

Physics 214 Final Exam Review Problems

The following questions are designed to give you some practice with concepts covered <u>since the midterm</u>. You should look at old practice midterms for sample problems covering the earlier course material. Some are specifically designed to be difficult in order to make sure you can go beyond simple "plug and chug" problems.



1. An electron has a wavefunction $\Psi(r, \theta, \phi) = Cr^3e^{-r/a}$. At what radius is one most likely to find the electron?

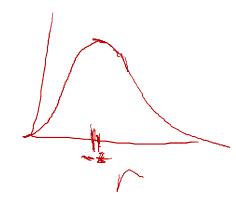
a. r = a

b. r = 2a

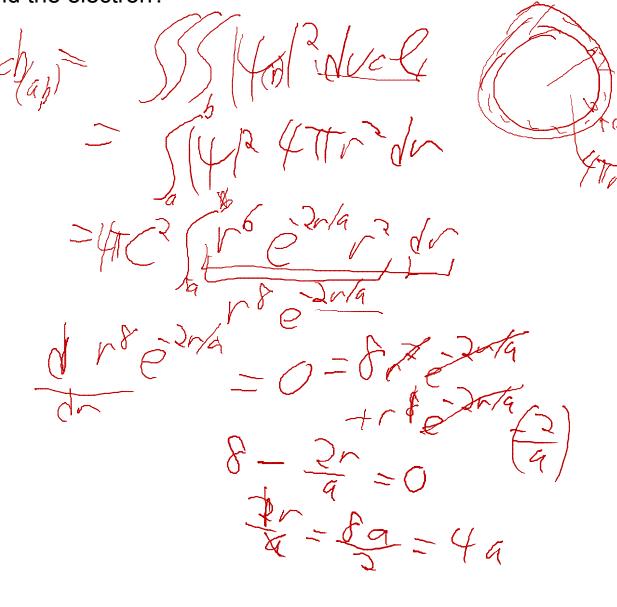
 $c_r = 3a$

 $d_{r} = 4a$

e. r = 5a



472 8 E2 r/a (b-a)



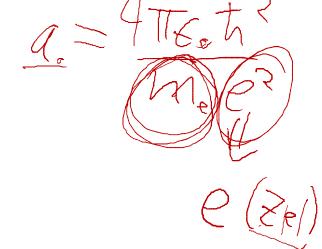
1'. What happens to this radius if one increases the charge of the nucleus?



