

Superconductivity in pictures

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ILLINOIS

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

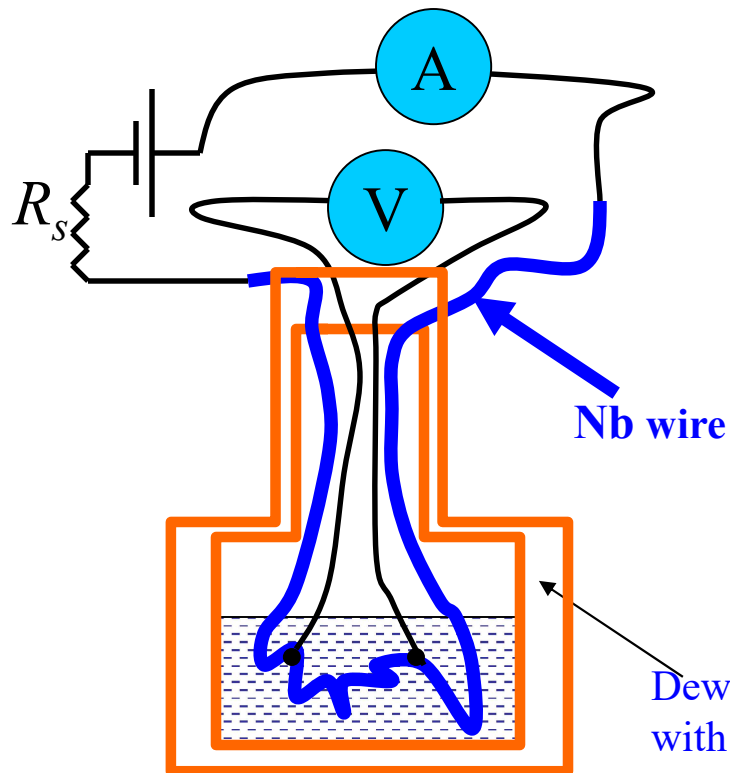


Superconductivity observation

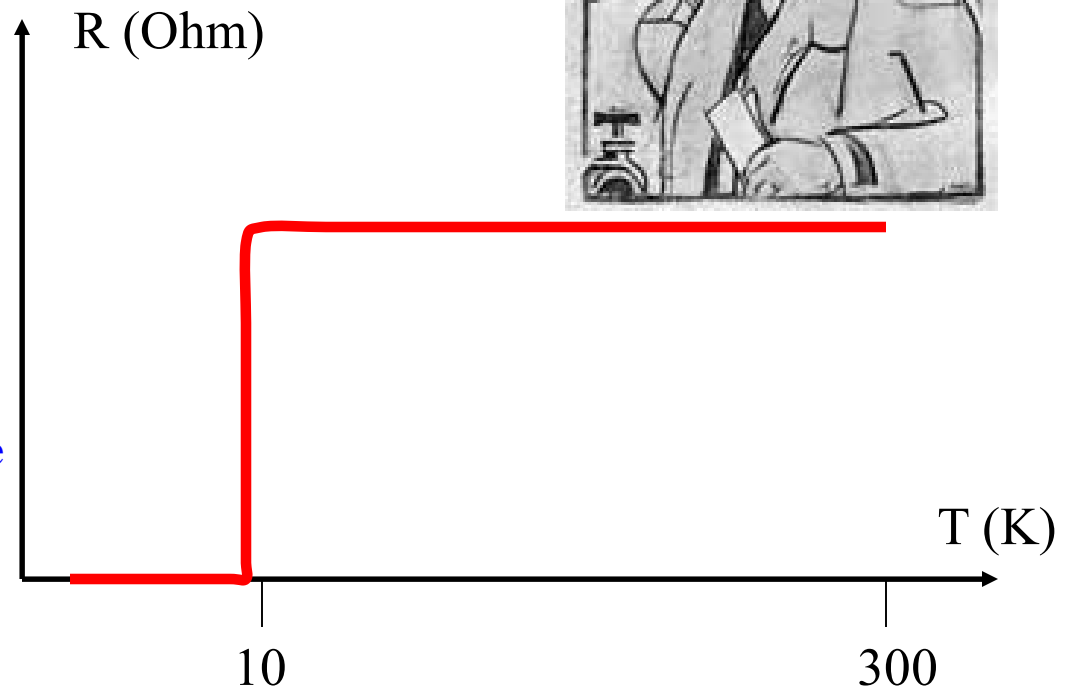
Electrical resistance of some metals drops to zero below a certain temperature which is called "critical temperature" (H. K. O. 1911)

How to observe superconductivity

- Take Nb wire
- Connect to a voltmeter and a current source
- Put into helium Dewar
- Measure electrical resistance

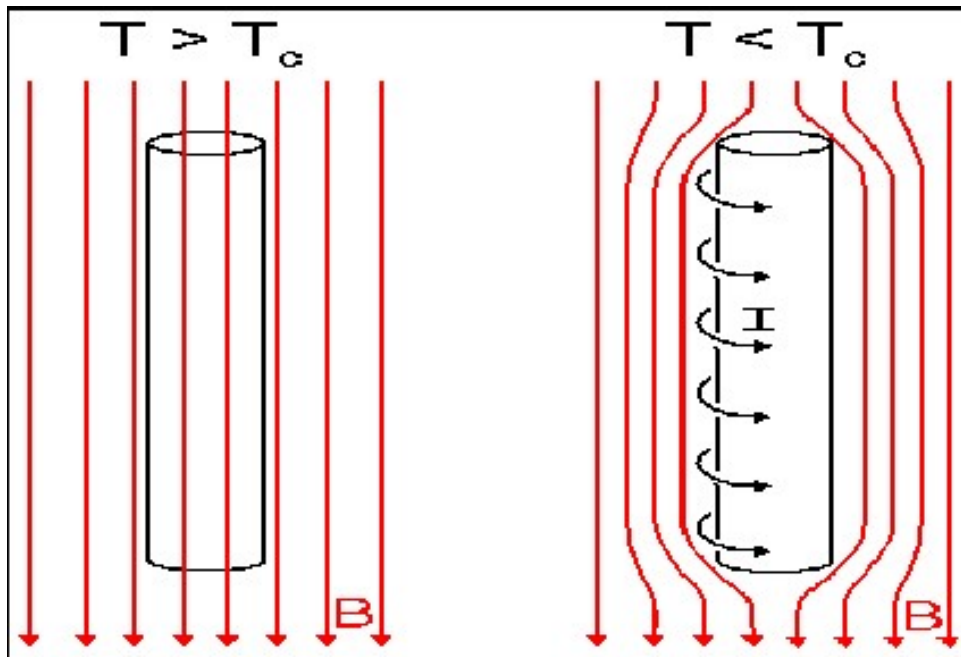


Heike Kamerling Onnes





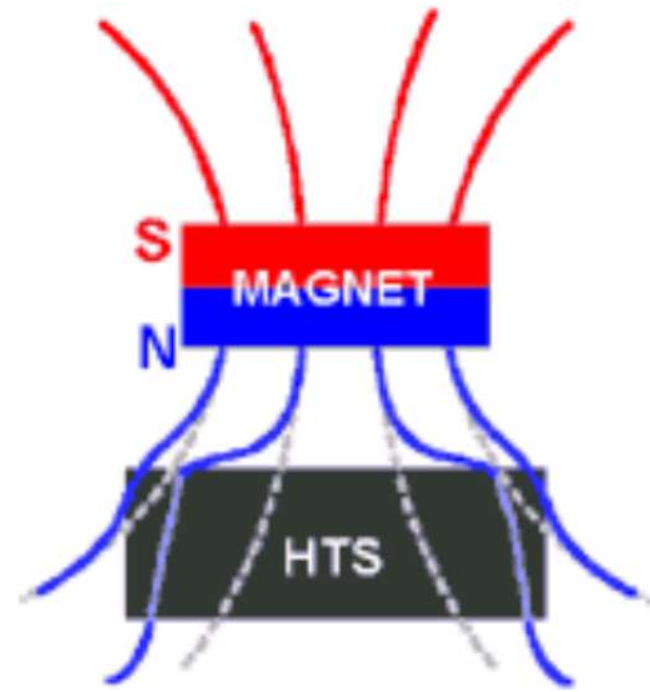
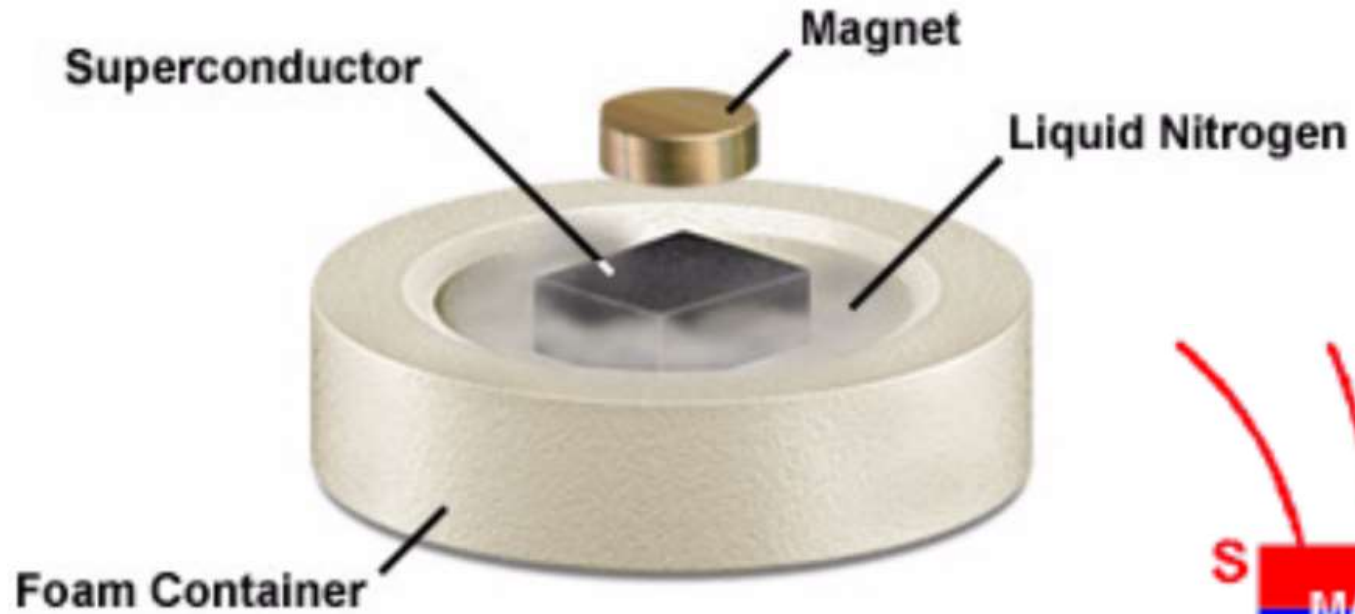
Meissner effect – the key signature of superconductivity



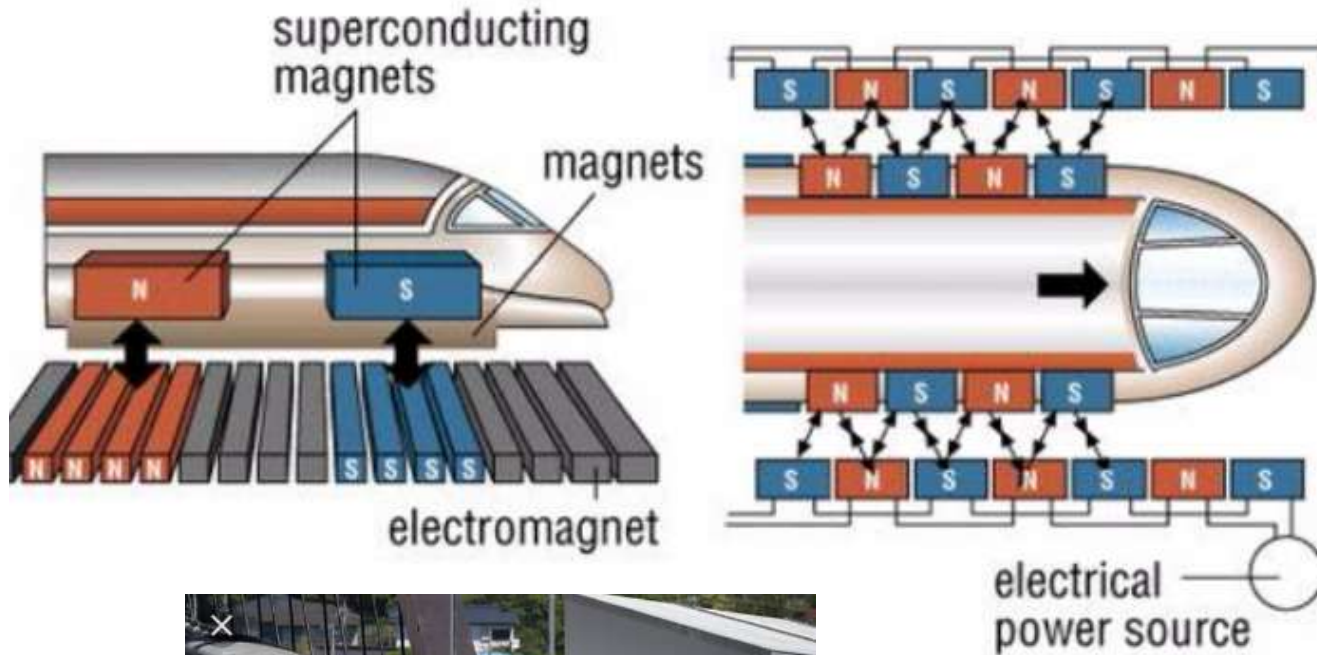
Formula	T_c (K)	H_c (T)	Type	BCS
Elements				
Al	1.20	0.01	I	yes
Cd	0.52	0.0028	I	yes
Diamond:B	11.4	4	II	yes
Ga	1.083	0.0058	I	yes
Hf	0.165		I	yes
α -Hg	4.15	0.04	I	yes
β -Hg	3.95	0.04	I	yes
In	3.4	0.03	I	yes
Ir	0.14	0.0016 ^[7]	I	yes
α -La	4.9		I	yes
β -La	6.3		I	yes
Mo	0.92	0.0096	I	yes
Nb	9.26	0.82	II	yes
Os	0.65	0.007	I	yes

