From The Stone Age to Today: Why Do Humans Love Music, And What Has Physics Got To Do With It?



"Music of the Spheres" by Michail Spiridonov, 1997-98

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Aside from having much fun & joy teaching POM at UIUC for > past decade, in the process of doing this, many related questions of interest (to me) arose, for which I personally had no expertise, and hence initially had no answers for; nevertheless I was strongly motivated {driven?} to find/seek answers to them – I am after all, a <u>physicist</u> – we're profoundly interested in understanding causal why/how relationships/connections...

I want to share & discuss with you – here, today <u>some</u> of these questions & {attempt to} present some answers to them – <u>certainly by no means complete</u> – I am also hoping to interest/motivate <u>you</u> to think about/delve into your own investigations of them – collectively, hopefully progress can be made on answering them!

Q1: Why is our music seeming <u>so</u> universally <u>important</u> to our species? Seems to be <u>genetically</u> imprinted in us! <u>How</u> did this come about, & <u>why</u> did this happen? Have you ever met anyone who absolutely <u>hates</u> music?

Q2: Why/how is it possible to remember entire albums {cd's} of music – even if we haven't played them for decades, playing them back in "real-time" in our heads, hearing everything as clearly as if we are listening to them for real, when we can't e.g. remember the names of people that we've been introduced to at a party, ~ 5 nsec after being introduced to them? Why is our musical memory so <u>strong</u>, relative to "ordinary" memory? Music {somehow} <u>must</u> have been very important to our species in ancient times, since musical memories are <u>so</u> robust! Why is this? How did this happen?

Nature is economical/Nature "gilds no lilies" = smoking gun - points to <u>importance</u> of music in human evolution!

Q3: Why do we feel "better" after listening to or better yet, actively playing music, or e.g. going to church/sunday school & singing songs/hymns with others?

<u>Q4</u>: Our species <u>is</u> unique amongst the totality of life forms extant on this planet. We're the <u>only</u> ones who, apparently are <u>driven</u> to learn/understand the universe in which we live, thus enabling us to master/control our environment... Why/how did this happen? Why are we the <u>only</u> such life form on <u>this</u> planet?

⇒ Did human <u>music</u> {somehow} play an important role in enabling/facilitating us to get to where we are today?

Or is human music just some kind of "<u>auditory cheesecake</u>" e.g. as Steven Pinker (1997) suggests...

<u>Q5</u>: If intelligent life exists elsewhere in the universe, would those life-forms also have music? If so, what would <u>their</u> music sound like? Did their music <u>also</u> play a role in that life-form's development/evolutional history?

From a physics perspective, life on our planet is <u>totally</u> dependent on the <u>constancy</u> of and the <u>strengths</u> of the <u>four</u> fundamental forces of nature that are operative in the universe in which we live:

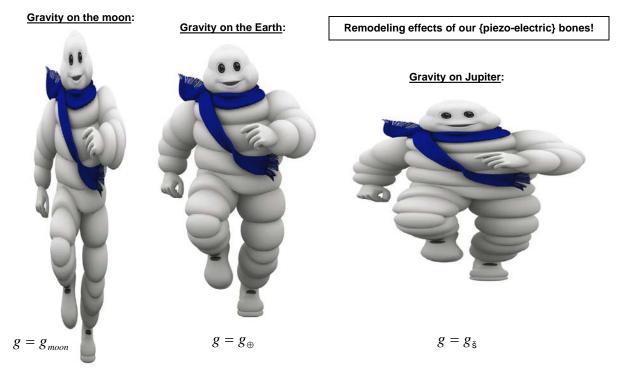
- o <u>Weak Force</u>: Responsible for radioactivity (β -decay) our sun's source of power generation!
- o Strong Force: Binds protons & neutrons together to form nuclei (also important for solar processes!)
- o <u>Electromagnetic Force</u>: Binds nuclei and electrons together to form atoms, atom-atom interactions (molecules, all chemical reactions, electromagnetic & acoustic wave phenomena, all life...)
- o Gravity (curvature of space-time): Binds atoms together to form stars, solar systems/planets, galaxies, ...

Gedanken experiment # 1:

Turn any one force completely <u>off</u> (i.e. coupling constant \rightarrow 0): Life as we know it cannot exist/survive!

Gedanken experiment # 2:

Change the <u>strength</u> of any one interaction (e.g. gravity, or charge(s)) – life as we know it radically changes!