b. increase

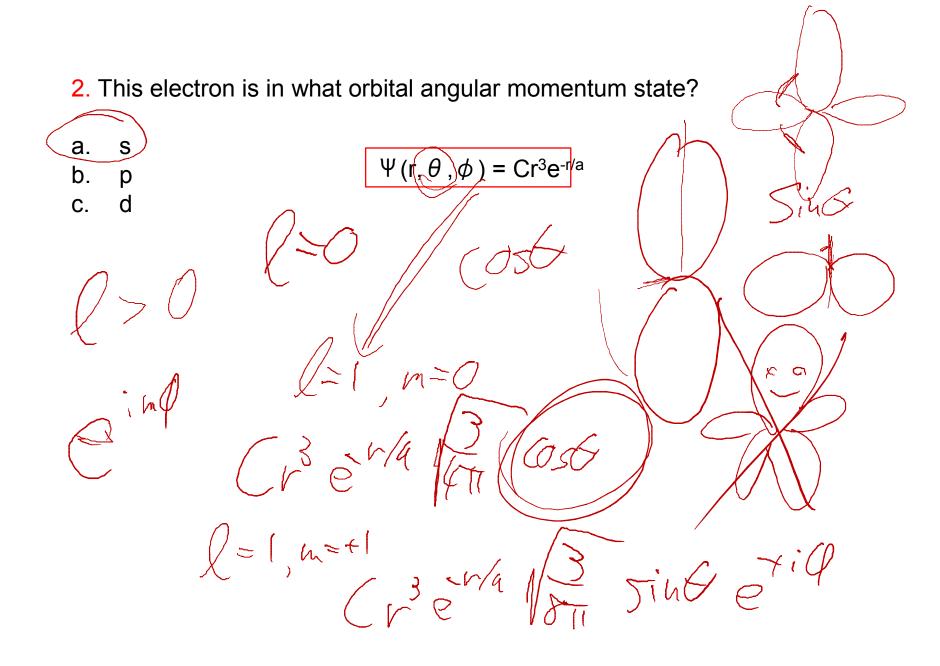
c. stay the same



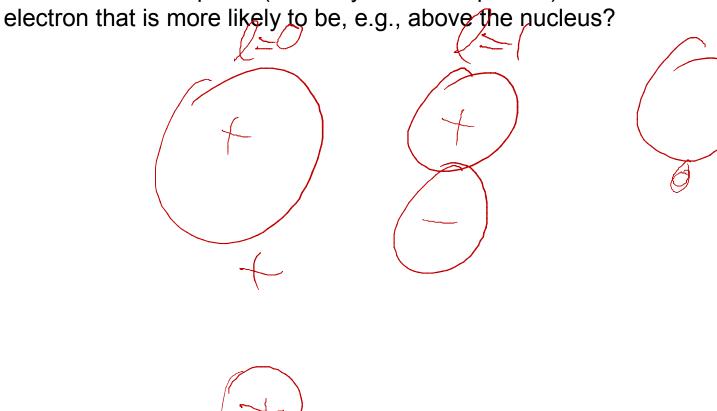


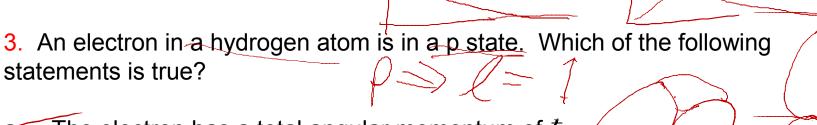
1". What happens to this radius if replace the electron by a muon (forming 'muoniom')? A muon is essentially a heavy electron: $m_{muon} \sim 200 \text{ m}_{e}$

- a. decrease
- b. increase
- c. stay the same



2'. The previous problem had a spherically symmetric wavefunction. We can also have wavefunctions that have various lobes. However, even in these cases, the electron is still equally likely to found in the top half plane, or the bottom half plane (or in any two hemispheres). How can we get an electron that is more likely to be equally above the nucleus?





- a. The electron has a total angular momentum of \hbar .
- b. The electron has an energy of -13.6 eV.
- The probability to find the electron within 0.1 nm of the origin changes in time.
- The electron's wave function has at least one node (i.e., at least one place in space where it goes to zero).
- e. The electron has a z-component of angular momentum equal to $\sqrt{2}\hbar$.

$$|Z| = |(l+1)t^{2} = ||x| + ||x|| + |$$

Problems 4,5, and 6 are related. N=5



4. An electron in an infinite square well of width L = 1 nm has the wavefunction:

$$\psi(x) \propto \sqrt{\frac{2}{L}} \left[\sin(\frac{3\pi x}{L}) + \sin(\frac{5\pi x}{L}) - 2\sin(\frac{\pi x}{L}) \right]$$



What is/are the possible result/results for a measurement of the electron's energy?

- a. 0.376 eV
- b. 2.38 eV
- c 0.376 eV, 3.39 eV, or 9.41 eV
- d. 11.3 eV
- e. 12.1 eV

5. What is the probability of measuring the electron in the previous problem to have an energy of 0.376 eV?

$$\psi(x) \propto \sqrt{\frac{2}{L}} \left[\sin(\frac{3\pi x}{L}) + \sin(\frac{5\pi x}{L}) - 2\sin(\frac{\pi x}{L}) \right]$$

E5 - 24, +43+45 => 4,

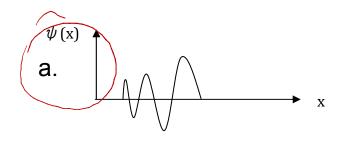
6. If indeed we measure the electron to have energy 0.376 eV, and then we shine on light of wavelength 824.5 nm, what will happen?

a. The electron will be excited to a state with energy 1.75 eV.

