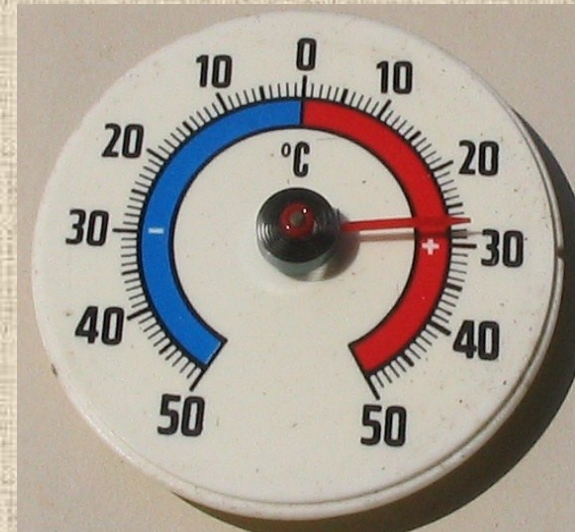


# Temperature. Sensors. Measuring technique.

*Eugene V. Colla*



# Outline

**Temperature Sensors**

**Measuring equipment and ideas**

**Sensor calibration**

**Temperature scales**

# Notcontacting devices:

# Pyrometers



Jožef Stefan  
(1835-1893)



Ludwig Eduard Boltzmann  
(1844-1906)

Stefan-Boltzmann law

$$P = e\sigma AT^4$$

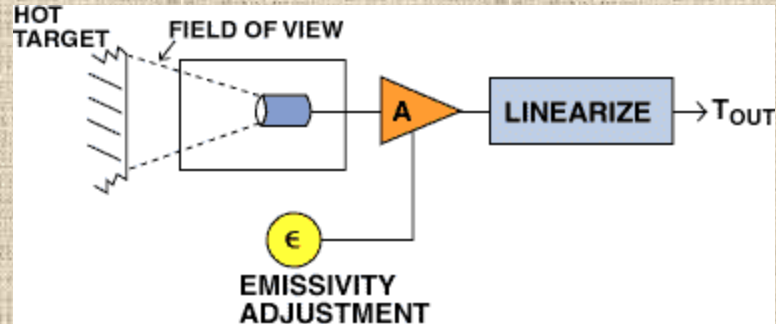
$e$  – emissivity;

$\sigma$  - Stefan-Boltzmann constant

( $\sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$ )

$A$  - surface area

$T$  - temperature



OS643



Range C°  
0÷260



Extech  
42545

Range C°  
-50÷1000



Range C°  
-40÷500

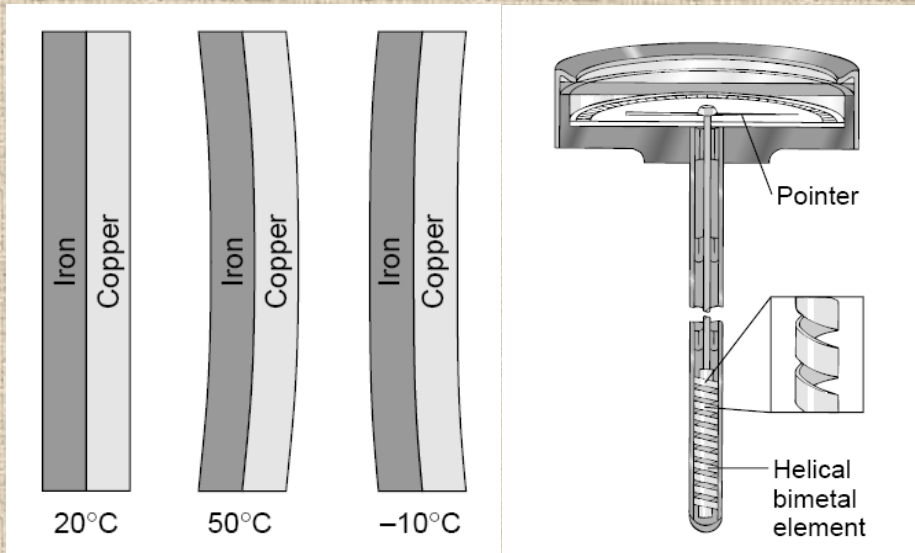
Extech  
42580

# Contacting devices: Bi-Metal Thermometers



Typical temperature range  
 $-10^{\circ}\text{C} \div 200^{\circ}\text{C}$

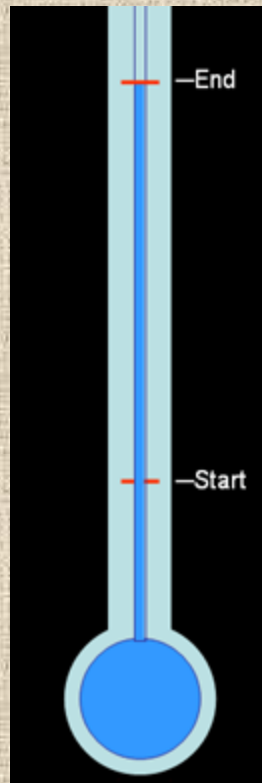
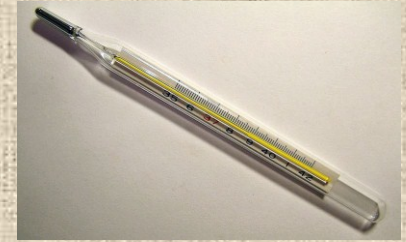
- Very cheap
- No electronics
- Easy to use
- Moderate precision ( $\pm 1\%$  from full scale)



# Contacting devices: Volume Expansion Thermometer

$$\Delta V = V \beta \Delta T$$

$\beta$  –coefficient of volume expansion



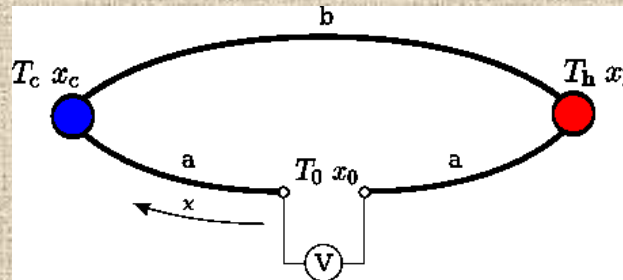
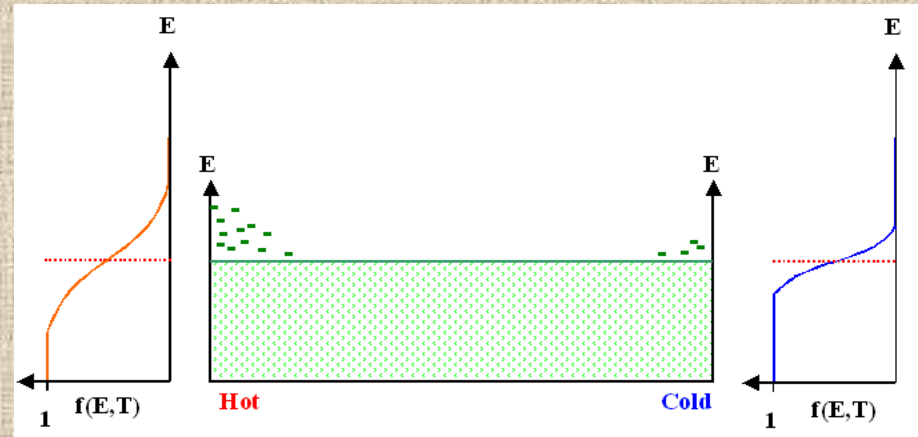
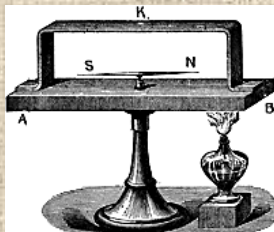
Average Expansion Coefficients for Some Materials Near Room Temperature

