Chancellor Phyllis Wise invites you to a birthday party!

50 years ago, Illinois alumnus Nick Holonyak Jr. demonstrated the first visible light-emitting diode (LED) while working at GE. Holonyak returned to Illinois as a professor in 1963, and has been unveiling new inventions on our campus ever since. Today, the LED he demonstrated in 1962 is used in everything from flashlights to spacecraft and countless applications in between.

You're invited to a campus-wide celebration in honor of Prof. Holonyak. Have a piece of cake and talk with him about his many discoveries.

Tuesday, October 9, 11 a.m. South Lounge of the Illini Union
Free DVDs of the documentary "A Brilliant Idea" for the first 100 people.

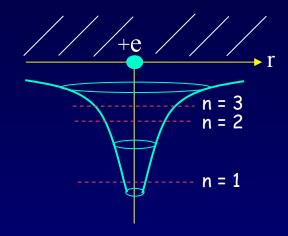


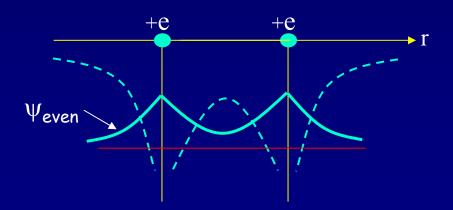
Bright light, big idea



Nick Holonyak Jr.
Inventor of the Visible LED

Lecture 19: Building Atoms and Molecules





Today

Atomic Configurations

States in atoms with many electrons – filled according to the Pauli exclusion principle

Molecular Wave Functions: origins of covalent bonds

Example: $H + H \rightarrow H_2$

Nuclear Magnetic Resonance

Just like electrons, the <u>proton</u> in the H atom also has a spin, which is described by an additional quantum number, m_p, and therefore also a magnetic moment. However, it is several orders of magnitude smaller than that of the electron.

- The energy difference between the two proton spin states in a magnetic field is 660 times smaller than for electron spin states!
- But... There are many more <u>unpaired</u> proton spins than <u>unpaired</u> electron spins in ordinary matter. Our bodies have many unpaired protons in H₂O. Detect them

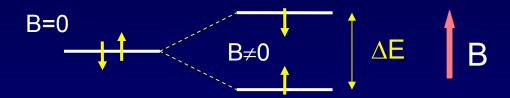
In order to image tissue of various types,

Magnetic Resonance Imaging detects the small
difference in the numbers of "up" and "down"
hydrogen proton spins generated when the
object studied is placed in a magnetic field.
Nobel Prize (2003): Lauterbur (UIUC)

www.beckman.uiuc.edu/research/mri.html

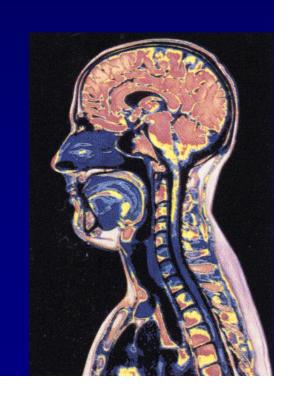
Example: Nuclear Spin and MRI

Magnetic resonance imaging (MRI) depends on the absorption of electromagnetic radiation by the nuclear spin of the hydrogen atoms in our bodies. The nucleus is a proton with spin ½, so in a magnetic field B there are two energy states. The proton's magnetic moment is $\mu_D = 1.41 \times 10^{-26} \text{ J/Tesla}$.

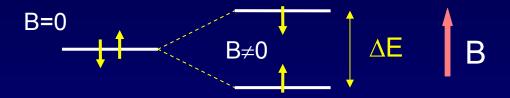


1) The person to be scanned by an MRI machine is placed in a strong (1 Tesla) magnetic field. What is the energy difference between spin-up and spin-down proton states in this field?

2) What photon frequency, f, will be absorbed?



Magnetic resonance imaging (MRI) depends on the absorption of electromagnetic radiation by the nuclear spin of the hydrogen atoms in our bodies. The nucleus is a proton with spin $\frac{1}{2}$, so in a magnetic field B there are two energy states. The proton's magnetic moment is $\mu_p = 1.41 \times 10^{-26} \text{ J/Tesla}$.