The electron will be excited to the state with energy 1.504 eV.

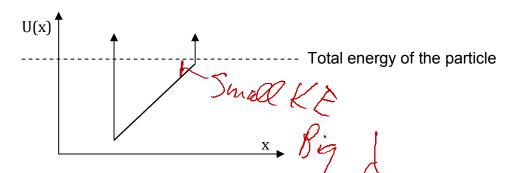
c.) The electron will not be excited.

7. A particle is trapped in the potential well below. Which of the wave functions most closely describes the particle?



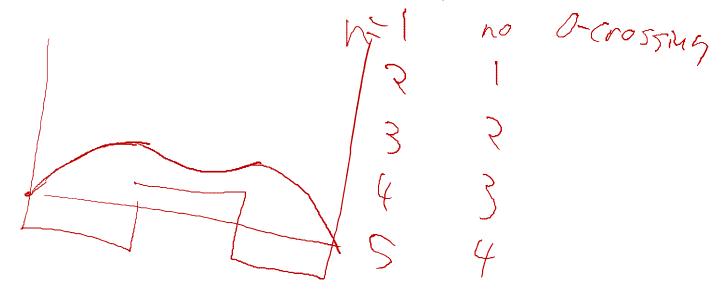




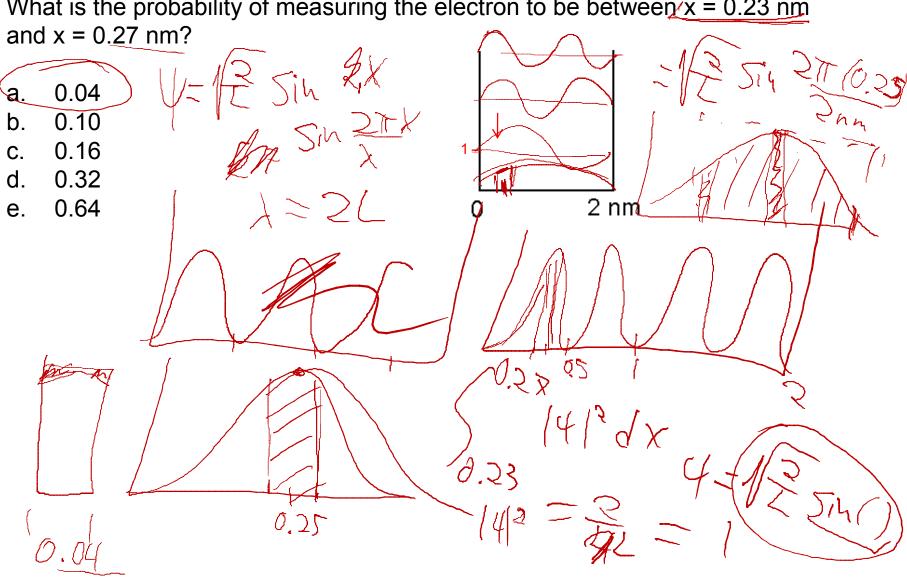


- 8. What state is this particle in (where n = 1 is the ground state)?
- a. n = 2
- b. n = 3
- c. n = 4
- d. n = 5
- e. n = 6

