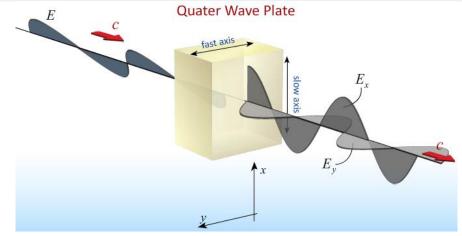
By picking the right thickness we can change the relative phase by exactly 90° .

This changes <u>linear</u> to <u>circular</u> polarization and is called a *quarter wave plate*

Intensity does not change!

"talk something about intensity"

NOTE: No Intensity is lost passing through the QWP!



BEFORE QWP:

$$E = E_o \sin(kz - \omega t) \left[\frac{\hat{i} + \hat{j}}{\sqrt{2}} \right] \longrightarrow I = c\varepsilon_o \langle E^2 \rangle = c\varepsilon_o \langle E_x^2 + E_y^2 \rangle$$

$$= c\varepsilon_o \left(\frac{E_o^2}{2} + \frac{E_o^2}{2} \right) \langle \sin^2(kz - \omega t) \rangle = c\varepsilon_o E_o^2 \frac{1}{2}$$

AFTER QWP:

$$E = \frac{E_o}{\sqrt{2}} \left[\hat{i} \cos(kz - \omega t) + \hat{j} \sin(kz - \omega t) \right]$$

AFTER QWP:
$$E = \frac{E_o}{\sqrt{2}} \left[\hat{i} \cos(kz - \omega t) + \hat{j} \sin(kz - \omega t) \right]$$

$$= c\varepsilon_o \left\langle E^2 \right\rangle = c\varepsilon_o \left\langle E_x^2 + E_y^2 \right\rangle$$

$$= c\varepsilon_o \frac{E_o^2}{2} \left\langle \cos^2(kz - \omega t) + \sin^2(kz - \omega t) \right\rangle$$

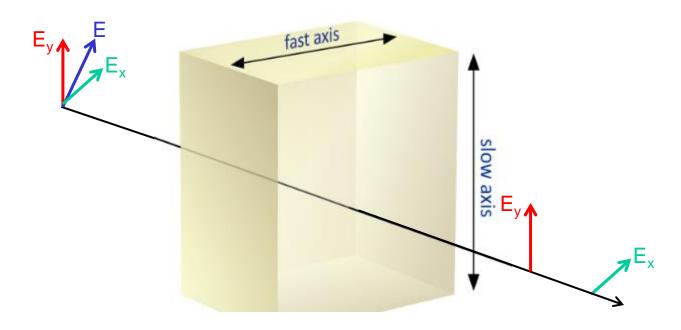
$$= c\varepsilon_o \frac{E_o^2}{2} \left\langle 1 \right\rangle = c\varepsilon_o \frac{E_o^2}{2} \left\langle 1 \right\rangle$$
THE SAME!

ctricity & Magnetism Lecture 24, Slide 13

Right or Left Circularly Polarized



Quarter-Wave Plate



A linearly polarized EM wave is incident on a quarter-wave plate as shown above. The resulting wave is

- A) Right Circularly Polarized
- B) Left Circularly Polarized
- C) Linearly Polarized

Curve fingers from slow to fast, thumb must be direction of propagation.

Circular Light on Linear Polarizer



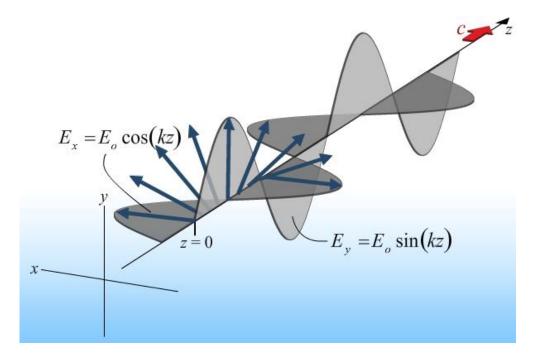
Q: What happens when circularly polarized light is put through a polarizer along the y (or x) axis?