| Material            | Average Coefficient<br>of Linear Expansion<br>( $\alpha$ ) ( $^{\circ}\text{C}^{-1}$ ) | Material                                | Average Coefficient<br>of Volume Expansion<br>( $\beta$ ) ( $^{\circ}\text{C}^{-1}$ ) |
|---------------------|----------------------------------------------------------------------------------------|-----------------------------------------|---------------------------------------------------------------------------------------|
| Aluminum            | $24 \times 10^{-6}$                                                                    | Acetone                                 | $1.5 \times 10^{-4}$                                                                  |
| Brass and bronze    | $19 \times 10^{-6}$                                                                    | Alcohol, ethyl                          | $1.12 \times 10^{-4}$                                                                 |
| Copper              | $17 \times 10^{-6}$                                                                    | Benzene                                 | $1.24 \times 10^{-4}$                                                                 |
| Glass (ordinary)    | $9 \times 10^{-6}$                                                                     | Gasoline                                | $9.6 \times 10^{-4}$                                                                  |
| Glass (Pyrex)       | $3.2 \times 10^{-6}$                                                                   | Glycerin                                | $4.85 \times 10^{-4}$                                                                 |
| Lead                | $29 \times 10^{-6}$                                                                    | Mercury                                 | $1.82 \times 10^{-4}$                                                                 |
| Steel               | $11 \times 10^{-6}$                                                                    | Turpentine                              | $9.0 \times 10^{-4}$                                                                  |
| Invar (Ni-Fe alloy) | $0.9 \times 10^{-6}$                                                                   | Air <sup>a</sup> at $0^{\circ}\text{C}$ | $3.67 \times 10^{-3}$                                                                 |
| Concrete            | $12 \times 10^{-6}$                                                                    | Helium <sup>a</sup>                     | $3.665 \times 10^{-3}$                                                                |

# Contacting devices: Seebeck Effect. Thermocouples



**Thomas Johann Seebeck**  
(1770-1831)



$$S = \frac{dU}{dT}$$

$$U_S = \int_{T_0}^{T_c} S_A dT + \int_{T_c}^{T_H} S_B dT + \int_{T_H}^{T_0} S_A dT = \int_{T_c}^{T_H} (S_B - S_A) dT$$

**S -Seebeck coefficient**

# Contacting devices: Seebeck Effect. Thermocouples

## Seebeck coefficients

| Material   | Seebeck Coeff. * | Material  | Seebeck Coeff. * | Material  | Seebeck Coeff. * |
|------------|------------------|-----------|------------------|-----------|------------------|
| Aluminum   | 3.5              | Gold      | 6.5              | Rhodium   | 6.0              |
| Antimony   | 47               | Iron      | 19               | Selenium  | 900              |
| Bismuth    | -72              | Lead      | 4.0              | Silicon   | 440              |
| Cadmium    | 7.5              | Mercury   | 0.60             | Silver    | 6.5              |
| Carbon     | 3.0              | Nichrome  | 25               | Sodium    | -2.0             |
| Constantan | -35              | Nickel    | -15              | Tantalum  | 4.5              |
| Copper     | 6.5              | Platinum  | 0                | Tellurium | 500              |
| Germanium  | 300              | Potassium | -9.0             | Tungsten  | 7.5              |

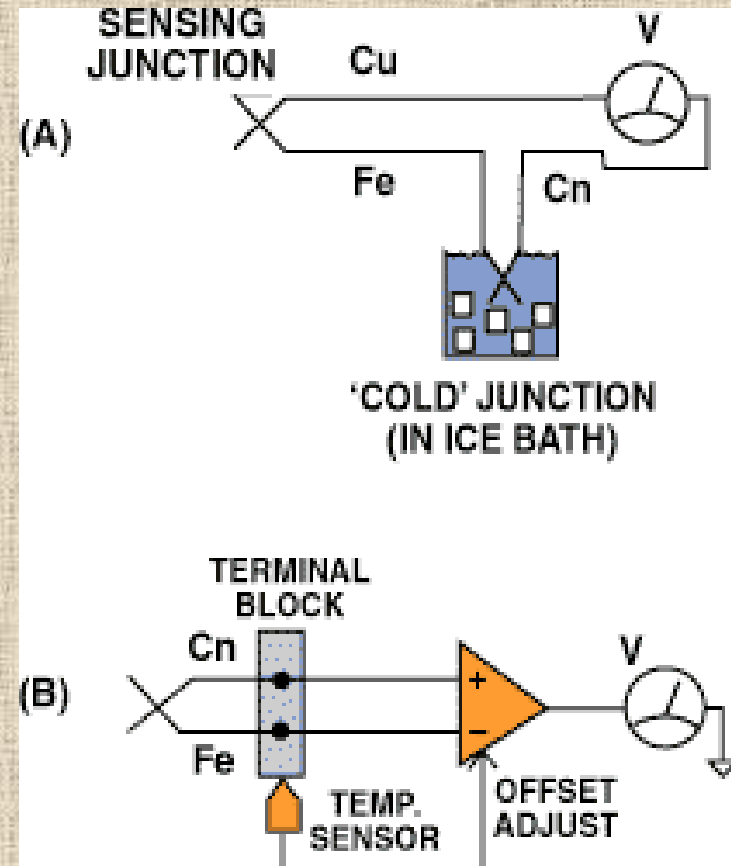
\*: Units are  $\mu\text{V}/^\circ\text{C}$ ; all data provided at a temperature of  $0^\circ\text{C}$

Type T (copper-constantan) has thermoemf at  $0^\circ\text{C}$   $41.5\mu\text{V}/^\circ\text{C}$ ;