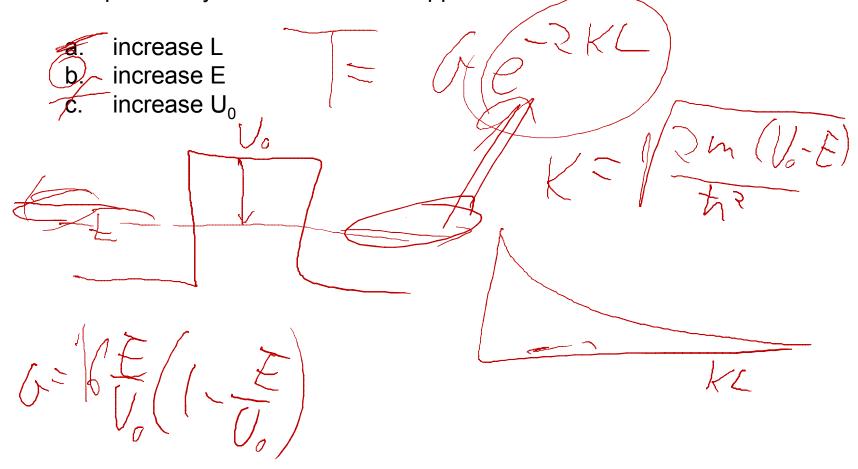




9. An electron is in the 3^{rd} excited state of a 2-nm wide infinite square well. What is the probability of measuring the electron to be between x = 0.23 nm

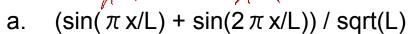


10. An electron with total energy E approaches a barrier of height U_0 and width L. Assuming E< U_0 , which one of the following changes will **increase** the probability for the electron to appear on the other side of the barrier?





has the shortest period of oscillation in time?

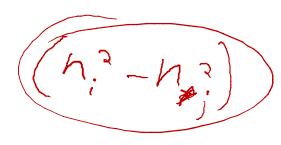


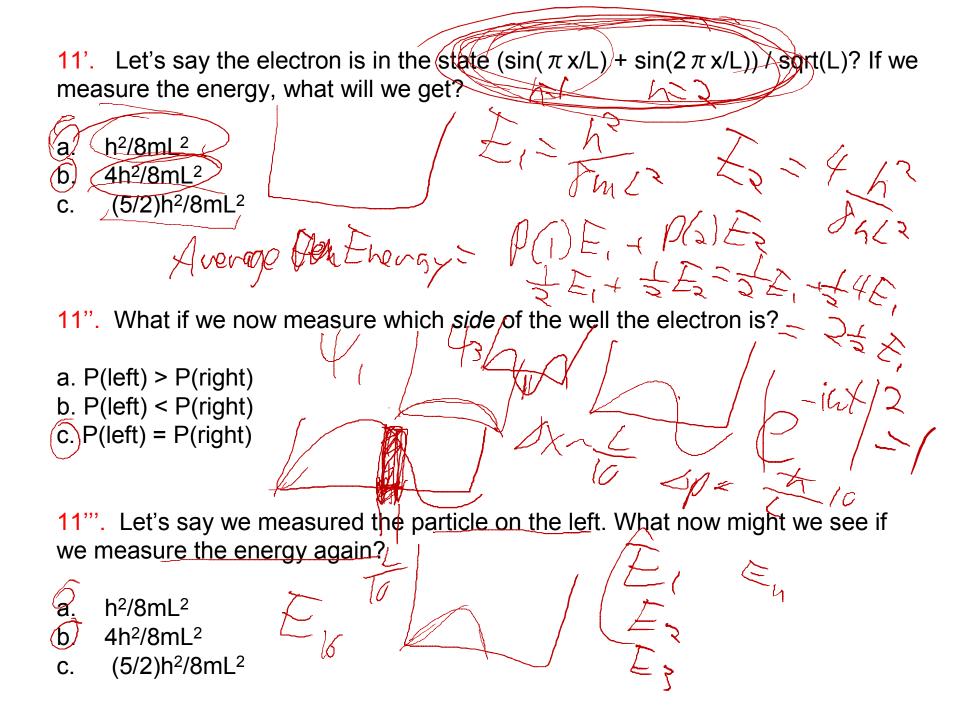
by
$$(\sin(2\pi x/L) + \sin(3\pi x/L)) / \operatorname{sqrt}(L)$$

c. (sin(
$$\pi$$
 x/L) + sin(3π x/L)) / sqrt(L)