A)
$$I = 0$$
B) $I = \frac{1}{2}I_0$
C) $I = I_0$

$$I = \varepsilon_0 c \langle E^2 \rangle$$

$$= \varepsilon_0 c \langle E_x^2 + \mathbf{K}_y^2 \rangle$$

$$= \varepsilon_0 c \frac{E_0^2}{2} \langle \cos^2(kz - \omega t) \rangle$$
1/2



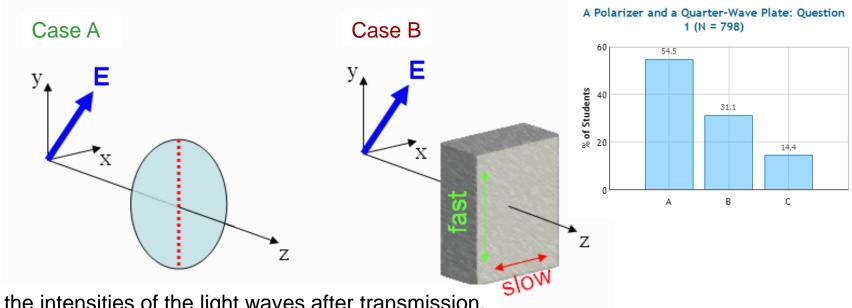
$$=\frac{1}{2}\cdot\frac{1}{2}\varepsilon_0cE_0^2$$

Half of before

CheckPoint 2a

Identical linearly polarized light at 45° from the y-axis and propagating along the z axis is incident on two different objects. In Case A the light intercepts a linear polarizer with polarization along the y-axis In Case B, the light intercepts a quarter wave plate with fast axis along the y-axis.





Compare the intensities of the light waves after transmission.



B.
$$I_{A} = I_{B}$$

C.
$$I_A > I_B$$

Case A:

 $E_{\rm v}$ is absorbed

$$I_A = I_0 \cos^2(45^\circ)$$

$$I_A = \frac{1}{2}I_0$$

Case B:

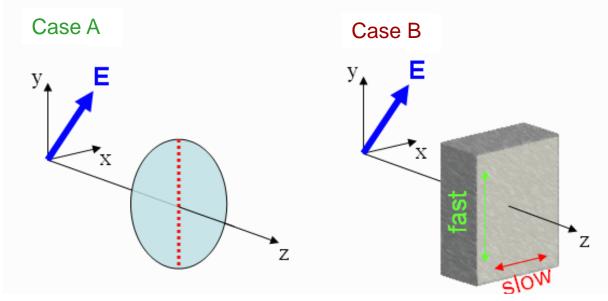
 (E_x, E_y) phase changed

$$I_B = I_0$$

Identical linearly polarized light at 45° from the y-axis and propagating along the z axis is incident on two different objects. In Case A the light intercepts a linear polarizer with polarization along the y-axis. In Case B, the light intercepts a quarter wave plate with vast axis along the y-axis.



the light intercepts a quarter wave plate with fast axis along the y-axis



What is the polarization of the light wave in Case B after it passes through the quarter wave plate?.

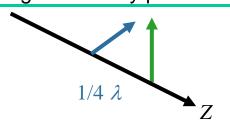
A Polarizer and a Quarter-Wave Plate: Question