Magnetic levitation

The Meissner Effect



Magnetic levitation train



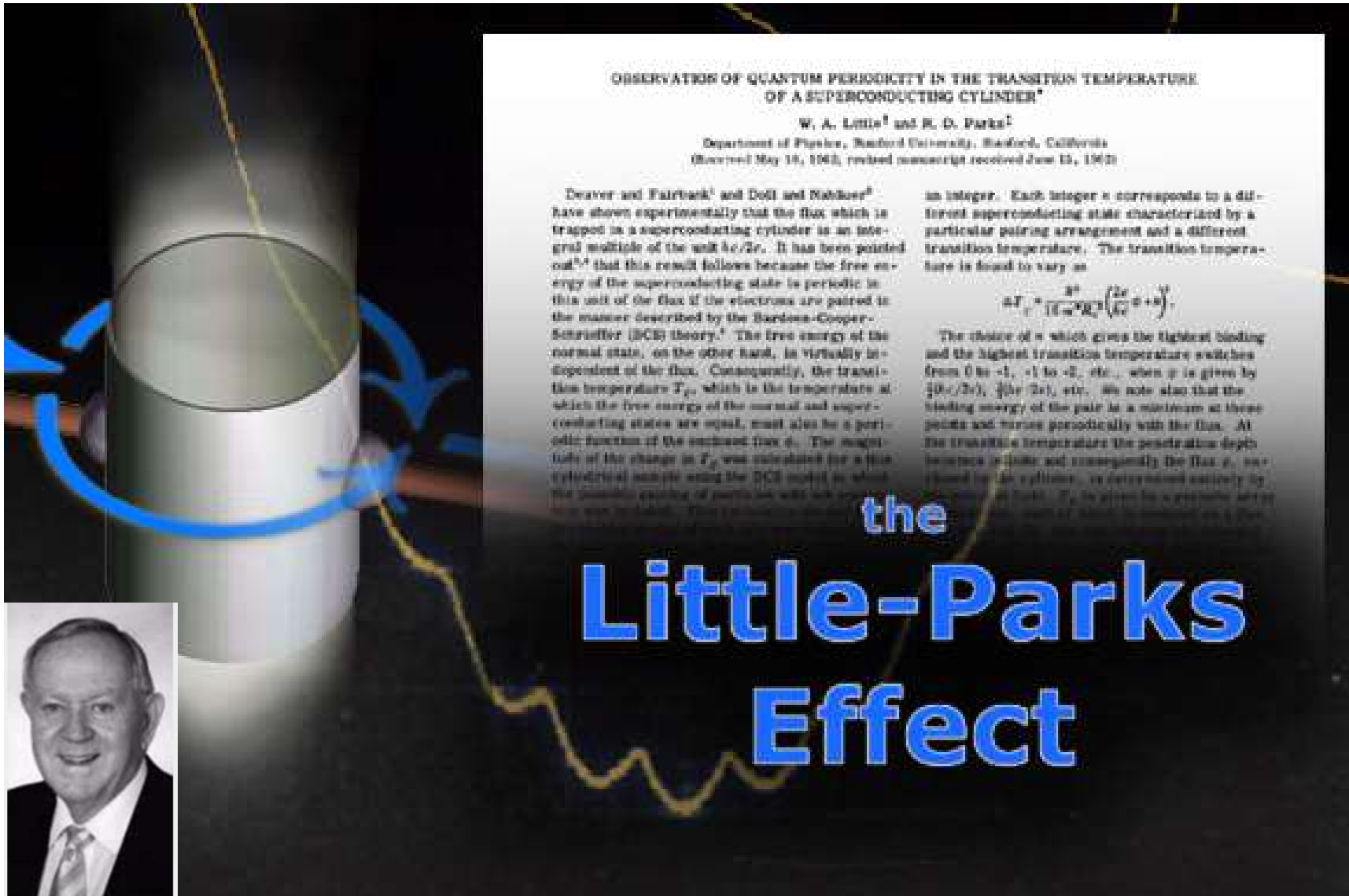
blogs.wsj.com

U.S. Transportation Secretary Foxx Rides on Japan's Maglev Train - Jap...



Fundamental property of superconductors: Little-Parks effect ('62)

The basic idea: magnetic field induces non-zero vector-potential, which produces non-zero superfluid velocity, thus reducing the T_c . Proves physical reality of the vector-potential



OBSERVATION OF QUANTUM PERIODICITY IN THE TRANSITION TEMPERATURE OF A SUPERCONDUCTING CYLINDER*

W. A. Little¹ and R. D. Parks²


Department of Physics, Stanford University, Stanford, California
(Received May 14, 1962; revised manuscript received June 12, 1962)

Deaver and Fairbank³ and Doll and Nabauer⁴ have shown experimentally that the flux which is trapped in a superconducting cylinder is an integral multiple of the unit $hc/2e$. It has been pointed out^{5,6} that this result follows because the free energy of the superconducting state is periodic in this unit of the flux if the electrons are paired in the manner described by the Bardeen-Cooper-Schrieffer (BCS) theory.⁷ The free energy of the normal state, on the other hand, is virtually independent of the flux. Consequently, the transition temperature T_c , which is the temperature at which the free energy of the normal and superconducting states are equal, must also be a periodic function of the enclosed flux ϕ . The magnitude of the change in T_c was calculated for a thin cylindrical sample using the BCS model in which the ground energy of particles with spin s is an integer. Each integer n corresponds to a different superconducting state characterized by a particular pairing arrangement and a different transition temperature. The transition temperature is found to vary as

$$\Delta T_c \approx \frac{3^2}{16\pi^2 k_B} \left(\frac{2e}{hc} \phi + n \right).$$

The choice of n which gives the tightest binding and the highest transition temperature switches from 0 to -1, -1 to -2, etc., when ϕ is given by $\{0c/2e\}$, $\{1c/2e\}$, etc. We note also that the binding energy of the pair is a maximum at these points and varies periodically with the flux. At the transition temperature the penetration depth becomes infinite and consequently the flux ϕ , enclosed by the cylinder, is determined entirely by the magnetic field H . Thus, T_c is given by a periodic series of peaks and valleys as a function of H .

the
**Little-Parks
Effect**



Discovery of the proximity effect: A supercurrent can flow through a thin layers of a non-superconducting metals "sandwiched" between two superconducting metals.

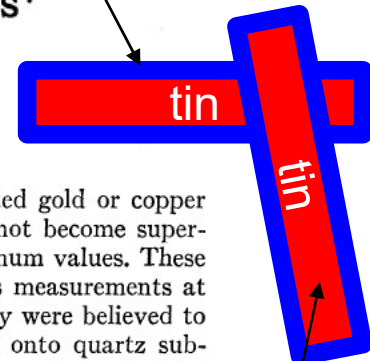
Superconductivity of Contacts with Interposed Barriers*

HANS MEISSNER†

Department of Physics, The Johns Hopkins University, Baltimore, Maryland

(Received August 25, 1959)

Non-superconductor (normal metal, i.e., Ag)



Resistance vs current diagrams and "Diagrams of State" have been obtained for 63 contacts between crossed wires of tin. The wires were plated with various thicknesses of the following metals: copper, silver, gold, chromium, iron, cobalt, nickel, and platinum. The contacts became superconducting, or showed a noticeable decrease of their resistance at lower temperatures if the plated films were not too thick. The limiting thicknesses were about 35×10^{-6} cm for Cu, Ag, and Au; 7.5×10^{-6} cm for Pt, 4×10^{-6} cm for Cr, and less than 2×10^{-6} cm for the ferromagnetic metals Fe, Co, and Ni. The investigation was extended to measurements of the resistance of contacts between crossed wires of copper or gold plated with various thicknesses of tin. Simultaneous measurements

of the (longitudinal) resistance of the tin-plated gold or copper wires showed that these thin films of tin do not become superconducting for thicknesses below certain minimum values. These latter findings are in agreement with previous measurements at Toronto. The measurements at Toronto usually were believed to be unreliable because films of tin evaporated onto quartz substrates can be superconducting at thicknesses as small as 1.6×10^{-6} cm. It is now believed that just as superconducting electrons can drift into an adjoining normal conducting layer and make it superconducting, normal electrons can drift into an adjoining superconducting layer and prevent superconductivity.

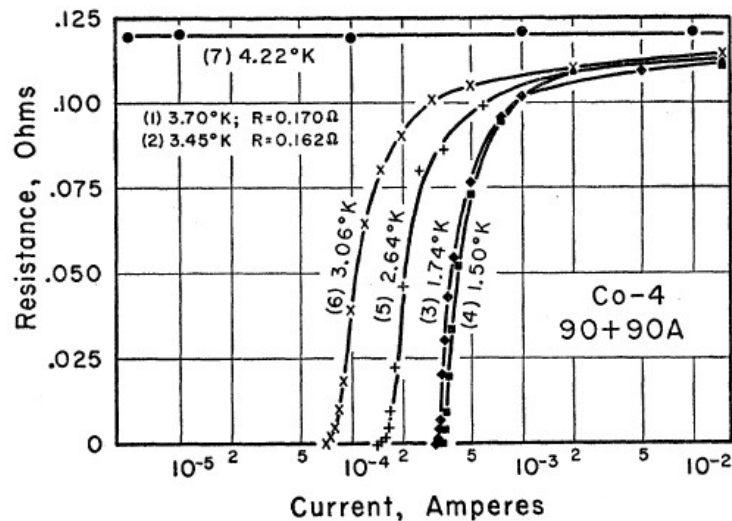


FIG. 1. Resistance vs current diagram of cobalt-plated contact Co 4, representative of diagrams type A.

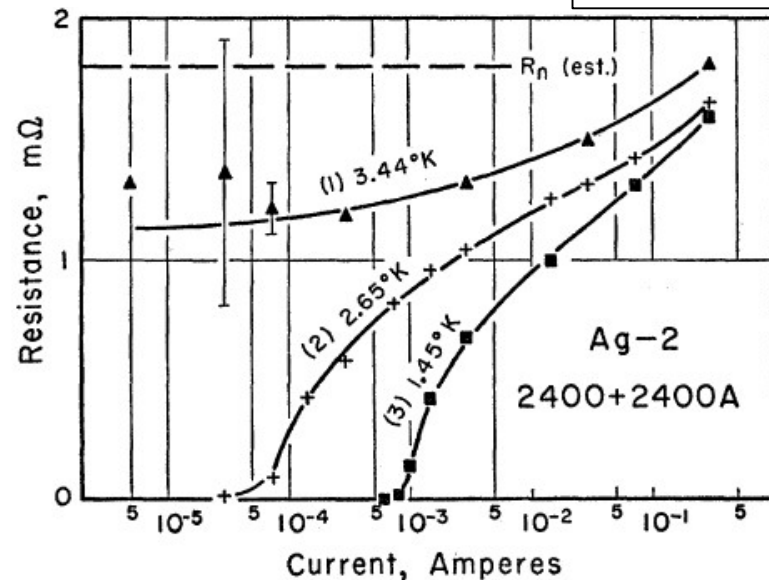
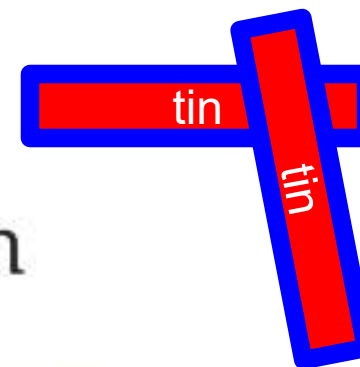


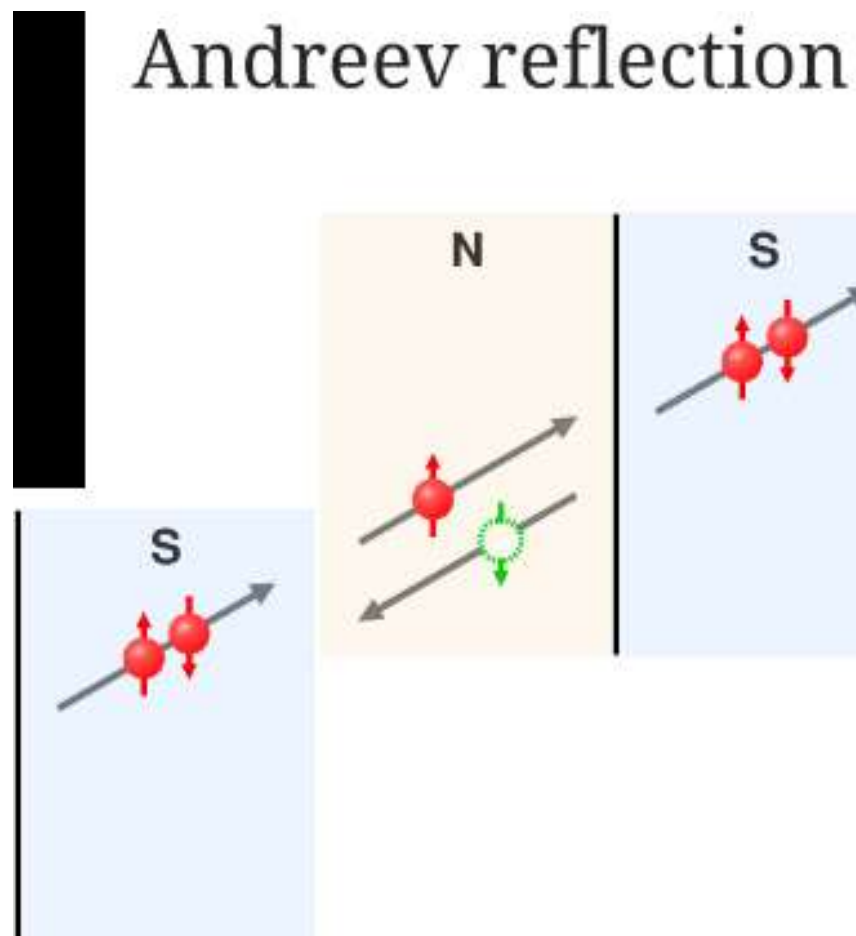
FIG. 2. Resistance vs current diagram of silver-plated contact Ag 2, representative of diagrams type B.



Explanation of the supercurrent in SNS junctions --- Andreev reflection



www.kapitza.ras.ru
www.kapitza.ras.ru/~andreev/afan...

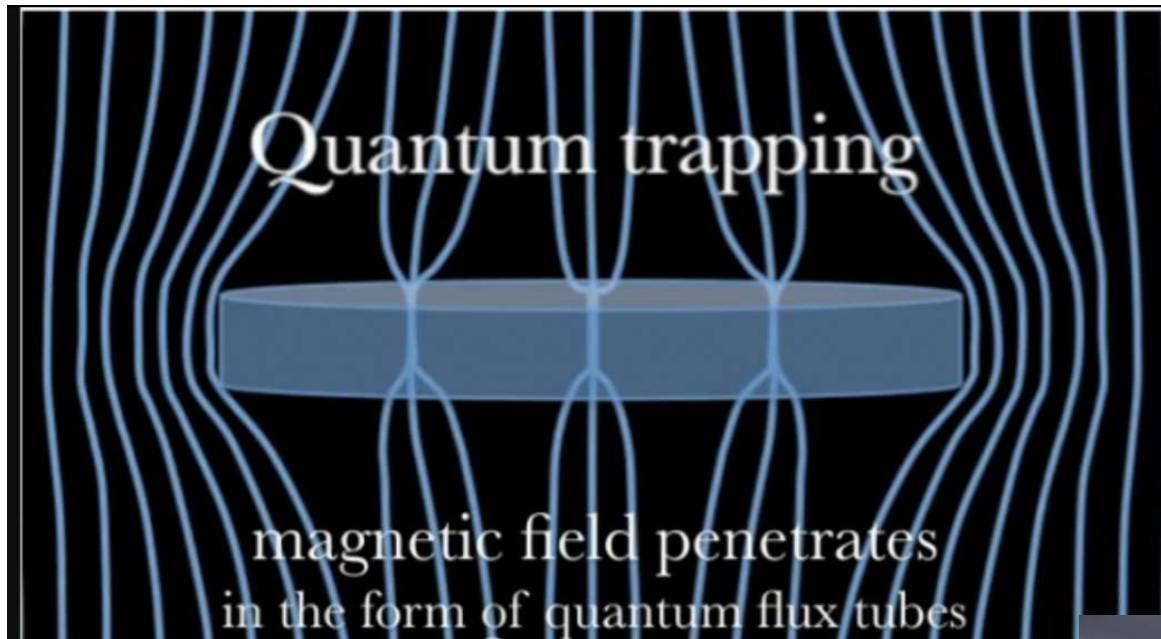


A.F. Andreev, 1964



TM

Superconducting vortices carry magnetic field into the superconductor (type-II superconductivity)



