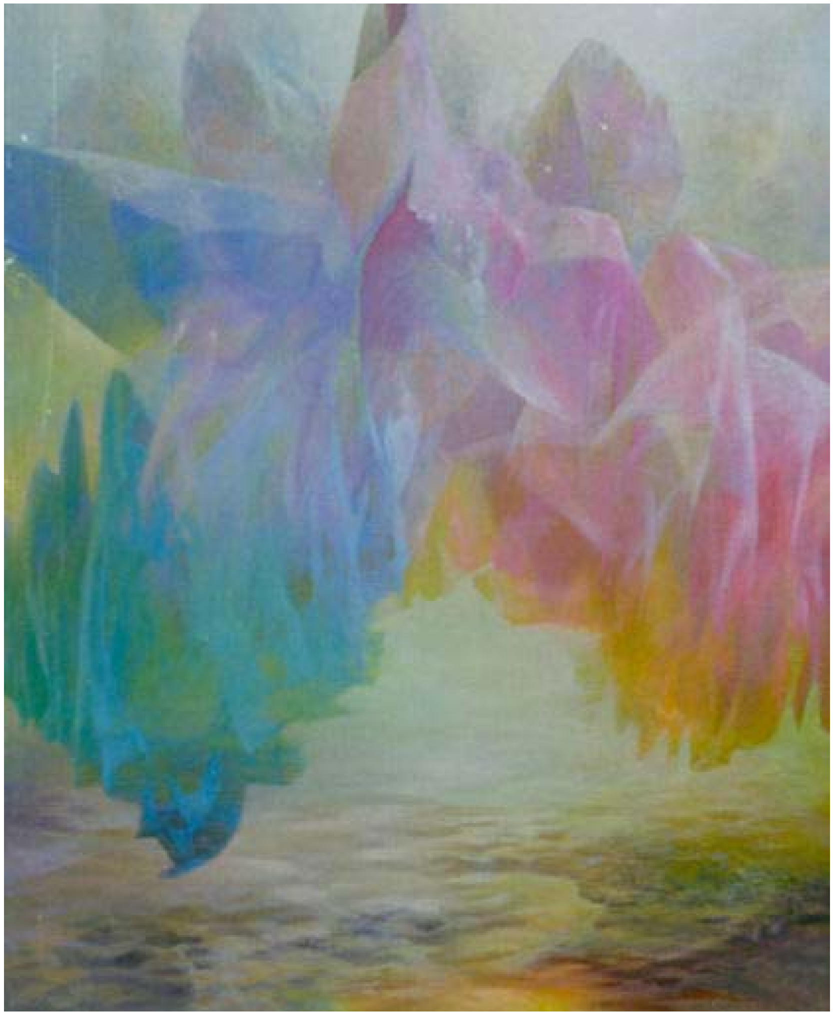
The Physics of Music & Musical Instruments



"Music of the Spheres"

Michail Spiridonov,

1997-98

Prof. Steven M. Errede, Department of Physics, UIUC, Urbana, IL

Aside from having much fun & joy teaching POM/MI {& much fun & joy learning much about acoustical physics} at UIUC for ~ past decade, in the process of doing this, many related questions of interest to me arose in my mind, for which I personally had no expertise, and hence initially had no answers for; nevertheless I was/am strongly motivated {driven?} to find/seek answers to them – I am after all, a physicist – we're profoundly interested in understanding causal relationships/connections…

I would like to share & discuss with you today some of these questions & {attempt to} present some answers to them – certainly by no means complete – am also hoping to interest/motivate *you* to think about them – collectively, hopefully progress can be made on answering them!

Q1: Why is music seeming *so* universally important to our species? Seems to be *genetically* imprinted in us! How did this come about, & why did this happen? Have you ever met anyone who absolutely *hates* music?

Q2: Why/how is it possible to remember entire albums {cd's} of music – even if I haven't played them for decades, playing them back in "real-time" in my head, hearing everything as clearly as if I am listening to them for real, when I can't remember the names of people that I've been introduced to at a party, ~ 5 nsec afterwards? ⇒ Music *must* have been very important to our species in ancient times, since musical memories are so robust!

Q3: Why did I always feel better after playing piano/violin, or going to Sunday school/church as a child {despite vigorous protestations to my parents aforehand…}? The same thing also happens now whenever I play music…

Q4: Our species *is* unique amongst the totality of life forms on this planet. We're the only ones who, apparently driven to learn/understand the universe in which we live, enabled us to master/control our environment.

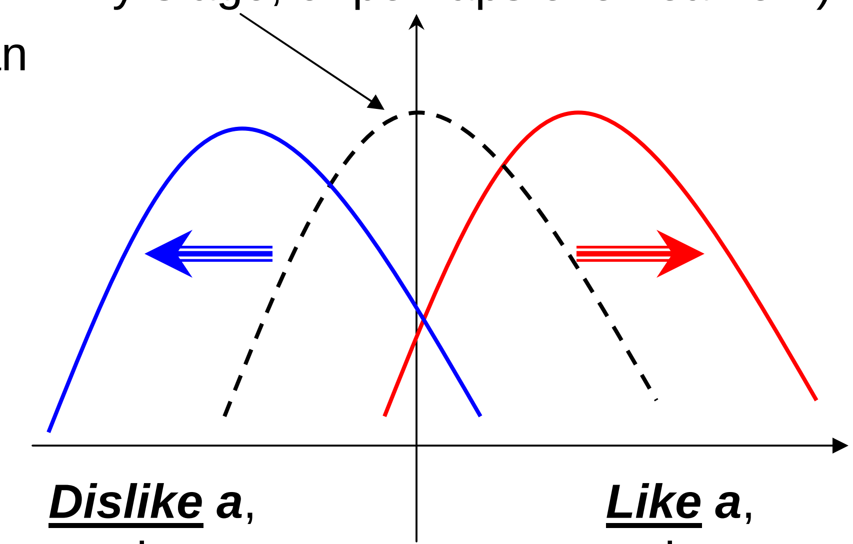
⇒ Did *music* {somehow} play an important role in enabling/facilitating us to get to where we are today?

Or is music just "*auditory cheesecake*" *e.g.* as *Steven Pinker* (1997) suggests…

Q5: If intelligent life exists elsewhere in the universe, did music also play a role in that life form's development?

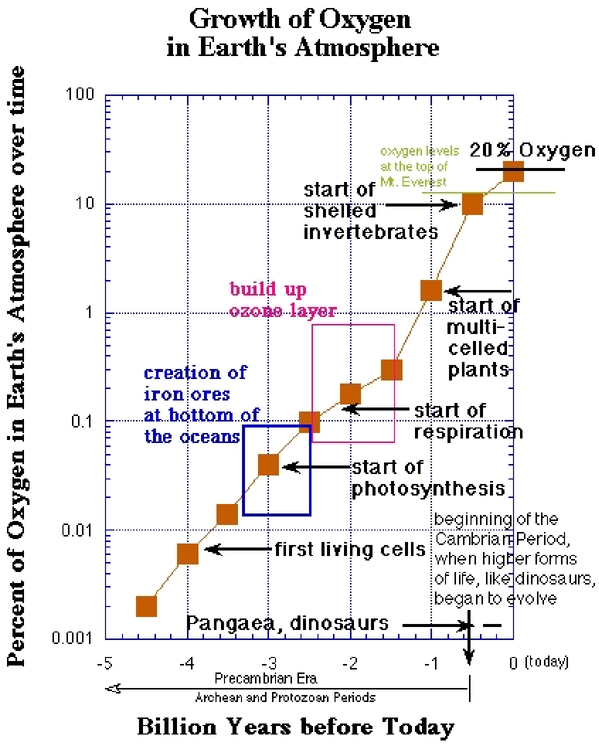
What would *their* music sound like?

Why do humans ***like*** music?
Is music ***just*** "auditory cheesecake"??

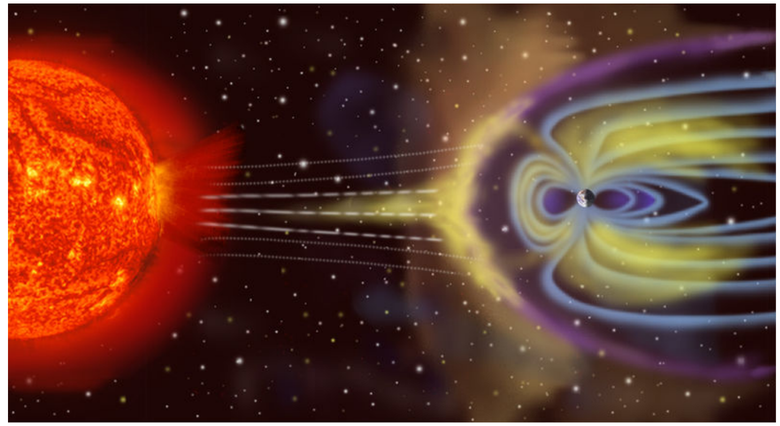


Did evolutionary "forces" – e.g. did "survival of the fittest" shift (via feedback mechanisms / genetic mutations over the millennia) each generic human attribute ***a*** from initial <***a***> = 0 to where it is today?

A (Very) Brief History of Planet Earth:



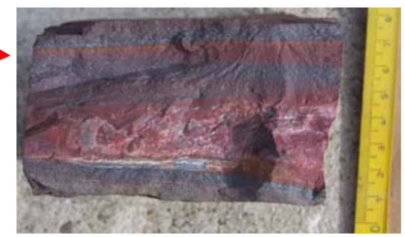
The earth's magnetic field (due to internal dynamo earth's outer core) shields planet from deadly solar X- & γ-radiation:



Photosynthesis drove oxygenation of earth's initially iron-rich oceans

Further oxygenation of earth's atmosphere by stromatolites

Sedimentary banded-iron formation



~ 4.5 Byrs ago: Solar System forms

~ 4.0 Byrs ago: late heavy bombardment in solar system ends;

The earth is in the "habitable zone", cools and {single-celled} life begins…

~ 3.5 Byrs ago: photosynthesis begins

~ 2.3 Byrs ago: earth's atmosphere becomes oxygen rich;

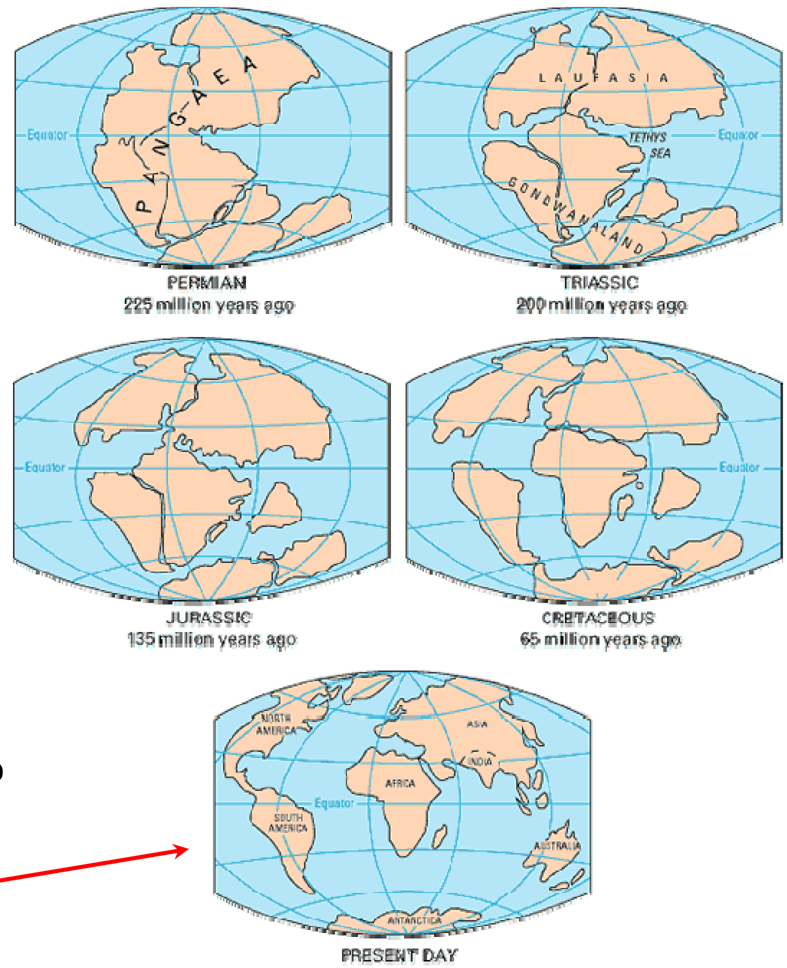
The first "snowball earth" occurs… but eventually warms up again…

Ozone layer forms at the top of earth's atmosphere, enabling life to exist on <u>land</u>

– shielding it from harmful UV radiation.

Breakup & formation of continents on earth – plate tectonics – appears to be cyclical;

Pangaea – last supercontinent in the Permian epoch (~ 225 Myrs ago):



Heat convection (due to planet's original formation & radioactive decay) inside the earth, breaks up Pangaea into 7 major parts –

continents – drift apart, such that today we have:

Life on our planet is *__totally__* dependent on {the constancy of} the four fundamental forces of nature that are operative in the universe in which we live:

- **o <u>Weak Force</u>: Responsible for radioactivity (β-decay) – our sun's source of power generation!**
- **o <u>Strong Force</u>: Binds protons & neutrons together to form nuclei (also important for solar processes!)**
- **o <u>Electromagnetic Force</u>: Binds nuclei and electrons together to form atoms, atom-atom interactions (molecules, all chemical reactions, electromagnetic & acoustic wave phenomena…)**
- **o <u>Gravity</u> (curvature of space-time): Binds atoms together to form stars, solar systems/planets, galaxies, …**

<u>Gedanken experiment # 1</u>:
Turn any one force completely *__off__* (i.e. coupling constant → 0): Life as we know it cannot exist/survive!

<u>Gedanken experiment # 2</u>:
Change the *__strength__* of any one interaction (e.g. gravity, or charge) – life as we know it radically changes!

Gravity on Earth:

$g = g_{\oplus}$

Gravity on Jupiter:

$g = g_{♃}$

Gravity in 11 Dimensions:

$g = g^{i\pi/N_{\dim}}$

<u>Life on our planet is shaped by the fundamental laws of physics operative in our universe</u>:

We live in 4-D space-time (3 spatial dimensions + 1 time dimension) – skeleton of bones + muscles enables locomotion in space-time – evolutionarily very beneficial for our survival – for finding food {& avoiding becoming food…}

We have developed a sense of the rate of passage of time – involves basal ganglia (deep within base of brain), cerebellum & parietal lobe (on surface of right side of our brains) critical areas for this time-keeping mechanism.

We have 3-D stereoscopic accelerometer/inertial guidance system {Newton's 2^{nd} law $F = ma$} – pair of semicircular canals for orientation {and maintaining our balance - helps us avoid injury/death} in local space-time. Gravitational acceleration g exists on our planet, tells us what up vs. down is…

EM radiation {from our Sun} exists – we have stereoscopic pair of eyes {sensitive to visible light portion of EM radiation spectrum} to navigate in/around/interact with our environment day/night to find food/avoid becoming food…

We live in a medium {air/water} which supports propagation of acoustic waves – we have stereoscopic pair of ears which enables us to hear sounds in our environment – helps us navigate in/around/interact with our environment day/night to find food/avoid becoming food…

We have vocal chords – mechanism for producing sound – helps us communicate with/find others of our species – evolutionarily very beneficial for our survival {we're a *<u>social</u>* species of animal}, group hunting for food/avoiding becoming food...

We have senses of taste & smell – tell us which food(s) are good/safe to eat, which food(s) are not good/safe to eat… Sense of smell also useful for finding food/avoid becoming food…

Skin (our largest organ) contains nerves – for sense of touch, pain & thermo-receptors – to help us avoid damage/injury to our bodies/death...

Nature makes amazing very effective/economical use of *many* physics processes operative in our world:

Some animals see in UV and IR portions of the EM radiation spectrum, some animals have 4-color vision…

Sunlight from sky is partially polarized by Rayleigh scattering – vision in some animals (birds & fish) make use of polarized light – e.g. for navigation and/or finding food…

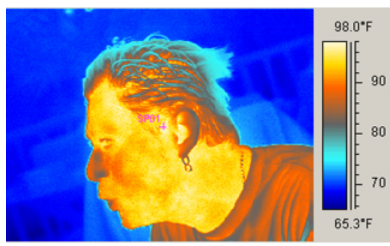
Some animals glow in the dark - i.e. emit visible light! Some animals can dramatically change colors (have chromophores)!

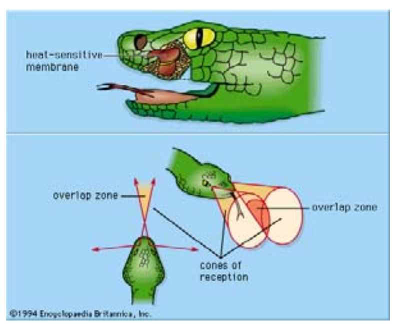
Some {deep-sea} life-forms based on sulfur chemistry, instead of carbon-based!
∃ Anerobic bacteria living in soil/rock of our planet – to depths 100's -1000's of meters below surface of earth!

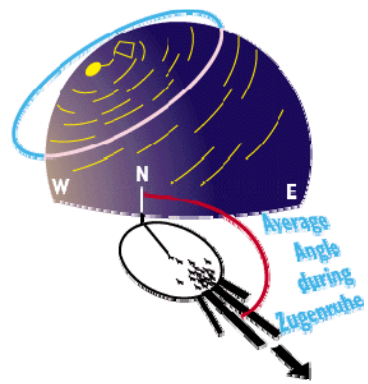
Some animals sensitive to electric and/or magnetic fields. Fish/sharks sensitive to E-fields – useful for finding food. Electric eels/rays stun prey; birds use B-field of earth for navigation, –ve ions in air (earth's E-field electrode layer @ surface of earth) important for plants (& animals)…

Some animals use infrasound {e.g. communication} and/or ultrasound {communication & sonar – for finding food}. Some insects (e.g. grasshoppers) utilize vector particle velocity $\vec{u}$ instead of scalar pressure *p* for hearing!

Earth's diurnal rotation – circadian rhythms in living creatures; Some birds {e.g. indigo bunting} use Polaris (North star) for navigation/migration!







Simply astounding !!!

⇒ Important for recognizing / detecting life-forms elsewhere in universe?

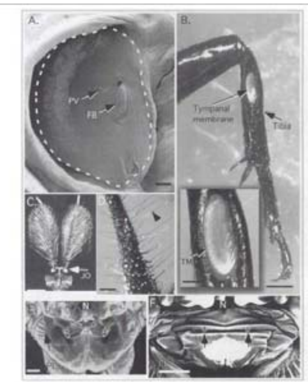
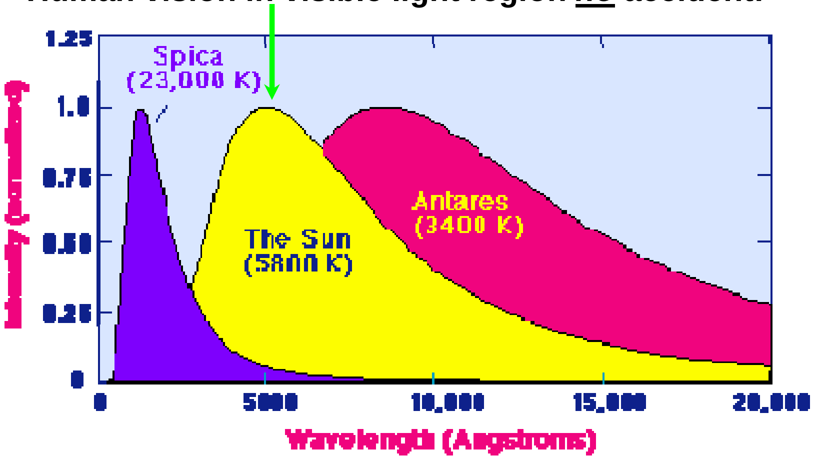


FIGURE 2.1. External auditory anatomy of a locust, a cricket, a mosquito, the cercal system of the cricket, and two parasitoid flies. (A) The tympanal ear of the locust. PV is the pyriform vesicle; FB the folded body to which high and low-frequency receptors respectively attach. The tympanal membrane is delineated by the *white stippled line*. Scale bar = 200 μm. (B) Posterior tympanum on the tibia of the first pair of legs of the cricket *Gryllus bimaculatus*. Scale bar = 1 mm (*inset*: 250 μm). (C) Light scanning micrograph of the antennae of the male mosquito *Toxorhynchites brevipalpis*. The ball-like structures at the base of the antenna are the mechanoreceptive organs. Scale bar = 500 μm. (D) Filiform hairs on the cercus of the field cricket *G. bimaculatus*. Scale bar = 200 μm. (E) Tympanal ears of a tachinid fly (*Ormia*). *Arrow*, tympanal membrane; *arrowhead*, insertion point of the mechanoreceptive organ; N, neck; PL, prothoracic leg. Scale bar = 200 μm. (Light scanning micrograph by D. Huber). (F) Tympanal ears of a sarcophagid fly (*Emblemasoma*). *Arrows* show insertion points of mechanoreceptive organs on the tympanal fold. Scale bar = 200 μm.

Human vision in visible light region *no* accident:



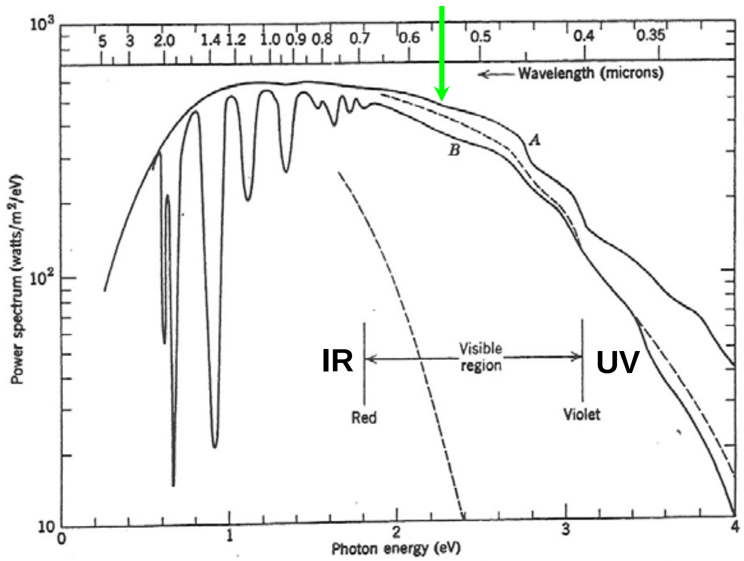
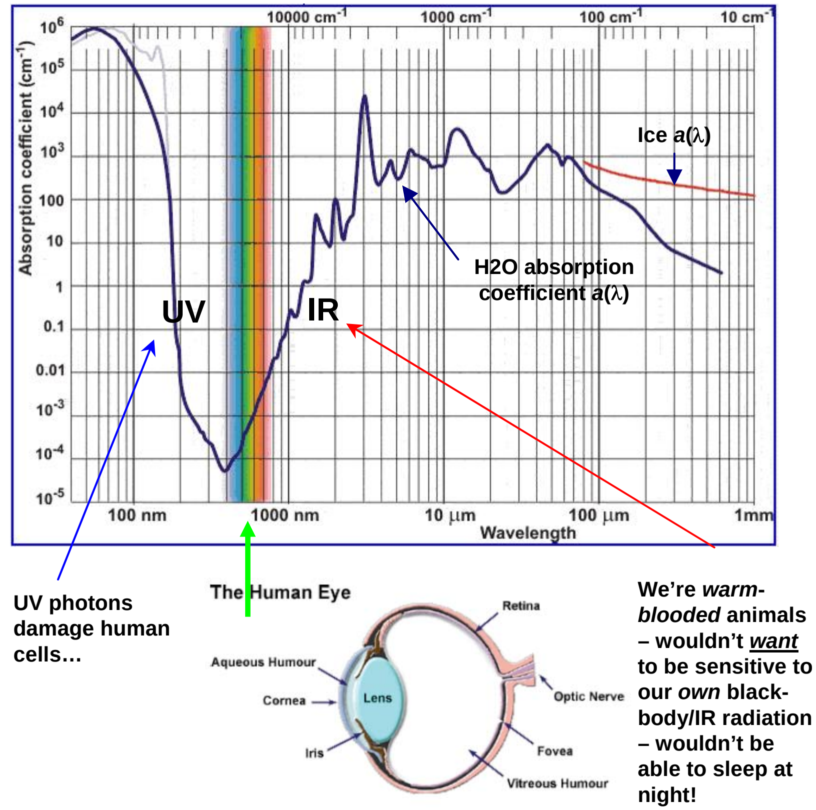
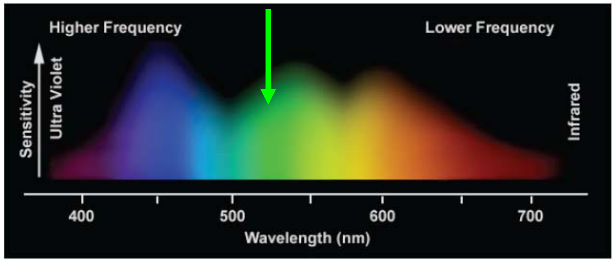


Figure 10.4 Power spectrum of solar radiation (in watts per square meter per electron volt) as a function of photon energy (in electron volts). Curve *A* is the incident spectrum above the atmosphere. Curve *B* is a typical sea-level spectrum with the sun at the zenith. The absorption bands below 2 eV are chiefly from water vapor and vary from site to site and day to day. The dashed curves give the expected sea-level spectrum at zenith and at sunrise-sunset if the only attenuation is from Rayleigh scattering by a dry, clean atmosphere.