## Contacting devices:

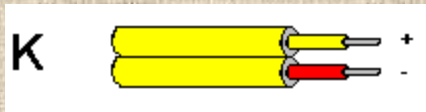
| Thermocouple Type | Names of Materials                                             | Useful Application Range  |
|-------------------|----------------------------------------------------------------|---------------------------|
| <b>B</b>          | Platinum30% Rhodium (+)<br>Platinum 6% Rhodium (-)             | 2500 -3100F<br>1370-1700C |
| <b>C</b>          | W5Re Tungsten 5% Rhenium (+)<br>W26Re Tungsten 26% Rhenium (-) | 3000-4200F<br>1650-2315C  |
| <b>E</b>          | Chromel (+)<br>Constantan (-)                                  | 200-1650F<br>95-900C      |
| <b>J</b>          | Iron (+)<br>Constantan (-)                                     | 200-1400F<br>95-760C      |
| <b>K</b>          | Chromel (+)<br>Alumel (-)                                      | 200-2300F<br>95-1260C     |
| <b>N</b>          | Nicrosil (+)<br>Nisil (-)                                      | 1200-2300F<br>650-1260C   |
| <b>R</b>          | Platinum 13% Rhodium (+)<br>Platinum (-)                       | 1600-2640F<br>870-1450C   |
| <b>S</b>          | Platinum 10% Rhodium (+)<br>Platinum (-)                       | 1800-2640F<br>980-1450C   |
| <b>T</b>          | Copper (+)<br>Constantan (-)                                   | -330-660F<br>-200-350C    |

## Thermocouples

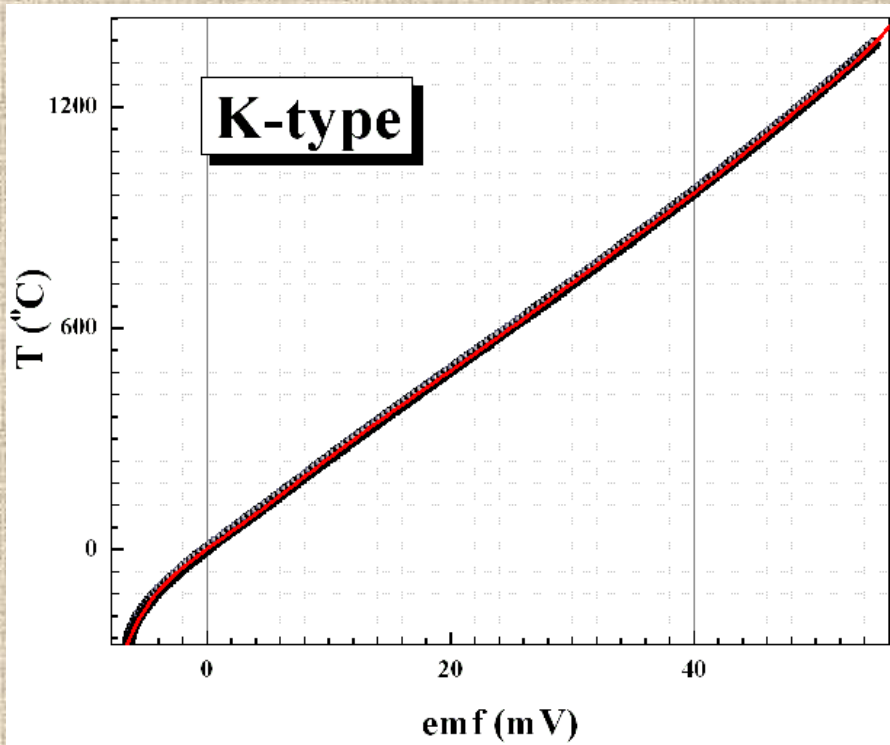


# Contacting devices:

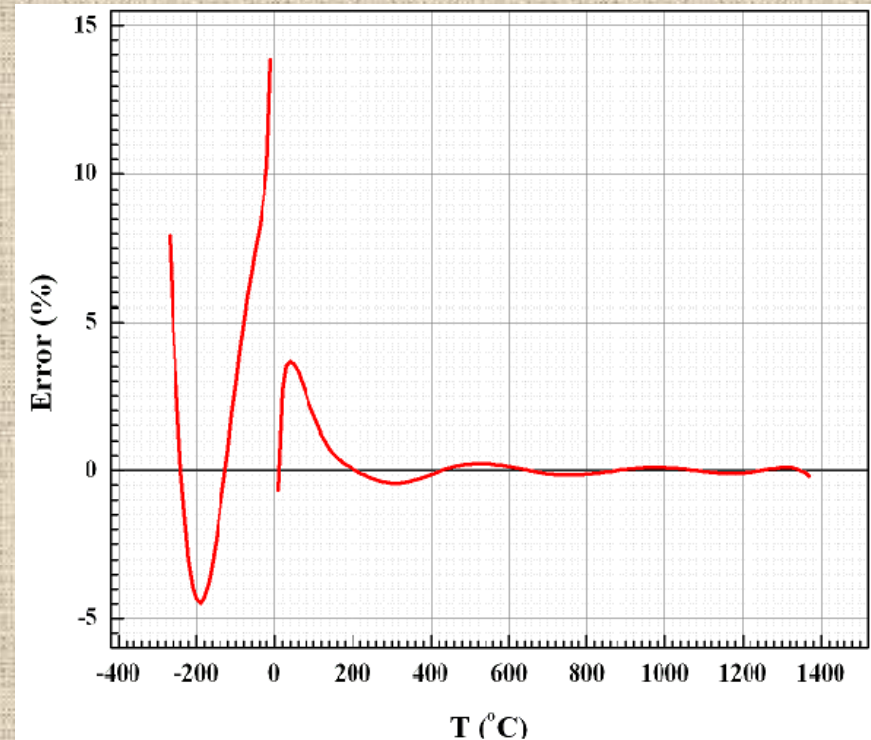
emf (T) dependence



# Thermocouples



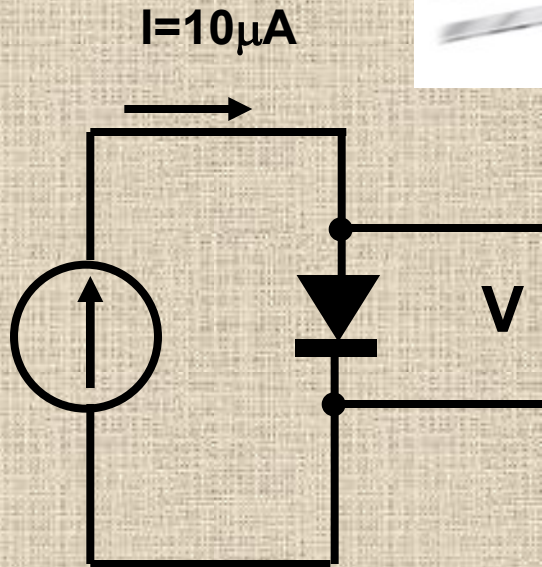
9<sup>th</sup> order polynomial fit



To reduce the error we have to split the temperature range in to a couple of segments