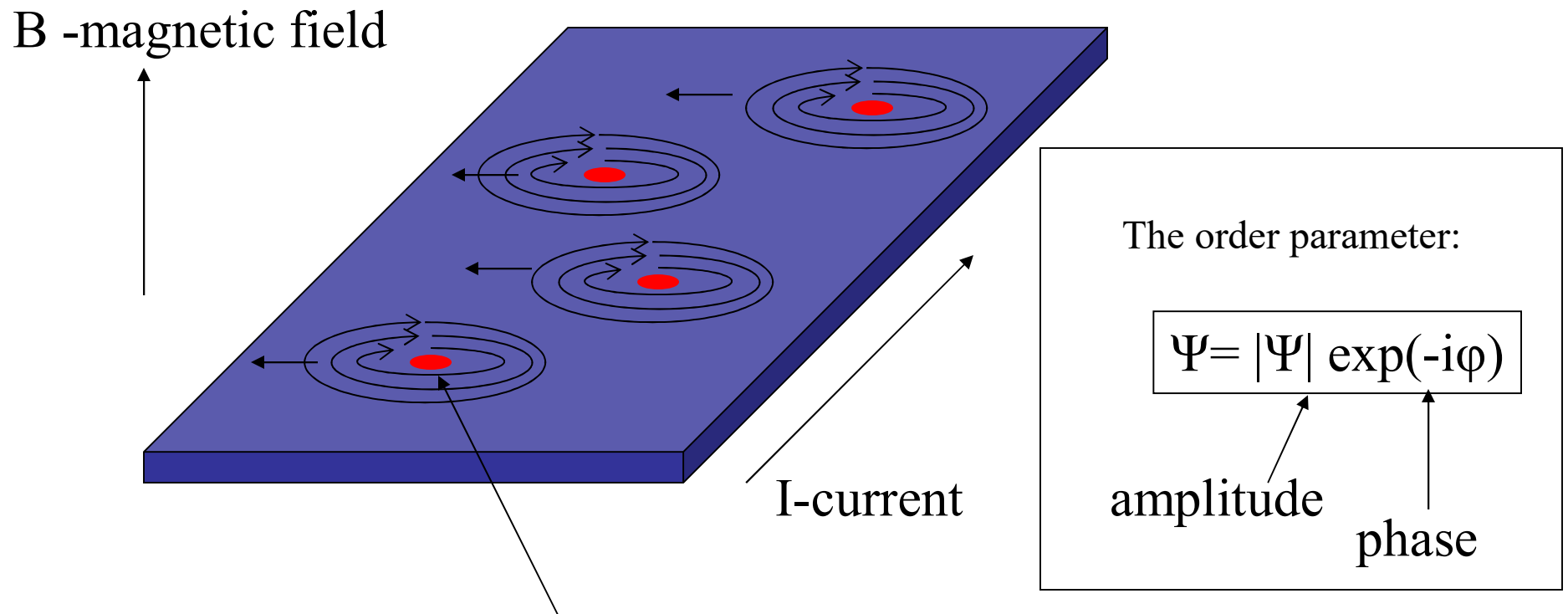
Amazing fact: unlike real tornadoes, superconducting vortices (also called Abrikosov vortices) are all exactly the same and carry one quantum of the Magnetic flux, $h/(2e)$. By the way, the factor “ $2e$ ”, not just “ e ”, proves that superconducting electrons move in pairs.



Vortices introduce electrical resistance to otherwise superconducting materials

Magnetic field creates vortices--

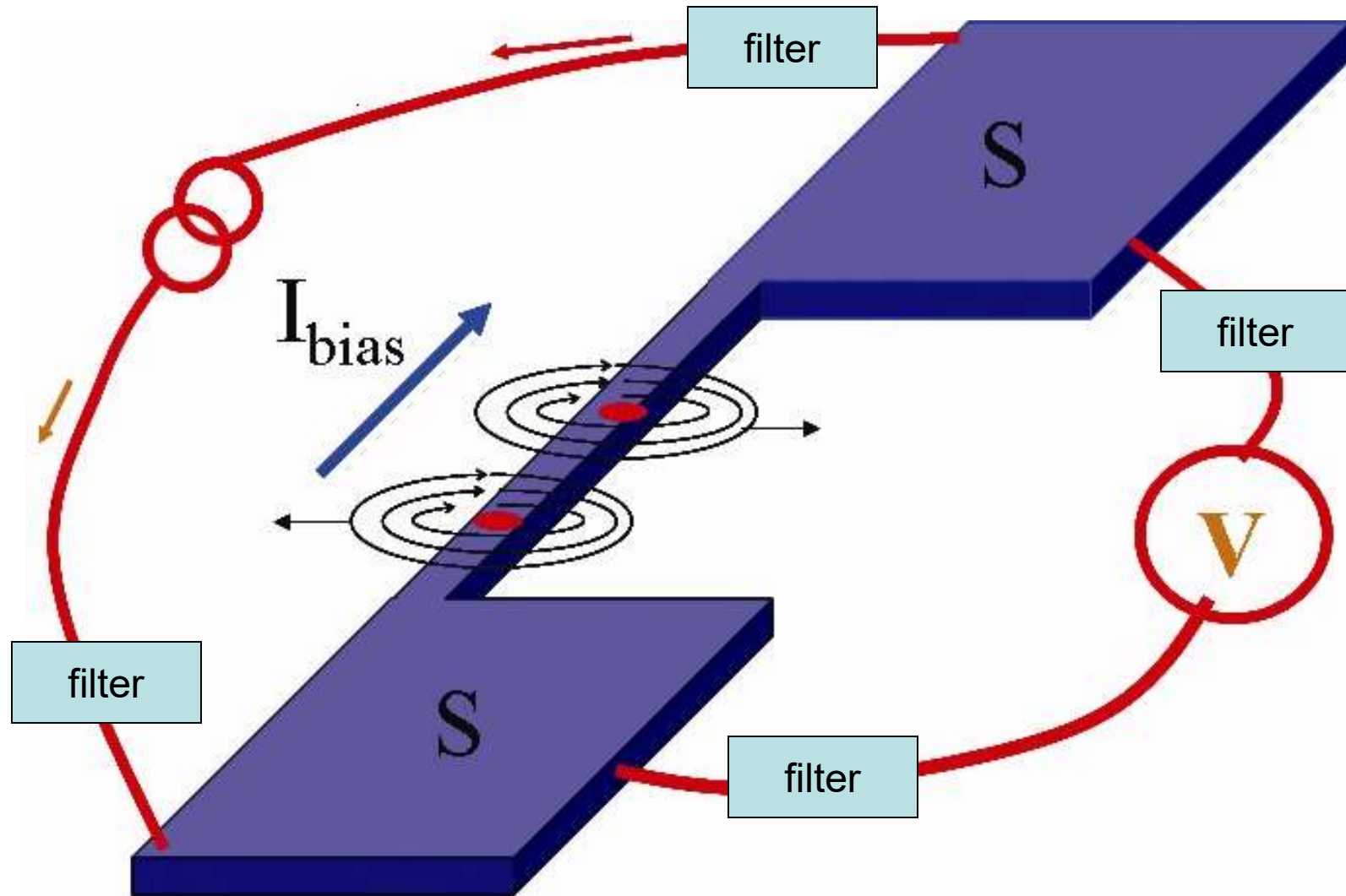
Vortices cause dissipation (i.e. a non-zero electrical resistance)!



Vortex core: normal, not superconducting; diameter $\xi \sim 10$ nm

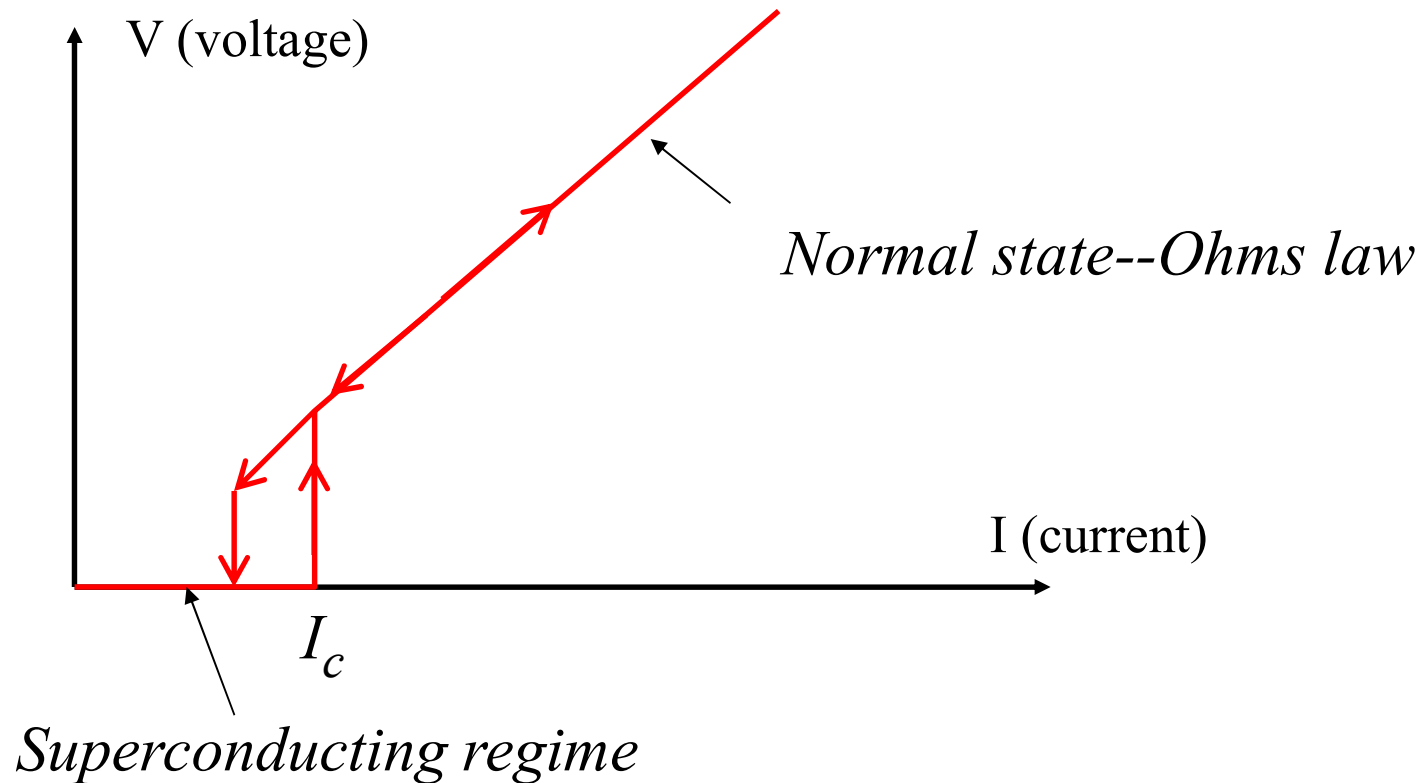
DC transport measurement schematic

Phase slip events are shown as red dots

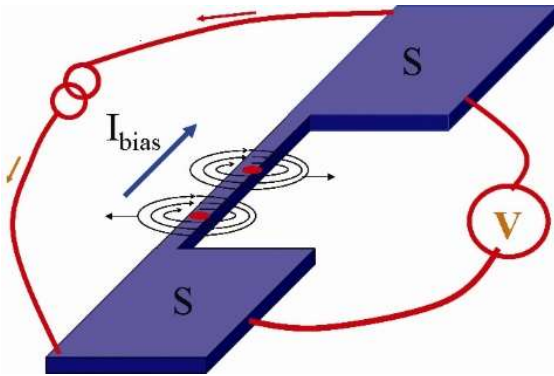


Superconductivity: very basic introduction

Electrical resistance is zero only if current is not too strong



How to use voltage to figure out the rate of phase slips?



Phase evolution equation: $2eV = \hbar \, d\phi/dt$

Gor'kov, L.P. (1958) *Exp. Theor. Phys. (USSR)*, 34, 735;
(English transl.: (1958) *Sov. Phys. JETP*, 7, 505.)

Remember the Schrodinger equation: $i\hbar \, (d\Psi/dt) = E \Psi$

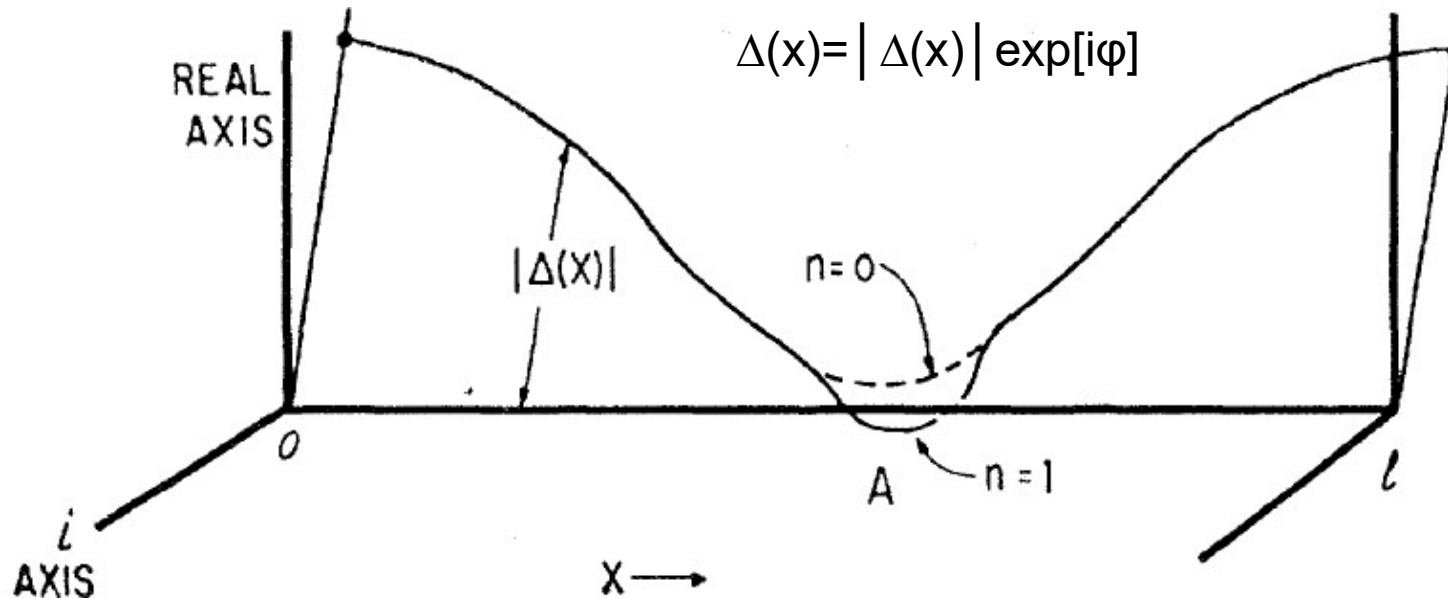
Thus the phase is: $\phi = Et/\hbar$

The energy of a pair of superconducting electrons is $E = 2eV$, where V is the electric potential.