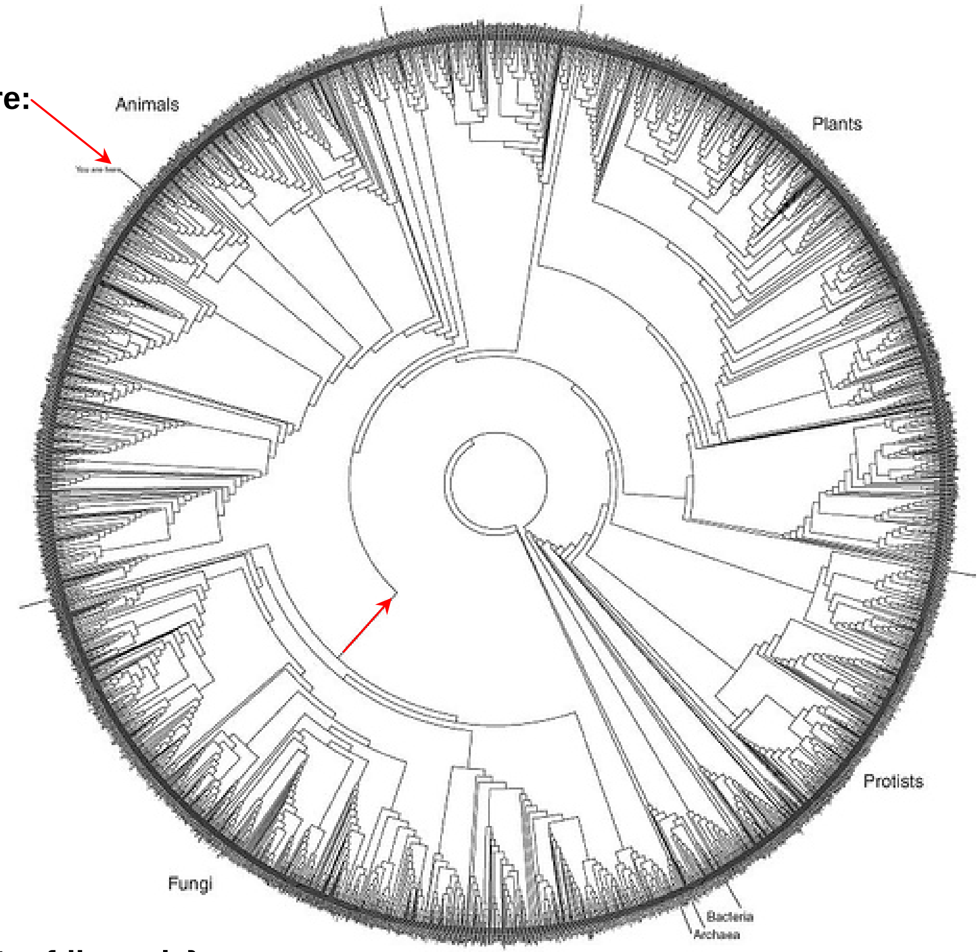
We're *warm-blooded* animals – wouldn't *want* to be sensitive to our *own* black-body/IR radiation – wouldn't be able to sleep at night!



Typical spectral response of human eye

<u>The {Vast} Tree of Life on Planet Earth</u>:

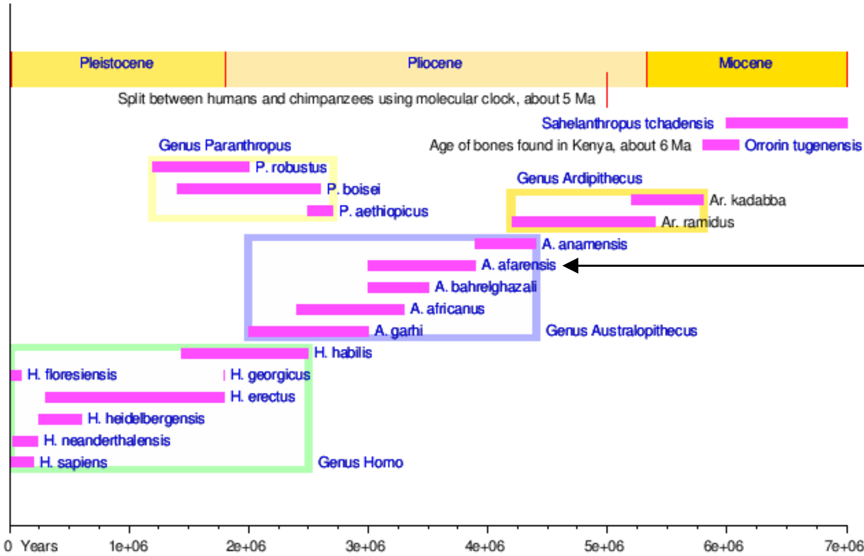
You **are here:**



Radius = time

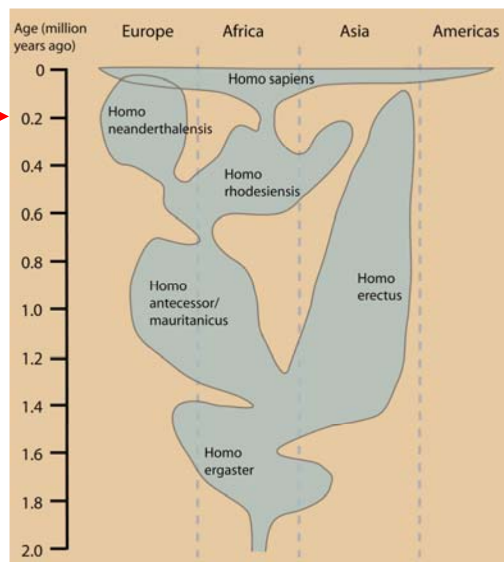
$\Rightarrow$ **We're {distantly} related to *<u>mold</u>* – *eeek* !!!**

The Human Tree of Life:



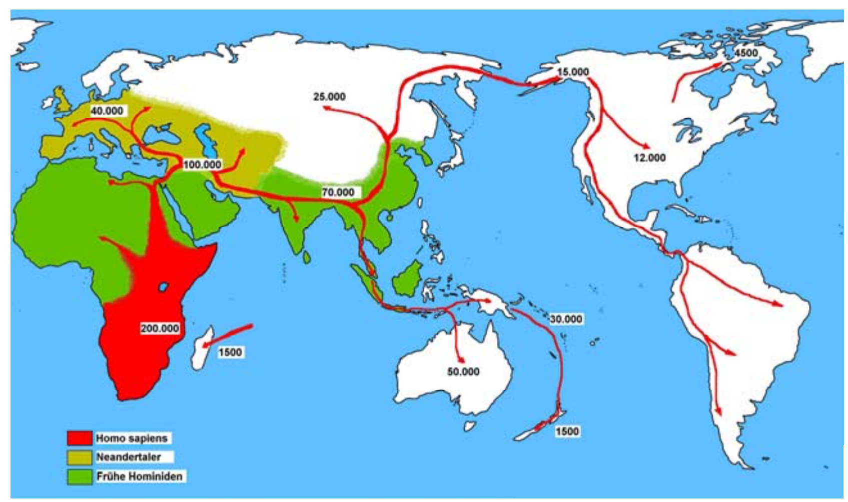
Australopithecus afarensis (2.9-3.9 Myr ago) – had developed bipedalism, but lacked the large brain that modern humans have today

Homo sapiens originated in East Africa ~ 200,000 years ago



⇒ We're literally the "new kids on the block", from a geological perspective!

Spreading of Homo sapiens as hunter-gatherers with time: Again driven by climate change?



Evolution of Homo Sapiens
As Relevant to the Development of Language & Music:

• Our ancient ancestors in Africa {n.b. social creatures!} came down out of the trees – began living on the ground – as hunter-gatherers – driven by climate change???

• We began walking ***upright***…evolutionarily advantageous/beneficial adaptation for life on the savannah…

• It's ***much*** hotter living on the ground than in the trees!!! We developed sweat glands and lost much of our body hair…

• No body hair, + sweat glands ⇒ now we don't have to ***pant*** to cool off !!!

• If don't have to ***pant***, opens up possibilities for evolutionarily beneficial changes to the *human voice box* – facilitates better communication amongst social group – e.g. collaborative/collective hunting, etc.

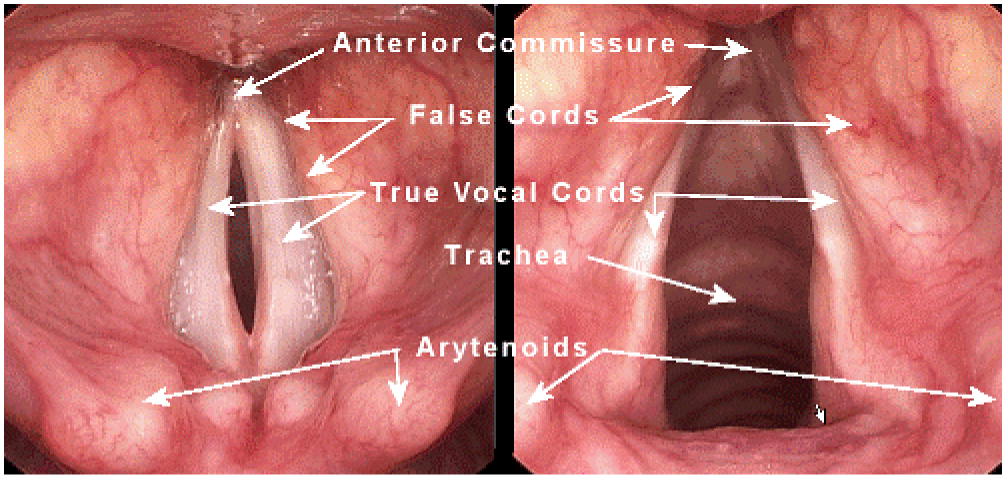
• Humans today have sophisticated voice box + hyoid bone – lower-positioned voice box works in unison w/ larynx and tongue – enables rich complexity/versatility in producing vocal sounds – e.g. vowels & consonants, and singing!

• Hyoid bone developed ~ 300 Kyrs ago (Homo heidelbergensis)…

⇒ Facilitated development of a more sophisticated language…

⇒ Facilitated development of music – human voice = 1st musical instrument!

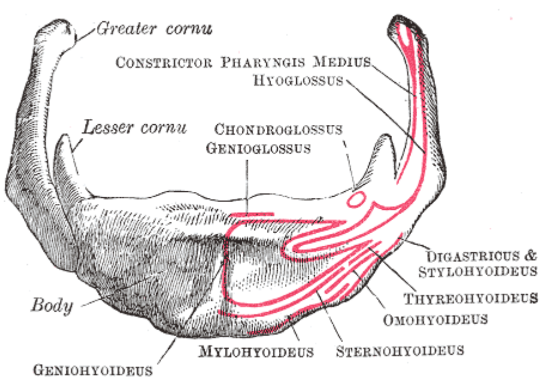
The Human Voice – The first / earliest musical instrument…unique to each human!



When singing (& talking), the human vocal cords vibrate as a 1-D system (e.g. like a guitar string) – production of *integer* related harmonics of fundamental:

$$f_n = nf_1 \quad n = 1, 2, 3, \ldots.$$

n.b. If we instead had e.g. a *2-D circular membrane* for producing musical sounds, would *not* have such a relation:



The hyoid bone (present in many mammals) is unique to Homo sapiens – enables production of a *wide* range of sounds that other animals *cannot* produce – allowing wider range of the tongue, pharyngeal and laryngeal movements – necessary for human speech (*and* song)…

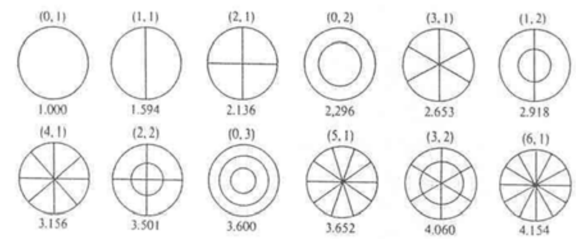
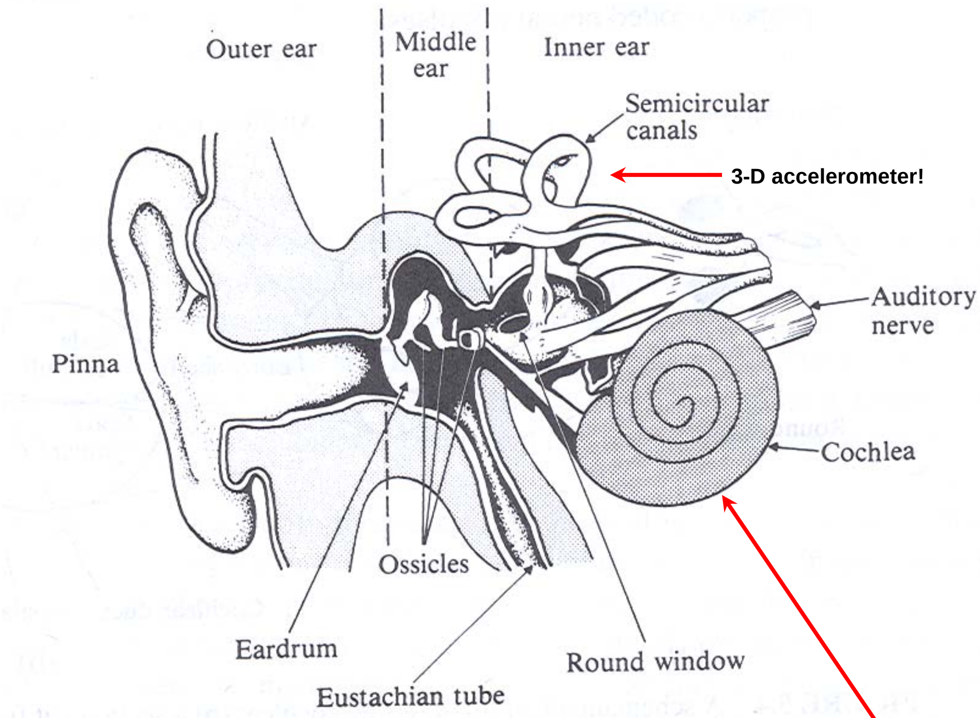


FIGURE 3.6. First 14 modes of an ideal membrane. The mode designation (m, n) is given above each figure and the relative frequency below. To convert these to actual frequencies, multiply by $(2.405/2\pi a)\sqrt{T/\sigma}$, where a is the membrane radius.

$$\nabla^2 \psi = \tfrac{1}{c^2} \partial^2 \psi \big/ \partial t^2$$

This fact has *important* / *profound* consequences for the development of music and musical instruments by humans….

Human Hearing:



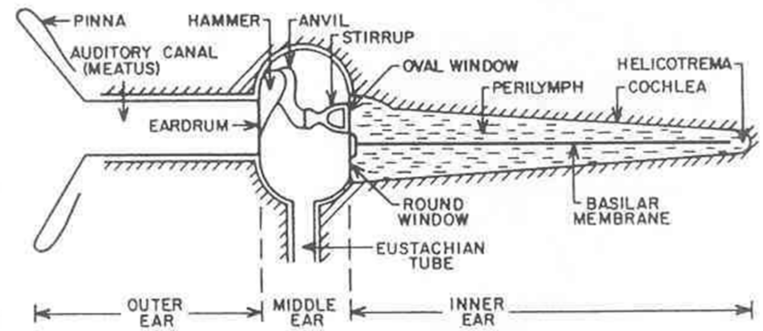
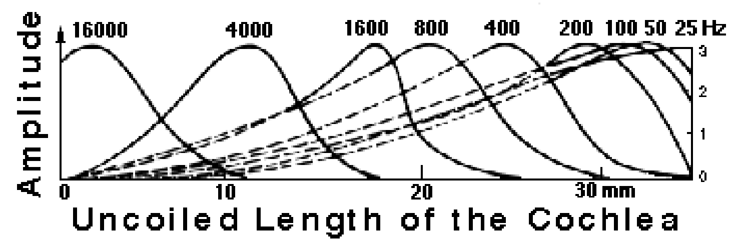


FIG. 1. Schematic diagram of the human ear, with the cochlea uncoiled.



Pinna acts as ~ parabolic collector of sound

Mechanical amplification factor of ear drum ⇒ ossicles (~ 1.3) ⇒ oval window ~ 13×

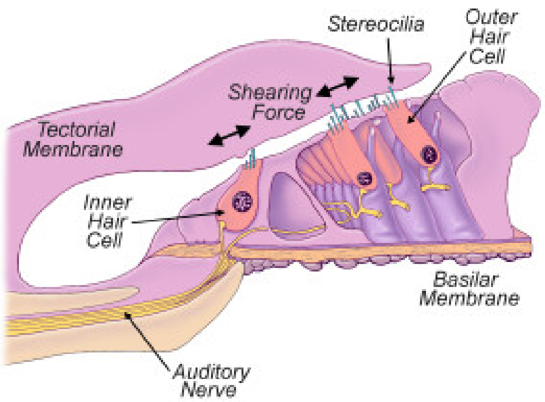
($A_{ear\ drum}/A_{oval\ window}$ ~ 10)

Resonances **in the auditory canal (~ 2 cm long ~ open-closed organ pipe) boost ear's sensitivity in ~ 2 - 5 KHz range**

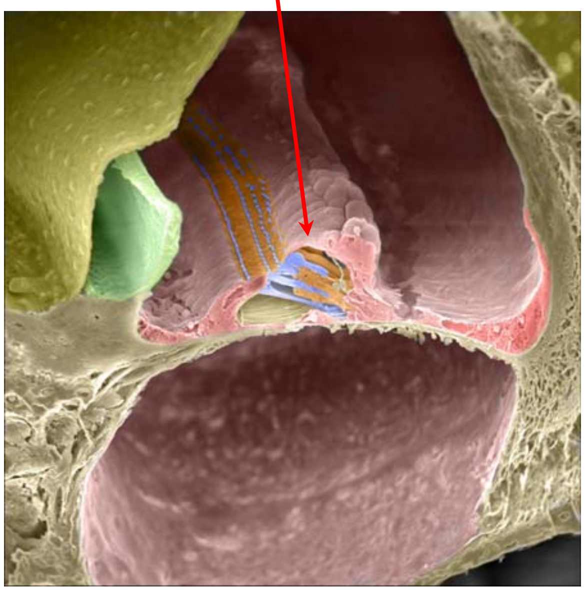
Nonlinear relationship between max A(f) vs. location along cochlea.

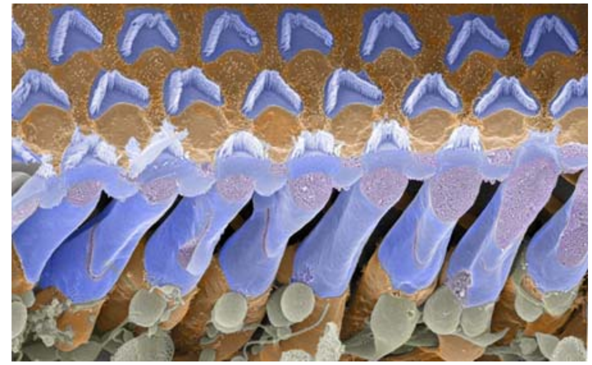
n.b. Spiral shape of cochlea boosts sensitivity to low frequencies by ~ 20 dB! D. Manoussaki, et al., Phys. Rev. Lett. 96, 088701 (2006)

<u>The Organ of Corti & Inner/Outer Hair Cells, Stereocilia</u>:



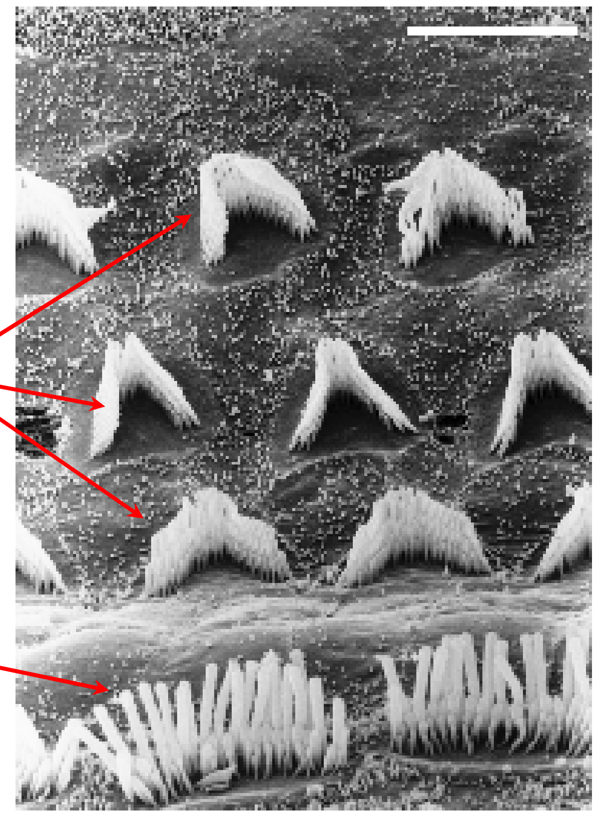
The Organ of Corti



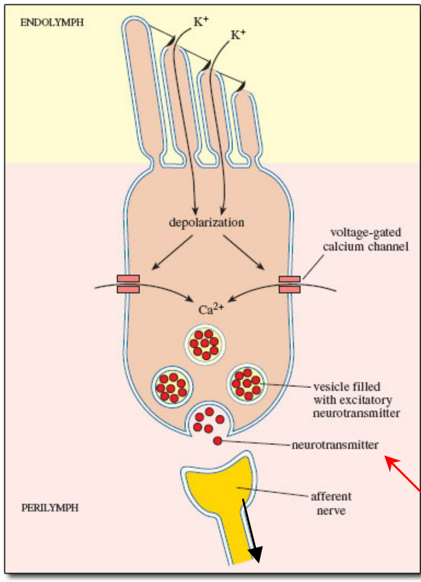


A triple-row of ~ 12,000 chevron-shaped *outer* hair cells – via their stereocilia act as *biological amplifiers*, boosting the sensitivity level of human hearing by ~ 40 dB!

~ 4000 *inner* hair cells – via their stereocilia generate the primary auditory signals sent along the auditory nerve to the brain



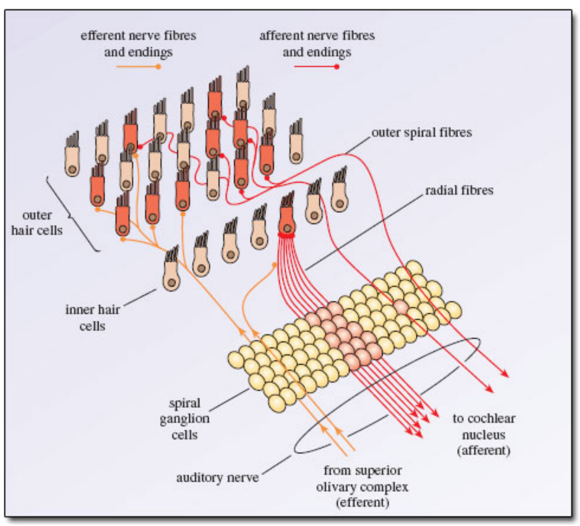
Action of Hair Cells, Auditory Nerve & Auditory Pathway to Brain:



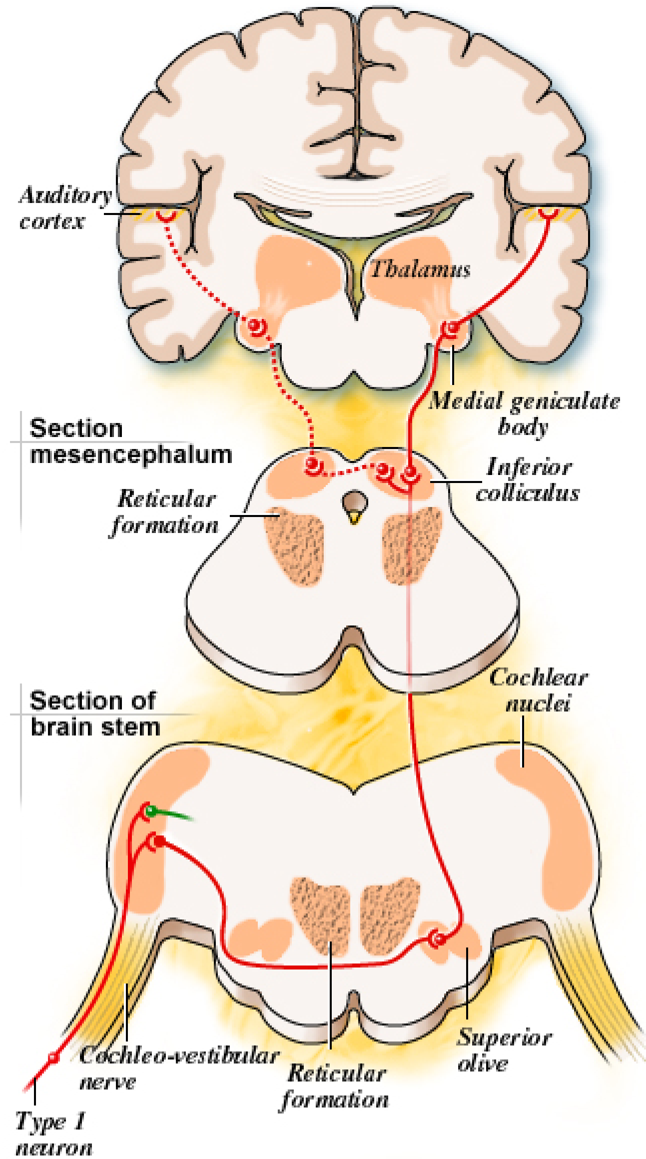
~ 95% of auditory nerve fibers (type I) are connected to ~ 4000 *inner* hair cells, each of which directs its output to up to ~ 10 type I auditory nerve fibers.