# Contacting devices:

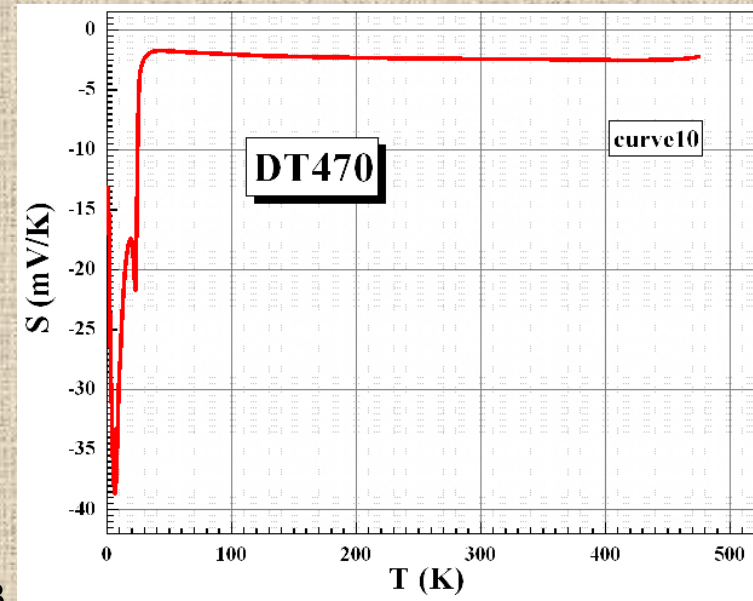
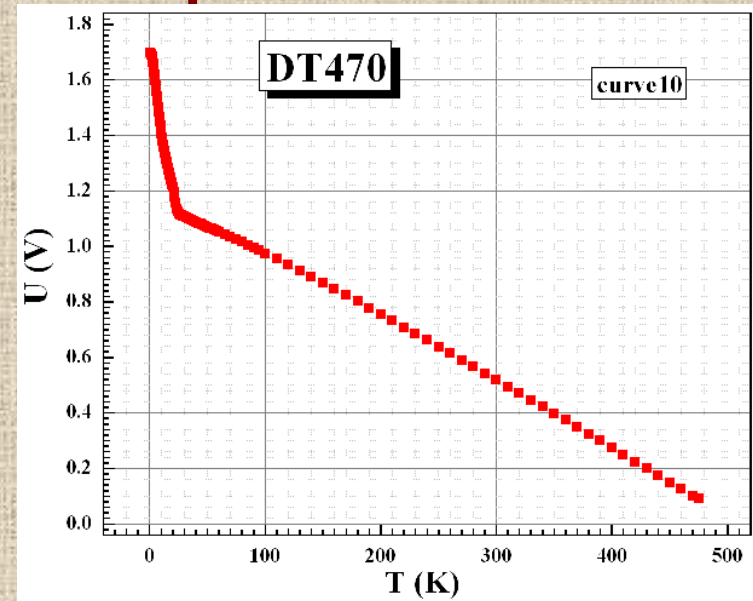
LakeShore



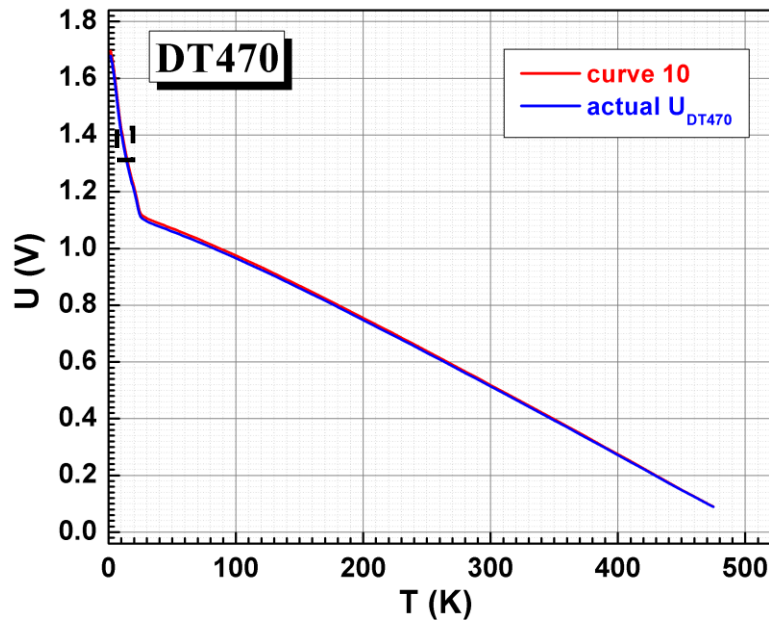
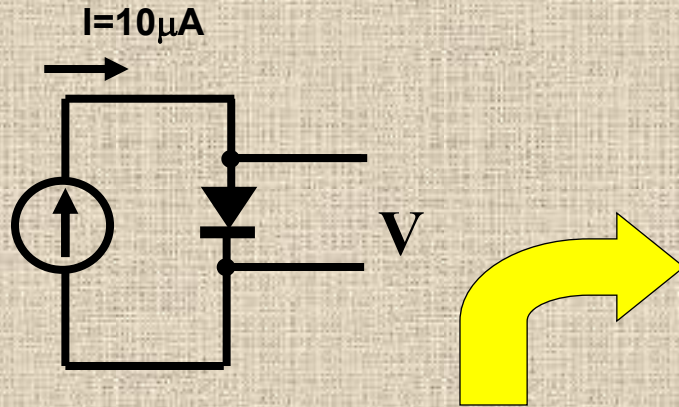
## DT-470-SD Features:

1. Monotonic temperature response from 1.4 K to 500 K.
2. Conformance to standard Curve 10 temperature response curve
3. Useful above 60 K in magnetic fields up to 5 T