Thus we obtain the phase evolution equation:

$$2eV = \hbar \, d\phi/dt$$

Transport properties: Little's Phase Slip



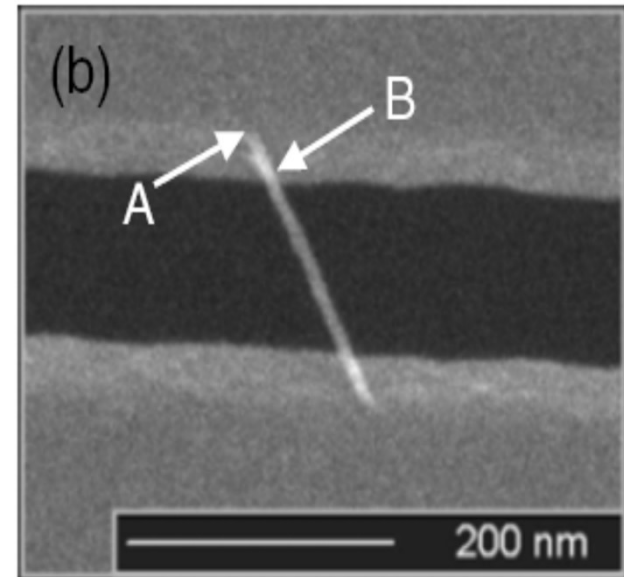
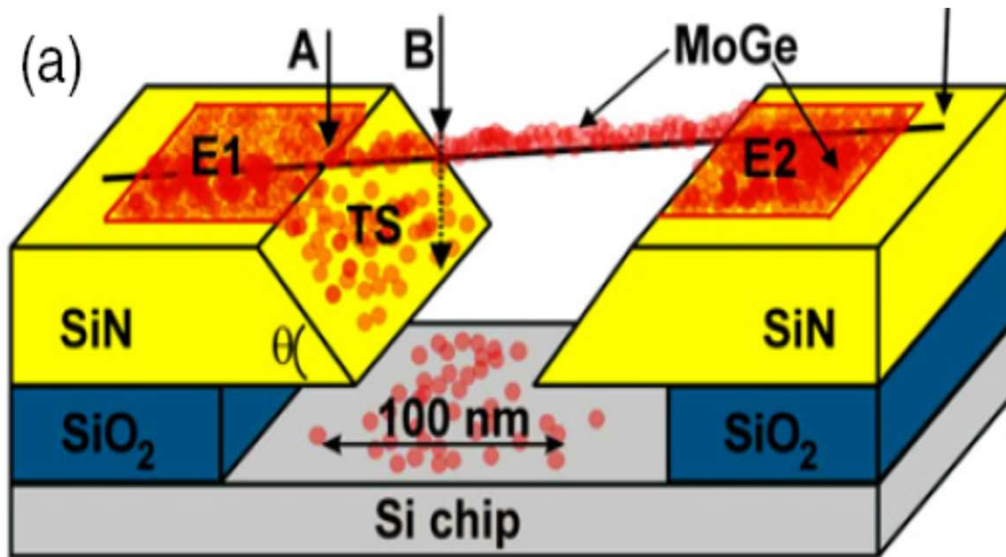
W. A. Little, "Decay of persistent currents in small superconductors", *Physical Review*, V.156, pp.396-403 (1967).

Two types of phase slips (PS) can be expected:

1. The usual, thermally activated PS (TAPS)
2. Quantum phase slip (QPS)

Fabrication of nanowires

Method of Molecular Templating



Si/ SiO₂/SiN substrate with undercut

~ 0.5 mm Si wafer

500 nm SiO₂

60 nm SiN

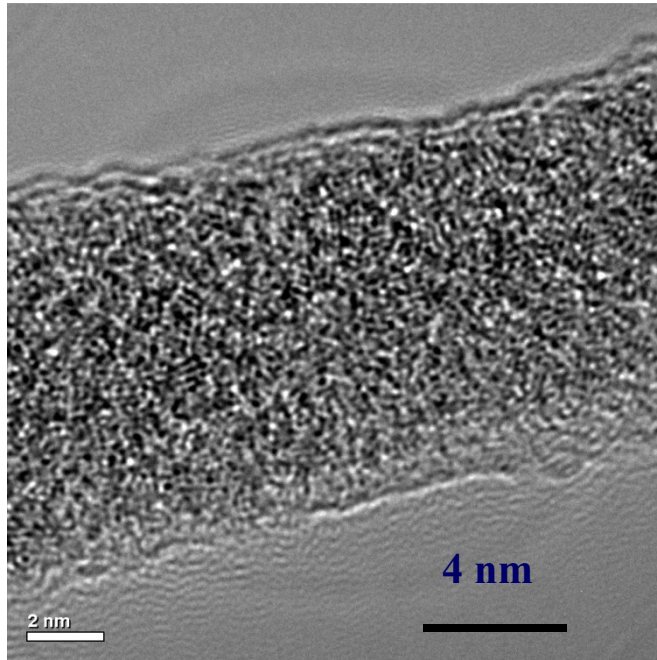
Width of the trenches ~ 50 - 500 nm

HF wet etch for ~10 seconds
to form undercut

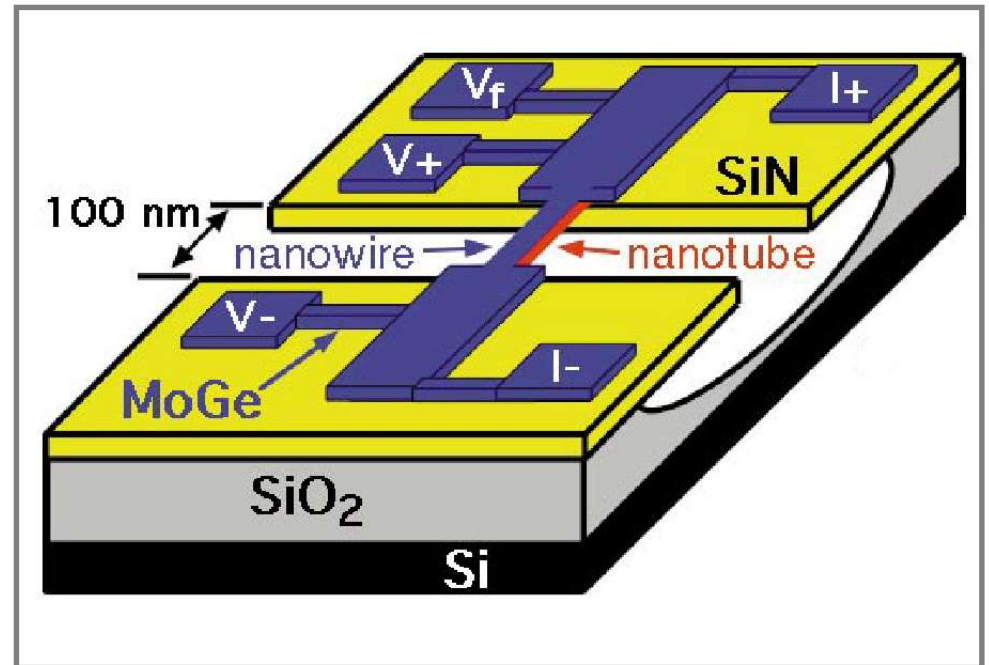


A. Bezryadin, C.N. Lau, M. Tinkham, *Nature* **404**, 971 (2000)

Sample Fabrication



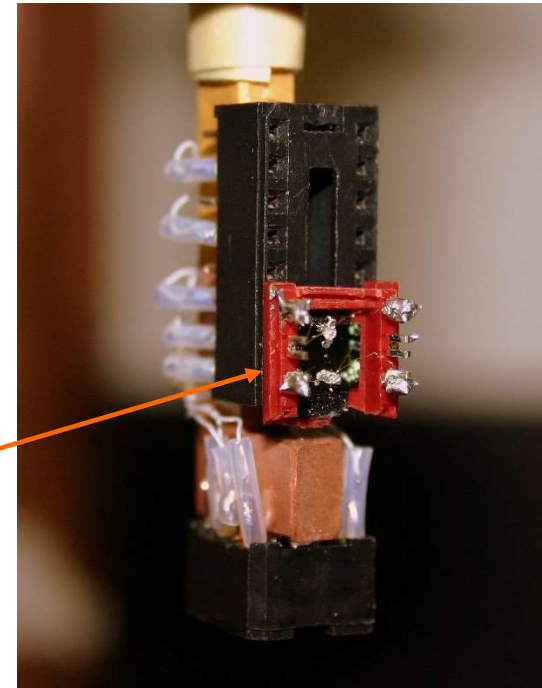
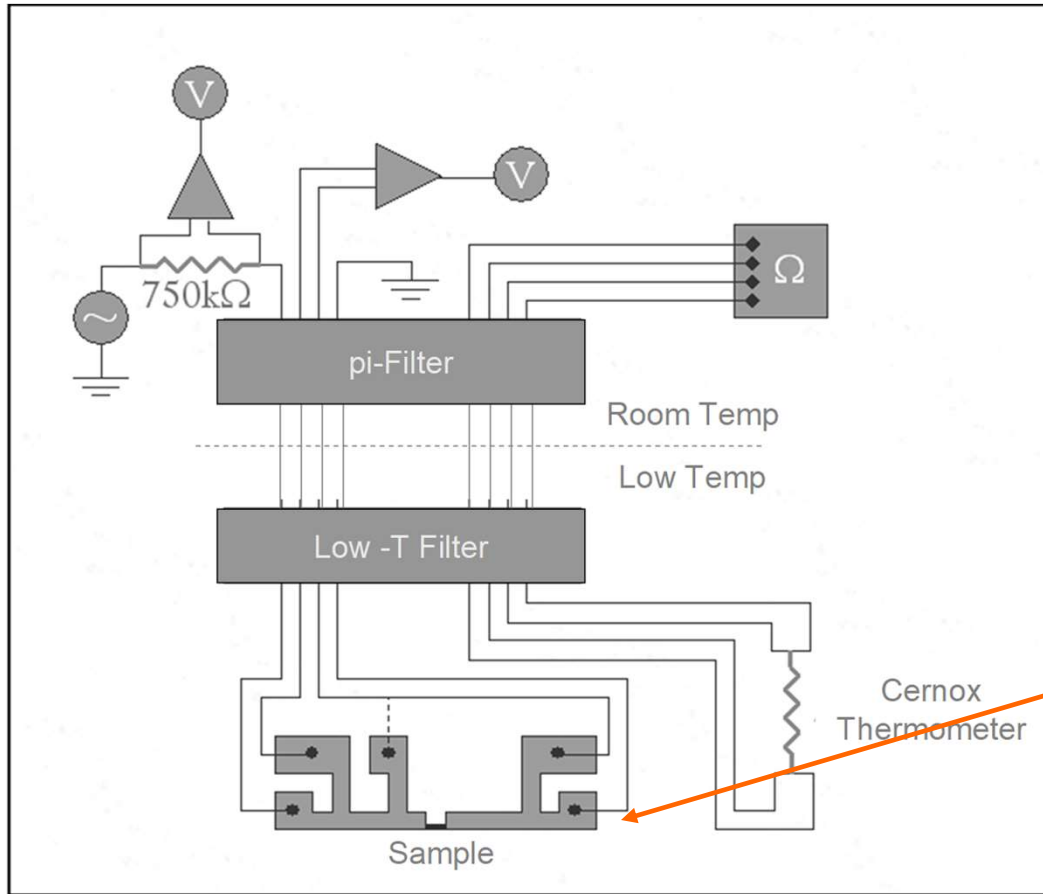
**TEM image of a wire shows amorphous morphology.
Nominal MoGe thickness = 3 nm**



**Schematic picture of the pattern
Nanowire + Film Electrodes used in
transport measurements**



Measurement Scheme



Circuit Diagram

Sample mounted on the ^3He insert.



TM

Tony Bollinger's sample-mounting procedure in winter in Urbana

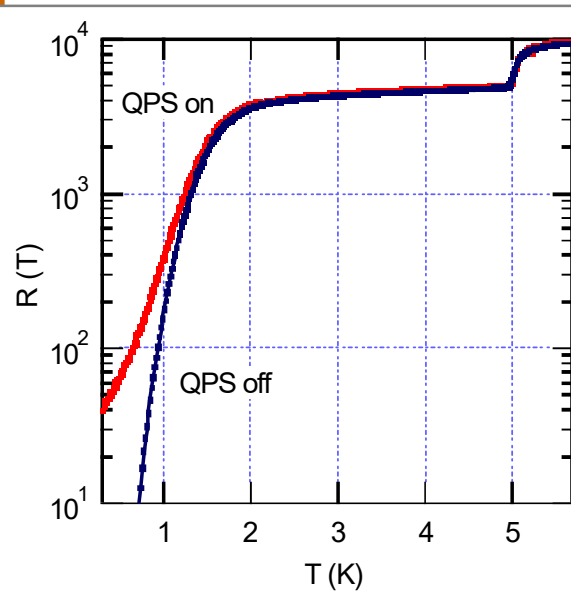
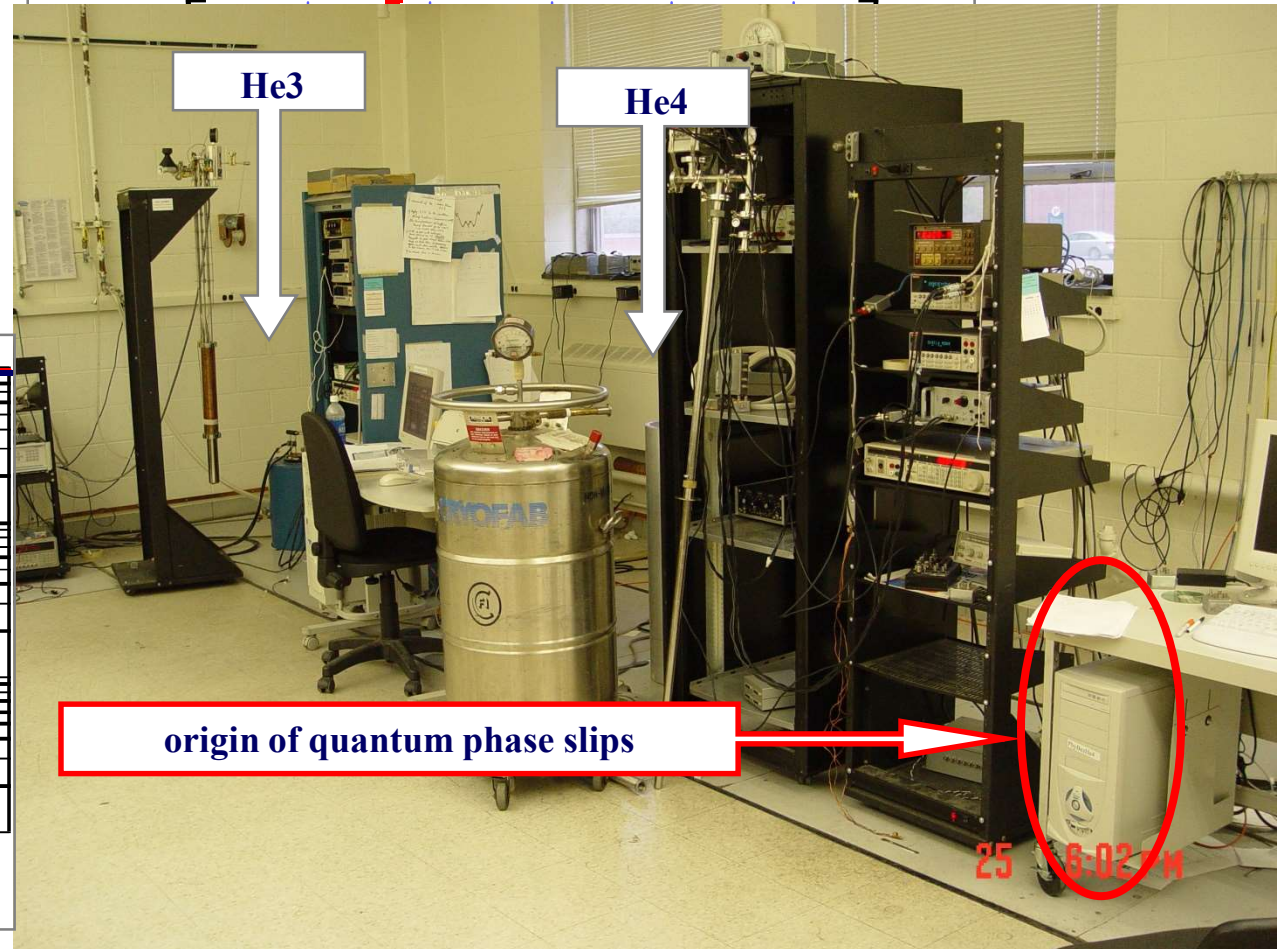
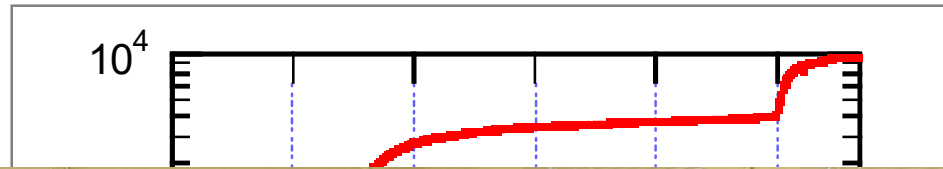