Type I auditory nerve fibers are *bipolar* and are *mylenated* (i.e. have nerve sheath) – boosts transmission speed of action potentials along nerve fiber by factor of up to ~ 300× over non-mylenated nerve fibers – evolutionarily *very* important – for our *auditory startle reflex*!

TRPA1 protein



~ 5% of auditory nerve fibers (type II) are connected to ~ 12,000 *outer* hair cells, are *monopolar* and are *not* mylenated (i.e. slow..)



Monaural Auditory Response to Two Pure Tones, Critical Band:

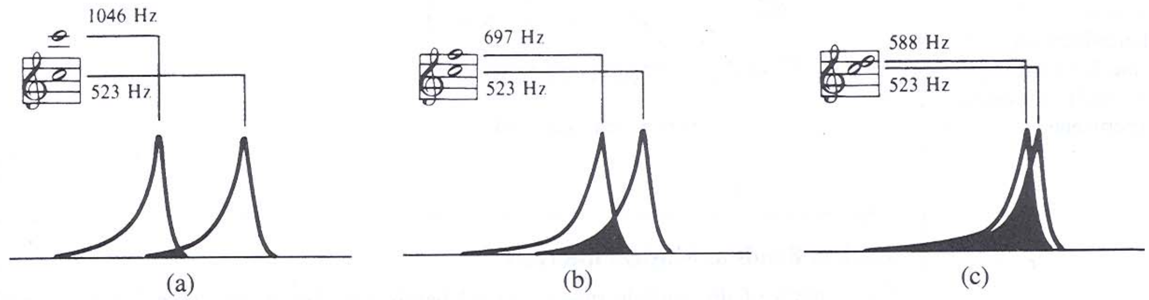
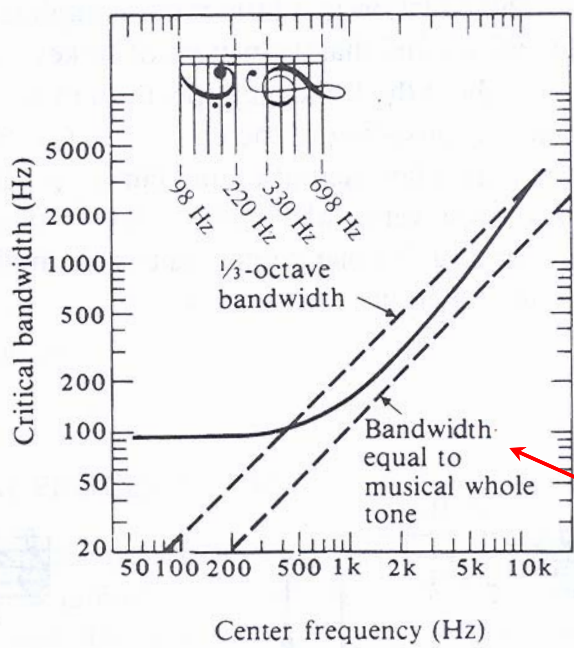


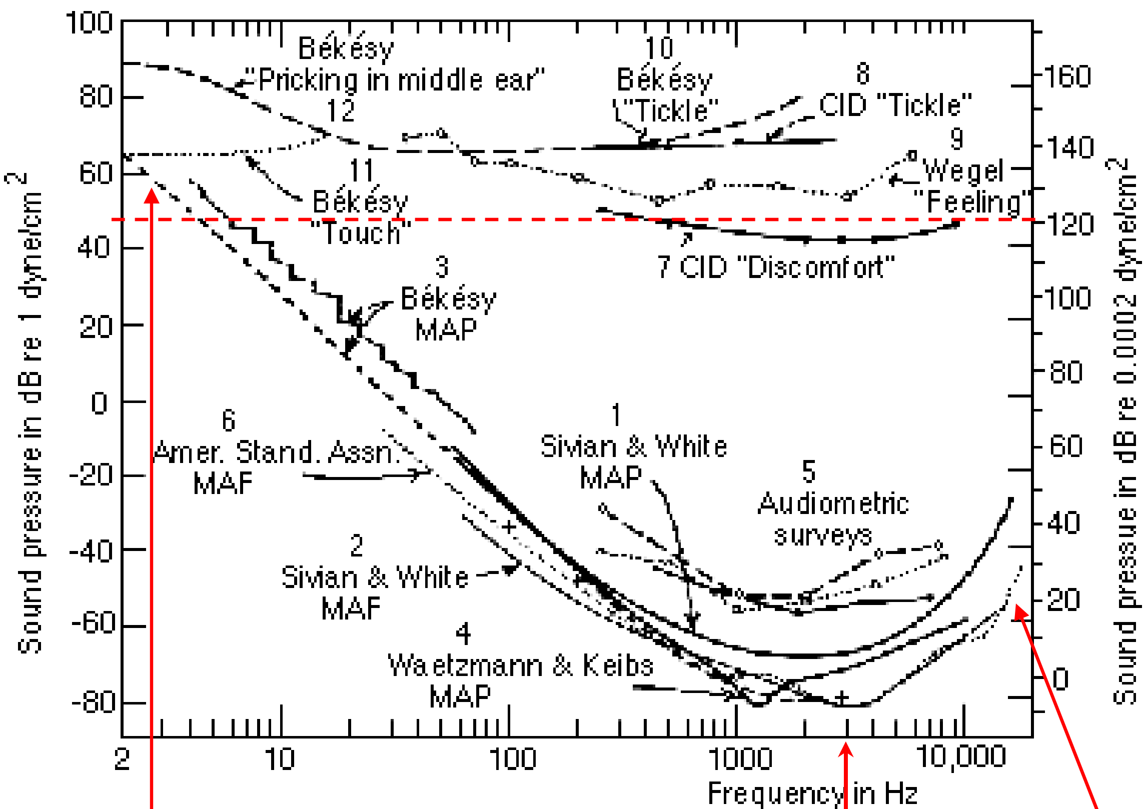
FIGURE 5.9 Frequency response curves for pairs of pure tones. As the interval between them decreases, their response curves show increasing overlap.



Center frequency (Hz)	Critical bandwidth (Hz)	
100	90	← Δf/f ~ 100%
200	90	
500	110	
1,000	150	
2,000	280	
5,000	700	
10,000	1,200	← Δf/f ~ 10%

Critical band *does* have an impact on/limits the # notes/granularity of our musical scale(s)…

Sensitivity of Human Hearing vs. Frequency:



n.b. Low-frequency roll-off totally desensitizes us e.g. to ambient 1/*f* noise, and also e.g. draft noise around ears while walking…

Frequency range of *low-order* harmonics of typical human voice

Max sensitivity here due to *resonance* in ear canal (open-closed organ pipe)

Sensitivity at high frequencies needed for transients – e.g. intelligibility of consonants & vowels…

The human ear responds ~ logarithmically to pressure. The minimum audible RMS over-pressure (MAP) amplitude defined at *f* = 1 *KHz*:

$$p_o(f = 1\,KHz) = 2\times10^{-5}\ RMS\ Pascals$$

Since p_{atm} = 10^5 *Pascals*, humans can detect pressure variations of order ~ 1 part in 10^{10} of atmospheric pressure (n.b. dogs ~ 100× better)!

Corresponding minimum audible longitudinal particle velocity, longitudinal particle displacement and sound intensity at *f* = 1 *KHz* are:

$$u_o(f = 1\,KHz) = 4.8\times10^{-8}\ RMS\ m/s$$

$$\xi_o(f = 1\,KHz) = 7.7\times10^{-12}\ RMS\ m$$

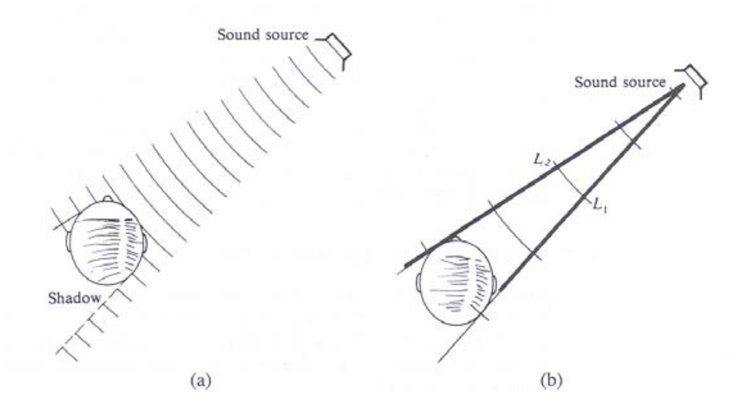
$$I_o(f = 1\,KHz) = 10^{-12}\ RMS\ Watts/m^2$$

n.b. typical size of an atom ~ few Angstroms (i.e. ~ few × 10^{-10} m)!

{Bohr radius of Hydrogen atom ~ ½ Angstrom}

Binaural Hearing and Sound Localization:

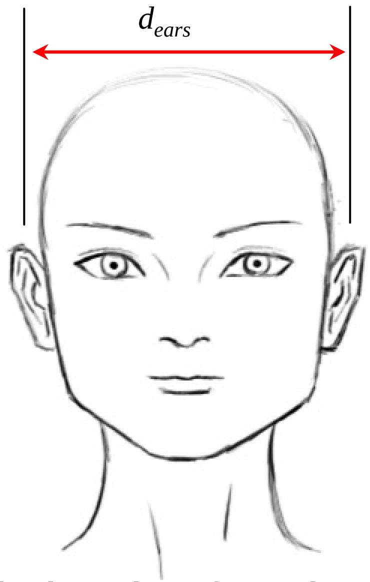
For frequencies between ~ 100 Hz < *f* < ~ 1.5 KHz, we use inter-aural arrival time difference information Δt (for impulse-type sounds) or equivalently, phase difference information $\Delta\varphi = \Delta t/\tau$ (for periodic sounds) for localizing source(s) of sounds:



For frequencies above ~ 4 KHz, sound localization increasingly relies on sound intensity difference information (JND ~ 1 dB) – Our head casts a shadow on the "away" side.

At *f* ~ 1 KHz, ΔSPL ~ 8dB; at *f* ~ 10 KHz, ΔSPL ~ 30 dB or more. This "algorithm" fails at low frequencies due to sound diffraction…

Typical {adult} ear-ear separation distance is d_{ears} ~ 15 cm. Corresponding *maximum* arrival time *difference* in air (@ NTP) is $\Delta t \sim d_{ears}/v \sim 0.44$ msec. Can easily localize sounds to within ~ 5º in horizontal plane in front of us $\Rightarrow \Delta t_{min} \sim 10\ \mu$sec!



n.b. Human's have a very difficult time localizing sounds in water v_{H2O} ~ 4.4x v_{air}, whereas e.g. dolphins, etc. have no such problems! $\Rightarrow$ their hearing adapted to sound propagation in water, our hearing is adapted to sound propagation in air!

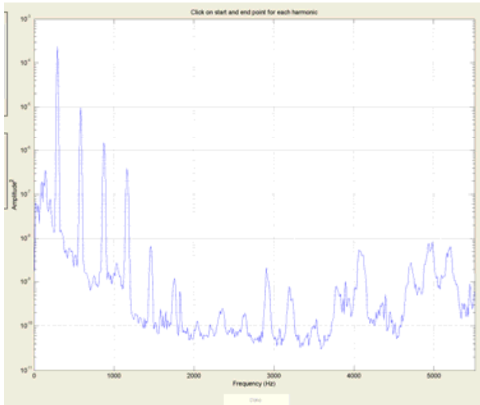
Forward orientation of our pinnae aids us {optimally} in localizing sounds in ~ horizontal plane in front of us (vertical & rearward sound localization degraded as a consequence).

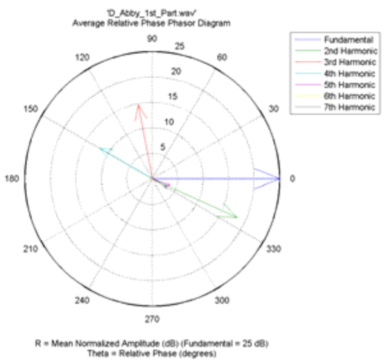
Folds in the pinnae (unique to each human!) enhance our ability to localize sounds in the higher frequency region.

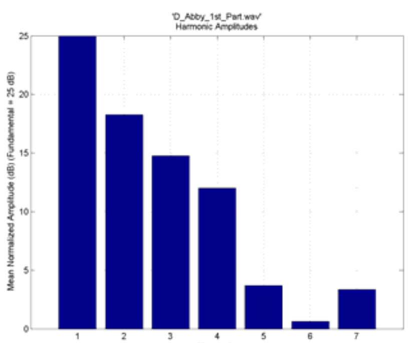
n.b. Long ago, we used to have *movable* ears (like donkeys)…

Comparison of 3 UIUC Physics 193POM/UIUC Women's Choir students singing D4 "Oooo" (293.66 Hz):

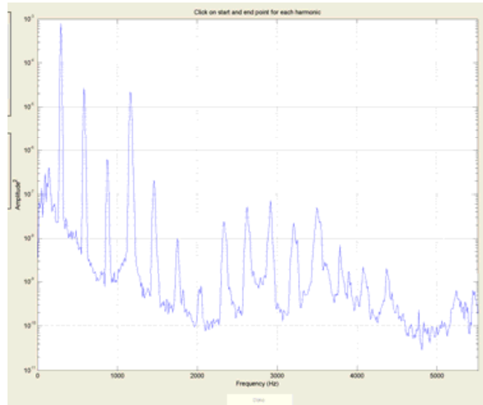
Abby

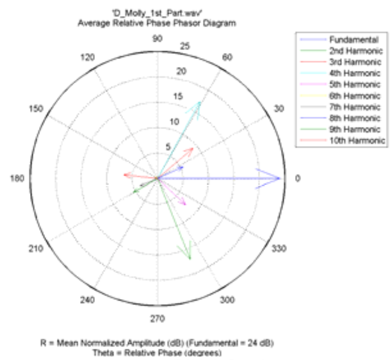


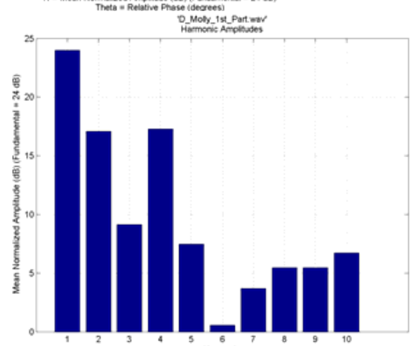




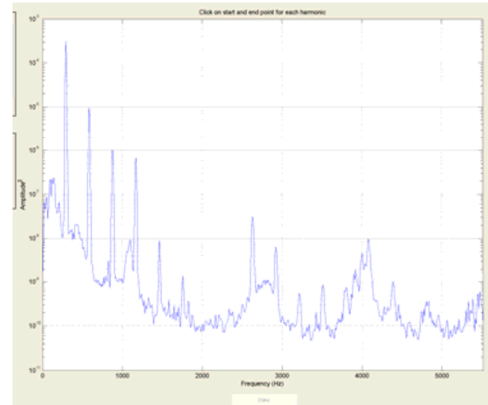
Molly

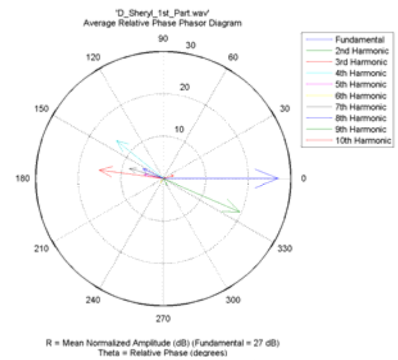


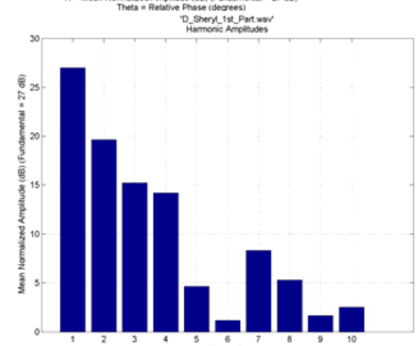




Cheryl







The Phenomenon of Consonance & Dissonance – Studied by Greek philosophers Pythagoras (~ 500 BCE) – e.g. using the monochord:

Two frequencies associated with the vibrating string segments:

$$f_x = v/2x \quad f_{L-x} = v/2(L-x)$$

Consonance occurs when frequency ratios = ratio of two integers *m*:*n*
⇒ *phase* *stable* waveforms, e.g:

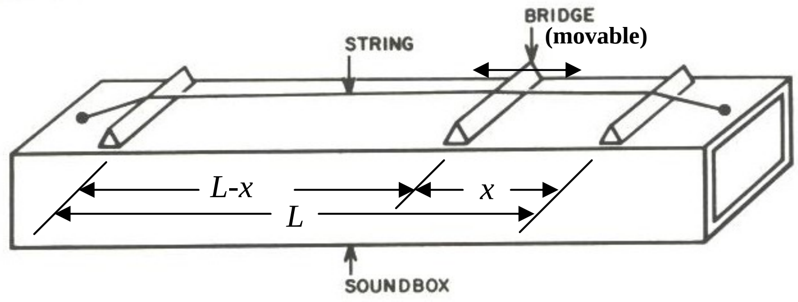
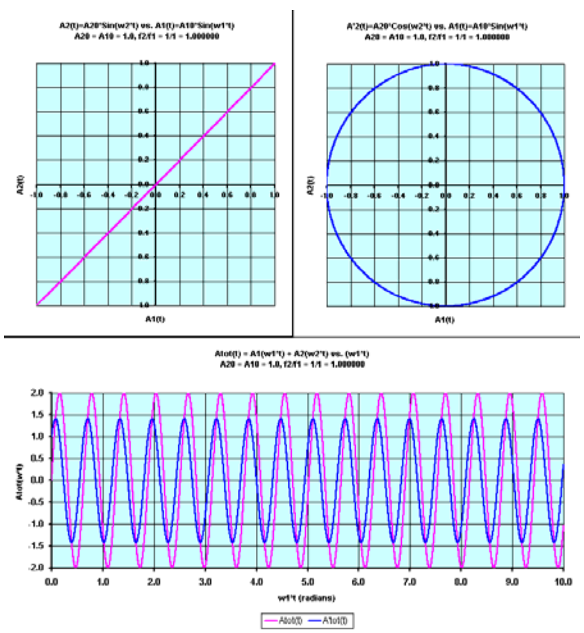


FIG. 1. The monochord.

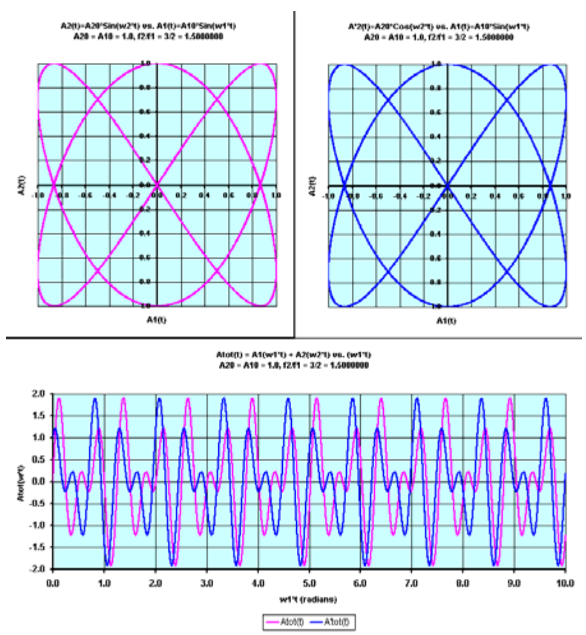
Unison {1:1}

In-Phase: **Quadrature:**



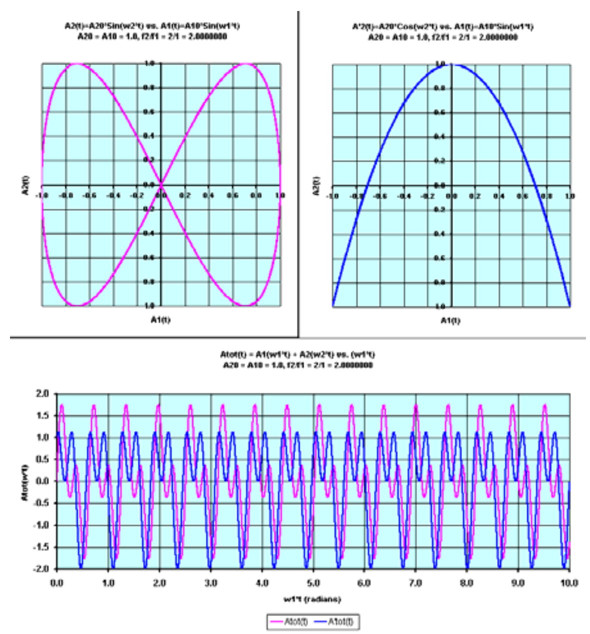
Major Fifth {3:2}

In-Phase: **Quadrature:**

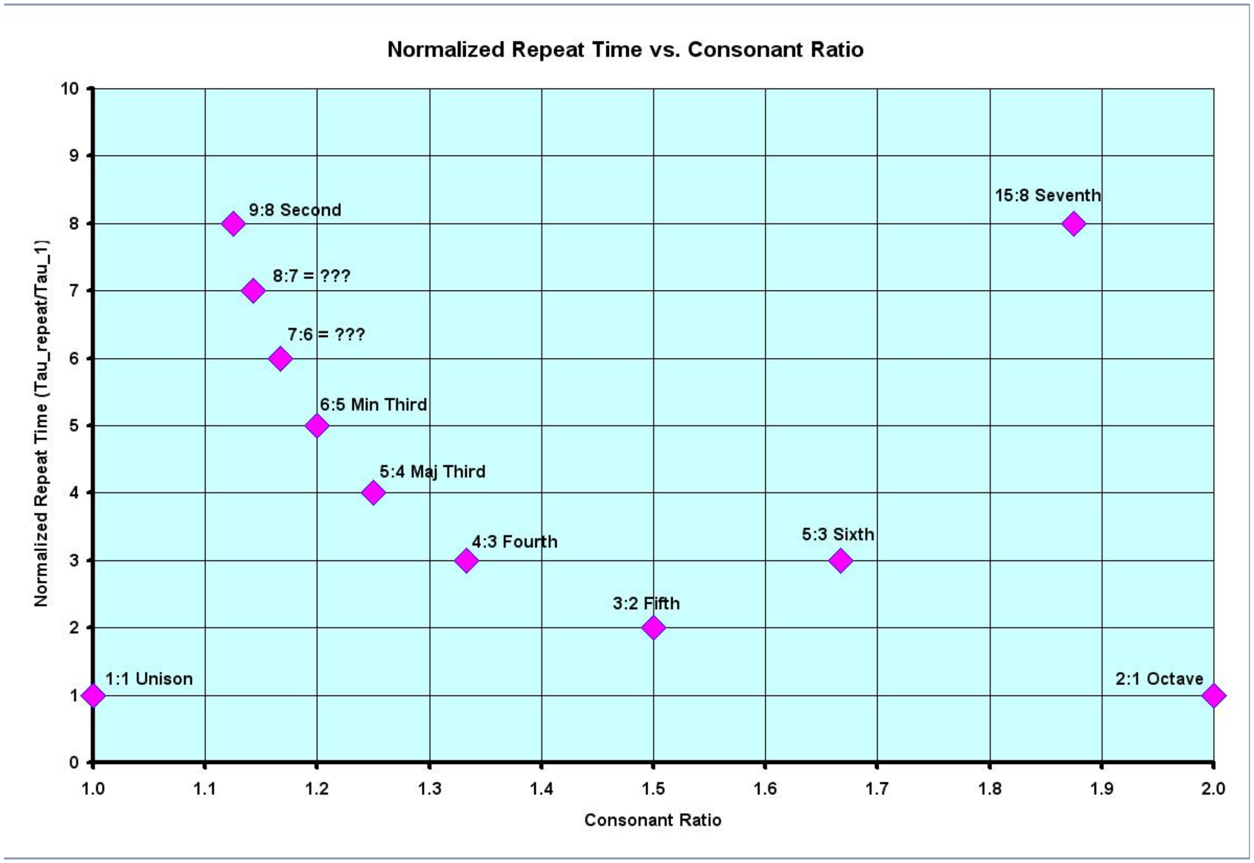


Octave {2:1}

In-Phase: **Quadrature:**



Consonant frequency intervals have phase-stable waveforms – with short repeat times – very easy for human ear to analyze:



The lower frequency determines the repeat time

No phase stability for dissonant/non-consonant/non-integer frequency ratios – repeat times can be infinitely long… requires more mental effort to analyze…

The human brain has *separate* circuits for analyzing sounds for consonance {human voice-like sound – i.e. integer-related harmonics} vs. dissonance {non-human voice-like sound} – outputs also wired to *different* emotional centers!