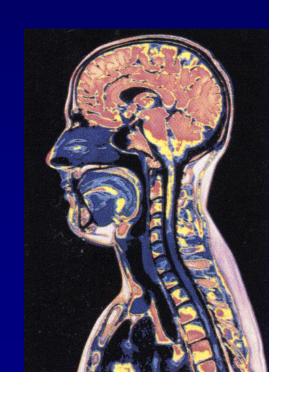


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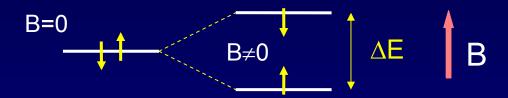
$$\Delta E = 2\mu_p B$$

= 2·(1.41×10⁻²⁶ J/T)·(1 T)
= 2.82×10⁻²⁶ J = 1.76×10⁻⁷ eV

2) What photon frequency, f, will be absorbed?



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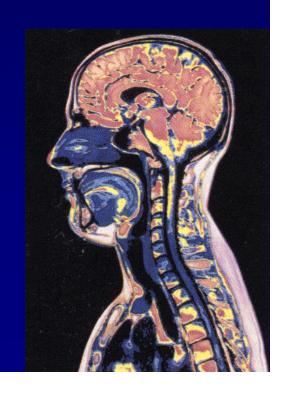
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2) What photon frequency, f, will be absorbed?

$$f = E/h$$

= $(2.82 \times 10^{-26} \text{ J})/(6.63 \times 10^{-34} \text{ J} \cdot \text{s})$
= $4.26 \times 10^7 \text{ Hz}$



Act 1

We just saw that radio frequency photons can cause a nuclear spin to flip. What is the angular momentum of each photon?

a. 0

b. ħ/2 c. ħ

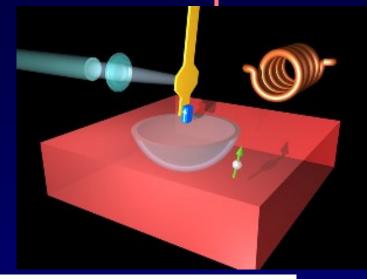
We just saw that radio frequency photons can cause a nuclear spin to flip. What is the angular momentum of each photon?

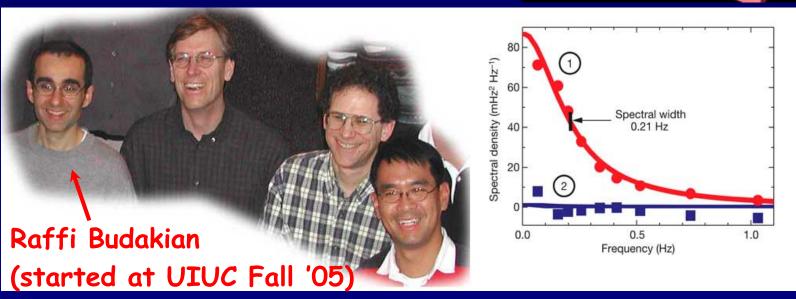
a. 0 b. ħ/2 c. ħ

The nuclear spin has flipped from † to ↓ (or vice versa). That is, its z-component has changed by ħ. Conservation of angular momentum requires that the photon have brought (at least) this much in.

FYI: Recent Breakthrough - Detection of a <u>single</u> electron spin!

• (Nature July 14, 2004) -- IBM scientists achieved a breakthrough in nanoscale magnetic resonance imaging (MRI) by directly detecting the faint magnetic signal from a <u>single</u> electron buried inside a solid sample.





Next step – detection of single nuclear spin (660x smaller).

Pauli Exclusion Principle

Let's start building more complicated atoms to study the Periodic Table. For atoms with many electrons (e.g., carbon: 6, iron: 26, etc.) ... What energies do the electrons have?

"Pauli Exclusion Principle" (1925)

No two electrons can be in the same quantum state.

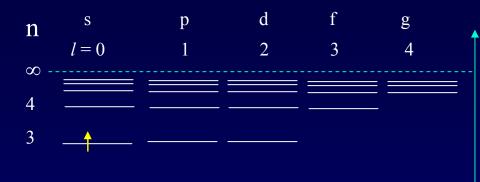
For example, in a given atom they cannot have the same set of quantum numbers n, l, m_l , m_s .

This means that each atomic orbital (n,l,m_l) can hold 2 electrons: $m_s = \pm \frac{1}{2}$.

Important consequence:

- Electrons do not pile up in the lowest energy state.
 It's more like filling a bucket with water.
- They are distributed among the energy levels according to the Exclusion Principle.
- Particles that obey this principle are called "fermions".
 Protons and neutrons are also fermions, but photons are not.

Filling Atomic Orbitals According to the Exclusion Principle



Example: Na (Z = 11)1s² 2s² 2p⁶ 3s¹

Energy
$$E_n = \frac{-13.6 \text{ eV}}{n^2} Z^2$$
 Lecture 15

In a multi-electron atom, the H-atom energy level diagram is distorted by Coulomb repulsion between electrons. Nevertheless, the H-atom diagram is useful (with some caveats) for figuring out the order in which orbitals are filled.