Procedure (~75% Success)

- Put on gloves
- Put grounded socket for mounting in vise with grounded indium dot tool connected
- Spray high-backed black chair all over and about 1 m square meter of ground with anti-static spray
 - DO NOT use green chair
 - Not sure about short-backed black chairs
- Sit down
- Spray bottom of feet with anti-static spray
- Plant feet on the ground. ***Do not move your feet again for any reason until mounting is finished.***
- Mount sample
- Keep sample in grounded socket until last possible moment
- Test samples in dipstick at ~1 nA



Electromagnetic noise can mimic “resistive tails” resembling quantum phase slips



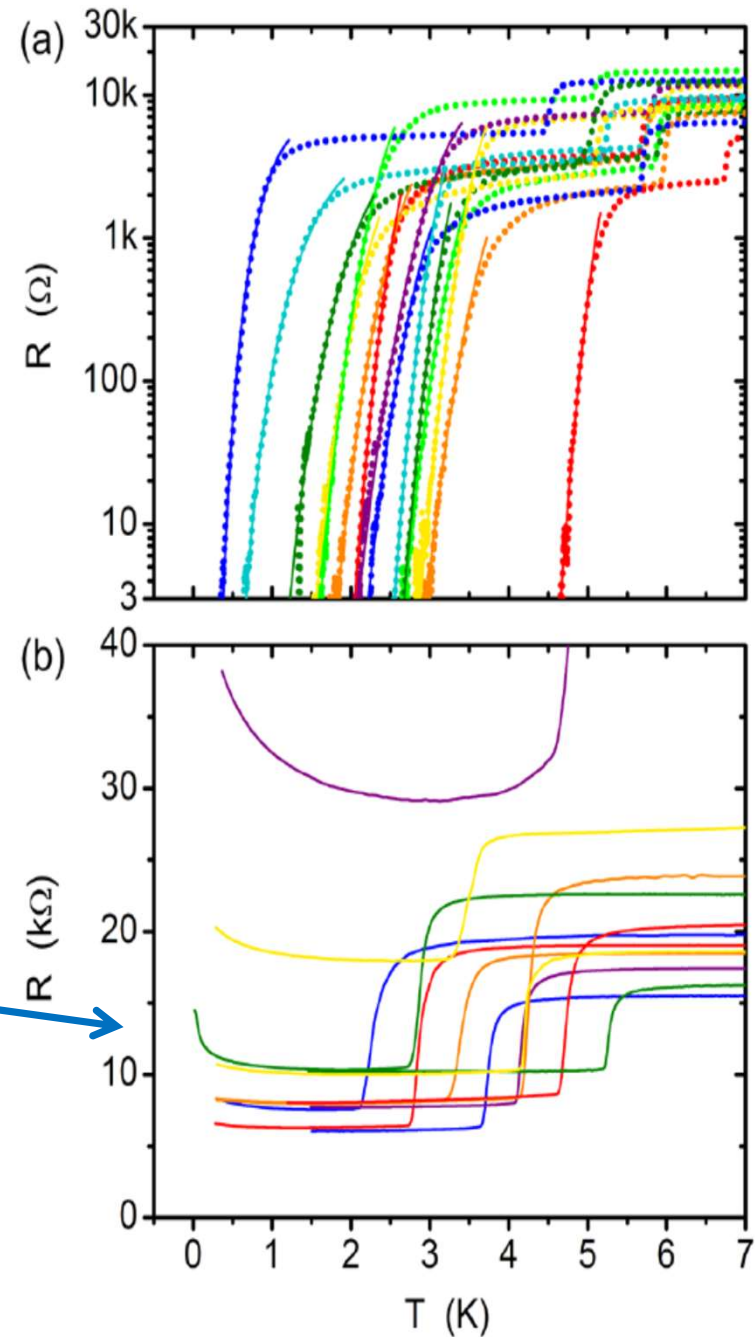
Dichotomy in nanowires: Evidence for superconductor- insulator transition (SIT)

$$R=V/I \quad I \sim 3 \text{ nA}$$

The difference between samples is the amount of the deposited Mo79Ge21.

$$R_{\text{sheet}} = 100 - 400 \Omega$$

Can the insulating behavior be due to Anderson localization of the BCS condensate?



Bollinger, Dinsmore, Rogachev, Bezryadin,
Phys. Rev. Lett. **101**, 227003 (2008)





Linearity of the Schrödinger's equation

Suppose Ψ_1 is a valid solution of the Schrödinger equation:

$$i\hbar \frac{\partial \psi_1}{\partial t} = \frac{\partial^2 \psi_1}{\partial x^2} + U(x)\psi_1$$

And suppose that Ψ_2 is another valid solution of the Schrödinger equation:

$$i\hbar \frac{\partial \psi_2}{\partial t} = \frac{\partial^2 \psi_2}{\partial x^2} + U(x)\psi_2$$

Then $(\Psi_1 + \Psi_2)/\sqrt{2}$ is also a valid solution, because:

$$i\hbar \frac{\partial (\psi_1 + \psi_2)}{\partial t} = \frac{\partial^2 (\psi_1 + \psi_2)}{\partial x^2} + U(x)(\psi_1 + \psi_2)$$

The state $(\Psi_1 + \Psi_2)/\sqrt{2}$ is a new combined state which is called “quantum superposition” of state (1) and (2)

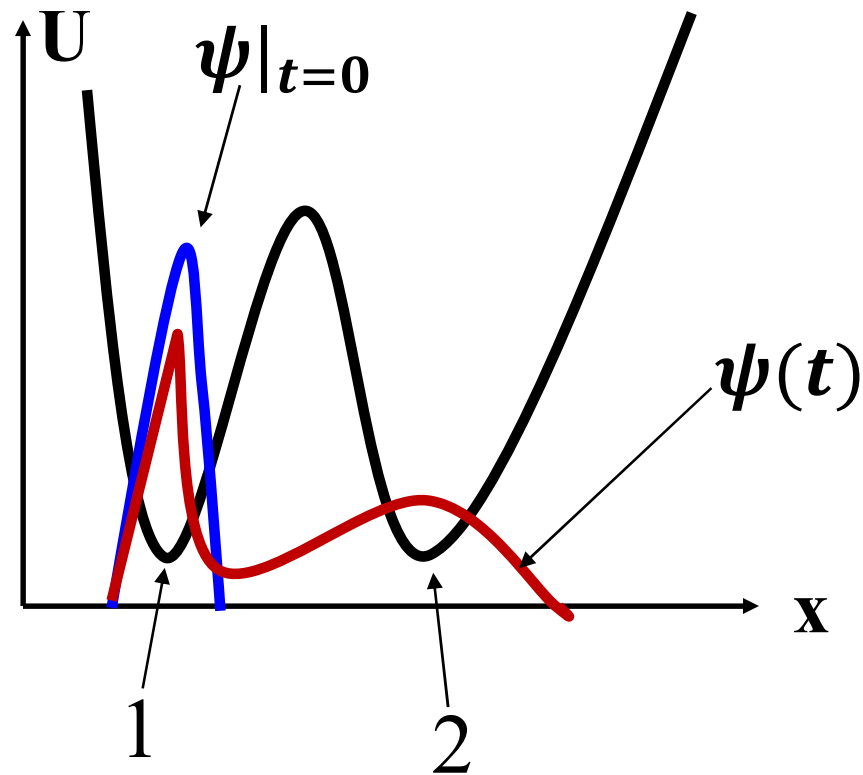




George Gamow

(Also known for the development of the “Big Bang” theory)

Quantum tunneling

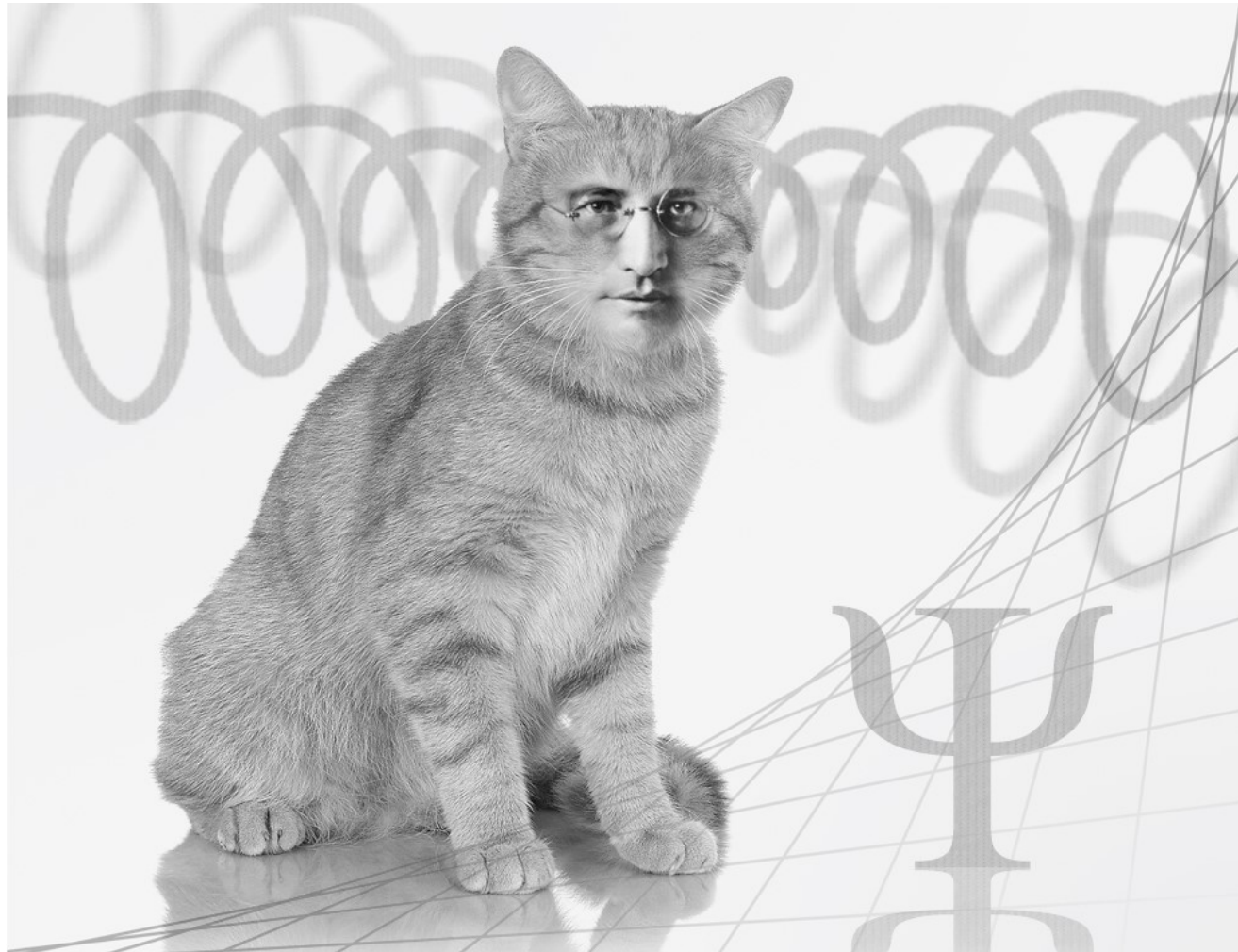


Quantum tunneling is possible since quantum superpositions of states are possible.



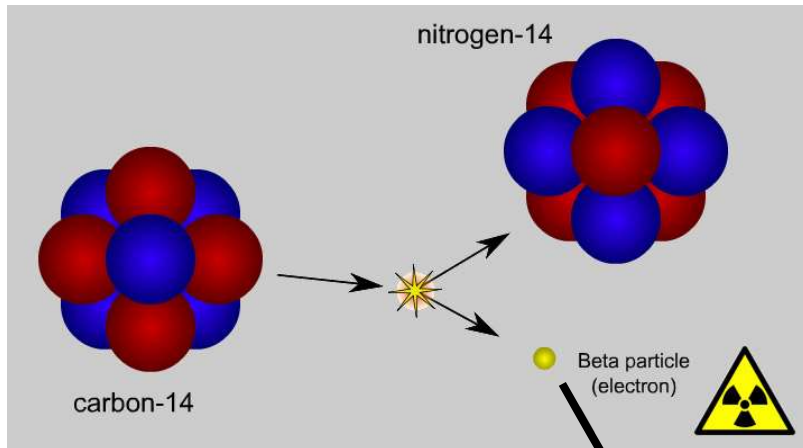
Schrödinger cat – the ultimate macroscopic quantum phenomenon

E. Schrödinger, Naturwiss. **23** (1935), 807.

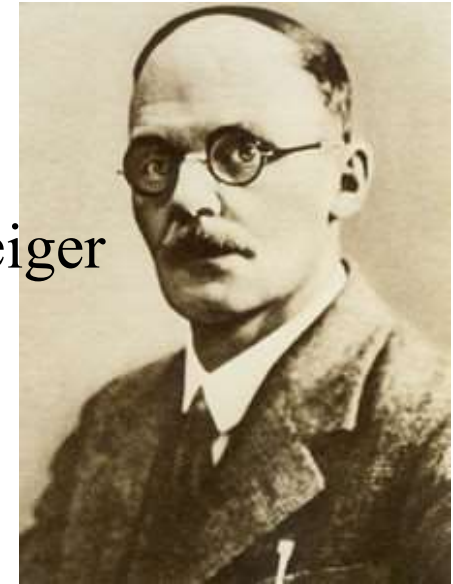


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Schrödinger cat – thought experiment