Our notion of musical scales (& circle of fifths) is <u>intimately</u> connected to consonant intervals:

Note:	C	D	F	G	A	C
Frequency:	f	$\frac{9}{8}f$	$\frac{4}{3}f$	$\frac{3}{2}f$	$\frac{27}{16}f$	$2f$

FIG. 3. A pentatonic scale.

Note:	C		D		E		F		G		A		B		C
Frequency:	1		$\frac{9}{8}$		$\frac{81}{64}$		$\frac{4}{3}$		$\frac{3}{2}$		$\frac{27}{16}$		$\frac{243}{128}$		2
Interval:		$\frac{9}{8}$		$\frac{9}{8}$		$\frac{256}{243}$		$\frac{9}{8}$		$\frac{9}{8}$		$\frac{9}{8}$		$\frac{256}{243}$	

FIG. 4. The Pythagorean scale.

Note:	C		D		E		F		G		A		B		C
Frequency:	1		$\frac{9}{8}$		$\frac{5}{4}$		$\frac{4}{3}$		$\frac{3}{2}$		$\frac{5}{3}$		$\frac{15}{8}$		2
Interval:		$\frac{9}{8}$		$\frac{10}{9}$		$\frac{16}{15}$		$\frac{9}{8}$		$\frac{10}{9}$		$\frac{9}{8}$		$\frac{16}{15}$	

FIG. 8. The just diatonic scale.

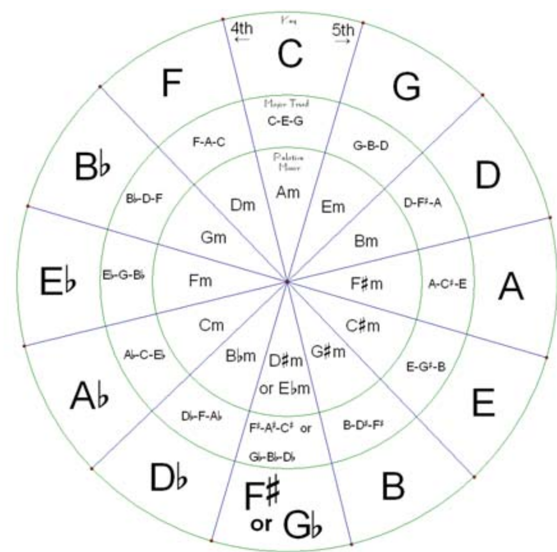
n.b. For musical instruments, if transpose songs in these scales to another key, won't sound the same because the *intervals* between the notes are not the same in all keys….

Musical scale is fundamentally imperfect (consonance perspective):

$a \equiv 2^{1/12}$

	C	D♭ / C♯	D	E♭ / D♯	E	F	G♭ / F♯	G	A♭ / G♯	A	B♭ / A♯	B	C
	1	a	a^2	a^3	a^4	a^5	a^6	a^7	a^8	a^9	a^{10}	a^{11}	a^{12}
	1.000	1.059	1.122	1.189	1.260	1.335	1.414	1.498	1.587	1.682	1.782	1.888	2.000

FIG. 10. The tempered scale.



The Circle of Fifths

Consonance & Dissonance of Complex Tones – Just Diatonic Scale

Consonance of Harmonics - Just Diatonic Scale

Explanation: If two complex tones – e.g. two square or triangle waves and/or two musical tones with integer-related harmonics are superposed/added together – e.g as unison, 2nd, minor 3rd, major 3rd, 4th, 5th, … octave in the just diatonic scale, the colored boxes in the tables below indicate the overlap of harmonics from the two sounds that will be consonant with each other. Thus, e.g. two complex tones in unison, a fifth apart or an octave apart are quite consonant with each other, whereas two complex tones that are e.g. a 2nd or a 7th apart are quite dissonant-sounding.

Fundamental Frequency, f_o = 100 Hz

Harmonic	Unison	Second	???	???	Minor 3rd	Major 3rd	Fourth	Fifth	Sixth	Seventh	Octave
	C-C	D-C	???-C	???-C	E_b-C	E-C	F-C	G-C	A-C	B-C	C-C
#	1:1	9:8	8:7	7:6	6:5	5:4	4:3	3:2	5:3	15:8	2:1
1	100.0	112.5	114.3	116.7	120.0	125.0	133.3	150.0	166.7	187.5	200.0
2	200.0	225.0	228.6	233.3	240.0	250.0	266.7	300.0	333.3	375.0	400.0
3	300.0	337.5	342.9	350.0	360.0	375.0	400.0	450.0	500.0	562.5	600.0
4	400.0	450.0	457.1	466.7	480.0	500.0	533.3	600.0	666.7	750.0	800.0
5	500.0	562.5	571.4	583.3	600.0	625.0	666.7	750.0	833.3	937.5	1000.0
6	600.0	675.0	685.7	700.0	720.0	750.0	800.0	900.0	1000.0	1125.0	1200.0
7	700.0	787.5	800.0	816.7	840.0	875.0	933.3	1050.0	1166.7	1312.5	1400.0
8	800.0	900.0	914.3	933.3	960.0	1000.0	1066.7	1200.0	1333.3	1500.0	1600.0
9	900.0	1012.5	1028.6	1050.0	1080.0	1125.0	1200.0	1350.0	1500.0	1687.5	1800.0
10	1000.0	1125.0	1142.9	1166.7	1200.0	1250.0	1333.3	1500.0	1666.7	1875.0	2000.0
11	1100.0	1237.5	1257.1	1283.3	1320.0	1375.0	1466.7	1650.0	1833.3	2062.5	2200.0
12	1200.0	1350.0	1371.4	1400.0	1440.0	1500.0	1600.0	1800.0	2000.0	2250.0	2400.0
13	1300.0	1462.5	1485.7	1516.7	1560.0	1625.0	1733.3	1950.0	2166.7	2437.5	2600.0
14	1400.0	1575.0	1600.0	1633.3	1680.0	1750.0	1866.7	2100.0	2333.3	2625.0	2800.0
15	1500.0	1687.5	1714.3	1750.0	1800.0	1875.0	2000.0	2250.0	2500.0	2812.5	3000.0
16	1600.0	1800.0	1828.6	1866.7	1920.0	2000.0	2133.3	2400.0	2666.7	3000.0	3200.0
17	1700.0	1912.5	1942.9	1983.3	2040.0	2125.0	2266.7	2550.0	2833.3	3187.5	3400.0
18	1800.0	2025.0	2057.1	2100.0	2160.0	2250.0	2400.0	2700.0	3000.0	3375.0	3600.0
19	1900.0	2137.5	2171.4	2216.7	2280.0	2375.0	2533.3	2850.0	3166.7	3562.5	3800.0
20	2000.0	2250.0	2285.7	2333.3	2400.0	2500.0	2666.7	3000.0	3333.3	3750.0	4000.0
21	2100.0	2362.5	2400.0	2450.0	2520.0	2625.0	2800.0	3150.0	3500.0	3937.5	4200.0
22	2200.0	2475.0	2514.3	2566.7	2640.0	2750.0	2933.3	3300.0	3666.7	4125.0	4400.0
23	2300.0	2587.5	2628.6	2683.3	2760.0	2875.0	3066.7	3450.0	3833.3	4312.5	4600.0
24	2400.0	2700.0	2742.9	2800.0	2880.0	3000.0	3200.0	3600.0	4000.0	4500.0	4800.0
25	2500.0	2812.5	2857.1	2916.7	3000.0	3125.0	3333.3	3750.0	4166.7	4687.5	5000.0
26	2600.0	2925.0	2971.4	3033.3	3120.0	3250.0	3466.7	3900.0	4333.3	4875.0	5200.0
27	2700.0	3037.5	3085.7	3150.0	3240.0	3375.0	3600.0	4050.0	4500.0	5062.5	5400.0
28	2800.0	3150.0	3200.0	3266.7	3360.0	3500.0	3733.3	4200.0	4666.7	5250.0	5600.0
29	2900.0	3262.5	3314.3	3383.3	3480.0	3625.0	3866.7	4350.0	4833.3	5437.5	5800.0
30	3000.0	3375.0	3428.6	3500.0	3600.0	3750.0	4000.0	4500.0	5000.0	5625.0	6000.0
31	3100.0	3487.5	3542.9	3616.7	3720.0	3875.0	4133.3	4650.0	5166.7	5812.5	6200.0
32	3200.0	3600.0	3657.1	3733.3	3840.0	4000.0	4266.7	4800.0	5333.3	6000.0	6400.0

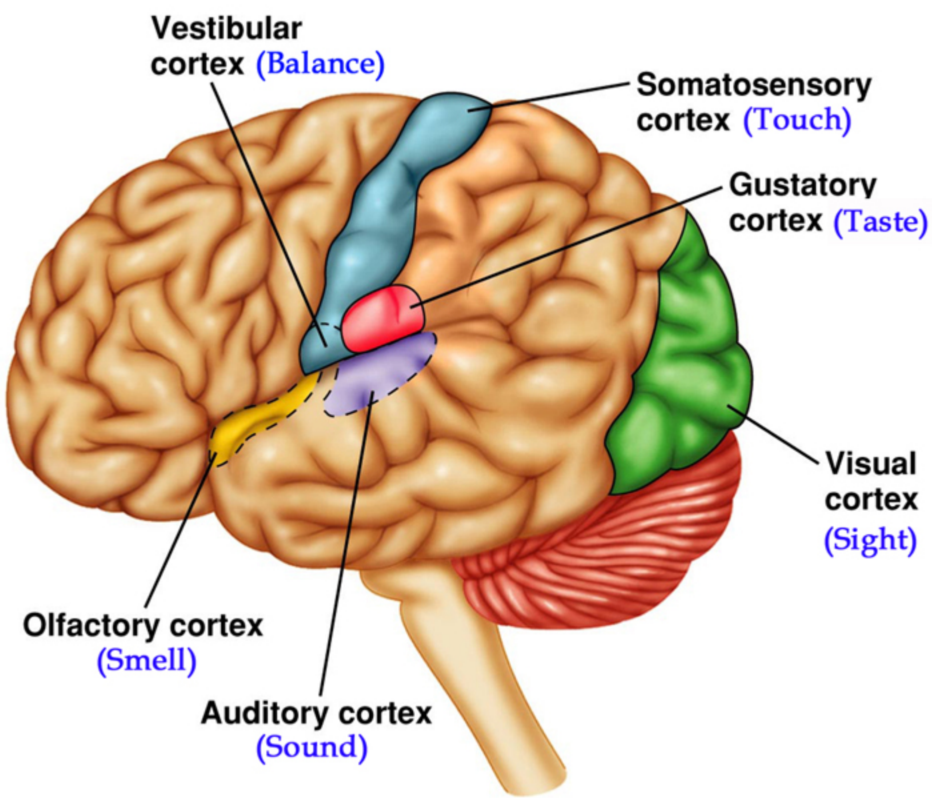
Dissonance of Harmonics - Just Diatonic Scale

Explanation: If two complex tones – e.g. two square or triangle waves and/or two musical tones with integer-related harmonics are superposed/added together – e.g as unison, 2nd, minor 3rd, major 3rd, 4th, 5th, … octave in the just diatonic scale, the colored boxes in the tables below indicate the overlap of harmonics from the two sounds are within the critical band of the human ear and hence will be dissonant with each other. Thus, e.g. two complex tones in unison, a fifth apart or an octave apart are quite consonant with each other, whereas two complex tones that are e.g. a 2nd or a 7th apart are quite dissonant-sounding.

Fundamental Frequency, f_o = 100 Hz

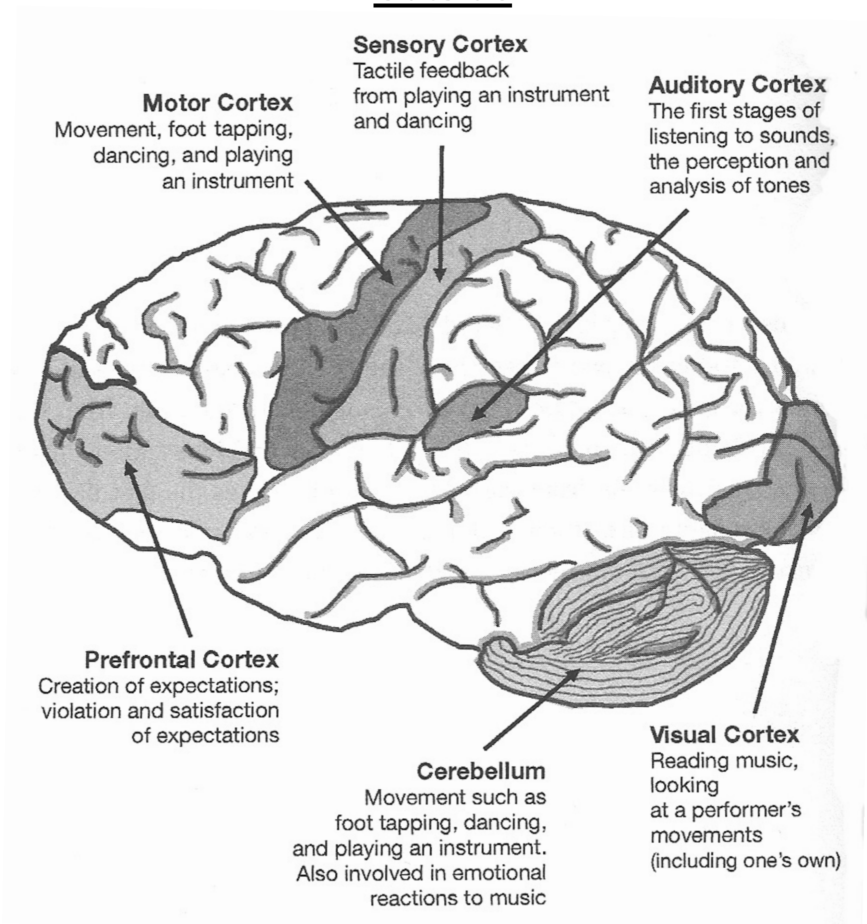
Harmonic	Unison	Second	???	???	Minor 3rd	Major 3rd	Fourth	Fifth	Sixth	Seventh	Octave
	C-C	D-C	???-C	???-C	E_b-C	E-C	F-C	G-C	A-C	B-C	C-C
#	1:1	9:8	8:7	7:6	6:5	5:4	4:3	3:2	5:3	15:8	2:1
1	100.0	112.5	114.3	116.7	120.0	125.0	133.3	150.0	166.7	187.5	200.0
2	200.0	225.0	228.6	233.3	240.0	250.0	266.7	300.0	333.3	375.0	400.0
3	300.0	337.5	342.9	350.0	360.0	375.0	400.0	450.0	500.0	562.5	600.0
4	400.0	450.0	457.1	466.7	480.0	500.0	533.3	600.0	666.7	750.0	800.0
5	500.0	562.5	571.4	583.3	600.0	625.0	666.7	750.0	833.3	937.5	1000.0
6	600.0	675.0	685.7	700.0	720.0	750.0	800.0	900.0	1000.0	1125.0	1200.0
7	700.0	787.5	800.0	816.7	840.0	875.0	933.3	1050.0	1166.7	1312.5	1400.0
8	800.0	900.0	914.3	933.3	960.0	1000.0	1066.7	1200.0	1333.3	1500.0	1600.0
9	900.0	1012.5	1028.6	1050.0	1080.0	1125.0	1200.0	1350.0	1500.0	1687.5	1800.0
10	1000.0	1125.0	1142.9	1166.7	1200.0	1250.0	1333.3	1500.0	1666.7	1875.0	2000.0
11	1100.0	1237.5	1257.1	1283.3	1320.0	1375.0	1466.7	1650.0	1833.3	2062.5	2200.0
12	1200.0	1350.0	1371.4	1400.0	1440.0	1500.0	1600.0	1800.0	2000.0	2250.0	2400.0
13	1300.0	1462.5	1485.7	1516.7	1560.0	1625.0	1733.3	1950.0	2166.7	2437.5	2600.0
14	1400.0	1575.0	1600.0	1633.3	1680.0	1750.0	1866.7	2100.0	2333.3	2625.0	2800.0
15	1500.0	1687.5	1714.3	1750.0	1800.0	1875.0	2000.0	2250.0	2500.0	2812.5	3000.0
16	1600.0	1800.0	1828.6	1866.7	1920.0	2000.0	2133.3	2400.0	2666.7	3000.0	3200.0
17	1700.0	1912.5	1942.9	1983.3	2040.0	2125.0	2266.7	2550.0	2833.3	3187.5	3400.0
18	1800.0	2025.0	2057.1	2100.0	2160.0	2250.0	2400.0	2700.0	3000.0	3375.0	3600.0
19	1900.0	2137.5	2171.4	2216.7	2280.0	2375.0	2533.3	2850.0	3166.7	3562.5	3800.0
20	2000.0	2250.0	2285.7	2333.3	2400.0	2500.0	2666.7	3000.0	3333.3	3750.0	4000.0
21	2100.0	2362.5	2400.0	2450.0	2520.0	2625.0	2800.0	3150.0	3500.0	3937.5	4200.0
22	2200.0	2475.0	2514.3	2566.7	2640.0	2750.0	2933.3	3300.0	3666.7	4125.0	4400.0
23	2300.0	2587.5	2628.6	2683.3	2760.0	2875.0	3066.7	3450.0	3833.3	4312.5	4600.0
24	2400.0	2700.0	2742.9	2800.0	2880.0	3000.0	3200.0	3600.0	4000.0	4500.0	4800.0
25	2500.0	2812.5	2857.1	2916.7	3000.0	3125.0	3333.3	3750.0	4166.7	4687.5	5000.0
26	2600.0	2925.0	2971.4	3033.3	3120.0	3250.0	3466.7	3900.0	4333.3	4875.0	5200.0
27	2700.0	3037.5	3085.7	3150.0	3240.0	3375.0	3600.0	4050.0	4500.0	5062.5	5400.0
28	2800.0	3150.0	3200.0	3266.7	3360.0	3500.0	3733.3	4200.0	4666.7	5250.0	5600.0
29	2900.0	3262.5	3314.3	3383.3	3480.0	3625.0	3866.7	4350.0	4833.3	5437.5	5800.0
30	3000.0	3375.0	3428.6	3500.0	3600.0	3750.0	4000.0	4500.0	5000.0	5625.0	6000.0
31	3100.0	3487.5	3542.9	3616.7	3720.0	3875.0	4133.3	4650.0	5166.7	5812.5	6200.0
32	3200.0	3600.0	3657.1	3733.3	3840.0	4000.0	4266.7	4800.0	5333.3	6000.0	6400.0

Basic Sensory Organization of the Human Brain:

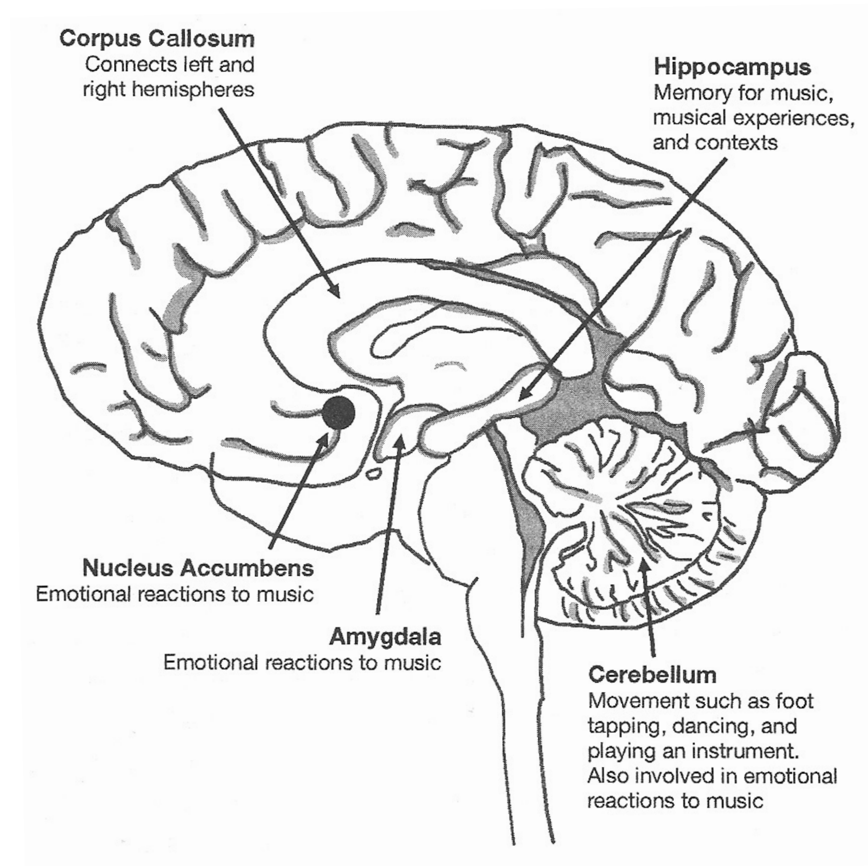


Regions of the Human Brain Associated with Music:

Outside:



Inside:



Tonotopic organization of the human auditory cortex – fMRI scans – pitch discrimination circuitry is *geometrically* laid out in ascending order – like keys on a piano!