<u>l</u>	label	#orbitals (2 <i>l</i> +1)
0	S	1
1	p	3
2	d	5
3	f	7

Act 2

1. Which of the following states (n,l,m_l,m_s) is/are NOT allowed?

- **a.** (2, 1, 1, -1/2)
- **b.** (4, 0, 0, 1/2)
- **c.** (3, 2, 3, -1/2)
- d. (5, 2, 2, 1/2)
- **e.** (4, 4, 2, -1/2)

2. Which of the following atomic electron configurations violates the Pauli Exclusion Principle?

- a. $1s^2$, $2s^2$, $2p^6$, $3s^2$, $3d^{10}$
- b. 1s², 2s², 2p⁶, 3s2, 3d⁴
- c. 1s², 2s², 2p⁸, 3s2, 3d⁸
- d. 1s², 2s², 2p⁶, 3s2, 3d⁵
- e. 1s², 2s², 2p³, 3s2, 3d¹¹

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e. $(4, 4, 2, -1/2)$ $l = n$

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a.
$$1s^2$$
, $2s^2$, $2p^6$, $3s^2$, $3d^{10}$

Only 6 p-states.

Only 10 d-states.

Filling Procedure for Atomic Orbitals

Due to electron-electron interactions, the hydrogen levels fail to give us the correct filling order as we go higher in the periodic table.

The actual filling order is given in the table below. Electrons are added by proceeding along the arrows shown.



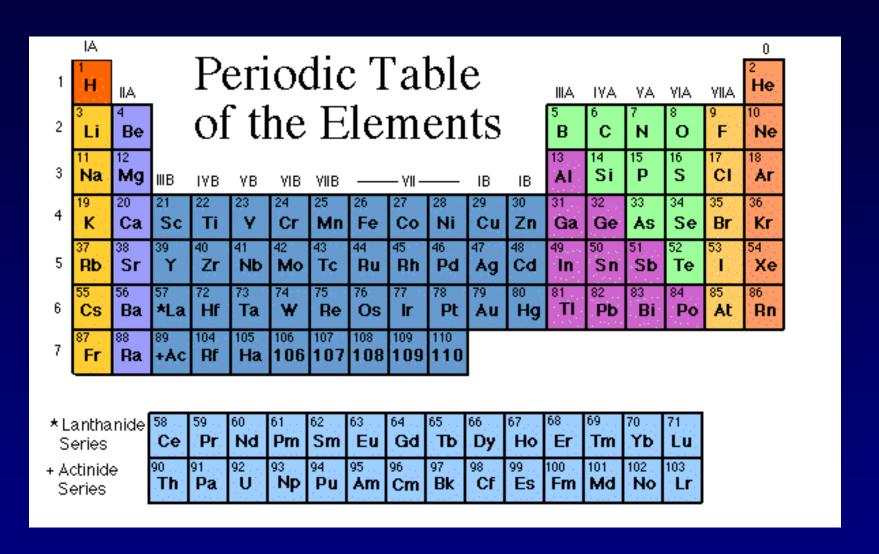
This is just a mnemonic.

Home exercise:

Bromine is an element with Z = 35. Find its electronic configuration (e.g., $1s^2 2s^2 2p^6 ...$).

Note:

The chemical properties of an atom are determined by the electrons in the orbitals with the largest n, because they are on the "surface" of the atom.

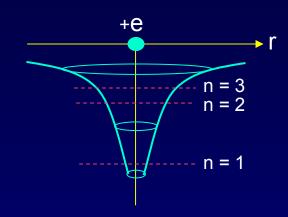


As you learned in chemistry, the various behaviors of all the elements (and all the molecules made up from them) is all due to the way the electrons organize themselves, according to quantum mechanics.

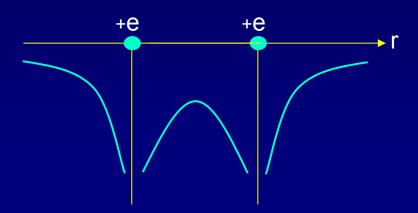
Bonding Between Atoms

How can two neutral objects stick together? $H + H \leftrightarrow H_2$

Let's represent the atom in space by its Coulomb potential centered on the proton (+e):



The potential energy due to the two protons in an H₂ molecule looks something like this:

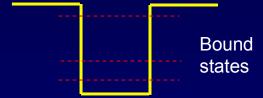


The energy levels for this potential are complicated, so we consider a simpler potential that we already know a lot about.