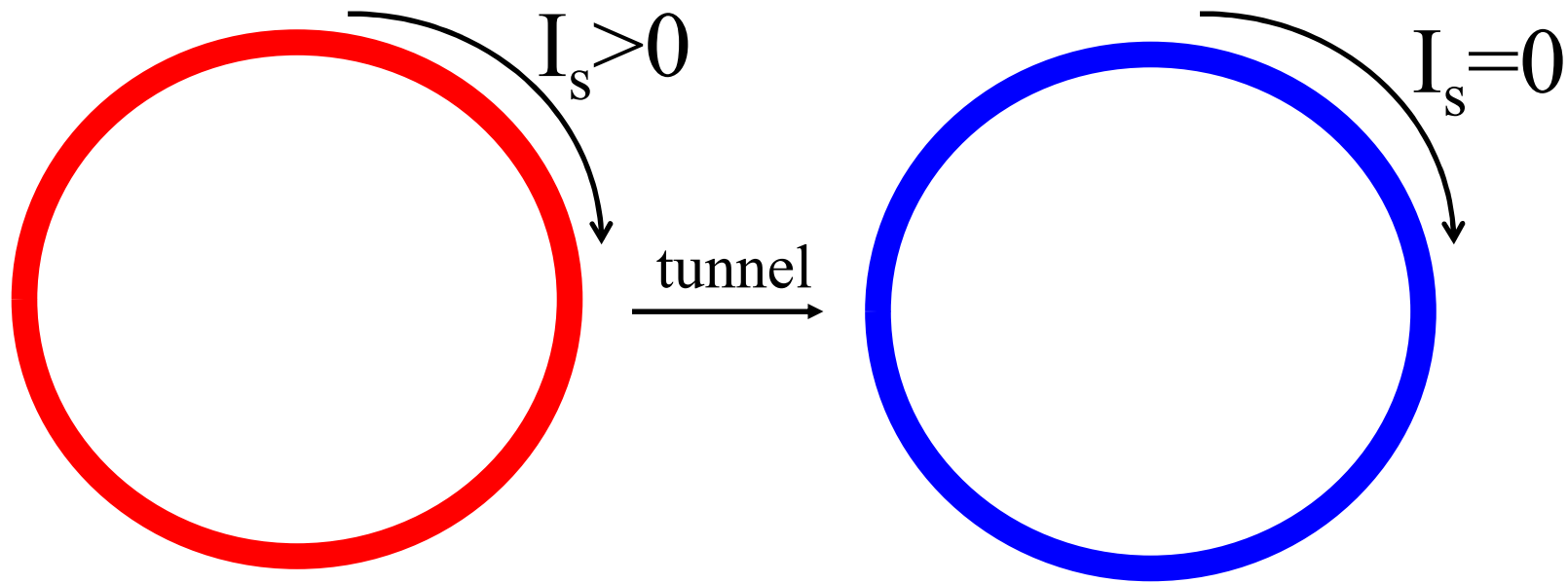
Hans Geiger



Geiger counter



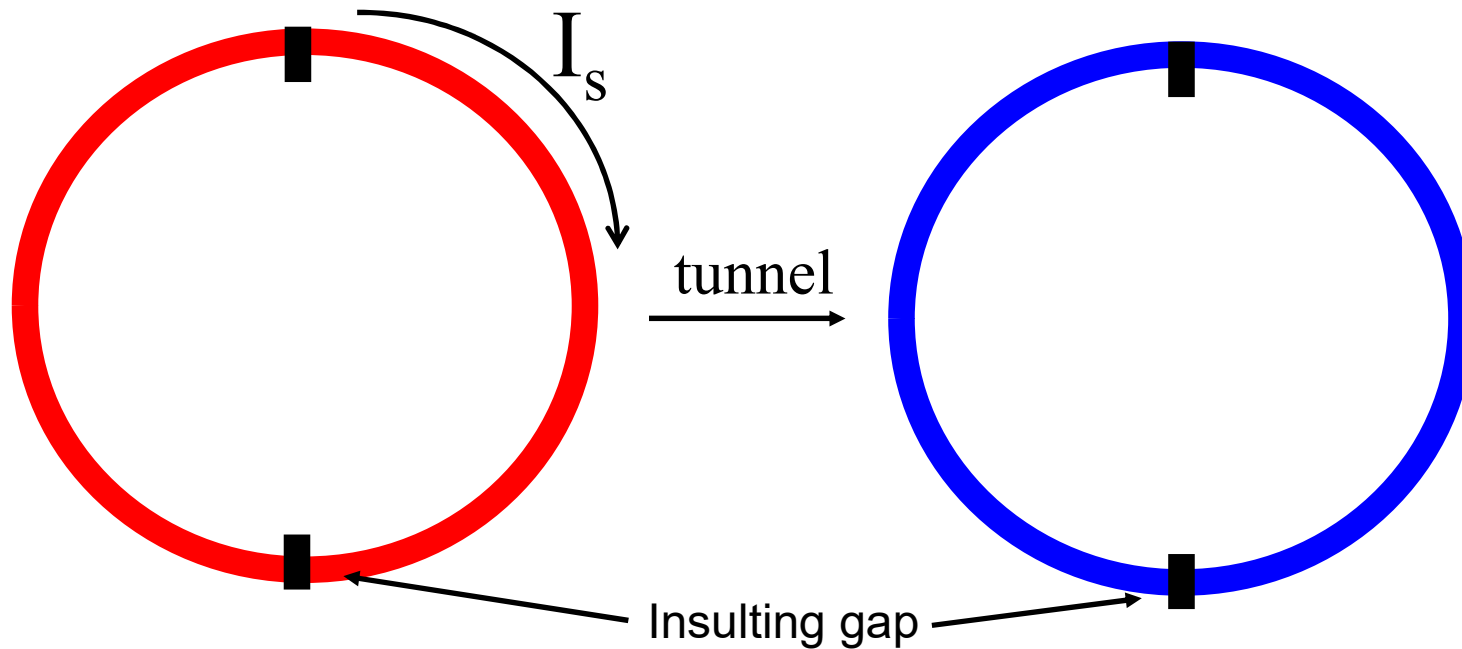
What sort of tunneling we will consider?



- Red color represents some strong current in the superconducting wire loop
- Blue color represents no current or a much smaller current in the loop



Previous results relate loops with insulating interruptions (SQUIDS)

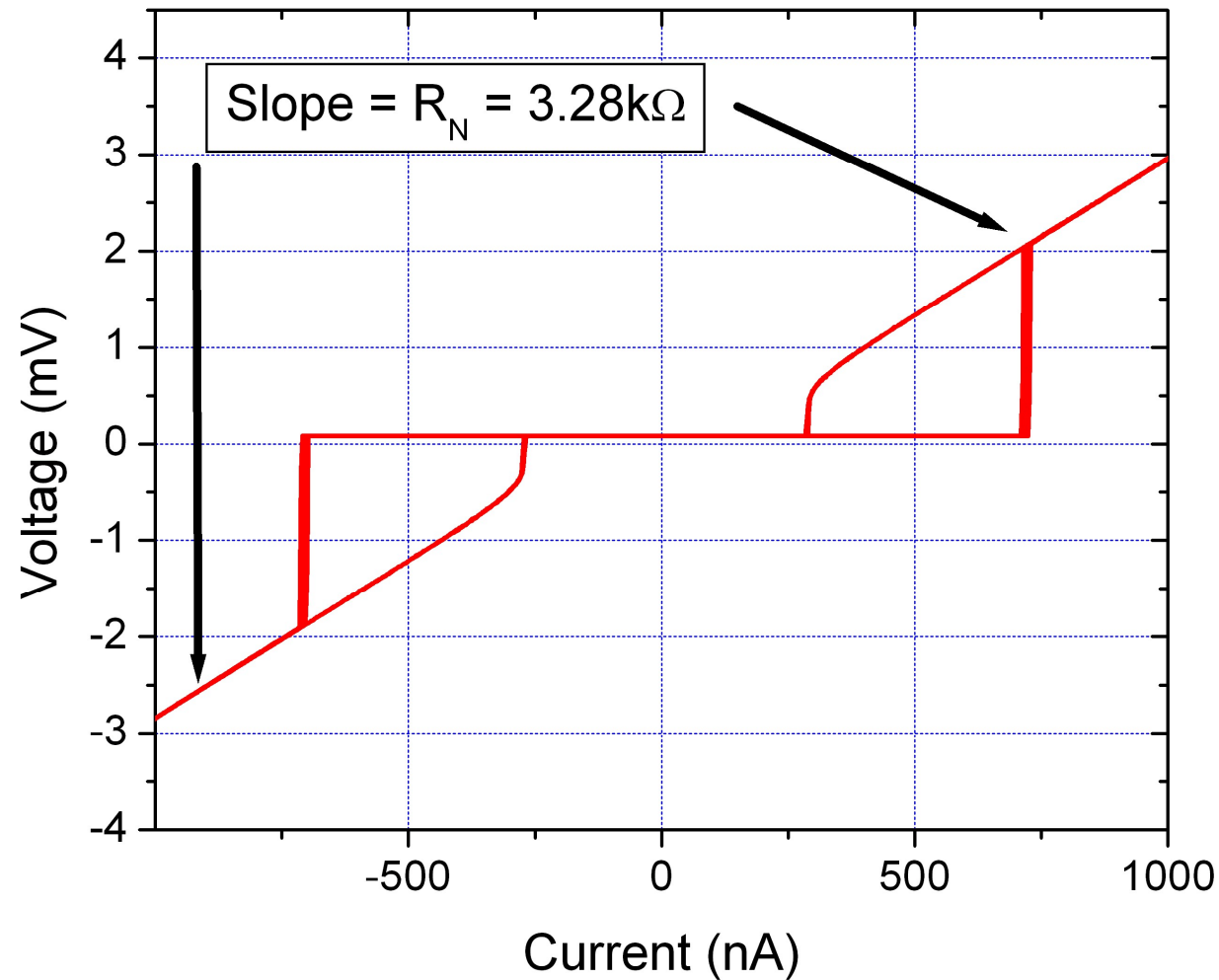


-Red color represents some strong current in the superconducting loop

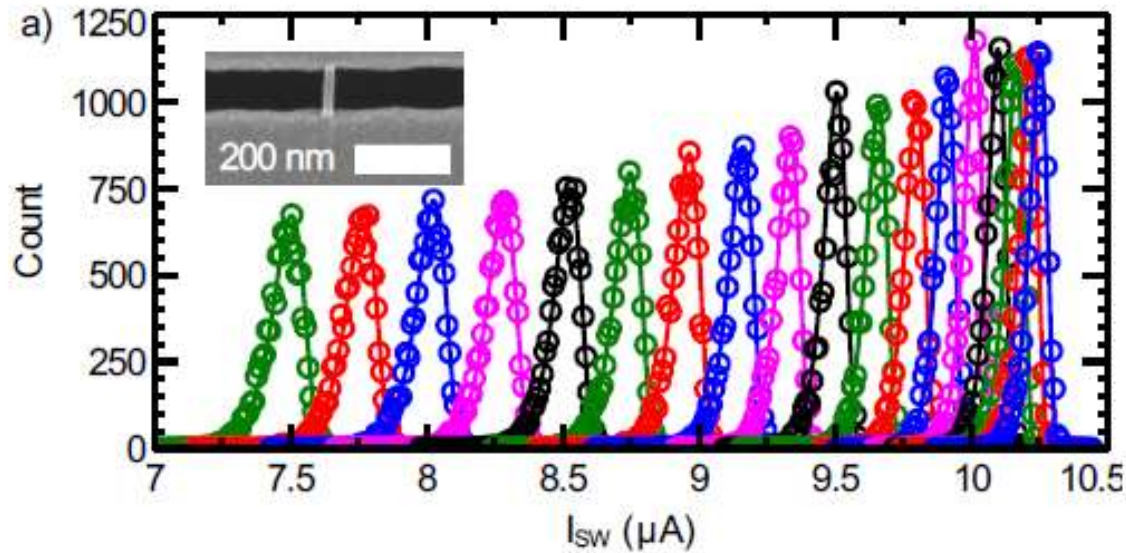
-Blue color represents no current or very little current in the superconducting loop



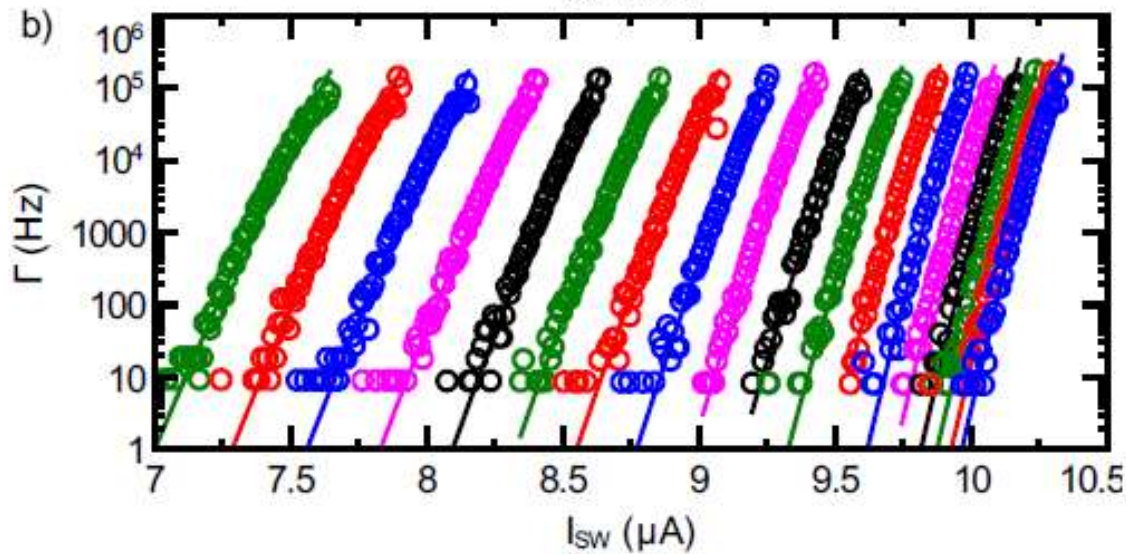
Search for QPS at high bias currents, by measuring the fluctuations of the switching current



Observation of the quantum fluctuations of the critical current, cause by the quantum phase slips

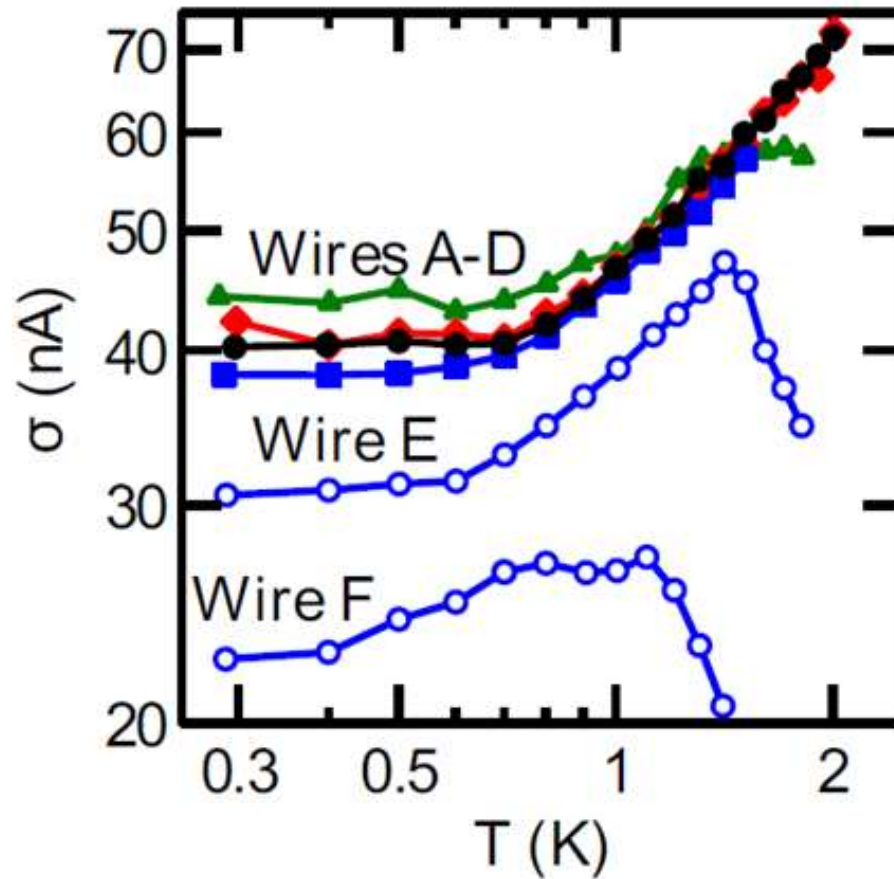


2 K - 0.3 K



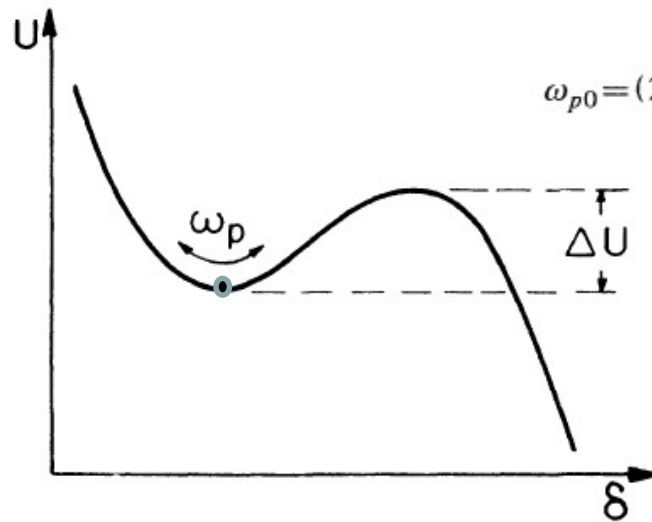
2 K - 0.3 K

Quantum Phase slisp: T_q scales linearly with T_c



Here “sigma” represents the fluctuations of the critical current. It saturates at low temperature due to quantum fluctuations