April 29, 2017

University of Toledo POM Talk

Life on our planet is shaped by the fundamental laws of physics operative in our universe:

We live in 4-D space-time (3 spatial dimensions + 1 time dimension) – skeleton of bones + muscles enables locomotion in space-time – evolutionarily very beneficial for our survival – for finding food {& avoiding becoming food...}

We have developed a sense of the rate of passage of time – involves basal ganglia (deep within base of brain), cerebellum & parietal lobe (on surface of right side of our brains) critical areas for this time-keeping mechanism...

We have a 3-D stereoscopic accelerometer/inertial guidance system {Newton's 2^{nd} law F = ma} – pair of semicircular canals for orientation {and maintaining our balance - helps us avoid injury/death} in space. Gravitational acceleration g exists on our planet, tells us the direction up vs. down is...

EM radiation (from our Sun) exists – we have stereoscopic pair of eyes (sensitive only to the <u>visible</u> light portion of EM radiation spectrum) – to navigate in/around/interact with our 3-D environment day/night to find food/avoid becoming food, and also to help avoid physical injuries (e.g. falling)...

We live in a medium {air/water} which supports the propagation of acoustic waves – sound waves – we have stereoscopic pair of ears which enables us to localize sounds in our 3-D environment – helps us navigate in/around/interact with our 3-D environment day/night – to find food/avoid becoming food...

We humans (like many other animals) are <u>social</u> creatures – we are <u>primarily</u> most interested in the sounds that we humans make, are secondarily interested in the sounds that <u>other</u> creatures make (e.g. for finding food/avoiding becoming food) – has implications for the low/high limits of human hearing.

We have vocal chords/voice box – a biological mechanism for producing sound – helps us communicate with/find others of our species – evolutionarily very beneficial for our survival {we're a <u>social</u> species of animal}, group hunting for food/avoiding becoming food...

We have senses of taste & smell – tell us which food(s) <u>are</u> good/safe to eat, which food(s) are <u>not</u> good/safe to eat... n.b. wired into our emotional centers... Sense of smell also useful for finding food/avoid becoming food...

Skin (our largest organ) contains nerves – for sense of touch, pain & thermo-receptors – helps us avoid damage/injury to our bodies/death...

Nature makes amazing very effective/economical use of many physics processes operative in our world:

Some animals can see in the UV and IR portions of the EM radiation spectrum, some animals have 4-color vision...

Sunlight from sky is partially polarized by Rayleigh scattering – vision in some animals (birds & fish) make use of *polarized* light – e.g. for navigation and/or finding food...

Some animals glow in the dark - i.e. emit visible light! Some animals can dramatically change colors (have chromophores)!

Some {deep-sea} life-forms based on sulfur chemistry, instead of carbon-based!

Anerobic bacteria living in soil/rock of our planet – to depths 100's -1000's of meters below surface of earth!

Some animals sensitive to electric and/or magnetic fields. Fish/sharks sensitive to E-fields – useful for finding food. Electric eels/rays stun prey; birds use B-field of earth for navigation, –ve ions in air (earth's E-field electrode layer @ surface of earth) important for plants (& animals)...

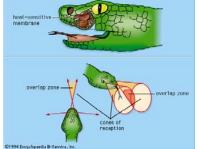
Some animals use infrasound or ultrasound for communication {ultrasound sonar used for finding food}. Some insects (e.g. grasshoppers) utilize vector particle velocity \vec{u} instead of scalar pressure p for hearing!

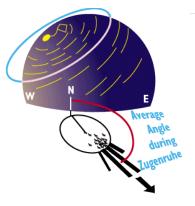
Earth's diurnal rotation – circadian rhythms in living creatures; Some birds {e.g. indigo bunting} use Polaris (North star) for navigation/migration!









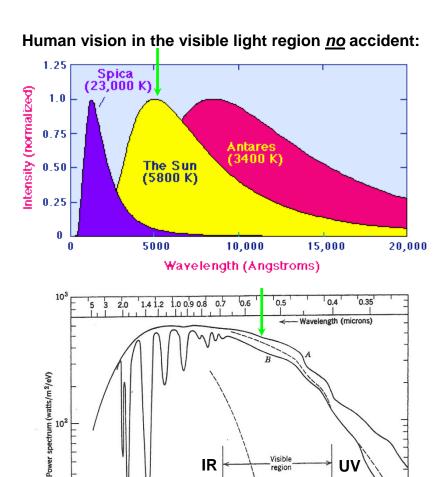


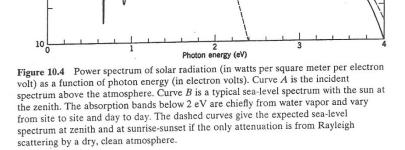
Simply astounding !!!