Particle in a Finite Square Well Potential

This has all of the qualitative features of molecular bonding, but is easier to analyze..

The 'atomic' potential:

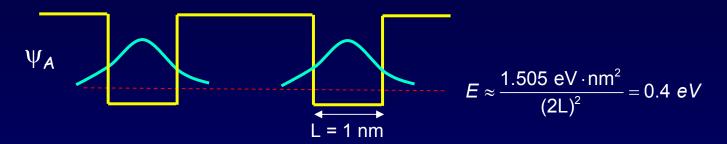


The 'molecular' potential:

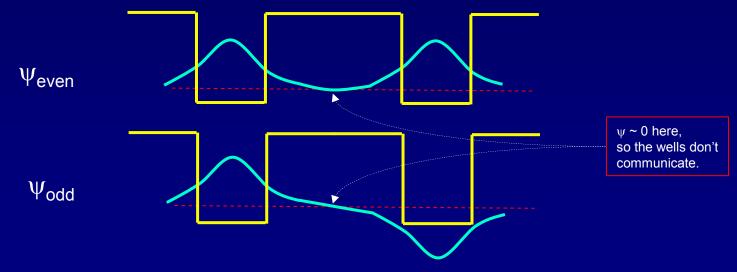
Consider what happens when two "atoms" approach one other. There is one electron, which can be in either well (or both!). This is a model of the H_2^+ molecule. We'll worry about the second electron later...

'Molecular' Wave functions and Energies

"Atomic' wave functions:

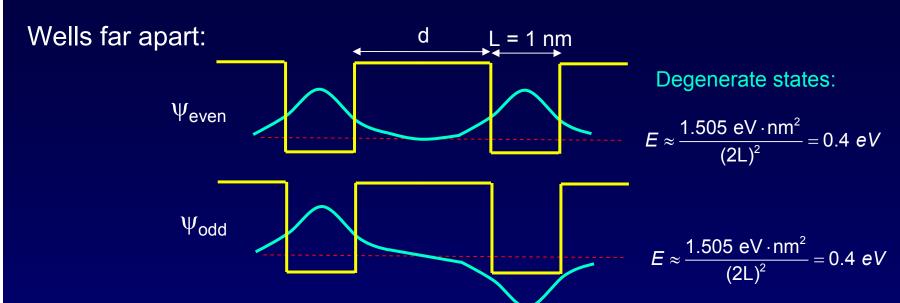


'Molecular' Wavefunctions: 2 'atomic' states → 2 'molecular' states

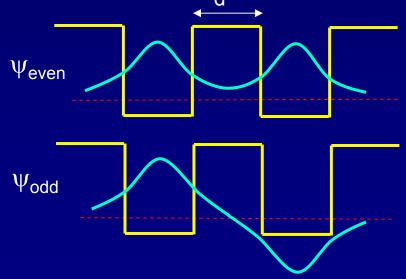


When the wells are far apart, the 'atomic' functions don't overlap. The single electron can be in either well with E = 0.4 eV.

'Molecular' Wave Functions and Energies





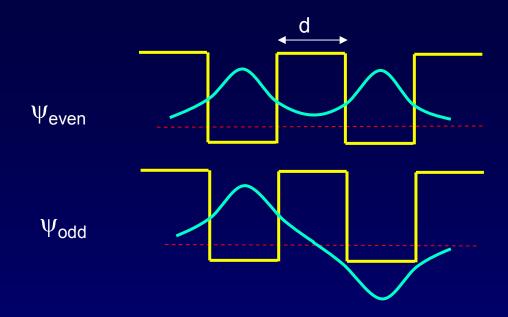


'Atomic' states are beginning to overlap and distort. ψ_{even} and ψ_{odd} are not the same. The degeneracy is broken:

$$E_{even} < E_{odd}$$
 (why?)

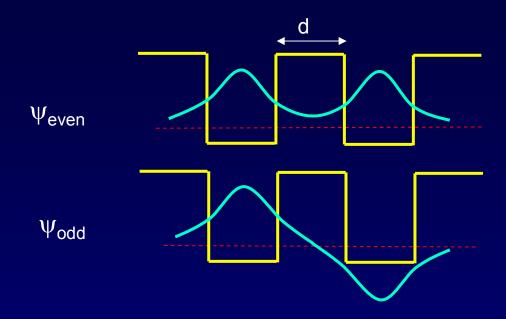
 $\begin{array}{ll} \psi_{\text{even}} \colon & \text{no nodes} \\ \Psi_{\text{odd}} \colon & \text{one node} \end{array}$

Act 3



What will happen to the energy of ψ_{even} as the two wells come together (i.e., as d is reduced)? [Hint: think of the limit as d \rightarrow 0]

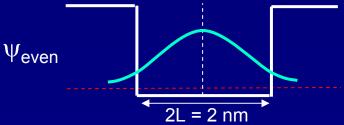
- a. E_{even} decreases.
- b. E_{even} stays the same.
- c. E_{even} increases.