Origin of the fluctuating critical current: The phase variable needs to escape “prematurely” in order to give nonzero fluctuations of the switching current. This escape can happen due to thermal fluctuations or by quantum tunneling



$$\omega_{p0} = (2\pi I_0 / \Phi_0 C)^{1/2} \quad \omega_p = \omega_{p0} [1 - (I/I_0)^2]^{1/4} \quad Q = \omega_p RC$$

Thermal escape- Arrhenius Law:

$$\Gamma_t = a_t (\omega_p / 2\pi) \exp(-\Delta U / k_B T) ,$$

FIG. 2. Potential well from which particle escapes.

the presence of a moderate level of dissipation, Caldeira and Leggett⁴ have shown that for a cubic potential²⁴

$$\Gamma_q = a_q \frac{\omega_p}{2\pi} \exp \left[-7.2 \frac{\Delta U}{\hbar \omega_p} \left[1 + \frac{0.87}{Q} + \dots \right] \right] , \quad (2.8)$$

where

$$a_q \approx [120\pi(7.2\Delta U / \hbar \omega_p)]^{1/2} . \quad (2.9)$$

Useful Expression for the Free Energy of a Phase Slip

“Arrhenius-Little” formula for the wire resistance:

$$R_{AL} \approx R_N \exp[-\Delta F(T)/k_B T]$$

$$\Delta F = (8\sqrt{2}/3)(H_c(T)^2/8\pi)(A\xi(T))$$

$$\frac{\Delta F(0)}{k_B T_c} = \sqrt{6} \frac{\hbar I_c(0)}{2ek_B T_c} = 0.83 \frac{R_q L}{R_n \xi(0)} = 0.83 \frac{R_q}{R_{\xi(0)}}$$

Quantum limit to phase coherence in thin superconducting wires

M. Tinkham^{a)} and C. N. Lau

Physics Department, Harvard University, Cambridge, Massachusetts 02138



Leggett's prediction for macroscopic quantum tunneling (MQT) in SQUIDs

80

Supplement of the Progress of Theoretical Physics, No. 69, 1980

Macroscopic Quantum Systems and the Quantum Theory of Measurement

A. J. LEGGETT

*School of Mathematical and Physical Sciences
University of Sussex, Brighton BN1 9QH*

(Received August 27, 1980)

It is this property which makes a SQUID the most promising candidate to date for observing macroscopic quantum tunnelling; if it should ever become possible to observe macroscopic quantum *coherence*, the low entropy and consequent lack of dissipation will be absolutely essential.²¹⁾



MQT report by Kurkijarvi and collaborators (1981)

VOLUME 47, NUMBER 9

PHYSICAL REVIEW LETTERS

31 AUGUST 1981

Decay of the Zero-Voltage State in Small-Area, High-Current-Density Josephson Junctions

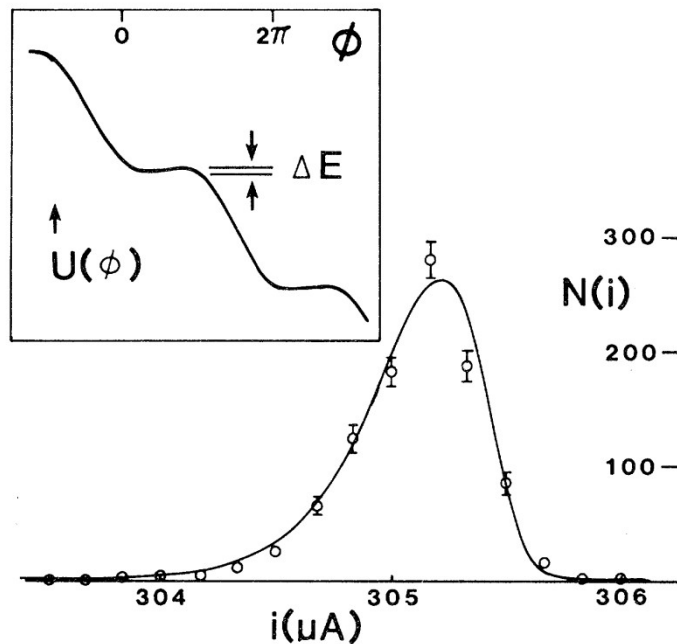


FIG. 1. Measured distribution for $T = 1.6$ K for small high-current-density junction. The solid line is a fit by the CL theory for $R = 20 \Omega$, $C = 8$ fF, and $i_{\text{CFF}} = 310.5 \mu\text{A}$. The inset is $U(\phi)$ for $x = 0.8$ with barrier ΔE .

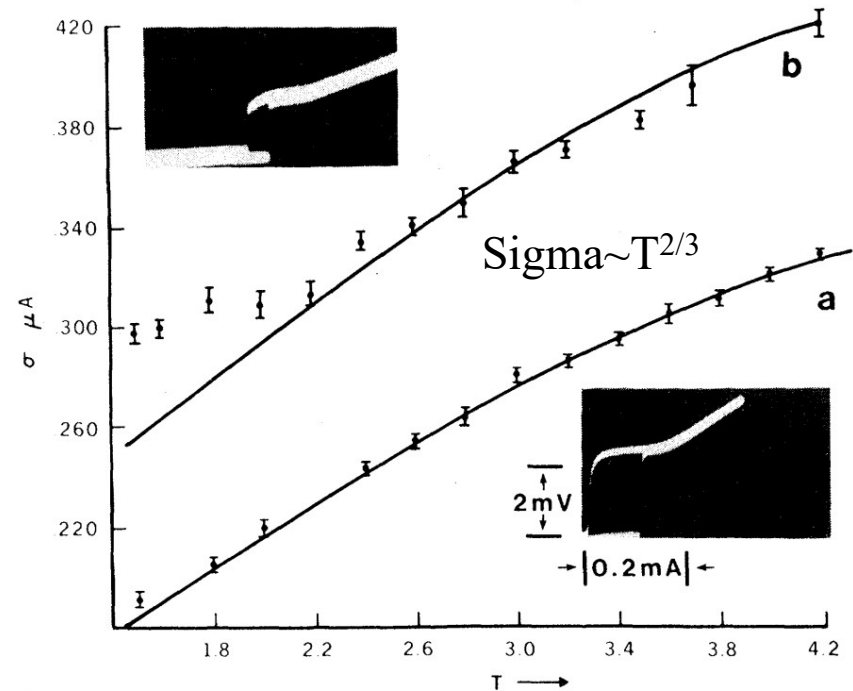


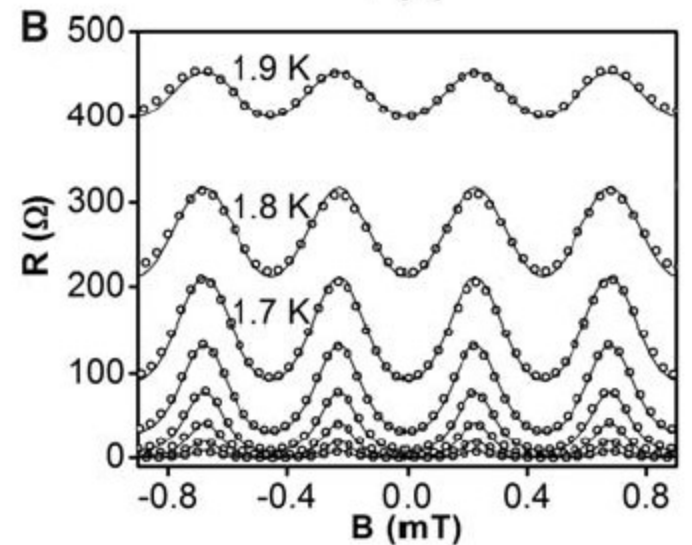
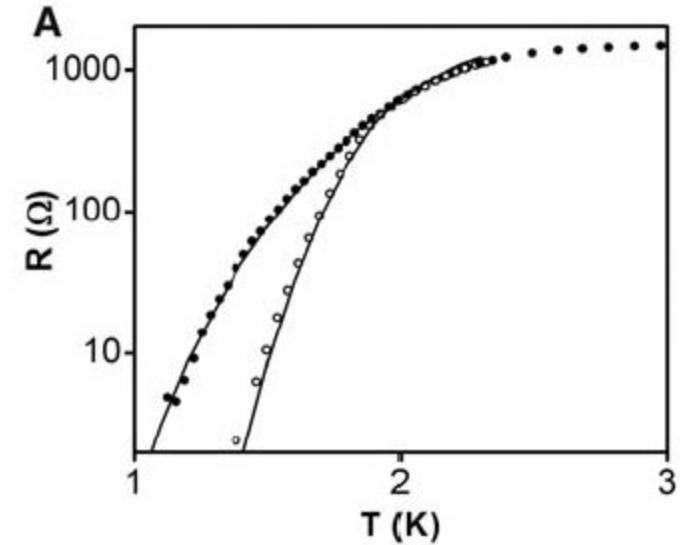
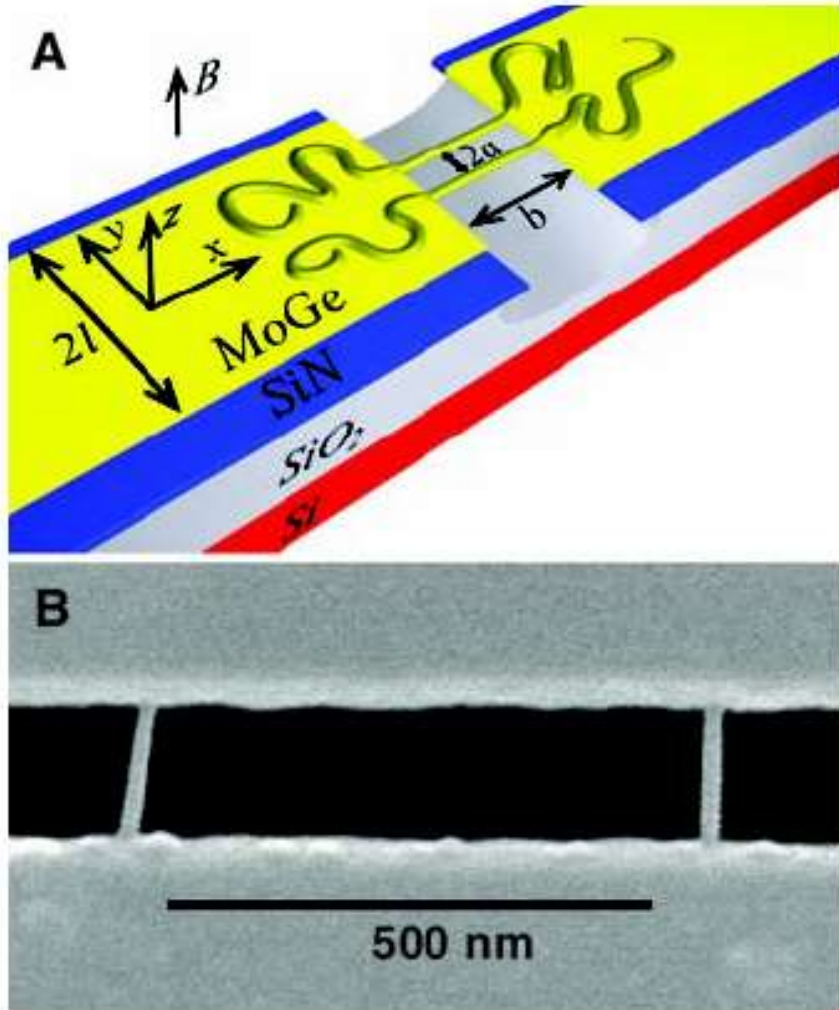
FIG. 2. Measured distribution widths σ vs T for two junctions with current sweep of $\sim 400 \mu\text{A}/\text{sec}$. Curve a is lower current density junction data and curve b is higher density junction data. The traces adjacent to the plots are the corresponding $I-V$ characteristics at 4.2 K. The scales are the same for both traces.