⇒ Important for recognizing / detecting life-forms elsewhere in universe?



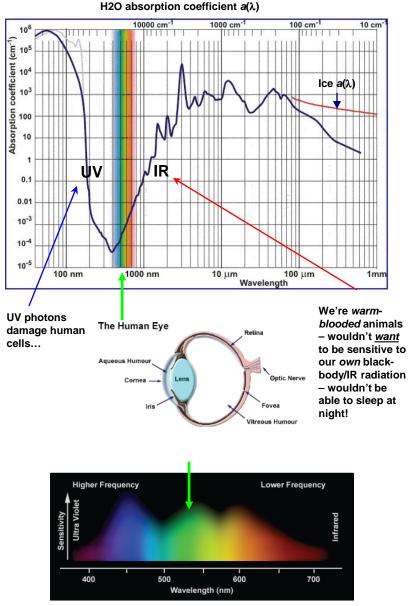
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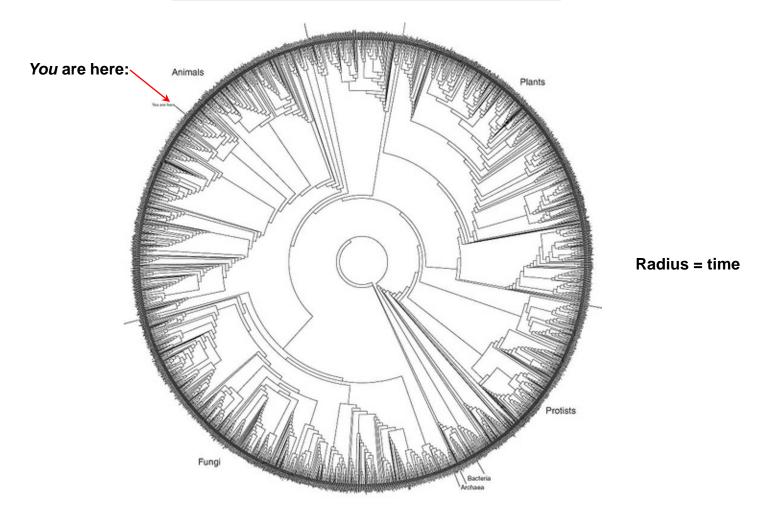
Red

Violet



Typical spectral response of human eye

The {Vast} Tree of Life on Planet Earth:



The Human Tree of Life:

Age (million

years ago)

0.4

0.6

1.0 -

1.2 -

1.4 -

1.6 -

1.8 -

Europe

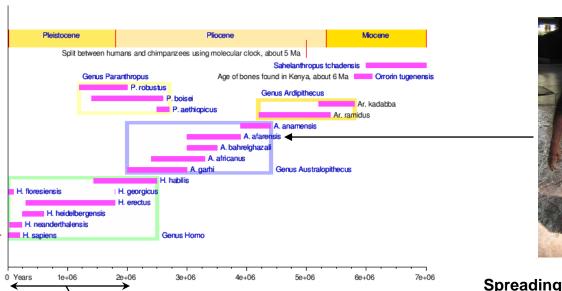
Homo

antecessor/

mauritanicus

ergaster

Homo neanderthalensis



Africa

Homo sapiens

rhodesiensis

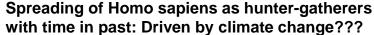
Asia

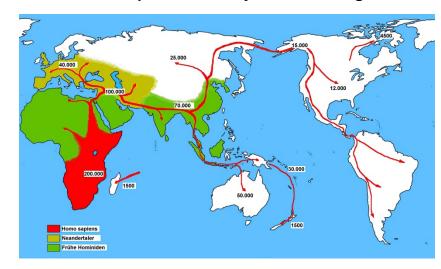
Homo

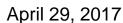
erectus

Americas

Australopithecus
afarensis (2.9-3.9
Myr ago) – had
developed
bipedalism, but
lacked the large
brain that modern
humans have today







Homo sapiens

originated in

East Africa ~

200,000 years

ago

⇒ We're literally

the "new kids on

the block", from a geological

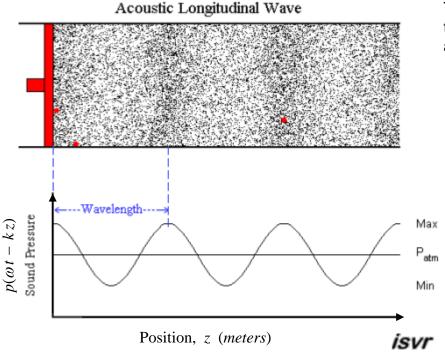
perspective!