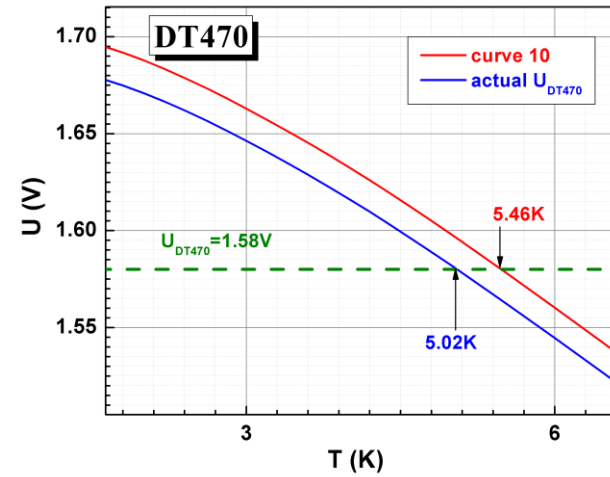
## p-n diodes



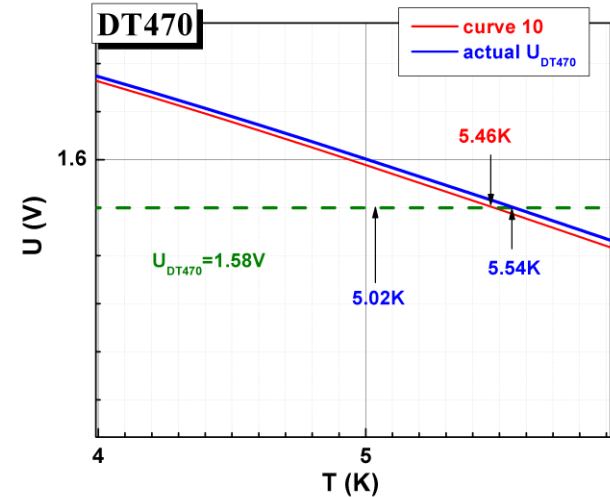
# Silicon diode DT470



# Calibration problems

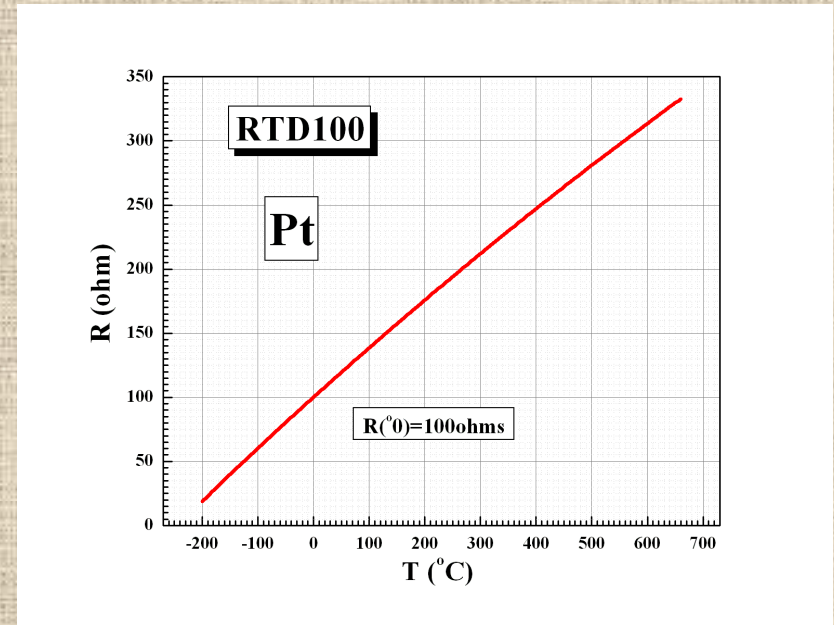
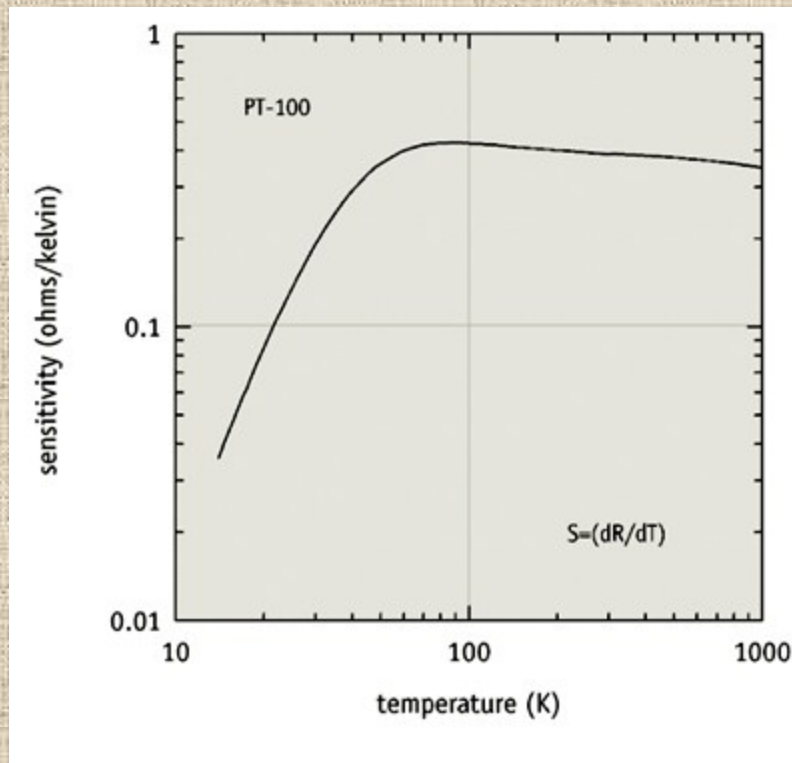


$$U^* = U_{DT470} \cdot k$$



# Contacting devices:

# Resistance Temperature Detectors

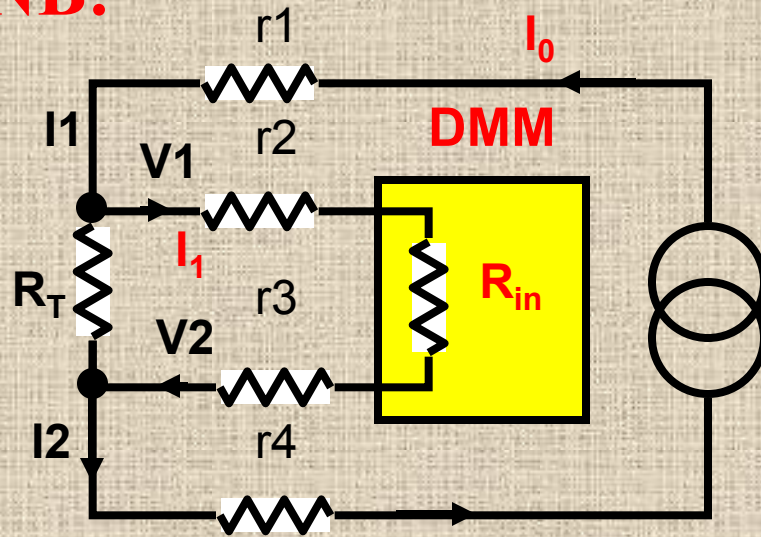


## RTD Features:

1. Temperature range: 14 K to 873 K
2. High reproducibility:  $\pm 5$  mK at 77 K
3. Low magnetic field dependence above 40 K
4. Excellent for use in ionizing radiation

## Measuring issue:

**NB!**



If the sensor is mounted in cryostat the overall leads resistance could reach a couple of ohms. This will In case of RTD100 the resistance at 0°C is 100Ω give an error of a couple percent!

## Four probe technique



Most of DMM's have four probe option for resistance measurements.