24 D. Bilecen et al. / Hearing Research 126 (1998) 19–27

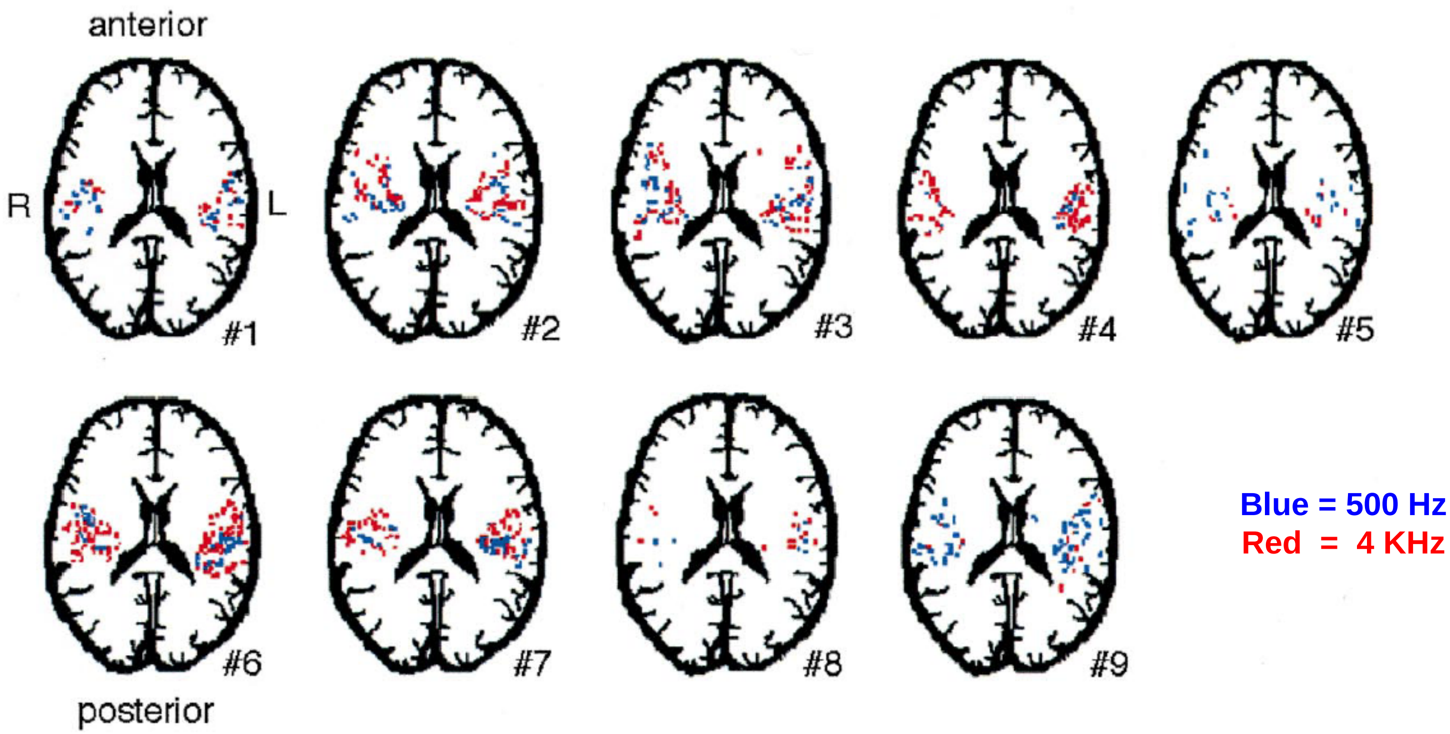
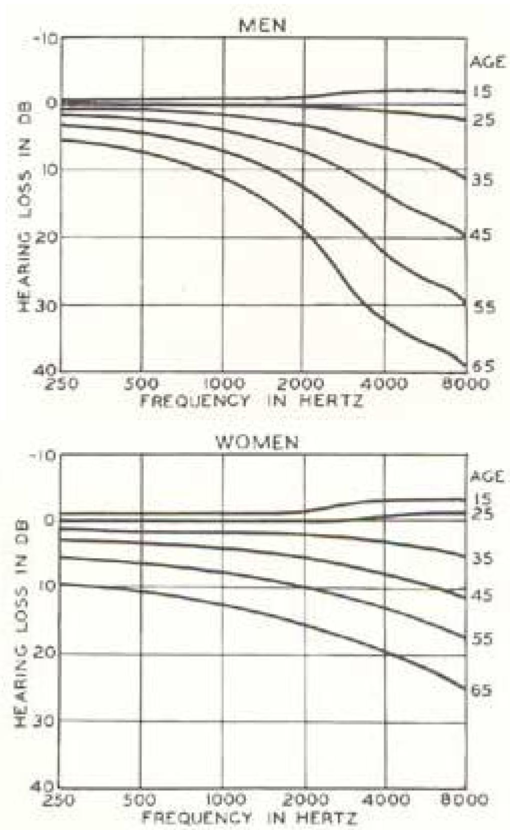


Fig. 5. Activated pixels in axial projection of all nine subjects. Blue pixels represent 500 Hz and red pixels 4000 Hz tone activated areas. All functional images were imposed on a schematic sketch. In general, high tone areas are located more frontally and closer to the medio-sagittal plane than the low tone activated areas.

“Natural” hearing loss as we age – worse for men than for women; Can also be cause for tinnitus – the brain apparently generates “spurious” signals…



<u>fMRI studies</u>: <u>Tonotopic reorganization of the auditory cortex in tinnitus</u>:

10342 Psychology: Mühlnickel *et al.*

Proc. Natl. Acad. Sci. USA 95 (1998)

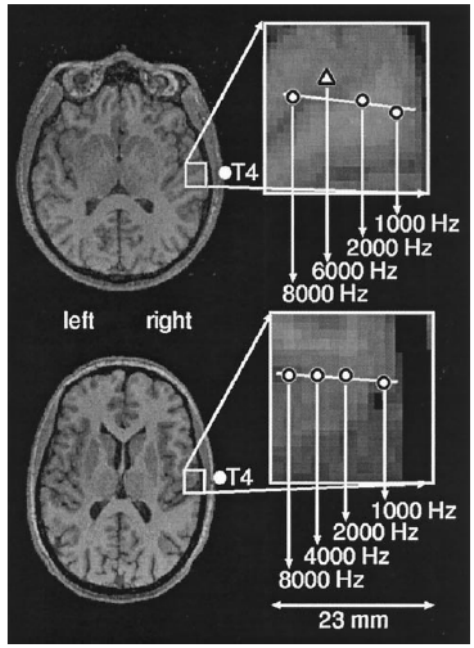


FIG. 1. A typical example of the tonotopic map is shown for a left ear tinnitus (*Upper*) and a control subject (*Lower*). Equivalent current dipoles elicited by auditory stimulation at the three standard and the tinnitus frequency in the tinnitus subject and the four standard frequencies in the healthy control are superimposed onto an axial slice of Brodman’s area 41 of the right hemisphere. The line in the upper portion of the figure shows the trajectory of the dipole locations of the three standard tones (circles). The triangle (*Upper*) represents the location of the tinnitus frequency (6,000 Hz in this case). Note that the trajectory of the dipole locations of the four standard frequencies in the healthy control subject (circles, *Lower*) is linear, whereas the dipole of the affected frequency in the tinnitus subject diverges from the linear trajectory established by the three standard frequencies. The location of T_4 as well as the scale of measurement are marked.

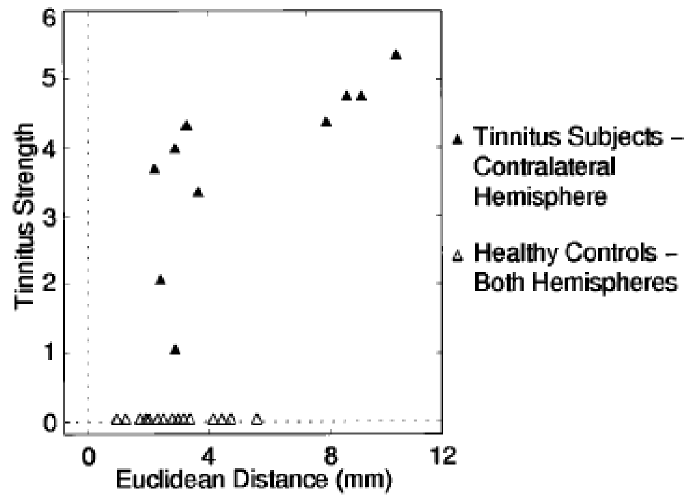


FIG. 2. Scatterplot of amount of subjective tinnitus strength and deviation of the tinnitus frequency from the tonotopic map in the contralateral hemisphere. A measure of deviation of the tinnitus frequency was obtained by determining the Euclidean distance between the trajectory of the standard tones and the location of the tinnitus frequency in tinnitus subjects or the corresponding comparison frequency in control subjects (see text). The tinnitus strength was assessed by the MTI. Greater subjective tinnitus strength was related to larger deviations from the trajectory of the standard frequencies. This figure suggests that there might not be a linear relationship between tinnitus and reorganization but rather a bimodal distribution of tinnitus sufferers with and without map distortions. The size of the sample studied is too small to clarify this point.

<u>Music and the Human Brain</u>:

Music is processed simultaneously in multiple regions of our brain – sequentially and in parallel – for frequency, amplitude/loudness, tempo/beat/rhythm, contour, as well as e.g. recalling memories of the same song and/or related songs – stored in *<u>several</u>* places in the brain – not just one place… explains why we have very robust recall of music! Alzheimer's patients remember songs/song lyrics long after forgetting everything else….

The outputs of these sound/music processing centers are also wired into our emotional centers in our brains – music *<u>can</u>* make us feel happy/sad/…

Various brain chemicals/neuro-transmitters are produced when listening to/participating in music:

<u>Serotonin</u> – produced by neurons of the raphe nuclei in the brain stem {regulates mood, appetite, sleep & metabolism}

<u>Dopamine</u> – released in nucleus accumbens {regulates emotions, mood, alertness and coordination of movement, aids in encoding of memory, and is also part of brain's pleasure and reward system – e.g. gamblers/drug addicts/chocoholics}. Its role in music was only recently discovered (V. Menon, D.J. Levitin, NeuroImage 28(1): 175-84, 2005).

<u>Oxytocin</u> – released by the pituitary gland, amygdala, ventromedial hypothalamus, septum and brain stem during communal singing, rituals & sexual arousal, enhances bonding & trust, reduces fear and/or apprehension, affects generosity by increasing empathy, … Its role in music was also only recently discovered {1995, 2003, 2005}.

<u>Endorphins</u> – released by the pituitary gland & hypothalamus during singing, strenuous exercise, pain, orgasm, death – resembles opiates in analgesic (painkiller) ability and produces a sense of well-being…

Music increases our alertness – via modulation of <u>norepinephrine</u> and <u>epinephrine</u> (aka <u>adrenaline</u>)…
Music also ameliorates the effects of stress – reduces <u>cortisol</u> levels (a hormone produced by stress).

The release of "feel-good" neuro-chemicals in human brain in response to playing / listening to music points to an ancient and evolutionarily beneficial connection to music, e.g. helps sooth/ease tensions/smooth over differences/forge social bonds/… helps to preserve/maintain/stabilize social structure of group…

The release of these brain chemicals also boosts the immune system – humans stay healthier/fend off illness/disease – again improves odds of one's survival!

Production of “feel-good” neurotransmitters human brains in response to music evolutionarily beneficial to humans – individuals who didn’t benefit from/have this response were at a disadvantage ⇒ reduced probability for passing on their genes. The humans who survived enjoyed/benefitted from music! ⇐ “positive” feedback mechanism!

Social interactions of early prehistoric tribes very likely coupled music, dance, food, celebration – benefitting everyone in group, also helping to ease tensions/squabbles, etc. – maintain stability of social structure of group…

Robust memory of music/song ⇒ effective tool e.g. for education of young – worldly do’s n’ don’ts, how-to’s, etc. and also oral/musical preservation of early human culture’s history…

n.b. written language developed only “very recently” (~ 6000 years ago – @ transition from hunter-gatherer to agrarian societies – to keep track of transactions of goods, etc. between members of society in that era…)

Earliest music presumably utilized only the human voice & e.g. clapping of hands, stomping of feet, etc. ⇒ naturally led to development of musical instruments such as early flutes, drums, etc. to accompany & thereby enhance such activities/ceremonies…

Early humans:

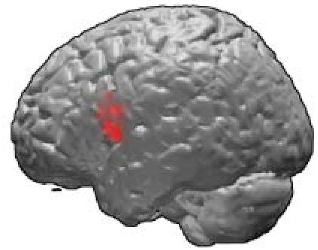
Likely entire group participated in music & dance celebrations…

Tradition still carried on today in many indigenous / native groups…

<u>Genes for Language and Music</u>:

Examination of fossil skulls reveals that Brodmann area 44 (BA44) – part of the frontal cortex {important for cognitive and perceptual tasks, as well as auditory motor imitation via *<u>mirror</u>* *<u>neurons</u>*} may well have been in place ~ 2 Myrs ago (i.e. *<u>long</u>* before Homo sapiens – first emerged ~ 200 Kyrs ago).

⇒ Neural mechanisms for *language* were in place long before they were fully exploited…



Brodmann area 44

The FOXP2 gene (located on chromosome 7) is closely associated with human language – also existed in Neanderthals {recent DNA analysis!}. Chimpanzees and songbirds, such as the zebra finch {as well as other animals - e.g. fish, mice, crocodiles,…} have their own versions of the FOXP2 gene.

Microcephalin is part of the human genome that encodes for brain development. A genetic variant of this gene emerged ~ 37,000 years ago – i.e. at the beginning of culturally modern humans, and coincides with the emergence of tonal languages and the appearance of artistic artifacts and bone flutes…

A second genetic variation of microcephalin arose ~ 5,800 yrs ago – coincides with the first record of written language, spread of agriculture, development of cities, …

n.b. Social interactions can/do alter gene expression in the brain {and vice versa}!

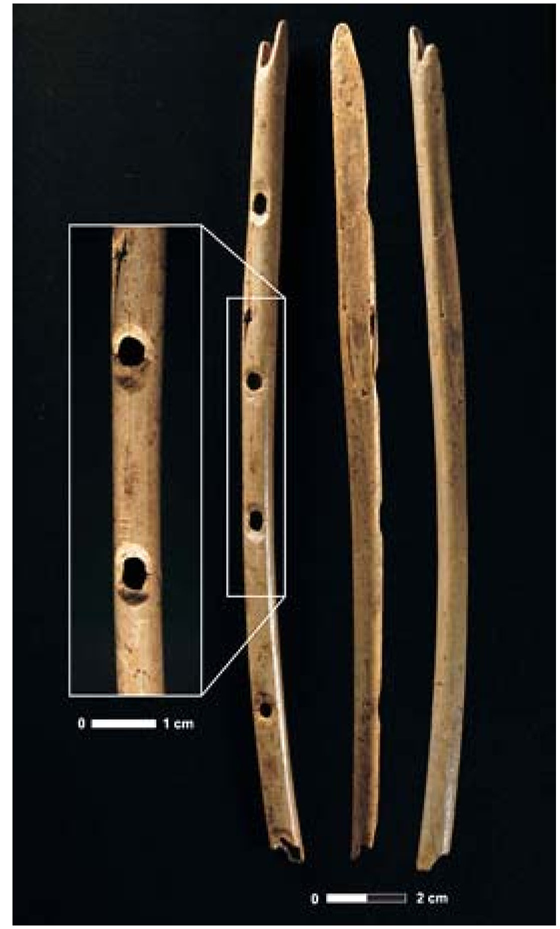
{what does this mean/imply about living in, and evolution in today's modern world???}

The earliest {unambiguously} known musical instrument – ivory flute (made from woolly mammoth tusk) found in a mountain cave {Geissenklösterle}, near Ulm, in southwestern Germany in 2004, ~ 37,000 years old, and is ~ 18.7 cm long:

n.b. other flutes (made from swan bones) discovered earlier in same cave;

A bone drumstick has also found in this cave….

2^{nd} Bone Flute (Griffon vulture, > 35K yrs old) recently found in cave near Hohle Fels (SW Germany) in 2008:

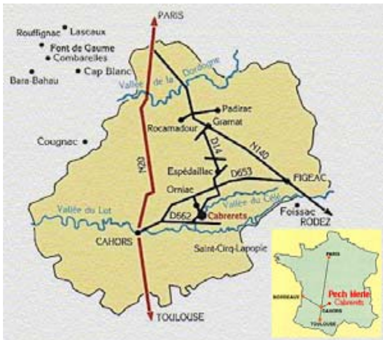


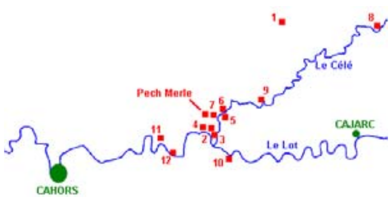
n.b. Exact copy of flute made (via laser scan ⇒ 3-D printing), given to professional musician, who, after learning how to play it, was able to play "Amazing Grace" on it (key of D - uses the white notes on piano) and the German National Anthem – (uses both the white and black notes on piano) !!!

⇒ Evidence for 12-note natural/"consonant" musical scale in existence at *that* time!!! n.b. Presumably this flute is also *not* a prototype!!!

Connection Between Prehistoric Art and Music in Palæolithic Caves:

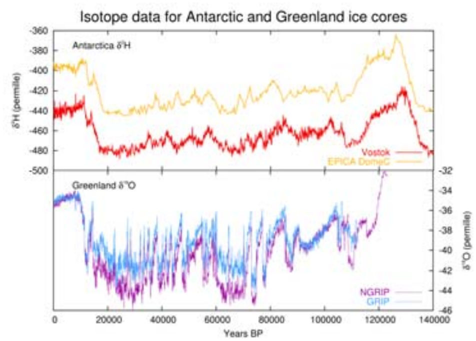
Grotte du Peche Merle {Blackbird Hill}, Caberets, Departement Lot, Southern France



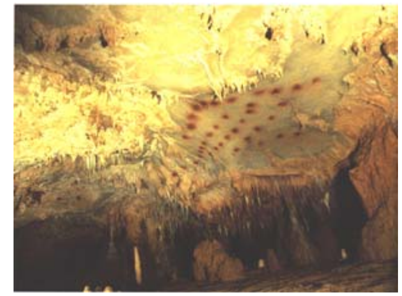


Paintings dated ~ 20,000 – 25,000 yrs old ⇒

Caves were a good place to live / camp out in during the last glacial period:



Red dots are markers for acoustic resonances !!!



<u>La Grotte du Portel, Ariège Pyrenees, Southern France</u>:

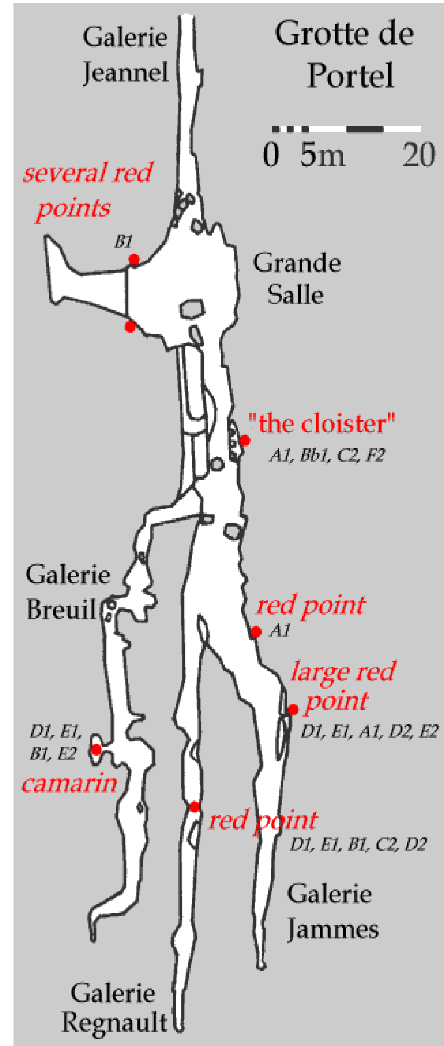
Acoustical resonance properties of this cave recently studied by Prof. Iegor Reznikoff & his University Paris/Nanterre research team.

Paeleolithic man would have explored caves by dull light of torches, and using his voice like sonar/echo-location to navigate around corners, avoid holes, explore nooks/crannies of the cave…

Reznikoff's team discovered that the red dots in this cave were *<u>markers</u>* of acoustic resonances – and were very often within ~ 1-2 meters of paintings in the cave.

Brought in trained vocalist to map out the acoustic resonances.

Also discovered that by modulating the harmonic content and amplitude, some acoustic resonances sounded very similar to those made by the animals painted on the nearby wall – i.e. animal paintings also a *<u>marker</u>* for humans to make the animal's sound !!!



From the perspective of "survival of the fittest", all animals living on our planet are fundamentally / primarily interested in their *own* species, and secondarily in other species (e.g. as food/keep from becoming food…)

We humans are *no* different in this regard. Our *anthropocentric* view of interest primarily in our own species is also reflected in our music - e.g. consonant intervals, musical scales, etc. as well as the sounds made by musical instruments that we have developed over the millennia….

It is *absolutely not* an accident that our musical instruments *mimic* the human voice – i.e. 1-D vibrating systems with integer-related harmonics {$f_n = nf_1$} for overtones – some musical instruments succeed in this more closely than others, which can be viewed as ~ artistic abstractions of the human voice. Skilled musicians playing such instruments can evoke in us strong emotions as if we were listening to a human in agony/pain, joy/ecstasy, sorrow, etc. Tempo/timing – which parallels the temporal aspects of various human gestures/movements recently found to be critical in this regard, in terms of evoking human emotion(s) in response to music!

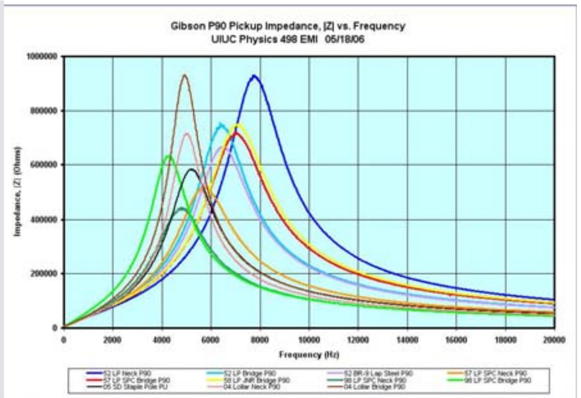
Similarly, it is also *not* an accident that {inharmonic $f_n \neq nf_1$} 2-D percussion instruments – drums etc. are used to mimic the impulsive sounds associated with internal human rhythms – e.g. our heart beat, blood pulsing through our veins, breathing, etc.

Both classes {1-D and 2-D} of musical instruments can also be/have been used in musically artistic ways to mimic the voices, etc. of animal species that are of secondary interest to us – e.g. the singing of birds, the roar of lions, howling of wolves, the clip-clop of horses hooves, etc.

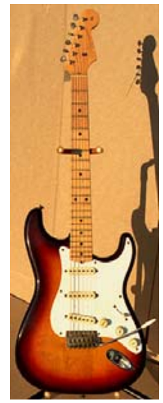
A Test of My Own Long-Term Musical Memories:

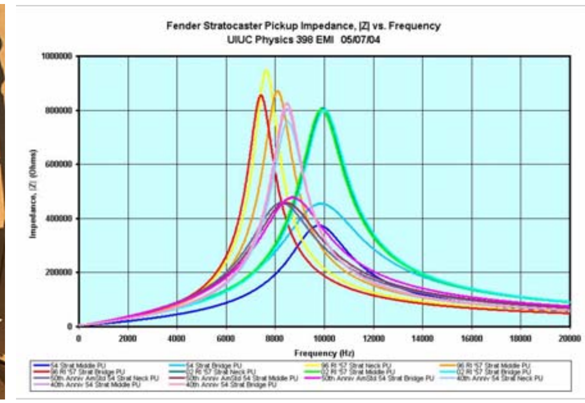
I played {electric} guitar in mid-60's – mid-70's; started playing again in ~ mid-90's: "Faithful" modern-day re-issues of vintage guitars didn't sound like the real deal to *my* ears... Due to false memories, or actual truth??? I explicitly checked:

Gibson P-90's in Les Pauls, Les Paul Jr, …

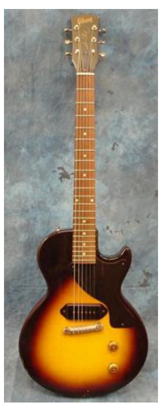


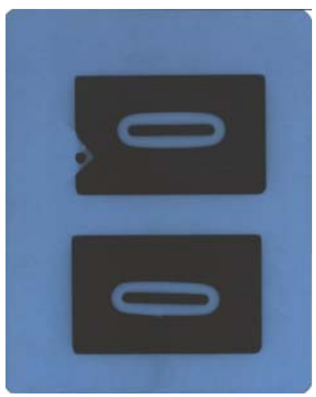
Fender Stratocaster Pickups



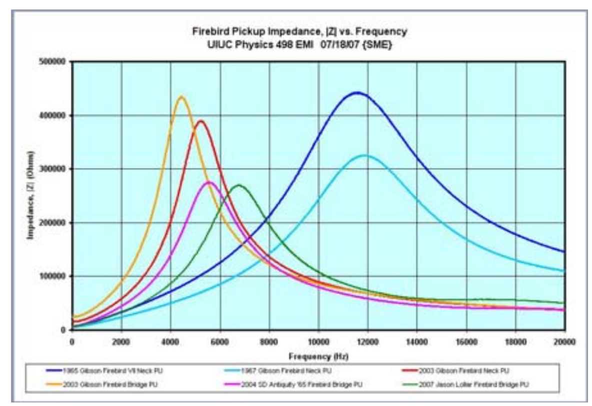


X-ray of P-90 PUs from '52 (top) vs. '98 RI (bottom) Gibson Les Paul Guitars:

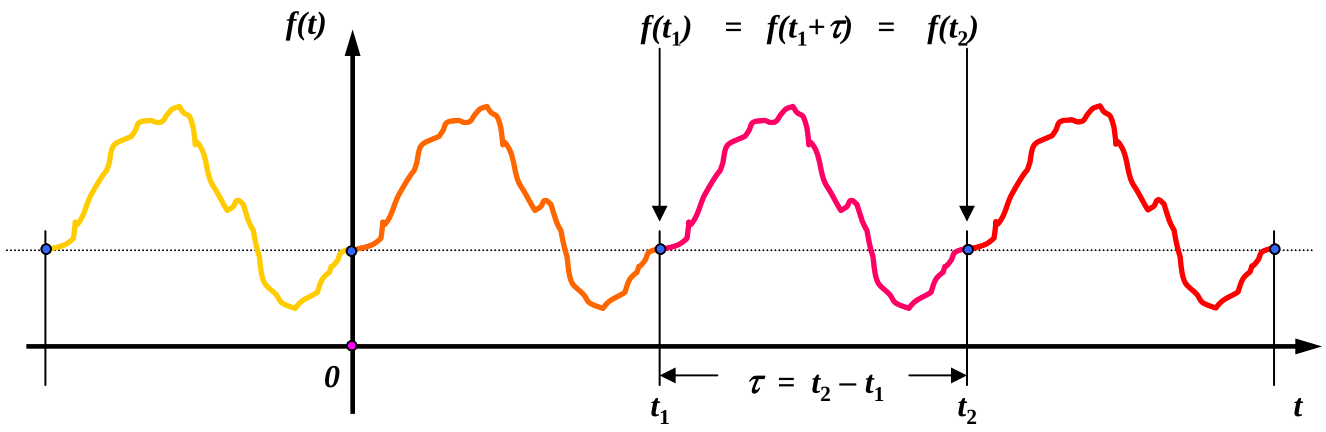




Gibson Firebird Pickups



Fourier {*aka* Harmonic} Analysis of Periodic Waveforms:



$$f(t) = a_o + \sum_{n=1}^{\infty} a_n \cos\omega_n t - \sum_{n=1}^{\infty} b_n \sin\omega_n t \quad (\omega_n = 2\pi f_n, \quad f_n = n f_1)$$