$$a. 2^2 - 1^2 = 3$$
 $b. 3^2 - 3^2 = 5$

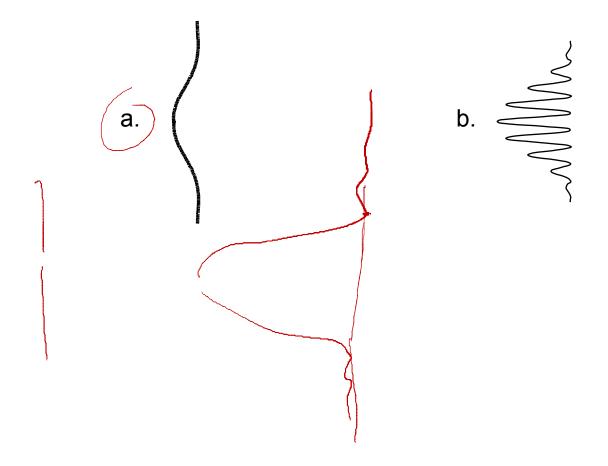
$$\left(\frac{1}{\sqrt{2}}\right)^{2} + \left(\frac{1}{\sqrt{2}}\right)^{2} = 1$$





Problems 12 and 13 are related.

12. Which of the following probability distributions will you observe from a beam of electrons passing through a double slit with one slit covered? (Assume that the detection screen is far away from the slits, i.e, the diagrams are not drawn to scale)?



13. Now both slits are unblocked. However, we modify the experiment in the following way: We prepare the electrons incident on the slits so that they <u>all</u> have their spins "pointing up", i.e., so that $m_s = +1/2$. We install a tiny radio-coil near the top slit (this is only a thought experiment!), so that the spin of any electron that passes through the top slit is flipped (without affecting the spin of electron passing through the bottom slit). Now which pattern do we see?

a.

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14. What frequency of electromagnetic radiation will flip a "spin up" electron to a "spin down" electron in a magnetic field of 2.0 T?



b. 4.1*109 Hz

c. 5.6*10¹⁰ Hz

d. 7.1*10¹¹ Hz

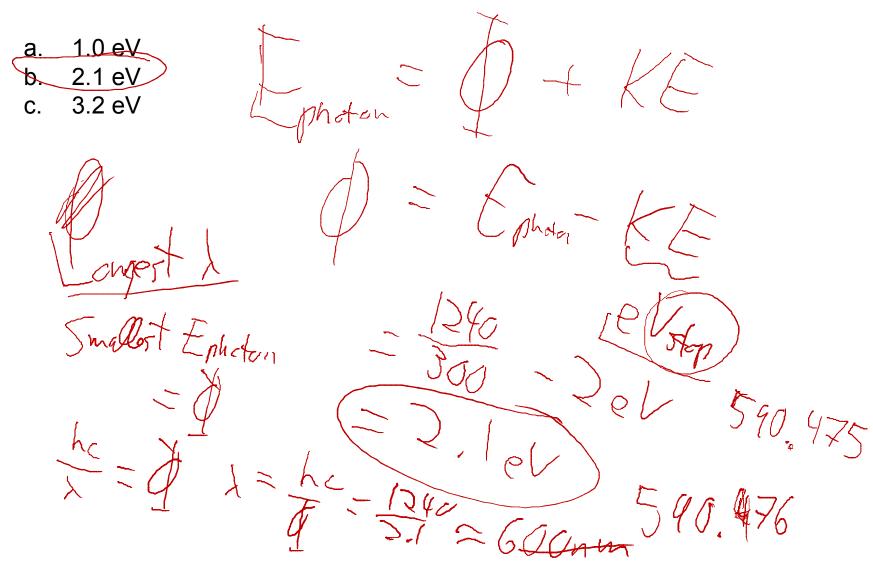
e. 8.8*10¹² Hz

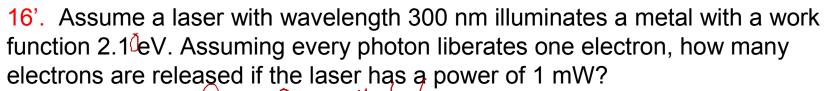
15. A photon has energy 3 eV. What is its momentum?