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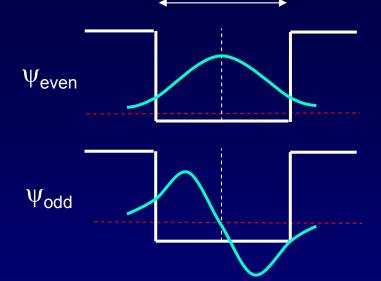
- a. E_{even} decreases.
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- c. E_{even} increases.

As the two wells come together, the barrier disappears, and the wave function spreads out over a single double-width well. Therefore the energy goes down (by a factor of ~4).



Energy as a Function of Well Separation

When the wells just touch (d = 0, becoming one well) we know the energies: 2L = 2 nm



$$E_1 \approx \frac{1.505 \text{ eV} \cdot \text{nm}^2}{(4\text{L})^2} = 0.1 \text{ eV}$$

$$(n = 1 state)$$

$$E_2 \approx \frac{1.505 \text{ eV} \cdot \text{nm}^2}{(4\text{L})^2} \cdot 2^2 = 0.4 \text{ eV}$$

(n = 2 state)

As the wells are brought together, the even state always has lower kinetic energy (smaller curvature, because it spreads out). The odd state stays at about the same energy. The node prevents it from spreading.



Splitting between even and odd states:

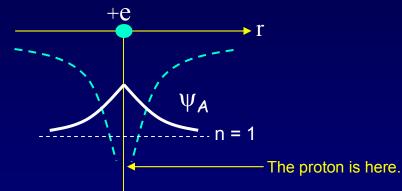
$$\Delta E = 0.4 - 0.1 \text{ eV} = 0.3 \text{ eV}$$

Molecular Wave functions and Energies with the Coulomb Potential

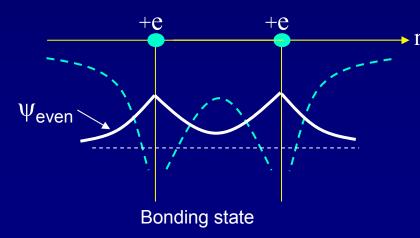
To understand real molecular bonding, we must deal with two issues:

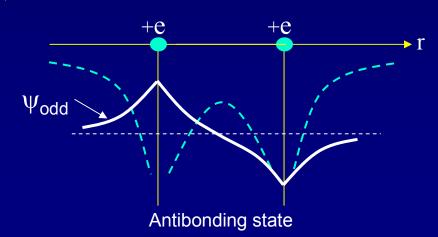
- The atomic potential is not a square well.
- There is more than one electron in the well.

Atomic ground state (1s):



Molecular states:

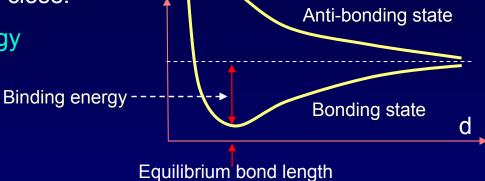




Energy as a Function of Atom Separation

The even and odd states behave similarly to the square well, but there is also repulsion between the nuclei that prevents them from coming too close.

Schematic picture for the total energy of two nuclei and one electron:



Let's consider what happens when there is more than one electron:

- 2 electrons (two neutral H atoms): Both electrons occupy the bonding state (with different m_s). This is neutral H₂.
- 4 electrons (two neutral He atoms). Two electron must be in the anti-bonding state. The repulsive force cancels the bonding, and the atoms don't stick. The He₂ molecule does not exist!

Summary

Atomic configurations

- States in atoms with many electrons
- Filled according to the Pauli exclusion principle

Molecular wave functions: origins of covalent bonds

Example: H + H → H₂

Electron energy bands in crystals

- Bands and band gaps are properties of waves in periodic systems.
- There is a continuous range of energies for "allowed" states of an electron in a crystal.
- A Band Gap is a range of energies where there are no allowed states
 Bands are filled according to the Pauli exclusion principle

Next time

Some practical uses of QM:

- Why do some solids conduct others do not
- Solid-state semiconductor devices
- Lasers
- Superconductivity