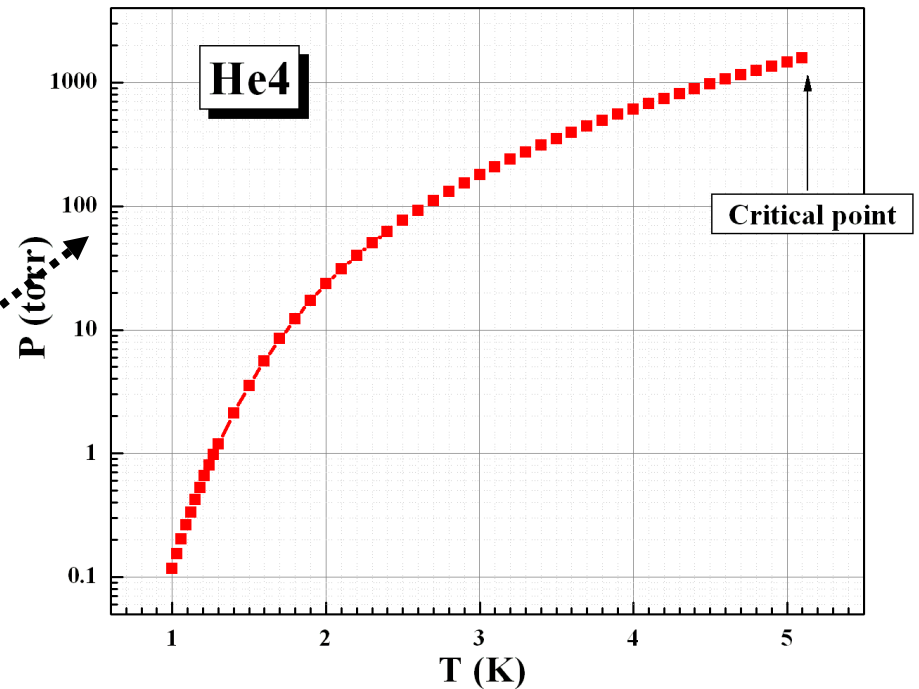
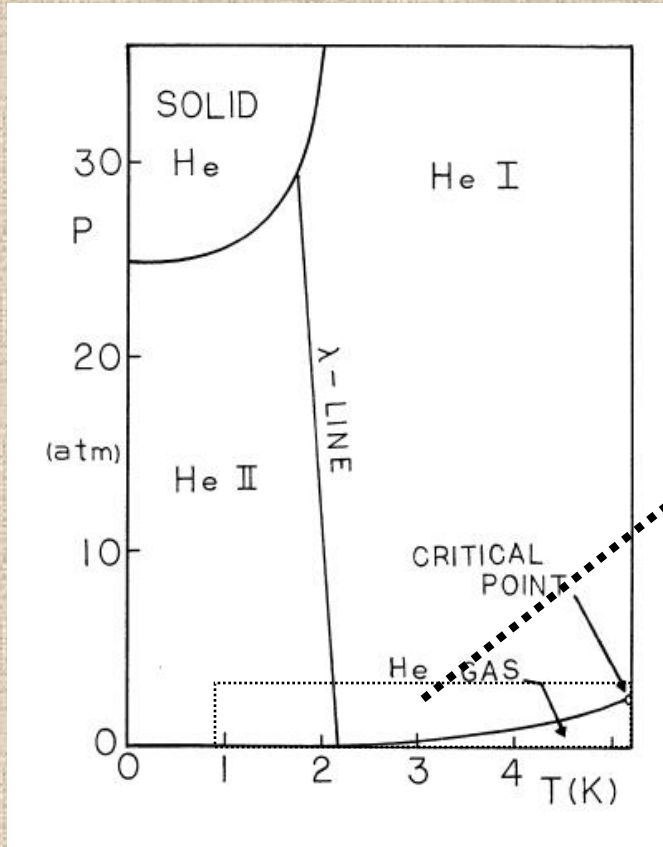
$$I_1 = I_0 * R_T / (r_2 + r_3 + R_{in}) \sim 0$$

$$R_{in} \sim 10^{10} \Omega$$

# Vapor Pressure Thermometry

## He4 P-T phase diagram

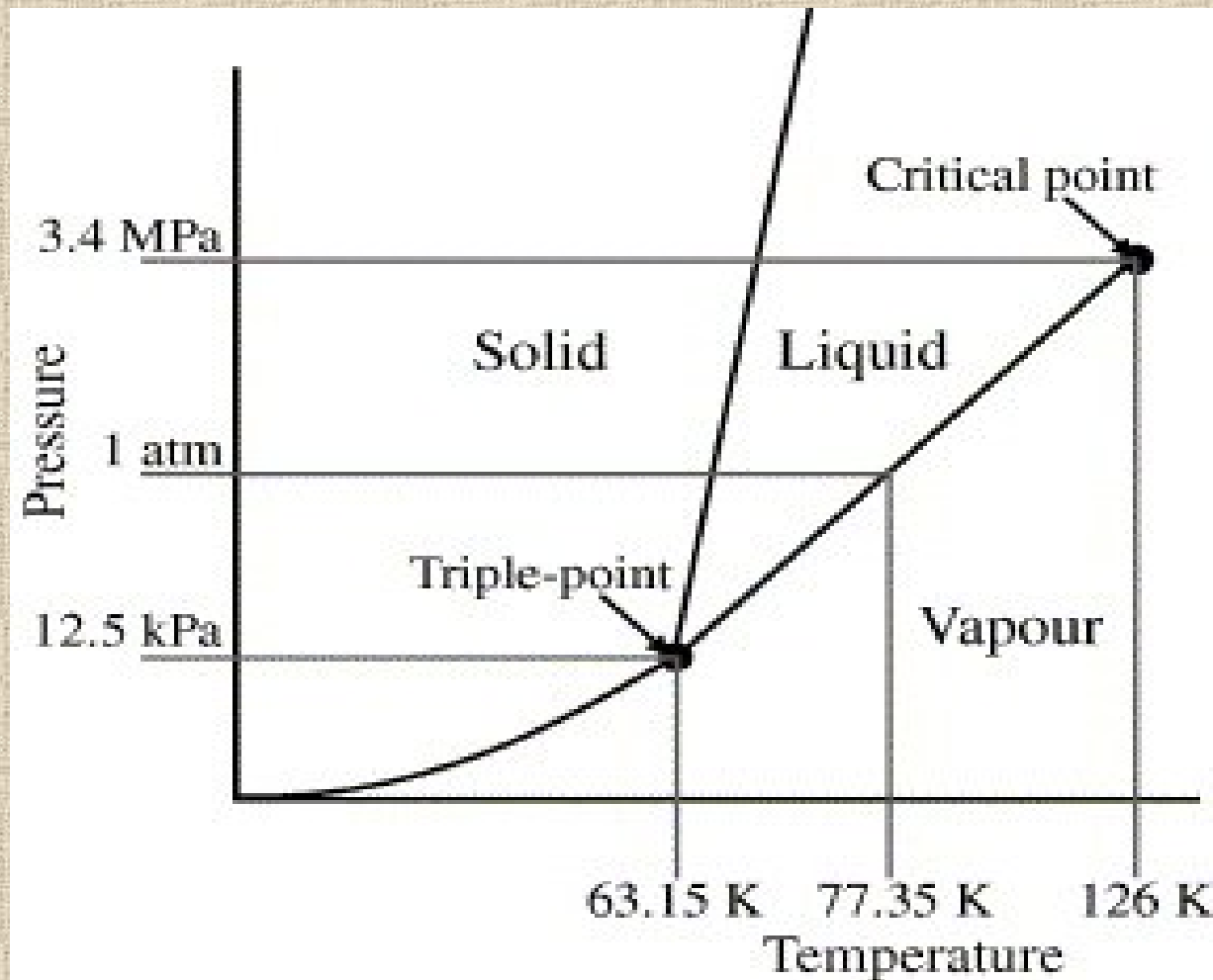
$$T_{90}/K = A_0 + \sum_{i=1}^9 A_i [(\ln(p/\text{Pa}) - B)/C]^i. \quad (3)$$