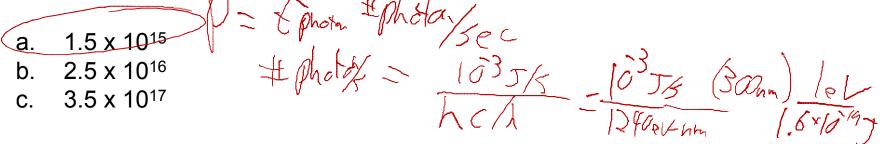
a.

1.6*10⁻²⁷ kg m/s 9.4*10⁻³⁴ kg m/s

16. A laser with wavelength 300 nm illuminates a metal in a photoelectric effect experiment. It takes a stopping potential of 2 Volts to halt the ejected electrons. What is the work function of the metal?







16". What if we keep the power fixed, but use a laser with half the wavelength (i.e., 150 nm)?

- a. N_{emitted} stays the same
- b. N_{emitted} decreases
- c. N_{emitted} increases

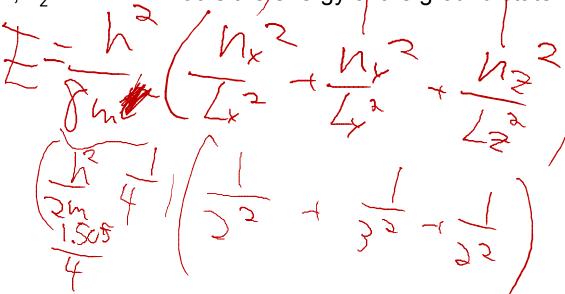
16". What if we keep the power fixed, but use a laser with twice the wavelength (i.e., 600 nm)?

- a. N_{emitted} stays the same
- b N_{emitted} decreases
- c. N_{emitted} increases

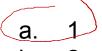
Problems 17 and 18 are related.

17. An electron is confined to a rectangular region in space with sides $L_x = 2$ nm, $L_y = 3$ nm, $L_z = 2$ nm. What is the energy of the ground state?

- a. 0.094 eV
- b. 0.19 eV
- c. 0.23 eV

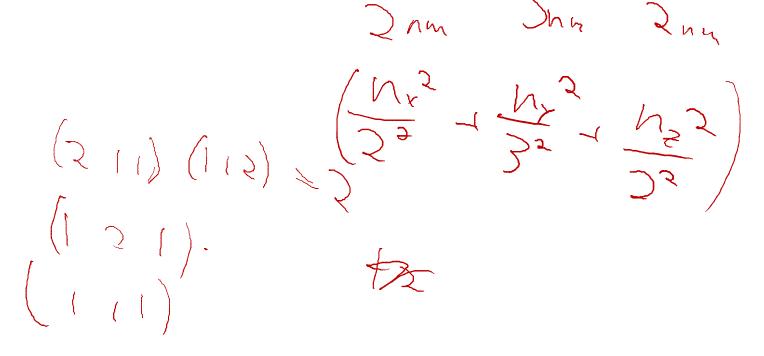


18. What is the degeneracy of the 1st excited state for the electron in the previous problem (neglecting the effect of spin)?