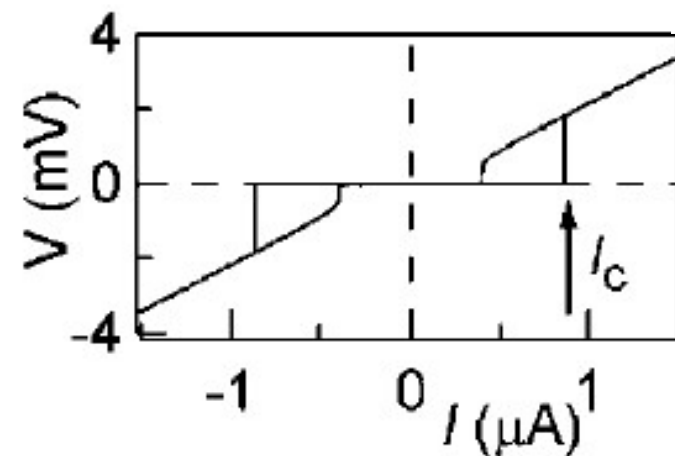
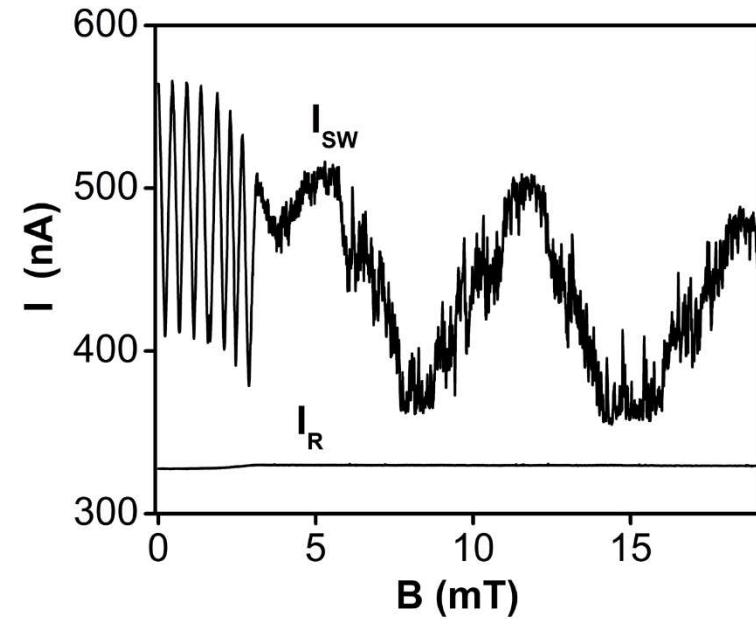
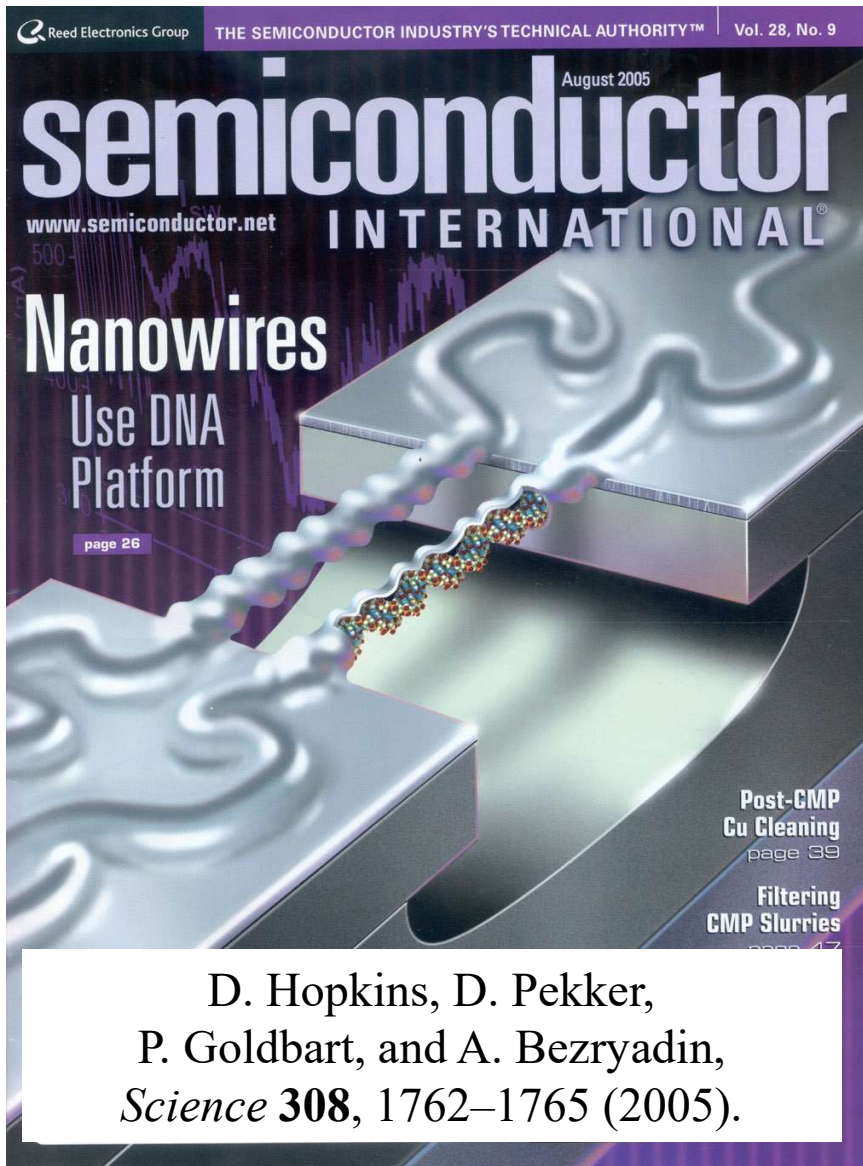
What determines the period of oscillation?

(A simple guess for the period would be $\Delta B \sim \Phi_0/2ab$.

This prediction deviates from the result by a factor 100!)

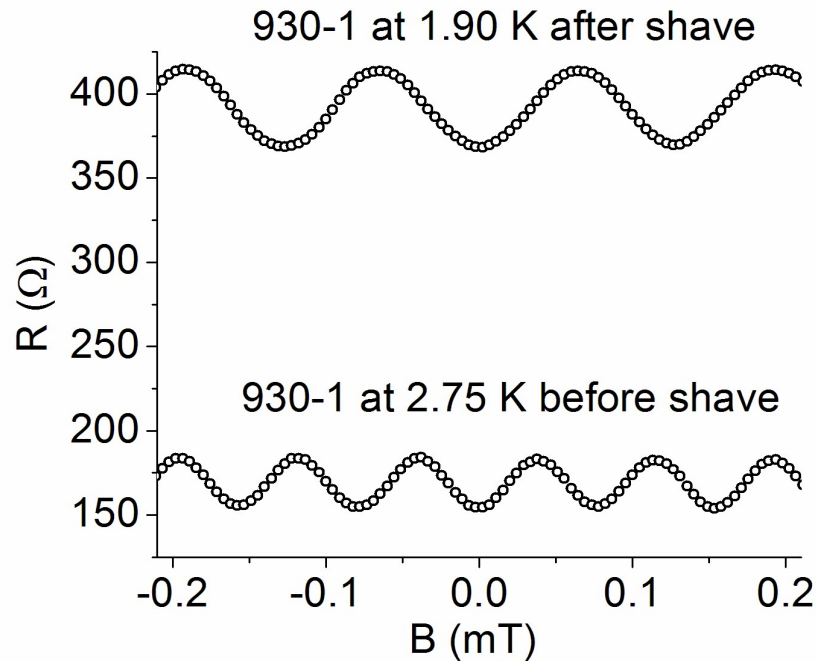


Phase gradiometers templated by DNA



Little-Parks effect.

The period of the oscillation is inversely proportional to the width of the electrodes



The width of the leads was changed from 14480 nm to 8930 nm

The period changed from 77.5 μT to 128 μT

usual SQUID estimate:

$$Period = \frac{\Phi_0}{2ab} \sim 10mT$$

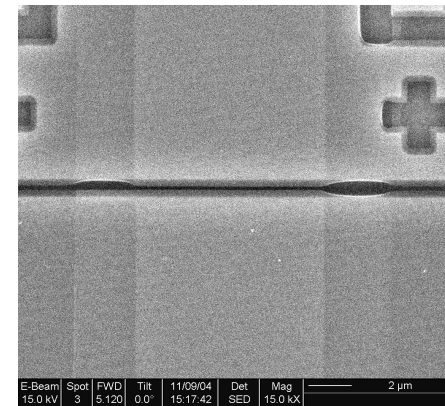
here $2a$ -distance between the wires;

b - length of wires

Correct field period:

$$\Delta B = \frac{\pi^2 \Phi_0}{8G 4al}$$

here $2l$ - the width of the leads



$G = .916$ is the Catalan number

SQUID – superconducting quantum interference device

SQUID helmet project at Los Alamos



Magnetic field scales:

Earth field: $\sim 1\text{G}$

Fields inside animals:
 $\sim 0.01\text{G}-0.00001\text{G}$

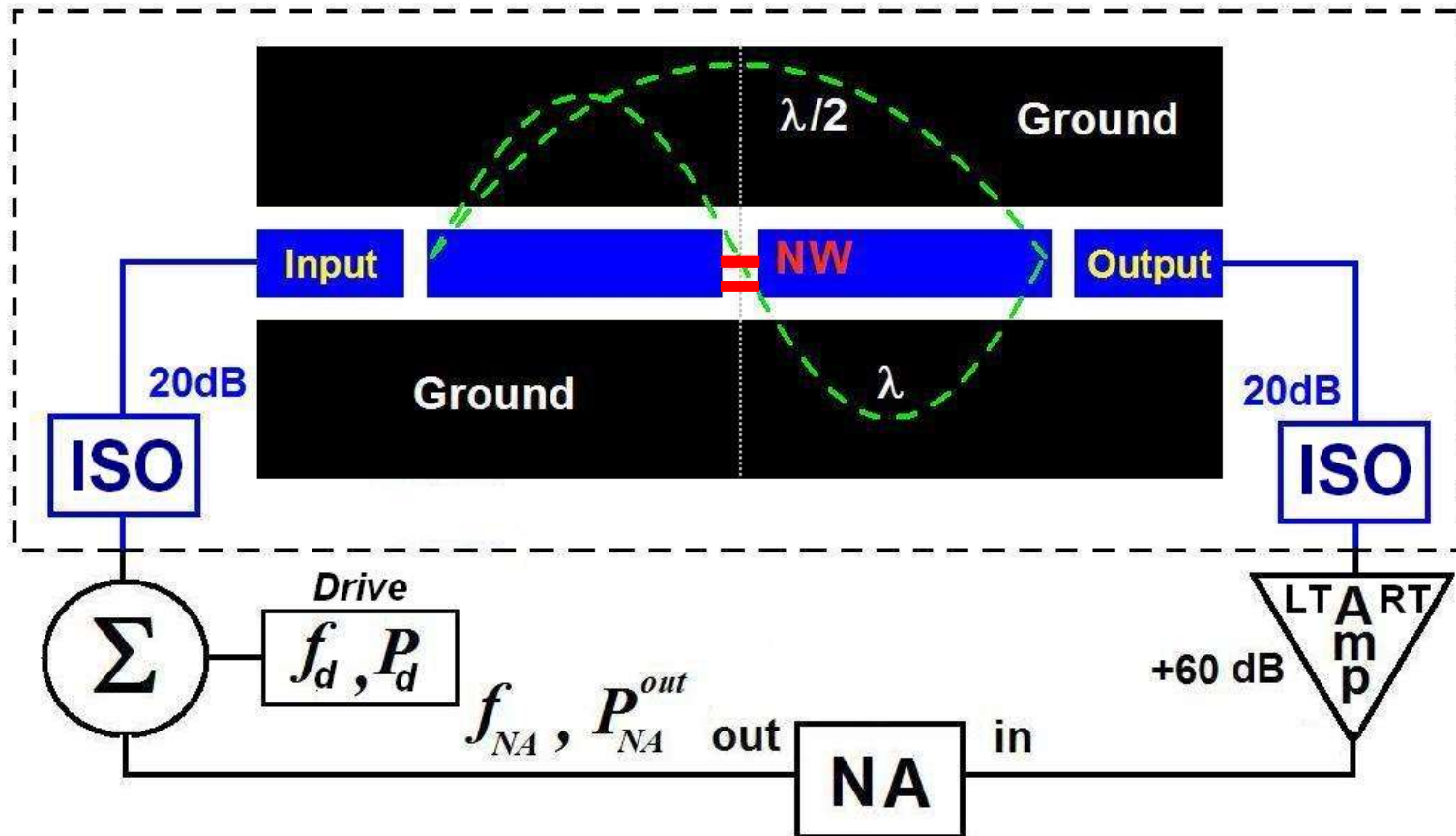
Fields on the **human brain**:
 $\sim 0.3\text{nG}$

This is less than a hundred-millionth of the Earth's magnetic field.

SQUIDs, or Superconducting Quantum Interference Devices, invented in 1964 by Robert Jaklevic, John Lambe, Arnold Silver, and James Mercereau of Ford Scientific Laboratories, are used to measure extremely small magnetic fields. They are currently the most sensitive magnetometers known, with the noise level as low as $3\text{ fT}\cdot\text{Hz}^{-1/2}$. While, for example, the Earth magnet field is only about 0.0001 Tesla, some electrical processes in animals produce very small magnetic fields, typically between 0.000001 Tesla and 0.000000001 Tesla. SQUIDs are especially well suited for studying magnetic fields this small.

Measuring the brain's magnetic fields is even much more difficult because just above the skull the strength of the magnetic field is only about 0.3 picoTesla (0.00000000000003 Tesla). This is less than a hundred-millionth of Earth's magnetic field. In fact, brain fields can be measured only with the most sensitive magnetic-field sensor, i.e. with the superconducting quantum interference device, or SQUID.

Measuring nanowires within GHz resonators. Detection of individual phase slips.

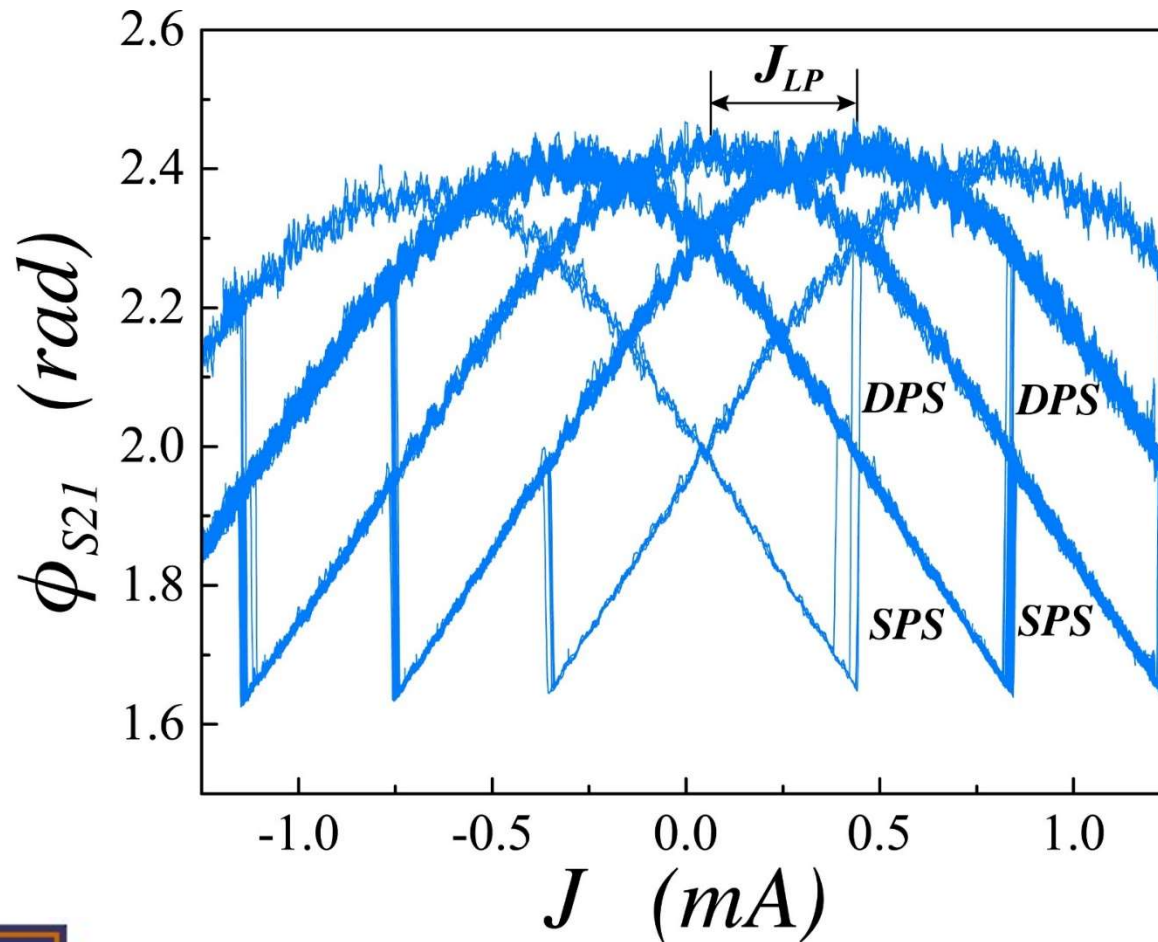


A. Belkin et al, *Appl. Phys. Lett.* **98**, 242504 (2011)
 Ku, J., Manucharyan, V., and
 Bezryadin, A. (2010) *Phys. Rev. B*, **82**, 134518.



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Resonators used to detect single phase slips (SPS) and double phase slips (DPS)



$T = 360$ mK
 $f = f_0(H=0)$

A. Belkin et al, PRX **5**, 021023 (2015)



Conclusions

- Superconductivity is fun and very useful for modern technology and even for quantum information processing (e.g., using futuristic superconducting quantum computers)



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