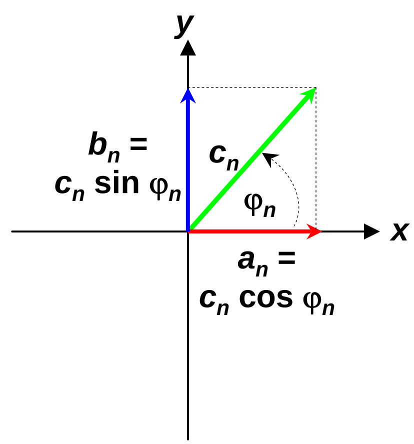
$$a_n = \tfrac{1}{\tau}\int_0^\tau f(t')\cos\omega_n t'\,dt' \quad b_n = \tfrac{1}{\tau}\int_0^\tau f(t')\sin\omega_n t'\,dt'$$

Define: $a_o \equiv c_o \quad a_n \equiv c_n\cos\varphi_n \quad b_n \equiv c_n \sin\varphi_n \quad \varphi_n = \tan^{-1}(b_n/a_n)$

$$f(t) = c_o + \sum_{n=1}^{\infty} c_n\cos(\omega_n t + \varphi_n) = \sum_{n=0}^{\infty} c_n\cos(\omega_n t + \varphi_n) \quad (\omega_o = \varphi_o \equiv 0)$$

$$c_n = \tfrac{1}{\tau}\int_0^\tau f(t')\cos(\omega_n t' + \varphi_n)\,dt'$$

Complexify: $\tilde{f}(t) = \sum_{n=0}^{\infty} c_n e^{i(\omega_n t + \varphi_n)} \quad c_n = \tfrac{1}{\tau}\int_0^\tau \tilde{f}(t') e^{i(\omega_n t' + \varphi_n)}\,dt'$

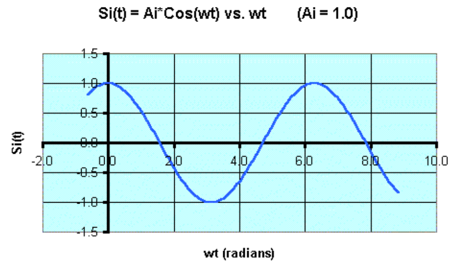


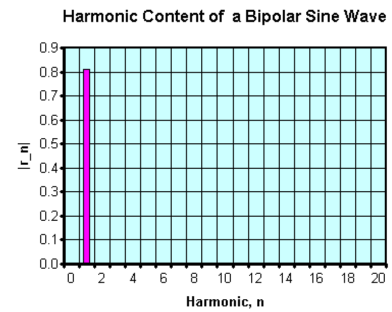
Harmonic Content of "Basic" Musical Waveforms:

⇒ Spatial (or temporal) ***shape*** of periodic waveform ***specifies*** what harmonics are present

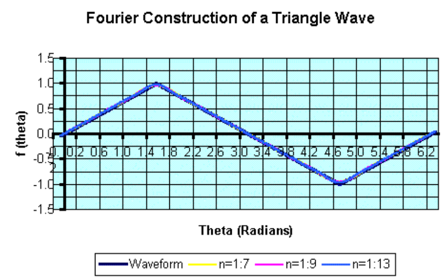
e.g. Pluck a guitar string near bridge (over neck) ⇒ brighter (mellower) sound, respectively

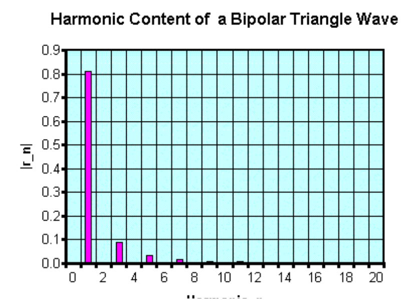
[1] Sine Wave: mellow sound (no harmonics)



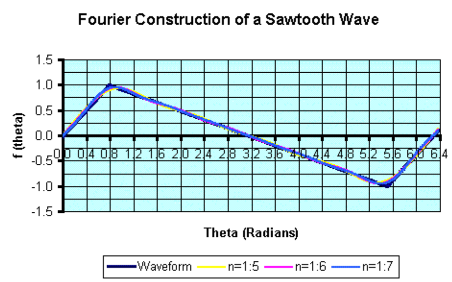


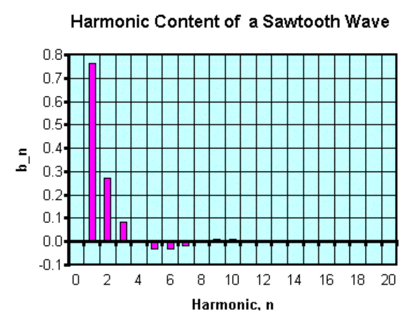
[2] Symmetrical Triangle Wave: A bit brighter sounding (low-order ODD harmonics)



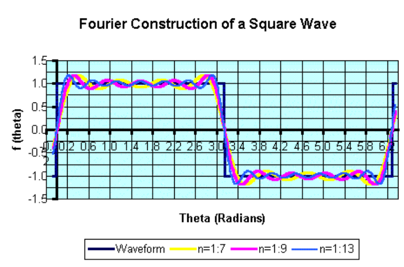


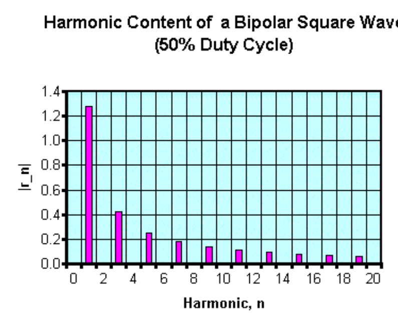
[3] Asymmetrical Triangle Wave: Brighter sounding (has EVEN & ODD harmonics)





[4] Symmetrical Square Wave: Brighter sounding (has ODD harmonics)

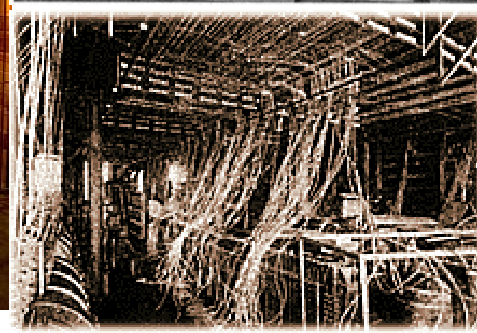




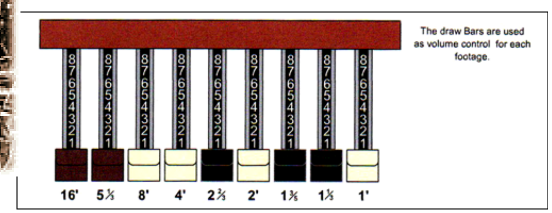
Early Waveform Synthesizers:

Greek Hydraulus (water organ): Ctesibius of Alexandria, 3rd century BCE

Pipe Organs: 2nd century ACE – present



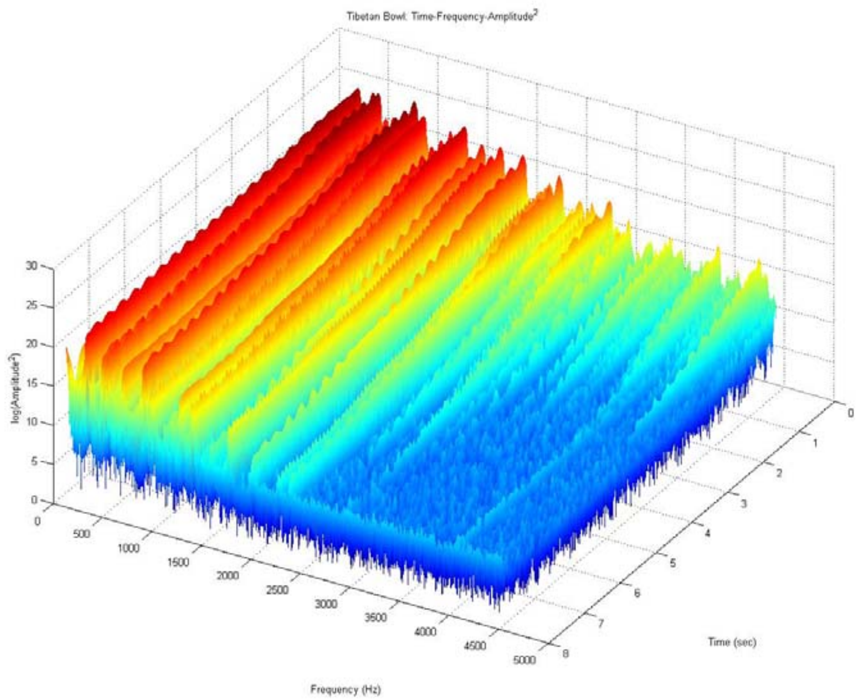
Telharmonium Mk-I,II & III, NYC: Thaddeus Cahill 1897-1916

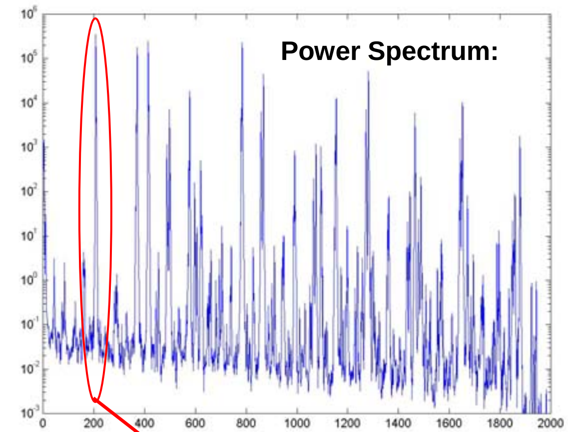


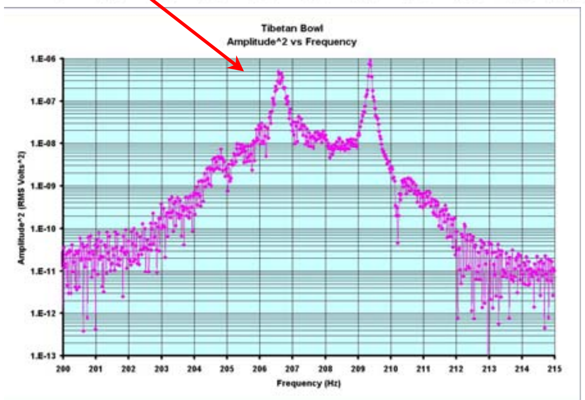
Hammond Organ: 1934 - present

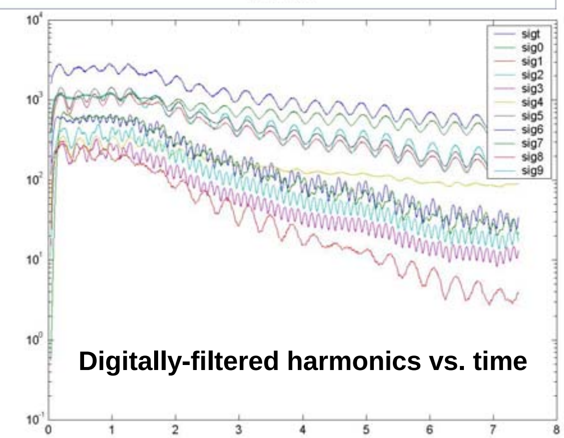
Some Experimental Results from UIUC Physics of Music/Musical Instruments Course(s):

Analyze the harmonic content (amplitude, frequency *and* phase info *vs*. time) of quasi-steady complex sounds produced by musical instruments, human voice, etc. using 24-bit digital audio recorder + reference omni-directional condensor mic ⇒ .wav file – e.g. Tibetan Bowl:



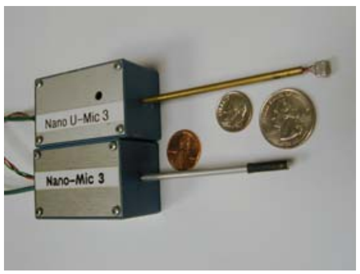


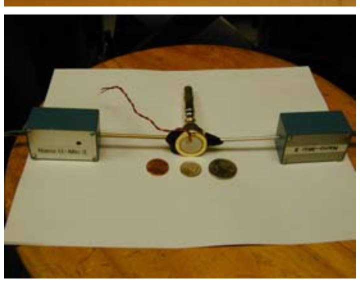


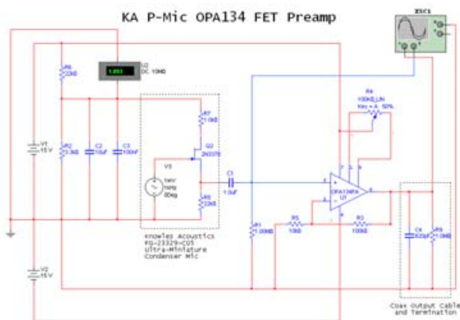


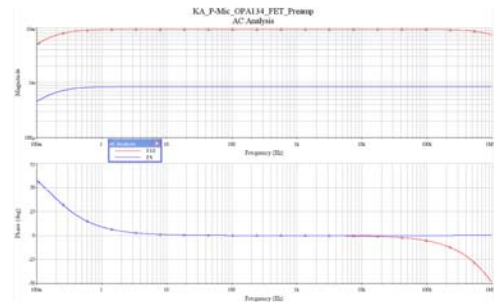
Measurement of Complex Harmonic/Periodic Sound Fields

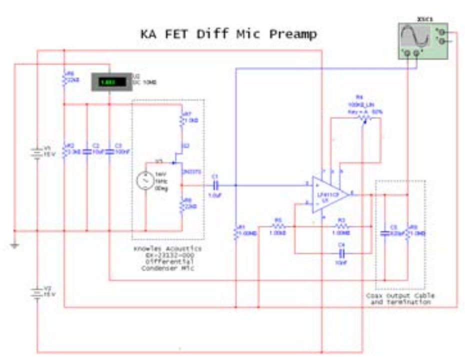
Complex sound field at point in space uniquely determined if simultaneously measure pressure *p* and particle velocity $\vec{u}$ (= <velocity> of air molecules, spatially averaged over an infinitesimal volume element d^3V).

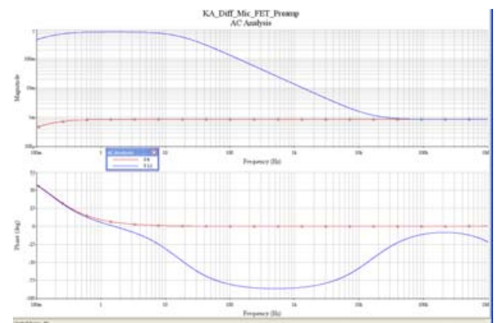












1-D Euler Eqn for *inviscid* fluid flow:

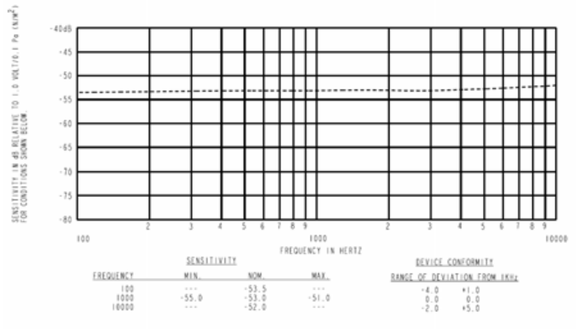
$$\frac{\partial \tilde{u}_z(z,t)}{\partial t} = -\frac{1}{\rho_o}\frac{\partial \tilde{p}(z,t)}{\partial z} \qquad \rho_o = 1.204\, kg/m^3 \text{ for air @ } NTP$$

Integrate:

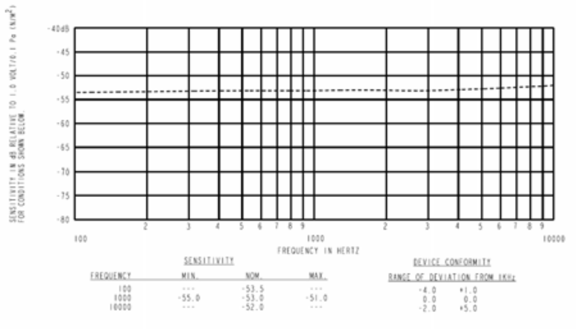
$$\tilde{u}_z(z,t) = -\frac{1}{\rho_o}\int_{-\infty}^{t}\frac{\partial \tilde{p}(z,t')}{\partial z}dt' \simeq -\frac{1}{\rho_o \Delta z}\underbrace{\int_{-\infty}^{t}\Delta\tilde{p}(z,t')\,dt'}_{op-amp\ integrator}$$

Sensitivity & Calibration of Mics

Omni-directional Condensor P-mic



Differential P-mic



Calibrate Mics e.g. in *SPL* = 94.0 *dB* sound field:

$$SPL = 94.0\,dB = 20\log_{10}\left(p/p_{ref}\right) = 20\log_{10}\left(u_z/u_{ref}\right)$$

$$\Rightarrow\ p = 1.0\ RMS\ Pascals,\quad u_z = 2.42\ RMS\ mm/sec$$

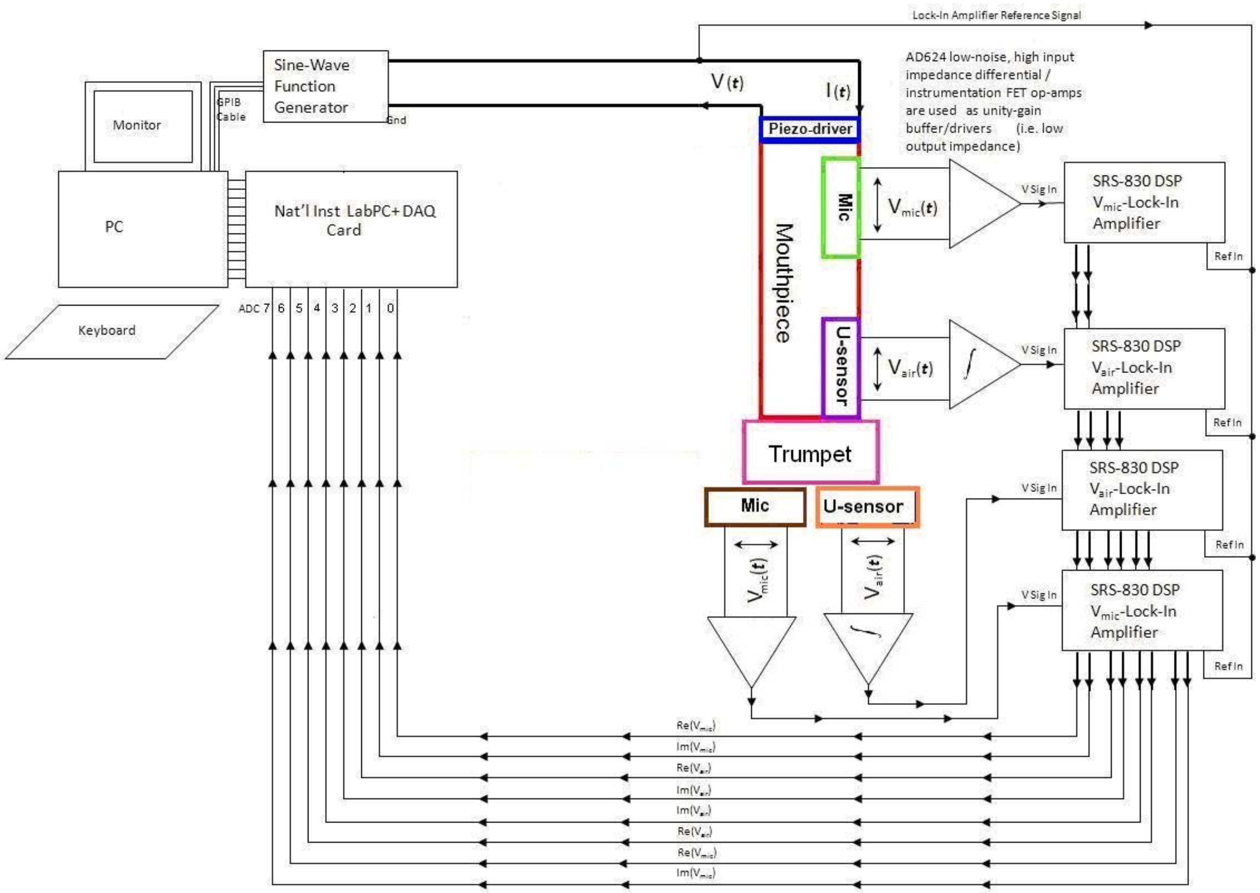
Typical Mic Sensitivities:

$$S_{p-mic} \sim 280\ \ RMS\ mV/RMS\ Pa$$

$$S_{u-mic} \sim\ \ 90\ \ RMS\ mV/RMS\ Pa^*,\quad 1.0\ RMS\ Pa^* = 2.42\ RMS\ mm/sec$$

Extech SPL Calibrator

Block Diagram of PC-Based DAQ System



Lock-in Amplifiers (LIA's) measure the in-phase (="Real") and 90º out-of phase {*aka* "quadrature"} (="Imaginary") amplitude components (w.r.t. reference sine-wave function generator signal, e.g.