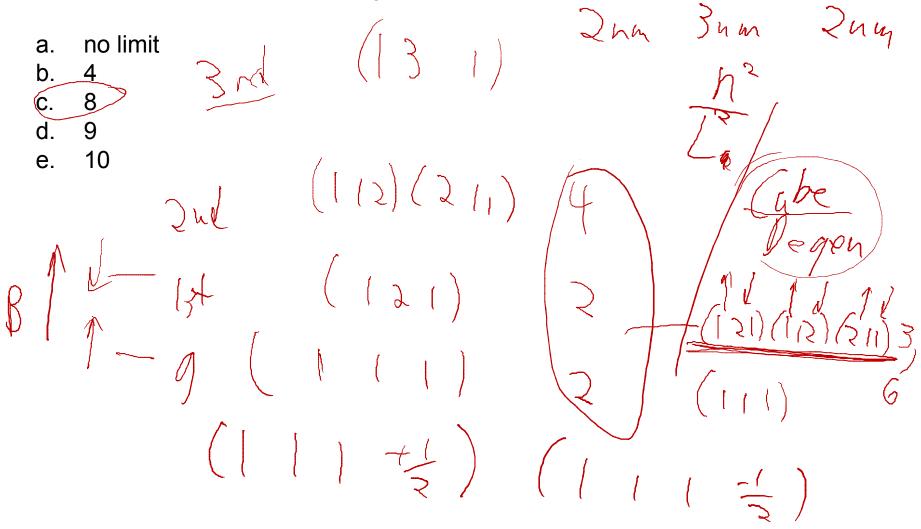


b. 2

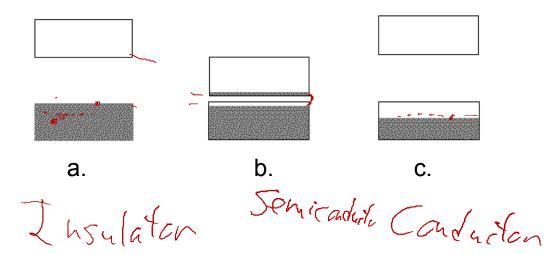
c. 3



18'. How many electrons can the well hold, and still not have any in the third excited state (now including spin effects)?



19. Which of the following energy band pictures corresponds to a conductor?



Problems 20 and 21 are related.

20. Two harmonic oscillators in their ground states are brought near each other. Which of the following pictures shows the correct 1st excited state for the combined system?

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15t - odd > 1 occassing

in middle

21. Assume there is one electron from each harmonic oscillator (and neglect electrostatic interactions between the electrons). If the "molecule" is in its lowest energy state, one of the electrons is in state (b.) above. Which of the above pictures is appropriate for the wave function of the second electron?

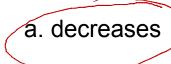




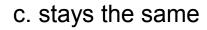


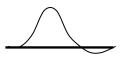
c. _____

21'. If we allow the two wells to move closer together, how does the energy of the ground state change?













22. A beam of electrons is sent toward a potential barrier (height = 2 eV) with velocity 6x10⁵ m/s. If 97.5% of the incident beam is reflected, what is the width of the barrier?

a. 0.01 nm

b. 0.05 nm

Problems 23 and 24 are related.

(=0 m=0

23. A hydrogen atom in its ground state traveling in the +x-direction is passed along the through a Stern-Gerlach apparatus, producing a set of peaks. The uppermost peak only is then passed through *another* Stern-Gerlach apparatus (with the same magnetic field gradient dB/dz as the first). How many peaks are observed in the output of the second Stern-Gerlach apparatus?

a. 0 h 1

c. 2

d. 3

e. 4

24. If instead we were to rotate the second Stern-Gerlach apparatus by 90°, so that the gradient was dB/dy instead, now how many peaks would be observed?

a. 0

b. 1

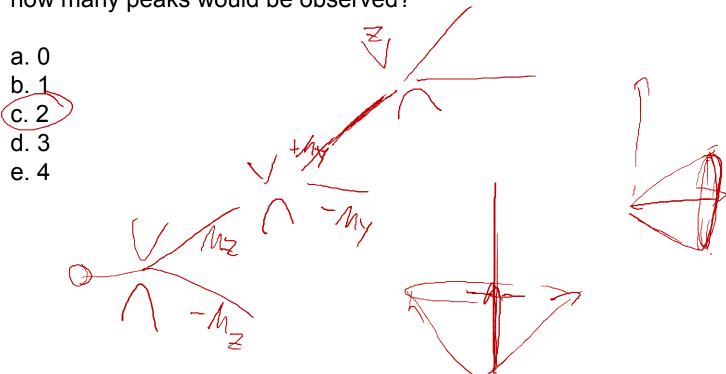
C. 2

d. 3

e. 4

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24'. If after the second Stern-Gerlach apparatus with gradient dB/dy, we now install a third Stern-Gerlach apparatus, again with gradient dB/dz, how many peaks would be observed?



25. What are the quantum numbers n and I of the outermost electron of a Br atom? Br has 35 electrons. m n=3, I=0 a. n=3, I=1 n=4, l=0n=4, l= n=4, l=2 e.