The Evolution of Homo Sapiens As Relevant to the Development of Human Language & Music:

- Long ago, our (hairy) ancient ancestors in Africa {n.b. <u>social</u> creatures!} came down out of the trees began living on the ground savannah (grasslands) as hunter-gatherers likely driven by climate change (???)... Insufficient food (+ water) resources in the trees, but food (+ water) resources more plentiful on ground (???)
- Our ancestors began walking *upright*... evolutionarily advantageous/beneficial for life on the savannah...
- However, it's <u>much</u> hotter living on the ground than in the trees!!! Hairy animals must <u>pant</u> in order to cool off! Our ancestor's hair follicles evolved over time into <u>sweat glands</u>, losing much of their body hair...
- If have sweat glands ⇒ now humans don't have to **pant** in order to cool off can use evaporative cooling FX of sweat!!!
- Homo Sapiens evolved to excel at <u>long-distance running</u> success in social groups of humans doggedly chasing down and killing much faster-running <u>hairy</u> prey to their <u>exhaustion</u>, by their <u>over-heating</u> from the exertion of being chased.
- Long-distance running in turn served as a evolutionary force for improved/stronger-pumping heart & more efficient vascular system, providing ~ 3x greater blood flow to human brain, in turn resulting in larger/more complex brain, greater intelligence.
- If humans no longer have to <u>pant</u> to cool off, this in turn also opens up possibilities for evolutionarily-beneficial changes to the <u>human voice box</u> over millennia, the location of our voice box dropped from initially high up in our throat to lower down, today facilitated improved ability to produce wider range/kinds of vocalization(s) hence facilitated development of language & communication amongst members of a human social group e.g. for enhanced success in collaborative/collective hunting, etc...
- Humans today have a sophisticated voice box + <u>hyoid bone</u> our lower-positioned voice box/larynx works in unison with our tongue enables a *rich* complexity/versatility in producing vocal sounds e.g. vowels & consonants, and singing!
- Human *hyoid bone* developed ~ 300 Kyrs ago (Homo heidelbergensis)...
 - ⇒ Facilitated the development of a more sophisticated human language...
 - ⇒ Facilitated the development of music the human voice = *the* 1st musical instrument!

Production of Sound

A mechanically vibrating object e.g. in air (or water) transfers energy to air (or water) molecules in proximity to vibrating object. These molecules subsequently elastically collide with other molecules – a sound wave/acoustic wave is created:

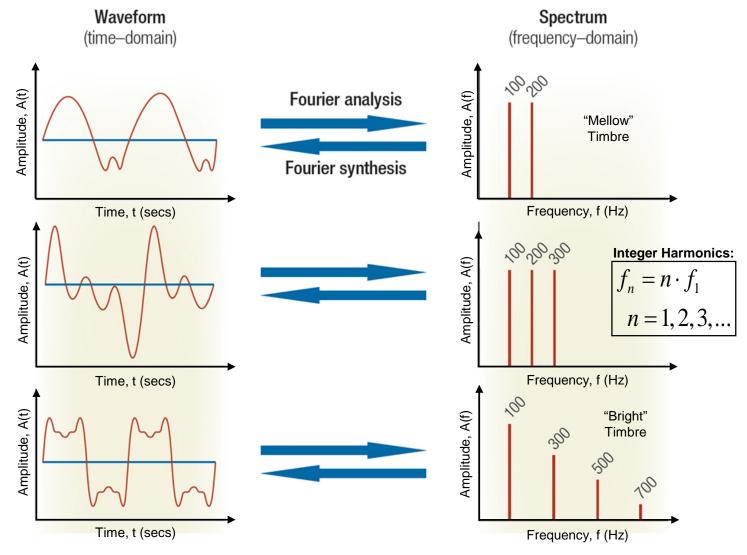


The spatial-temporal (z, t) dependence of an acoustic traveling plane longitudinal pressure wave – consisting of a single frequency – can mathematically be written as:

$$p(z,t) = p_o \sin(\omega t - kz)$$
 (SI units: Pascals)