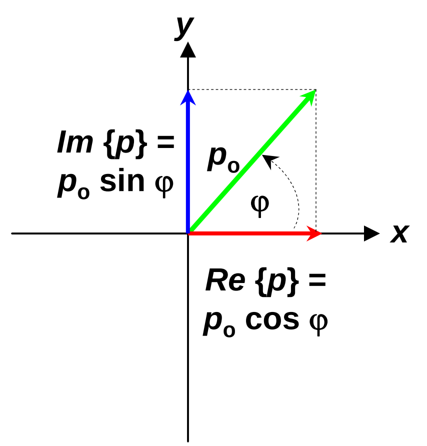
$$p(t) = p_o \cos(\omega t + \varphi)$$

$$= p_o \cos \omega t \cos \varphi$$

$$- p_o \sin \omega t \sin \varphi$$

$$Re\{p\} = p_o \cos \varphi$$

$$Im\{p\} = p_o \sin \varphi$$



Time Domain (*instantaneous* pressure/particle velocity):

Use e.g. Digital Oscilloscope/Digital Recorder to Measure:

$$p(\vec{r},t) = p_o(\omega)\cos\left[\omega t + \varphi_p(\omega)\right]$$

$$u_z(\vec{r},t) = u_{o_z}(\omega)\cos\left[\omega t + \varphi_{u_z}(\omega)\right]$$

n.b. phase-referenced w.r.t. sine-wave fcn generator

Complexify:

$$\tilde{p}(\vec{r},t) = p_o(\omega)e^{i(\omega t+\varphi_p(\omega))} = FT\{\tilde{p}(\vec{r},\omega)\}$$

$$\tilde{u}_z(\vec{r},t) = u_{o_z}(\omega)e^{i(\omega t+\varphi_{u_z}(\omega))} = FT\{\tilde{u}_z(\vec{r},t)\}$$

Compute:

$$\xi_z(\vec{r},t) = \int \tilde{u}_z(\vec{r},t)\,dt = \frac{1}{i\omega}\tilde{u}_z(\vec{r},t)$$

$$a_z(\vec{r},t) = \frac{\partial \tilde{u}_z(\vec{r},t)}{\partial t} = i\omega\tilde{u}_z(\vec{r},t)$$

$$\tilde{Z}_z(\vec{r},t) = \tilde{p}(\vec{r},t)/\tilde{u}_z(\vec{r},t) = I.I.R.(\vec{r},t)$$

$$\tilde{I}_z(\vec{r},t) = \tfrac{1}{2}\tilde{p}(\vec{r},t)\cdot\tilde{u}_z(\vec{r},t)$$

$$= \tfrac{1}{2}p_o(\omega)\cdot u_{o_z}(\omega)e^{i[\varphi_p(\omega)-\varphi_{u_z}(\omega)]}\left[1+e^{-2i[\omega t+\varphi_p(\omega)]}\right]$$

$$= \tfrac{1}{2}I_{o_z}(\omega)e^{i\varphi_{I_z}(\omega)}\left[1+e^{-2i[\omega t+\varphi_p(\omega)]}\right]$$

$$w(\vec{r},t) = \frac{1}{4\rho_o c^2}\left|\tilde{p}(\vec{r},t)\right|^2 + \frac{1}{4}\rho_o\left|\tilde{u}_z(\vec{r},t)\right|^2$$

Frequency Domain:

Use e.g. LIA (and/or Spectral Analysis Techniques) to Measure:

$$\tilde{p}(\vec{r},\omega) = p_o(\omega)e^{i(\omega t+\varphi_p(\omega))} = FT\{\tilde{p}(\vec{r},t)\} \quad \{Pascals\}$$

$$\tilde{u}_z(\vec{r},\omega) = u_{o_z}(\omega)e^{i(\omega t+\varphi_{u_z}(\omega))} = FT\{\tilde{u}_z(\vec{r},t)\} \quad \{mm/sec\}$$

Compute:

$$\xi_z(\vec{r},\omega) = \int \tilde{u}_z(\vec{r},\omega)\,dt = \frac{1}{i\omega}\tilde{u}_z(\vec{r},\omega) \quad \{mm\}$$

$$a_z(\vec{r},\omega) = \frac{\partial \tilde{u}_z(\vec{r},\omega)}{\partial t} = i\omega\tilde{u}_z(\vec{r},\omega) \quad \{mm/sec^2\}$$

$$\tilde{Z}_z(\vec{r},\omega) = \tilde{p}(\vec{r},\omega)/\tilde{u}_z(\vec{r},\omega) \quad \{Acoustic\ Ohms\,(Pa\text{-}sec/m)\}$$

$$= \tfrac{1}{2}p_o(\omega)\cdot u_{o_z}(\omega)e^{i[\varphi_p(\omega)-\varphi_{u_z}(\omega)]} = Z_{o_z}e^{i\varphi_{Z_z}(\omega)}$$

$$\tilde{I}_z(\vec{r},\omega) = \tfrac{1}{2}\tilde{p}(\vec{r},\omega)\cdot\tilde{u}_z^*(\vec{r},\omega) \quad \{Watts/m^2\}$$

$$= \tfrac{1}{2}p_o(\omega)\cdot u_{o_z}(\omega)e^{i[\varphi_p(\omega)-\varphi_{u_z}(\omega)]} = I_o e^{i\varphi_{I_z}(\omega)}$$

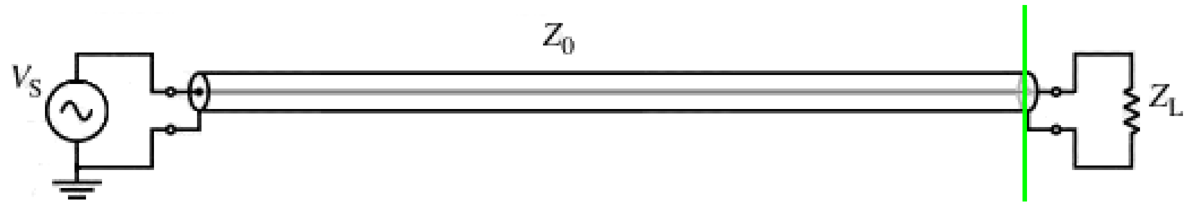
$$w(\vec{r},\omega) = \frac{1}{4\rho_o c^2}\left|\tilde{p}(\vec{r},\omega)\right|^2 + \frac{1}{4}\rho_o\left|\tilde{u}_z(\vec{r},\omega)\right|^2 \{Joules/m^3\}$$

Real part of complex ***I***, ***Z*** associated with *propagating* sound

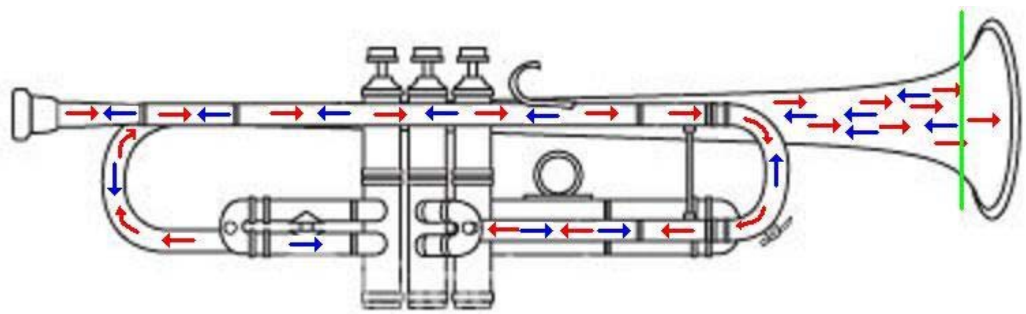
Imaginary part of complex ***I***, ***Z*** associated with *non-propagating* sound energy (e.g. in "near-field" r << λ of sound source, or e.g. in SWT (where **Re{*I*, *Z*}** ~ 0))

Acoustic Impedance analogous to Electrical Impedance

Electrical Impedance $\tilde{Z}_e = \dfrac{\tilde{V}}{\tilde{I}}$



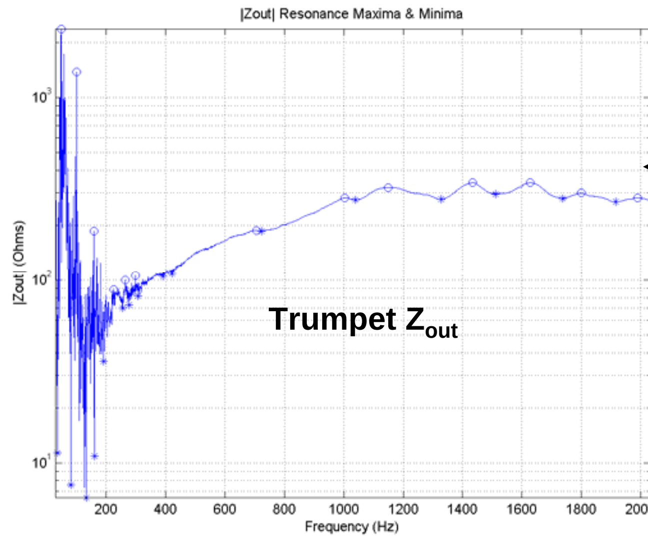
Acoustic Impedance $\tilde{Z}_a = \dfrac{\tilde{P}}{\tilde{U}}$



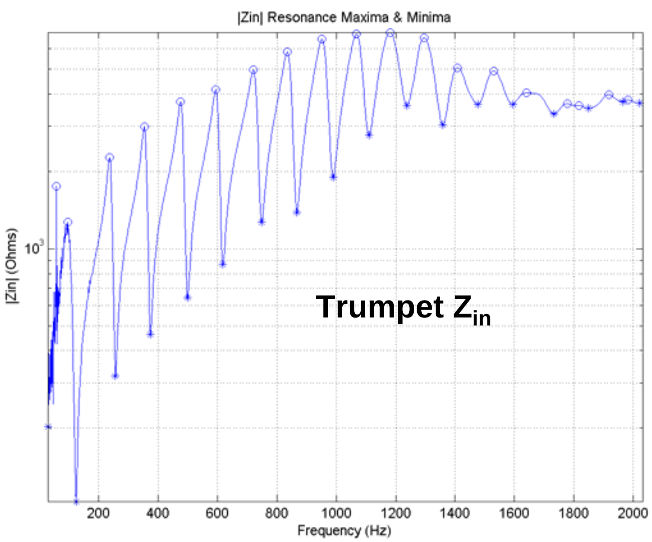
Impedance mismatch @ bell end means wave reflection, constructive interference of standing waves @ mouthpiece reinforces buzzing of player's lips!

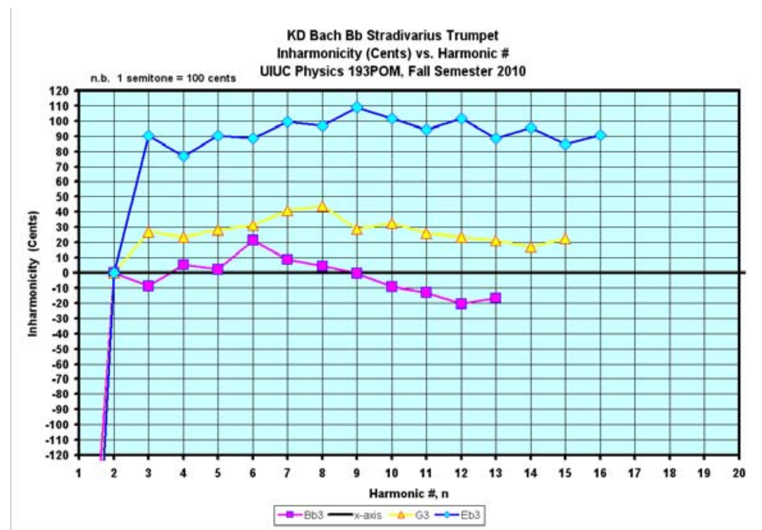
|Zin| maxima (pressure maxima, particle velocity minima occur for constructive interference) corresponds to standing waves, i.e. playable notes!

Measure Input Impedances Z(f) = p(f)/u(f) of Brass/Wind Instruments
$\Rightarrow$ Defines which notes are playable on the instrument:



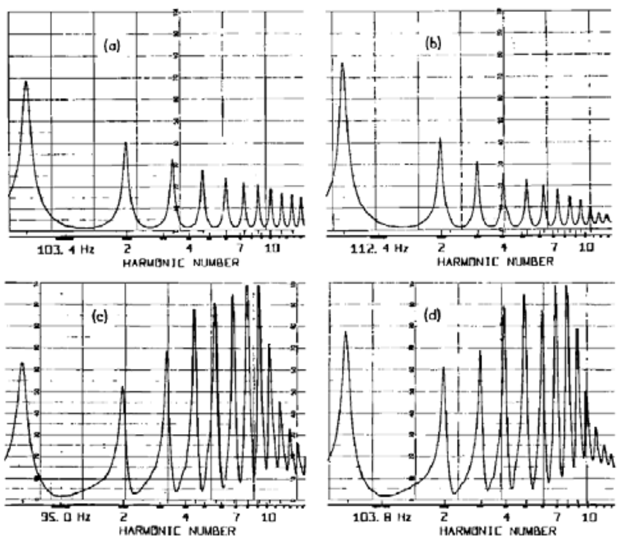
Free-Field
$Z_o = \rho_o c$
~ 415 Ac. Ohms





Acoustical Properties of Individual Components of Trumpet
J. Backus, JASA 60, 460-80, 1976

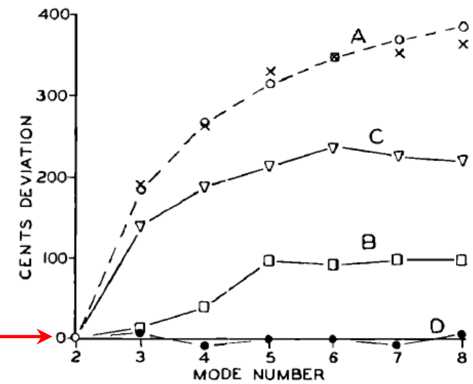
(a) Z (Tubing) **(b) Z (Tubing + Bell)**



(c) Z (Mouthpiece + Leader Pipe + Tubing) **(d) Z (MP+LP +Tubing + Bell)**

FIG. 2. Input impedance curves for (a) a length of cylindrical tubing; (b) tubing plus trumpet bell; (c) tubing plus mouthpiece and leader pipe; and (d) tubing plus bell plus mouthpiece and leader pipe. Full scale is 1000 Ω.

"A miracle occurs!" →



(A) Tubing

(C) Mouthpiece + Leader Pipe + Tubing

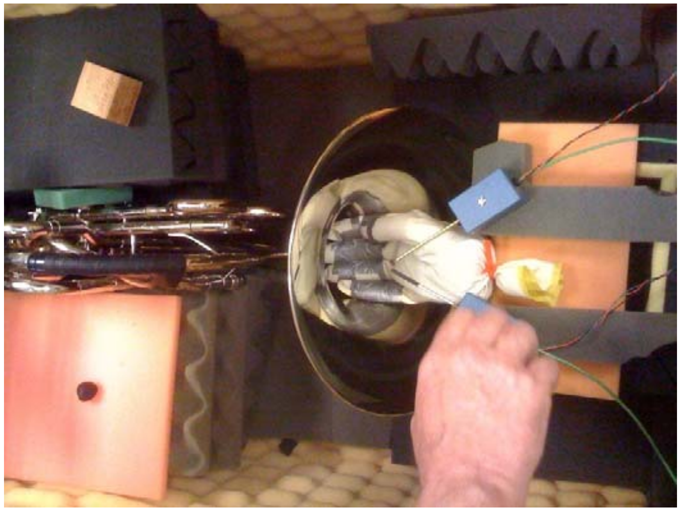
(B) Tubing + Bell

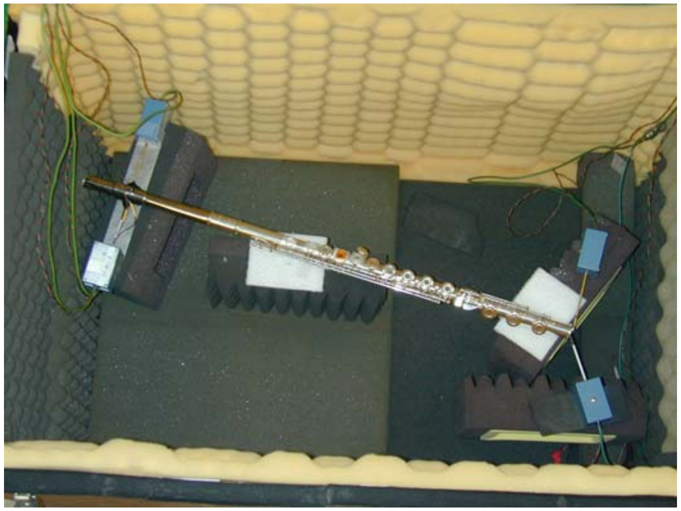
(D) MP+LP +Tubing + Bell

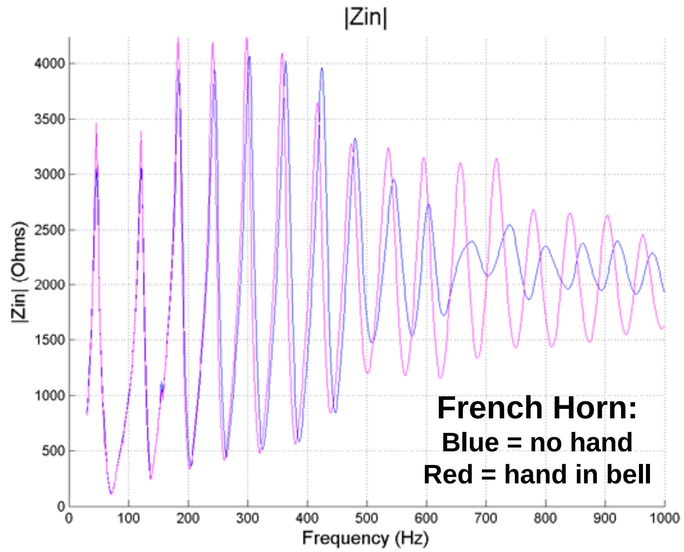
FIG. 3. Plots of the discrepancies in cents between the *n*th resonance and the *n*th harmonic, with the second resonance coinciding with the second harmonic. (a) Cylindrical tubing; (b) tubing plus bell; (c) tubing plus leader pipe and mouthpiece; and (d) tubing plus bell plus leader pipe and mouthpiece.

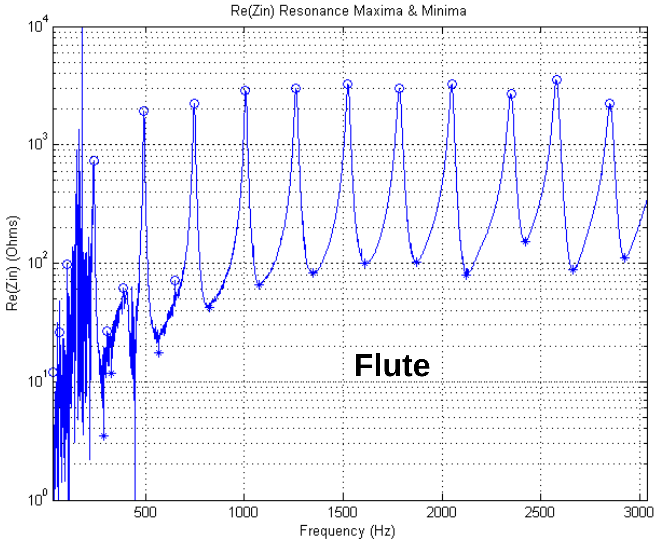
n.b. The design of the trumpet – centuries old instrument {1500 BCE; valves added ~ 1793) {as well as many other musical instruments} didn't have the benefit of the modern scientific knowledge of acoustics that we have today – musical solution(s) arrived at iteratively, by persistent effort(s) !!!

Have Measured Acoustic Properties of {Many Other} Other Brass/Wind Instruments, e.g.

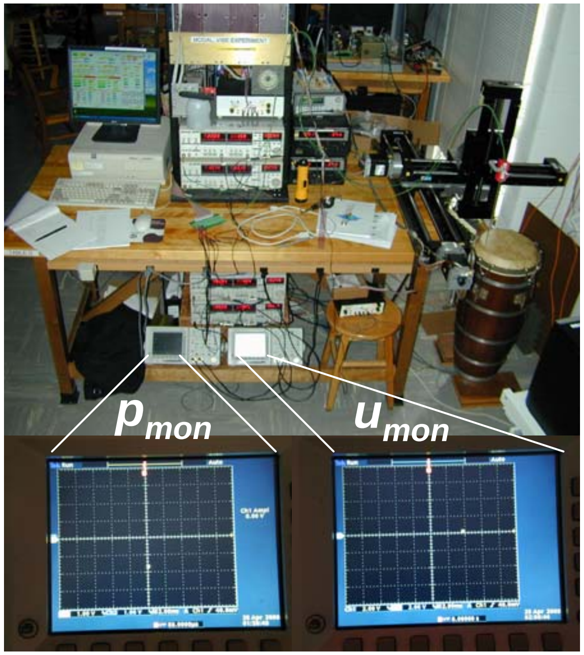




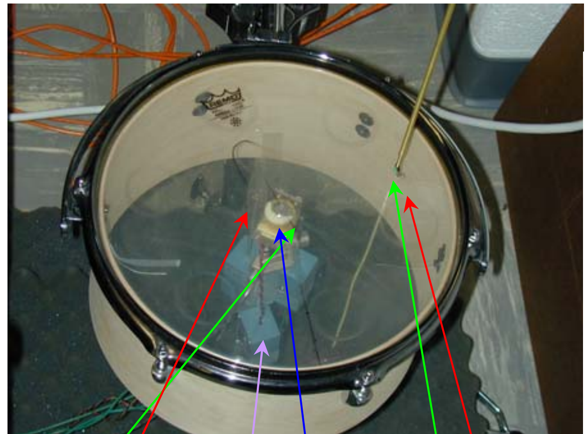




UIUC P498POM Modal Vibes DAQ Experiment: *Phase-Sensitive* Near-Field Acoustic Holography!



p-complex plane   *u*-complex plane

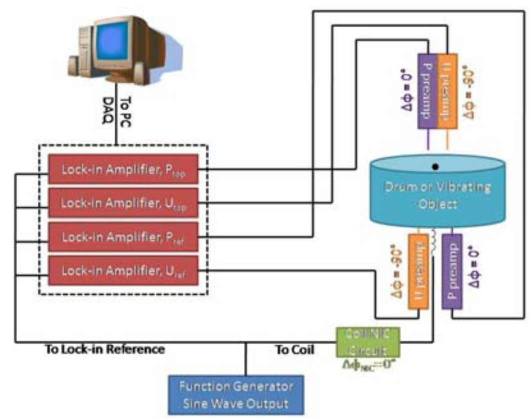


p*, *u **monitor mics**

CC NIC + coil driver + rare-earth magnet pair

p*, *u **scan mics**

Block Diagram of Modal_Vibes DAQ System:

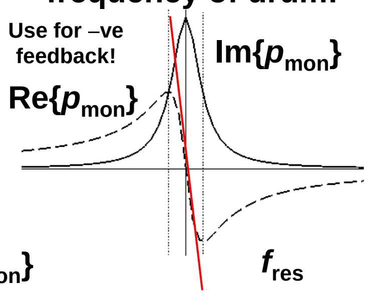


Mode-lock to resonant frequency of drum:

Use for –ve feedback!

Im{p_{mon}}

Re{p_{mon}}

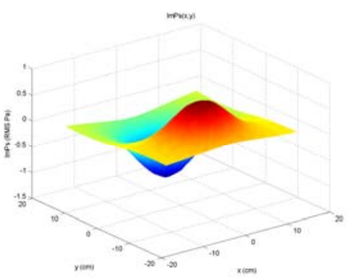


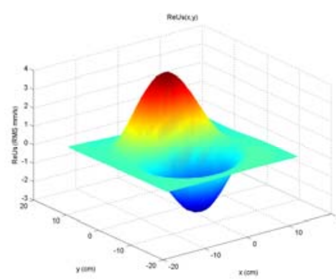
Phase{p_{mon}} f_{res}

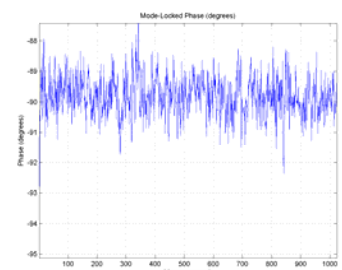
Doumbek:

J_{11} Vibrational Mode of Doumbek:
(32x32 = 1024 scan points, 1 cm step size)

Im{*p*(x,y)}   **Re{*u*(x,y)}**

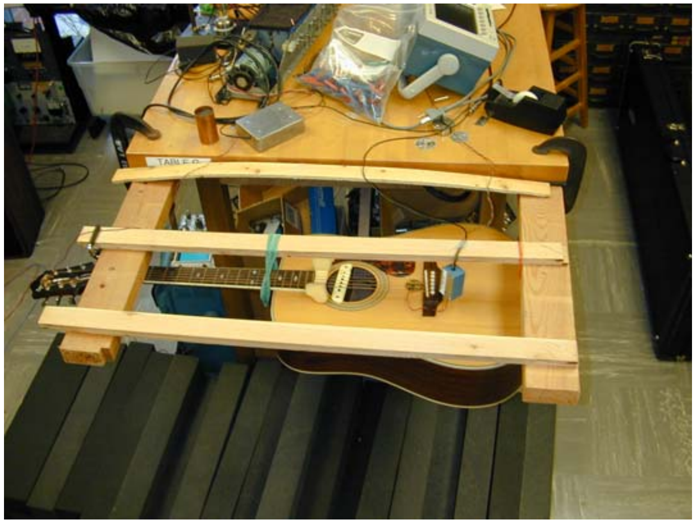


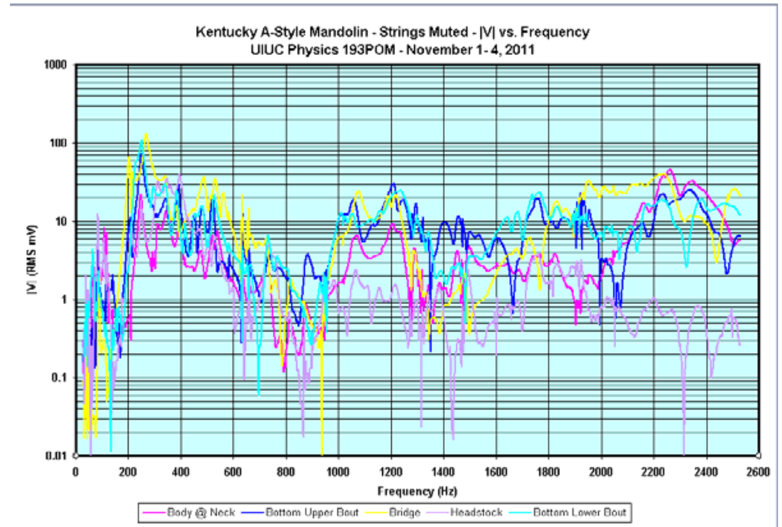


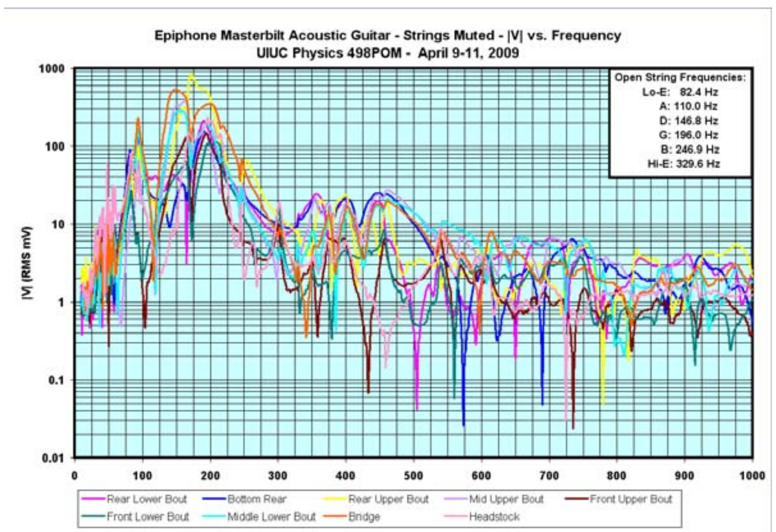


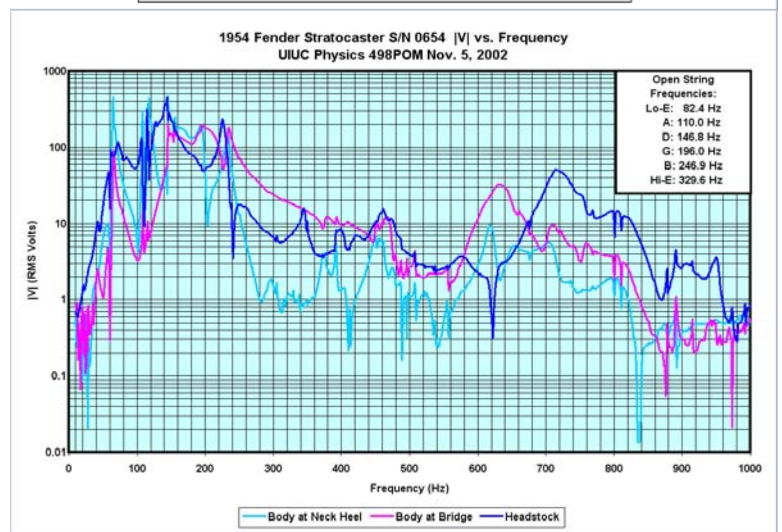
Drums *very* sensitive to ambient temperature changes!