A. linearly polarized

B. left circularly polarized

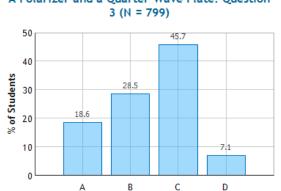
C. right circularly polarized

D. undefined



RCP

Curl fingers from slow to fast, thumb should point in direction of propagation

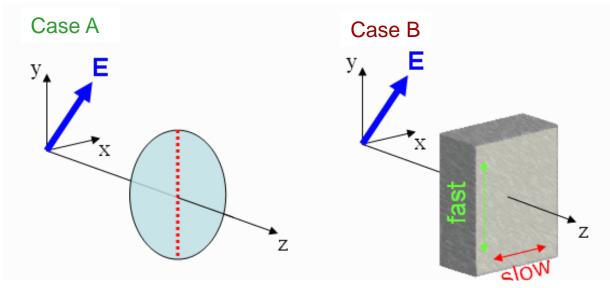


Electricity & Magnetism Lecture 24, Slide 20

CheckPoint 2c

Identical linearly polarized light at 45° from the y-axis and propagating along the z axis is incident on two different objects. In Case A the light intercepts a linear polarizer with polarization along the y-axis In Case B, the light intercepts a quarter wave plate with vast axis along the y-axis.





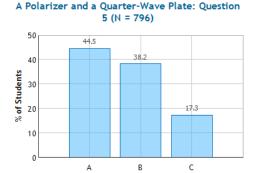
If the thickness of the quarter-wave plate in Case B is doubled, what is the polarization of the wave after passing through the wave plate?

A. linearly polarized

B. circularly polarized

C. undefined

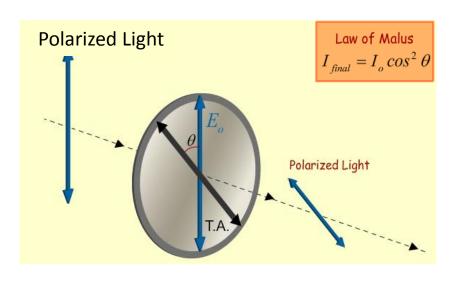


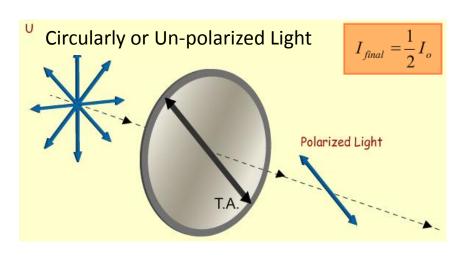


Electricity & Magnetism Lecture 24, Slide 21

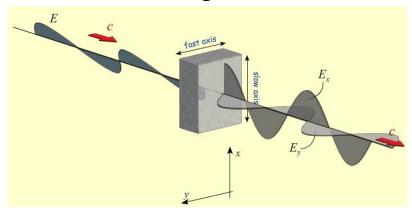
Executive Summary:

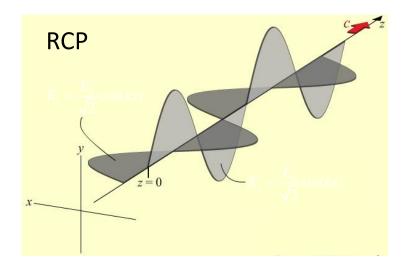
Polarizers & QW Plates:





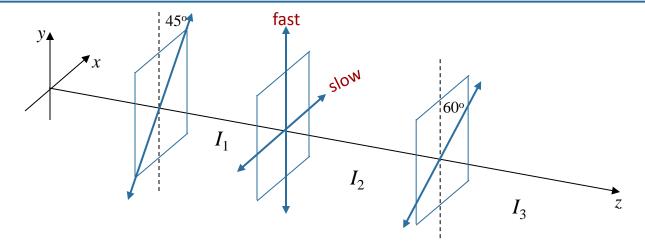
Birefringence





Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.

What is the intensity I_3 in terms of I_1 ?



Conceptual Analysis

Linear Polarizers: absorbs E field component perpendicular to TA

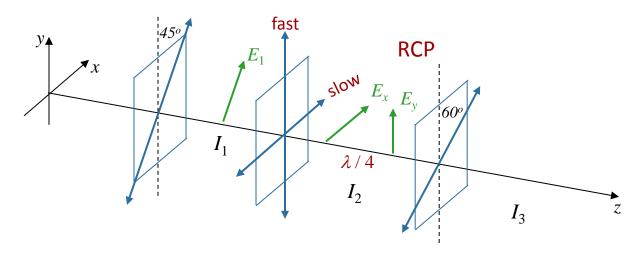
Quarter Wave Plates: Shifts phase of E field components in fast-slow directions

Strategic Analysis

Determine state of polarization and intensity reduction after each object Multiply individual intensity reductions to get final reduction.