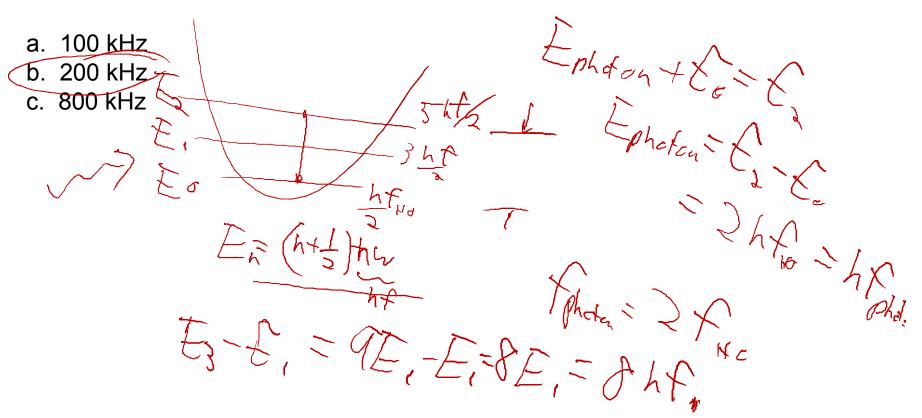
26. If the outermost electron is now excited (e.g., by a collision) to the n = 5, l = 1 state, to which final state(s) could the electron fall back down by emitting a photon?

- a. n=4, l=3
- b. n=4, l=2
- c. n=5, l=0
- d. n=4, l=1
- e. n=3, l=2

Problems 27-29 refer to this situation:

A calcium ion (charge |e|, mass = 6.65×10^{-26} kg) is trapped in an electromagnetic potential that approximates a **harmonic oscillator**. The frequency associated with the oscillation of the ion in the trap is 100 kHz.

27. If one wanted to excite the ion from the ground state of the trap <u>directly</u> to the <u>second excited state</u>, one might shine on radio waves with frequency:



- 28. At time t = 0, the ion is prepared into an equal superposition of the ground state and the <u>second</u> excited state, $\psi = \frac{1}{\sqrt{2}}(\psi_0 + \psi_2)$. Which of the following describes the likely location of the ion:
- a. The ion is more likely to be found in the left-hand side of the trap.
- b. The ion is more likely to be found in the right-hand side of the trap.
- c. The ion is equally likely to be found in either half of the trap.

Symmetrice potential

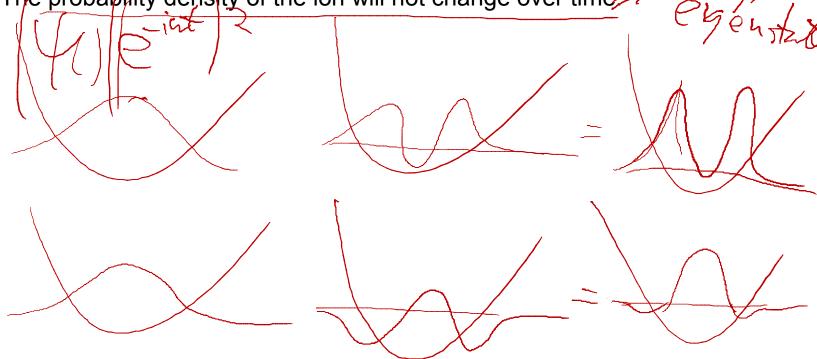
95. even
15t excited odd
24d " oven

29. We now let the system evolve in time. Which of the following best describes the future behavior of the ion:

a. The ion will "slosh" back and forth from the left-hand side of the well to the right-hand side.

b.) The ion will "slosh" back and forth from being mostly located near the center of the well to being mostly located away from the center (i.e., nearer the "edges" of the well).

c. The probability density of the ion will not change over time



30. Consider the following curve of resistance versus temperature.

What kind of material is this?

- a. insulator
- b. semiconductor
- c. Metal