**Critical point of He4 T=5.19K ,P= 0.227 MPa**

# Vapor Pressure Thermometry

## Nitrogen P-T phase diagram



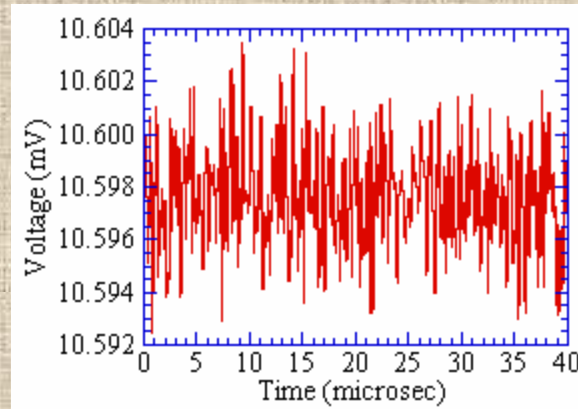
# Some more exotic techniques of measuring the temperature



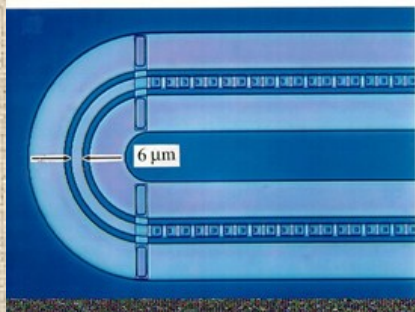
**John Bertrand Johnson**  
(1887–1970)

## Johnson–Nyquist noise Thermometry

$$S^R = 4kTR(T)$$



**Harry Nyquist**  
(1889–1976)



2004 IEEE Aerospace Conference Proceedings

### Johnson Noise Thermometry for Harsh Environments

R. Kisner<sup>1</sup>, C. L. Britton<sup>1,2</sup>, U. Jagadish<sup>1</sup>, J. B. Wilgen<sup>1</sup>, M. Roberts<sup>2</sup>, T. V. Blalock<sup>2,3</sup>, D. Holcomb<sup>1</sup>,  
M. Bohrek<sup>1,2</sup>, M. N. Ericson<sup>1,2</sup>

<sup>1</sup>Oak Ridge National Laboratory, MS6006, Oak Ridge, TN 37831-6006, BRITTONCL@ornl.gov

<sup>2</sup>Dept. of Electrical and Computer Engineering, The University of Tennessee, Knoxville TN

<sup>3</sup>Deceased

Courtesy by NIST

3/9/2012

Physics 403

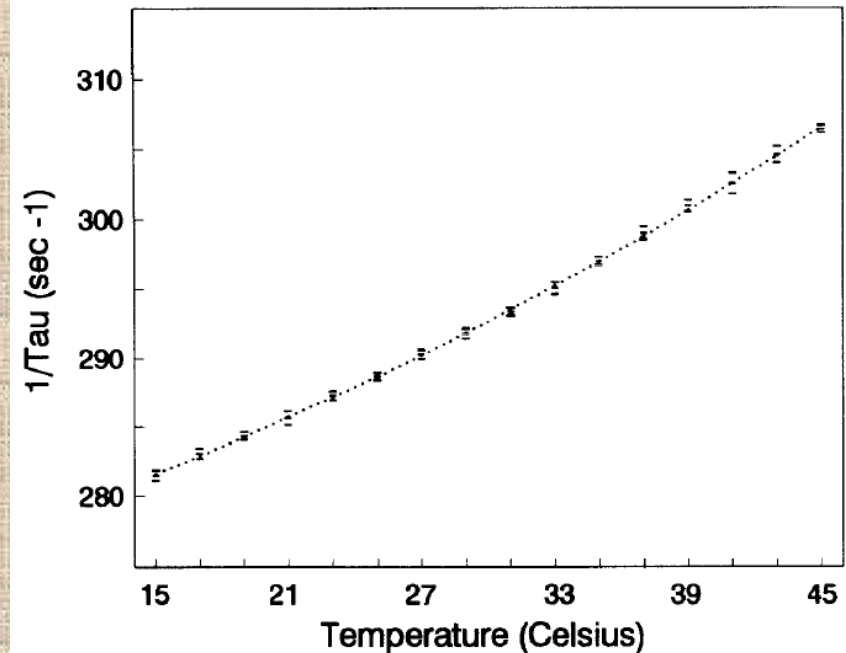
16

## Some more exotic techniques of measuring the temperature

### Real time frequency domain fibreoptic temperature sensor using ruby crystals

J. R. Alcala, S-C. Liao and J. Zheng

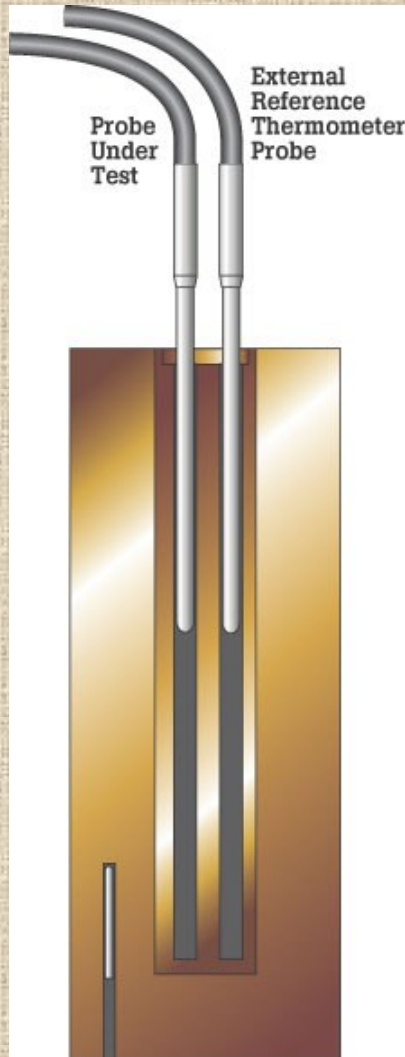
Department of Biomedical Engineering, Case Western Reserve University,  
Cleveland, OH 44106, USA



The use of optical methods, to invasively measure temperature, offers the advantage of electrical isolation, when compared to the traditional use of electronic thermometers. In some instances, optical techniques are necessary as in the case of clinical radio-frequency heat treatment, where interference from electromagnetic fields makes electronic thermometers unreliable. Optical tem-