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the QWP?

A) LCP

B) RCP

D) -----x

E) un-polarized

Light incident on QWP is linearly polarized at 45° to fast axis

 \longrightarrow

Light will be circularly polarized after QWP

LCP or RCP? Easiest way: Right Hand Rule:

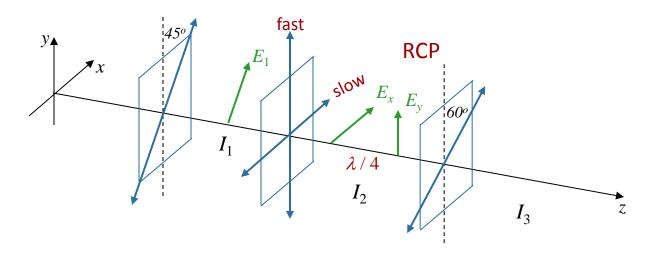
Curl fingers of RH back to front Thumb points in dir of propagation if right hand polarized.



RCP



Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_2 of the light after the QWP?

A)
$$I_2 = I_1$$

B)
$$I_2 = \frac{1}{2} I_1$$

C)
$$I_2 = \frac{1}{4} I_1$$

Before:

$$E_{x} = \frac{E_{1}}{\sqrt{2}}\sin(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}} \sin(kz - \omega t)$$

No absorption: Just a phase change!

$$I = \varepsilon_0 c \left| \left\langle E_x^2 \right\rangle + \left\langle E_y^2 \right\rangle \right|$$

Same before & after!

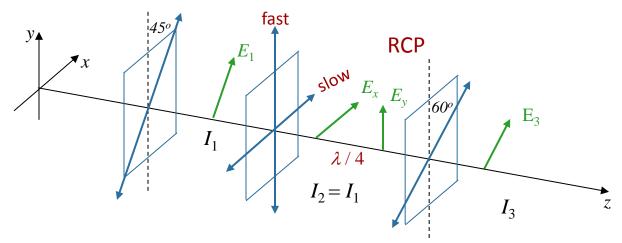
After:

$$E_{x} = \frac{E_{1}}{\sqrt{2}}\cos\left(kz - \omega t\right)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}} \sin(kz - \omega t)$$

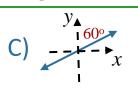


Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the polarization of the light after the 60° polarizer?

A) LCP B) RCP



Absorption: only passes components of *E* parallel to *TA* ($\theta = 60^{\circ}$)

$$E_y$$
 E_3
 E_3
 E_3

$$E_3 = E_x \sin \theta + E_y \cos \theta$$

$$E_3 = \frac{E_1}{\sqrt{2}} \left(\sin(kz - \omega t + \theta) \right)$$

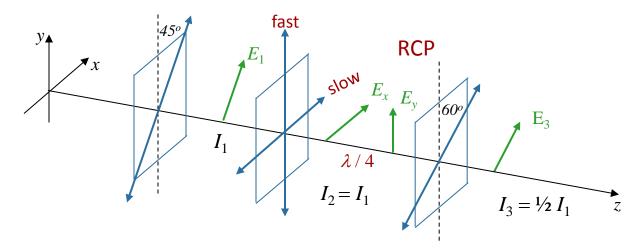
$$E_{3} = E_{x} \sin \theta + E_{y} \cos \theta$$

$$E_{3} = \frac{E_{1}}{\sqrt{2}} \left(\cos(kz - \omega t) \sin \theta + \sin(kz - \omega t) \cos \theta \right)$$





Light is incident on two linear polarizers and a quarter wave plate (QWP) as shown.