Mechanical Modal Vibrations of Stringed Instruments:



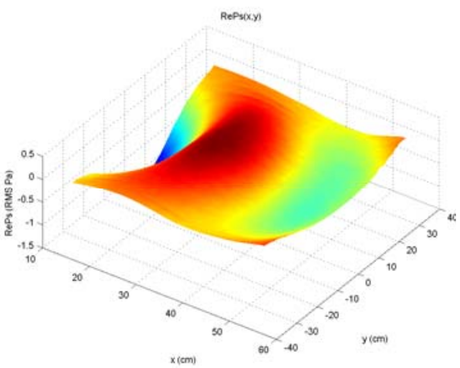




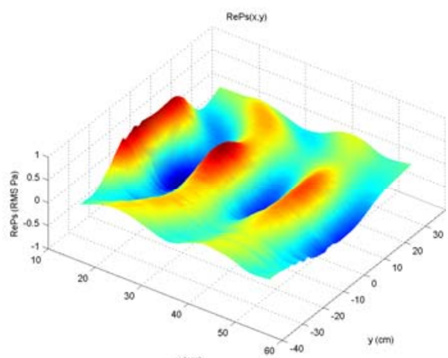


Complex Sound Field of Loudspeakers/Arrays of Loudspeakers:

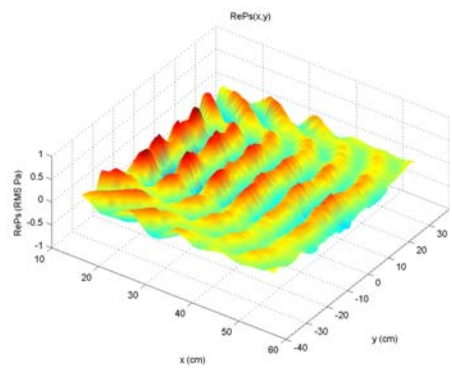
f = 1 KHz



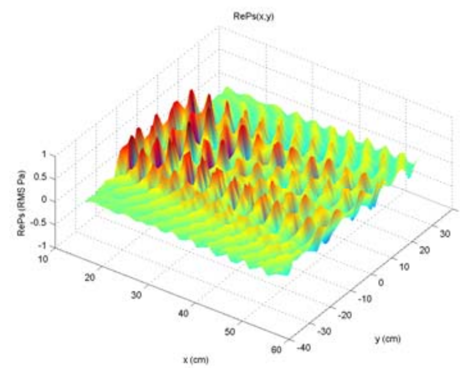
f = 2 KHz



f = 5 KHz

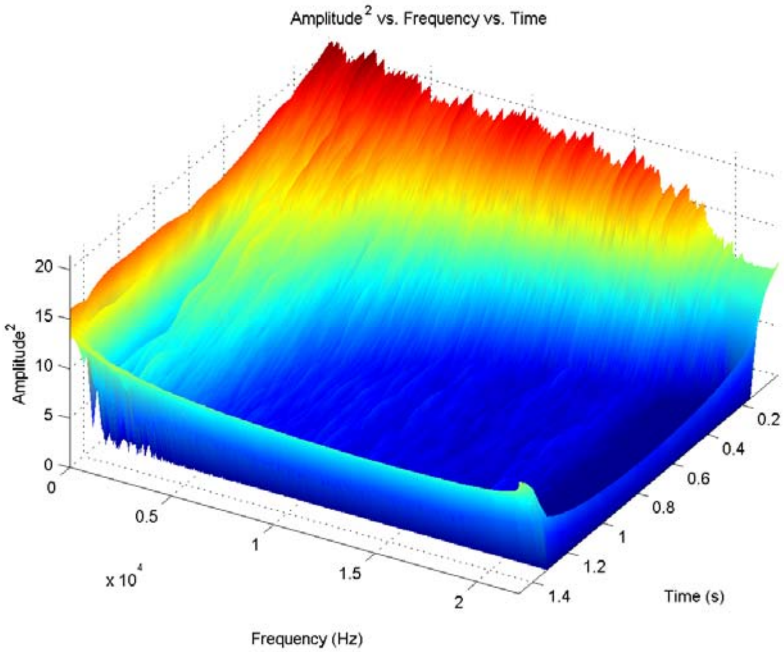


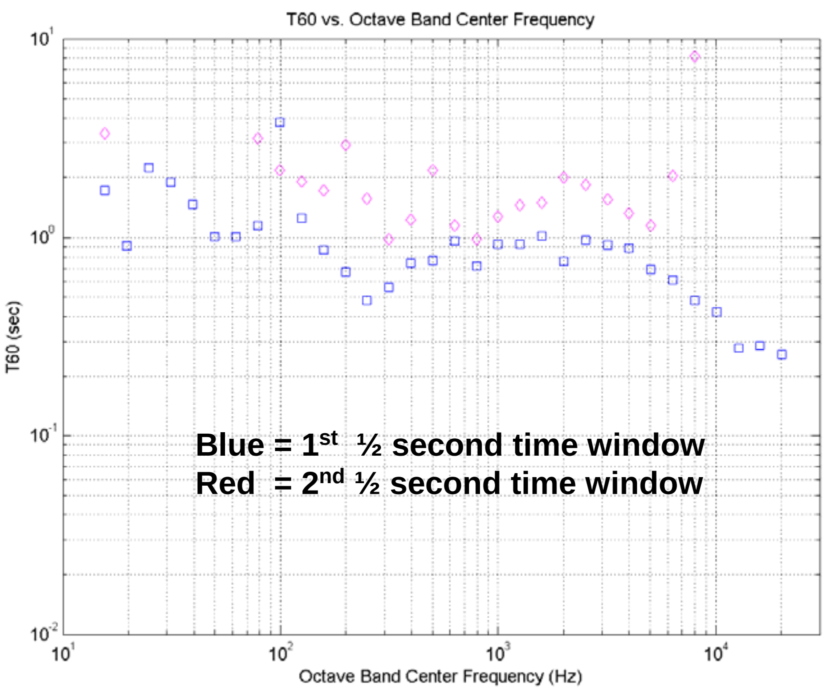
f = 10 KHz



Auditorium/Room Acoustics:

Inject white noise (flat frequency spectrum) into a room, allow it to equilibrate, then adiabatically rapidly shut off sound source and measure exponential decay rate of sound vs. frequency (32 1/3-octave bands):





Recording Studio, UIUC School of Music

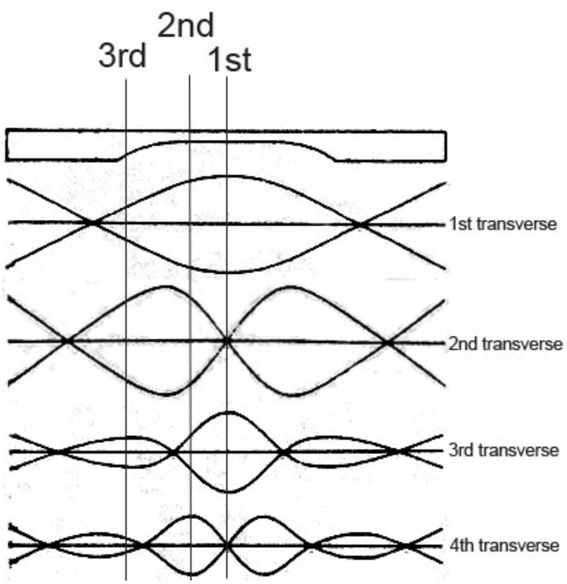
$$T_{60} \equiv -\tfrac{1}{2}\ln\left(10^{-6}\right)\cdot\tau_p \simeq 6.91\tau_p$$

Time for sound to fall to 1 millionth of initial intensity

(ΔSIL = –60 dB = $10\log_{10}(I_{final}/I_{init})$)

Marimba Studies:

Mallet strike location – varies harmonic content/tone:



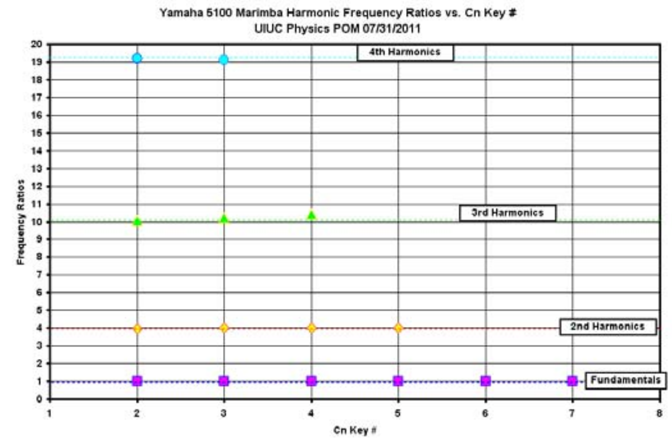
***n* = 1**

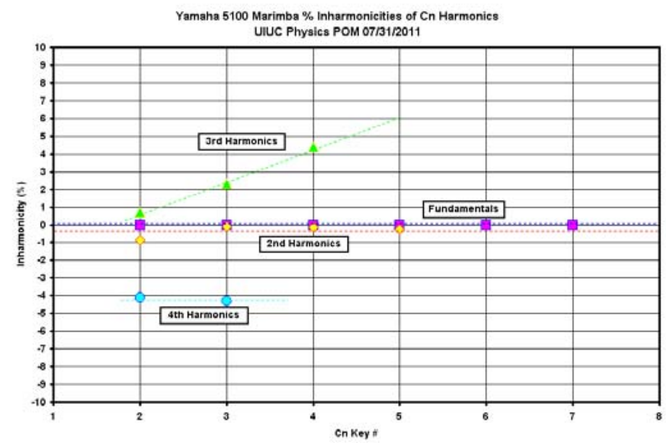
***n* = 4**

***n* = 10**

***n* = 20**

Sculpting of underside of marimba bar tunes bar, and harmonic content: 1 (fund), 4th, 10th & 20th…



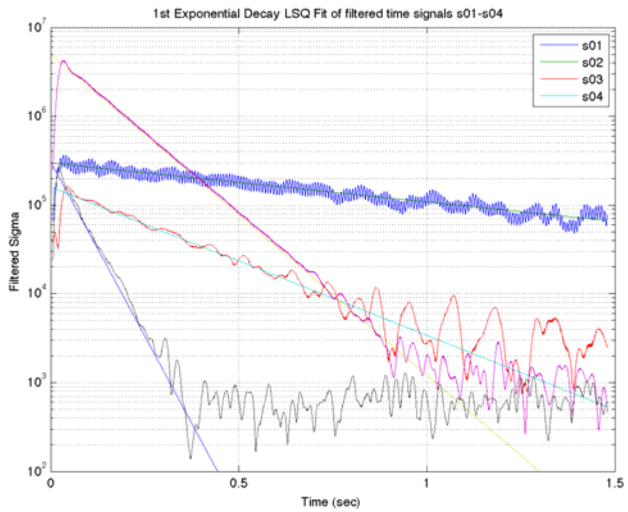


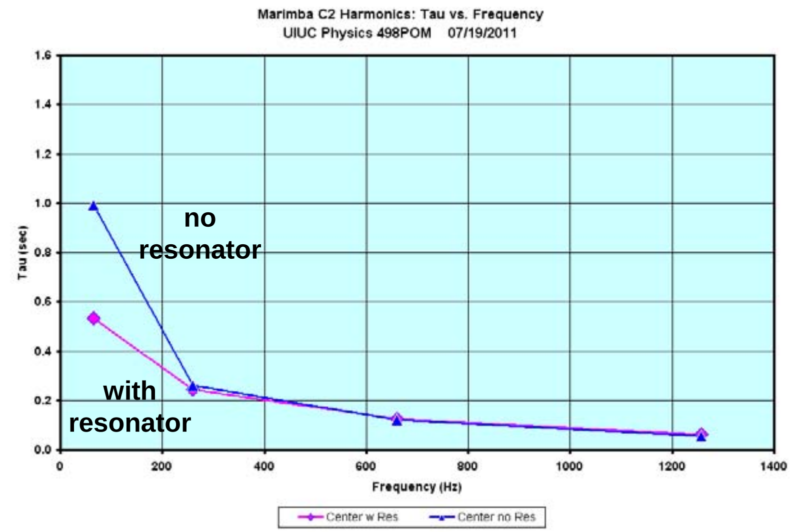
Resonators underneath marimba = open-closed organ pipe, matched to fundamental of each bar.

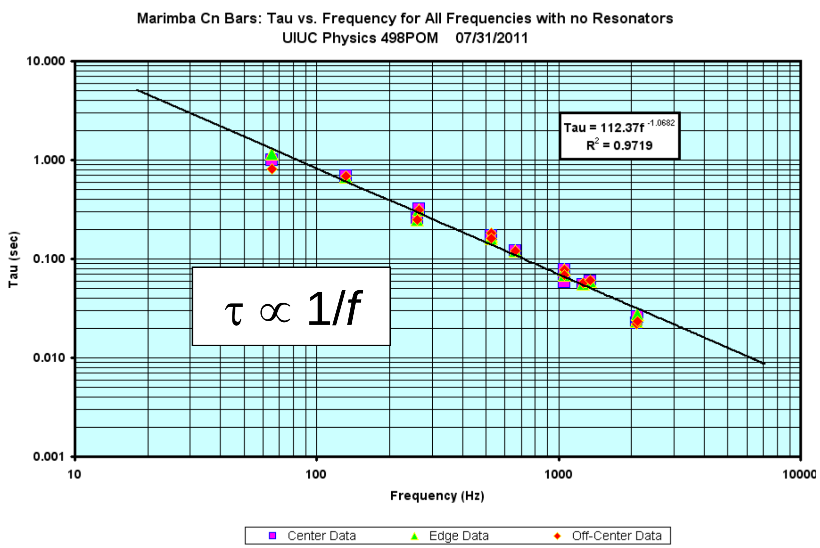
$f_n = nf_1$, n = 1,3,5,7…{odd harmonics}

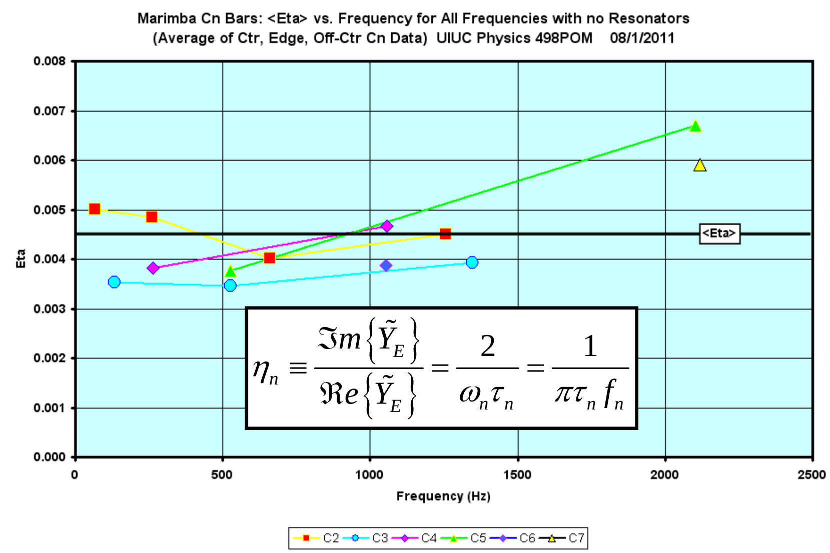
⇒ Boosts fundamental

Marimba Studies – Measurement of the decay time(s) of harmonics of the C_n marimba bars (n = 2:7) and extraction of absorption coefficient η of rosewood









Fun with Spectral Analysis of (Any Kind of/YOUR Favorite) Music: Use e.g. AUDACITY (free-ware)

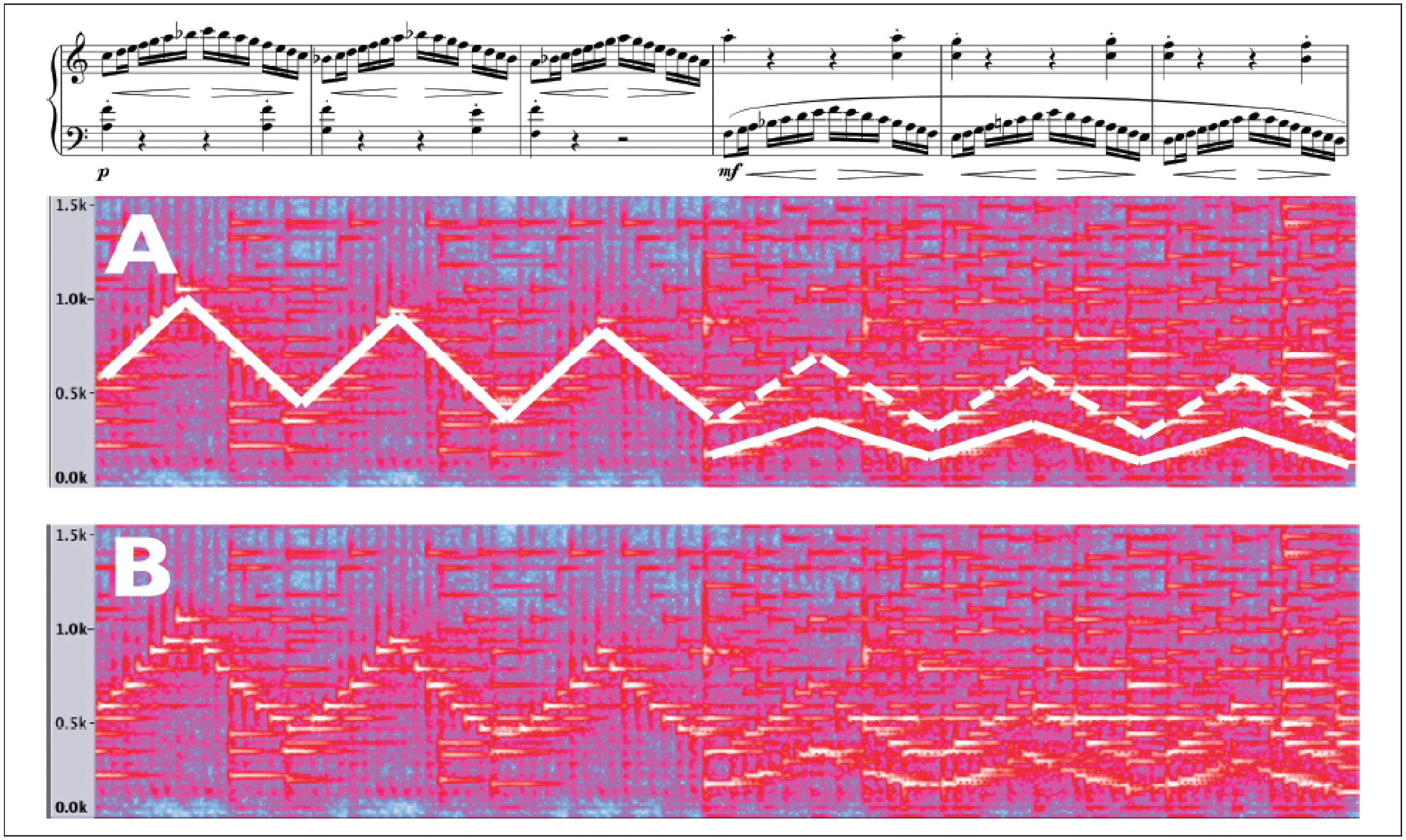


Figure 2. Underneath a standard score view, a spectrogram presents the false transition from Mozart K545. Image (A) is marked to help notice the octaves in unmarked image (B), which presents one reason listeners comfortably adapt to octave jumps. The top image (A) marks the fundamental pitch with a solid white line, which jumps down one octave halfway through the passage. When the line jumps, the dashed line makes clear that the overtone at the octave continues the original line

See e.g. Matthew D. Thibeault paper at: http://gmt.sagepub.com/content/25/1/50

Some Closing Comments:

Nature vs. Nurture: Infants & young children (< 8 yrs) undergo enormous development in their brains – literally wiring the connections in their brains in a myriad of ways. Children deprived of sight/vision for any significant length of time (e.g. due to eye infection) are at risk of life-long adverse impact because of this. Presume similar/analogous adverse effect(s) will occur if children grow up in environment completely *devoid* of all music – those brain areas not used for processing of music will be wired for other uses… Would we eventually lose our musical roots? {n.b. We've lost the ability to internally produce vitamin C because of eating fruit in our diet – still internally produce other vitamins, e.g. vitamin D, etc. Our appendix is also a legacy-organ…}

⇒ Importance of music in fostering development of our children, and *synergy* in their education! {n.b. I have quiet consciously/deliberately utilized/relied on/capitalized on the intrinsic human interest/enjoyment/ pleasure in music – using it to get students *excited* about acoustical physics {& science in general} in teaching the physics of music/musical instruments courses at UIUC – it *really* works, amazingly well !!!}

Information Overload: What is the impact – *short* and *long-term* – on us humans (and other creatures) living in the modern-day world, filling our heads 24/7 with overdoses of information & sounds coming at us seemingly from all directions, and at an ever-increasing pace? Think about this in terms of our biological origins… will our heads explode at some point??? Human culture planet-wide is exponentially changing, far faster than human evolutionary time scales…what are long-term implications of this?

The development of new technologies {e.g. fMRI, DNA sequencing, …} in multiple areas of research has led to many exciting discoveries in the past few years, in terms of us gaining a better understanding of the importance of music in our daily lives in the here-and-now, and how this all came about – i.e. our past – *Did* music play an important evolutionary role in our development???

The current picture on this topic is *far* from complete… However, more and more people appear to be getting involved & investigating as more becomes known – the pace is accelerating…. The nature of this subject is such that it requires/would benefit greatly from multi-disciplinary research/collaboration…

***If* intelligent life does exist elsewhere in the universe, would such beings *also* have music in their culture? *If* so, did music also play an important role in their evolution? What would *their* music sound like? Would their musical instruments mimic their own voices, their own internal rhythms?**

Many, many things to think about, investigate & study!

We live in *very* exciting times in this regard {as well as in *many* others}!

If Interested: Suggested/Recommended Books for Further Reading:

- **"*This is Your Brain on Music – The Science of Human Obsession*", Daniel Levitin, Dutton, 2006.**
- **"*The World in Six Songs*", Daniel Levitin, Dutton, 2008.**
- **"*The Singing Neanderthals – The Origins of Music, Language, Mind and Body*", Steven Mithen, Harvard University Press, 2007.**
- **"*The Origins of Music*", Nils Lennart Wallin, Björn Merker, Steven Brown, MIT Press, 2001.**
- **"*Musicophilia – Tales of Music and the Brain*", Oliver Sachs, Alfred A. Knopf, Inc., 2007.**

Website(s) for UIUC Physics of Music/Musical Instruments Courses (if interested):
Freshman "Discovery" Course: http://online.physics.uiuc.edu/courses/phys193/
Upper-Level Undergrad Physics Course: http://online.physics.uiuc.edu/courses/phys498pom/