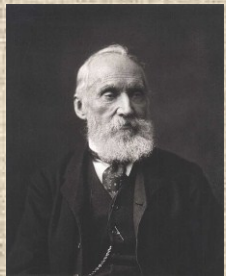
# Sensors Calibration

**Official list of a fixed temperature points recommended for sensor calibration (ITS-90)**



| Temperature<br>$T_{90}/\text{K}$ | Temperature<br>$t_{90}/^{\circ}\text{C}$ | Substance                | State                    |
|----------------------------------|------------------------------------------|--------------------------|--------------------------|
| from 3 to 5                      | from - 270,15<br>to - 268,15             | He - Helium              | Saturated vapor pressure |
| 83,805 8                         | - 189,344 2                              | Ar - Argon               | Triple point             |
| 234,315 6                        | - 38,834 4                               | Hg - Mercury             | Triple point             |
| 273,16                           | 0,01                                     | H <sub>2</sub> O - Water | Triple point             |
| 302,914 6                        | 29,764 6                                 | Ga - Gallium             | Melting point            |
| 429,748 5                        | 156,598 5                                | In - Indium              | Solidification point     |
| 505,078                          | 231,928                                  | Sn - Tin                 | Solidification point     |
| 692,677                          | 419,527                                  | Zn - Zinc                | Solidification point     |
| 933,473                          | 660,323                                  | Al - Aluminium           | Solidification point     |
| 1 234,93                         | 961,78                                   | Ag - Silver              | Solidification point     |
| 1 337,33                         | 1 064,18                                 | Au - Gold                | Solidification point     |
| 1 357,77                         | 1 084,62                                 | Cu - Copper              | Solidification point     |

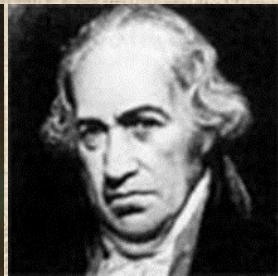
# Comparison of temperature scales



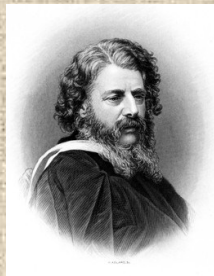
**Kelvin**



**Celsius**



**Fahrenheit**



**Rankine**



**Delisle**



**Newton**



**Réaumur**



**Rømer**

| <b>Comment</b>                                       | <b>Kelvin<br/>K</b> | <b>Celsius<br/>°C</b> | <b>Fahrenheit<br/>°F</b> | <b>Rankine<br/>°Ra (°R)</b> | <b>Delisle<br/>°D</b> | <b>Newton<br/>°N</b> | <b>Réaumur<br/>°R, (°Ré, °Re)</b> | <b>Rømer<br/>°Rø (°R)</b> |
|------------------------------------------------------|---------------------|-----------------------|--------------------------|-----------------------------|-----------------------|----------------------|-----------------------------------|---------------------------|
| <b>Absolute zero</b>                                 | <b>0</b>            | <b>−273.15</b>        | <b>−459.67</b>           | <b>0</b>                    | <b>559.725</b>        | <b>−90.14</b>        | <b>−218.52</b>                    | <b>−135.90</b>            |
| <b>Lowest recorded natural temperature on Earth</b>  | <b>184</b>          | <b>−89</b>            | <b>−128</b>              | <b>331</b>                  | <b>284</b>            | <b>−29</b>           | <b>−71</b>                        | <b>−39</b>                |
| <b>Water freezes (at standard pressure)</b>          | <b>273.15</b>       | <b>0</b>              | <b>32</b>                | <b>491.67</b>               | <b>150</b>            | <b>0</b>             | <b>0</b>                          | <b>7.5</b>                |
| <b>Average human body temperature <sup>2</sup></b>   | <b>310.0 ± 0.7</b>  | <b>36.8 ± 0.7</b>     | <b>98.2 ± 1.3</b>        | <b>557.9 ± 1.3</b>          | <b>94.8 ± 1.1</b>     | <b>12.1 ± 0.2</b>    | <b>29.4 ± 0.6</b>                 | <b>26.8 ± 0.4</b>         |
| <b>Highest recorded surface temperature on Earth</b> | <b>331</b>          | <b>58</b>             | <b>136</b>               | <b>596</b>                  | <b>63</b>             | <b>19</b>            | <b>46</b>                         | <b>38</b>                 |
| <b>Water boils (at standard pressure)</b>            | <b>373.13</b>       | <b>99.98</b>          | <b>211.97</b>            | <b>671.64</b>               | <b>0</b>              | <b>33</b>            | <b>80</b>                         | <b>60</b>                 |
| <b>Titanium melts</b>                                | <b>1941</b>         | <b>1668</b>           | <b>3034</b>              | <b>3494</b>                 | <b>−2352</b>          | <b>550</b>           | <b>1334</b>                       | <b>883</b>                |
| <b>The surface of the Sun</b>                        | <b>5800</b>         | <b>5526</b>           | <b>9980</b>              | <b>10440</b>                | <b>−8140</b>          | <b>1823</b>          | <b>4421</b>                       | <b>2909</b>               |

# Temperature scales: reference temperature points

| Temperature scale | Temperature point #1                    | Temperature point #2                                 | K to °X conversion                                                      |
|-------------------|-----------------------------------------|------------------------------------------------------|-------------------------------------------------------------------------|
| Rømer scale       | 0°Rø – temperature of freezing of brine | 60°Rø – temperature of boiling water                 | $[^{\circ}\text{Rø}] = ([\text{K}] - 273.15) \times \frac{21}{4} + 7.5$ |
| Réaumur scale     | 0°R – temperature of freezing water     | 80°R – temperature of boiling water                  | $[^{\circ}\text{Ré}] = ([\text{K}] - 273.15) \times \frac{4}{5}$        |
| Delisle scale     | 0°D - temperature of boiling water      | 150°D - temperature of freezing water                | $[^{\circ}\text{De}] = (373.15 - [\text{K}]) \times \frac{3}{2}$        |
| Rankine scale     | 0°Ra – absolute zero                    | 491.67°Ra temperature of water freezing. (1°Ra=1 °F) | $[^{\circ}\text{R}] = [\text{K}] \times \frac{9}{5}$                    |
| Fahrenheit scale  | 32 °F temperature of freezing water     | 212 °F temperature of boiling water                  | $[^{\circ}\text{F}] = [\text{K}] \times \frac{9}{5} - 459.67$           |
| Newton scale      | 0°N – temperature of freezing water     | 33°N – temperature of boiling water                  | $[^{\circ}\text{N}] = ([\text{K}] - 273.15) \times \frac{33}{100}$      |
| Celsius scale     | 0°C temperature of freezing water       | 100°C temperature of boiling water                   | $[^{\circ}\text{C}] = ([^{\circ}\text{R}] - 491.67) \times \frac{5}{9}$ |