What is the intensity I_3 of the light after the 60° polarizer?

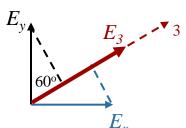
A)
$$I_3 = I_1$$

B)
$$I_3 = \frac{1}{2} I_1$$

C)
$$I_3 = \frac{1}{4} I_1$$

$$E_3 = \frac{E}{\sqrt{2}}$$

$$E_3 = \frac{E_1}{\sqrt{2}} \qquad I \propto E^2 \qquad \longrightarrow \qquad I_3 = \frac{1}{2}I_1$$

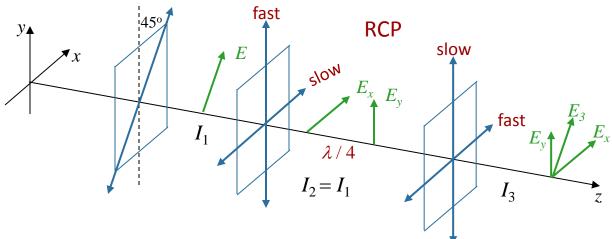


NOTE: This does not depend on θ !

Follow-Up 1



Replace the 60° polarizer with another QWP as shown.



What is the polarization of the light after the last QWP?

A) LCP

B) RCP

E) un-polarized

Easiest way:

 $E_{\it fast}$ is λ / 4 ahead of $E_{\it slow}$

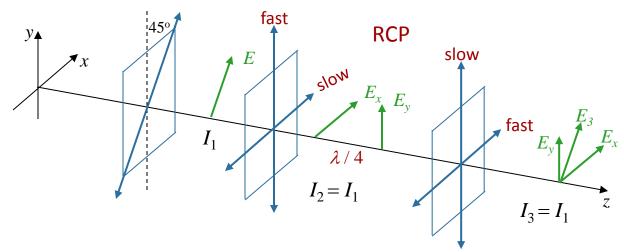


Brings E_x and E_y back in phase!

Follow-Up 2



Replace the 60° polarizer with another QWP as shown.



What is the intensity I_3 of the light after the last QWP?

C)
$$\frac{1}{4}I_1$$

Before:

$$E_x = \frac{E_1}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\sin(kz - \omega t) \qquad I_{before} = \frac{E_{1}^{2}}{2}$$

No absorption: Just a phase change!

Intensity
$$= < E^2 >$$

$$\frac{r^2}{r^2}$$

$$I_{after} = \frac{E_1^2}{2}$$

After:

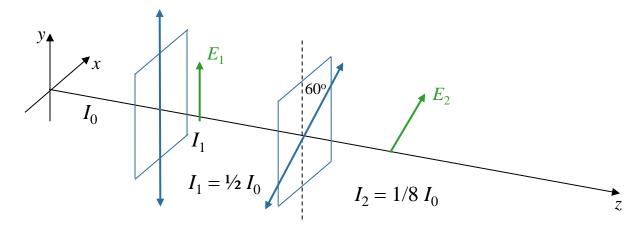
$$E_{x} = \frac{E_{1}}{\sqrt{2}}\cos(kz - \omega t)$$

$$E_{y} = \frac{E_{1}}{\sqrt{2}}\cos(kz - \omega t)$$

Follow-Up 3



Consider light incident on two linear polarizers as shown. Suppose $I_2 = 1/8 I_0$



What is the possible polarization of the input light?

- C) un-polarized
- D) all of above
- E) none of above

After first polarizer: LP along y-axis with intensity I_1 After second polarizer: LP at 60° wrt y-axis Intensity: $I_2 = I_1 \cos^2(60^{\circ}) = \frac{1}{4} I_1$ $I_2 = \frac{1}{8} I_0 \Rightarrow I_1 = \frac{1}{2} I_0$

Question is: What kind of light loses ½ of its intensity after passing through vertical polarizer?

Answer: Everything except LP at θ other than 45°