 $p_o = \text{acoustic over-pressure amplitude } (Pascals)$
 $\omega = 2\pi f = \text{angular frequency } (radians/second)$
 $f = \text{frequency } (cycles \ per \ second = Hz)$
 $t = \text{time } (seconds)$
 $\tau = 1/f = \text{oscillation period } (seconds)$
 $k = 2\pi/\lambda = \text{spatial wavenumber } (radians/meter)$
 $\lambda = \text{spatial wavelength } (meters)$
 $z = \text{spatial position } (meters)$
 $v = f \cdot \lambda = \omega/k = \text{speed of sound } (meters/second)$

The <u>Shape</u> of a <u>Periodic</u> Waveform Determines its <u>Harmonic</u> Content:

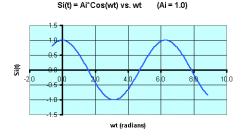


Harmonic Content of "Basic" Musical Waveforms:

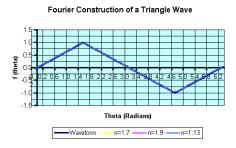
⇒ Spatial (or temporal) <u>shape</u> of periodic waveform <u>specifies</u> what harmonics are present

e.g. Pluck a guitar string near bridge (over neck) ⇒ brighter (mellower) sound, respectively

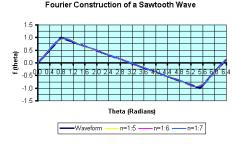
[1] Sine Wave: mellow sound (no harmonics)



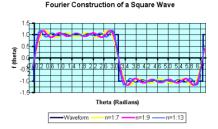
[2] Symmetrical Triangle Wave: A bit brighter sounding (low-order ODD harmonics)



[3] Asymmetrical Triangle Wave: Brighter sounding (has EVEN & ODD harmonics)



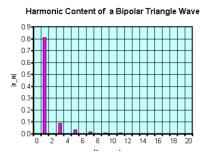
[4] Symmetrical Square Wave: Brighter sounding (has ODD harmonics)

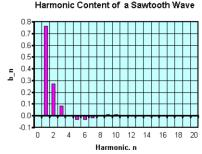


Harmonic Content of a Bipolar Sine Wave

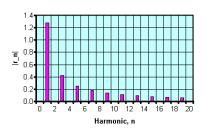
0.9
0.8
0.7
0.6
0.7
0.4
0.3
0.2
0.1
0.0
0 2 4 6 8 10 12 14 16 18 20

Harmonic, n

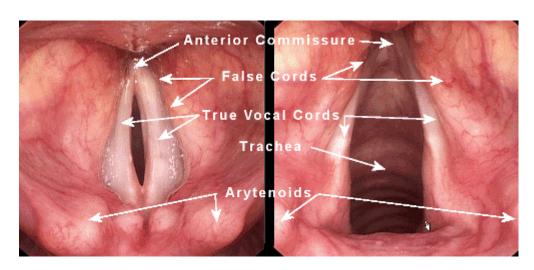


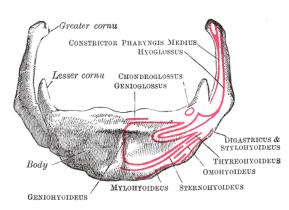


Harmonic Content of a Bipolar Square Wave (50% Duty Cycle)



The Human Voice – The first / earliest musical instrument... unique to each human!





The human <u>hyoid bone</u> (present in many <u>mammals</u>) is <u>unique</u> to Homo sapiens – it enables production of a <u>wide</u> range of sounds that other mammals <u>cannot</u> produce – allowing wider range of the tongue, pharyngeal and laryngeal movements – necessary for human speech (and song)...

⇒ It is NO accident that the musical instruments that we humans have developed mimic the human voice, human rhythms....

When singing (& talking), the human vocal cords vibrate as a <u>1-D system</u> (e.g. like a guitar string) – production of <u>integer</u> related harmonics of fundamental, f₁ (Hz):

$$f_n = nf_1$$
 $n = 1, 2, 3,$

n.b. If we instead had e.g. a <u>2-D circular</u> <u>membrane</u> for producing musical sounds, would *not* have such a relation:

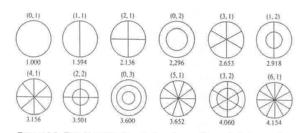


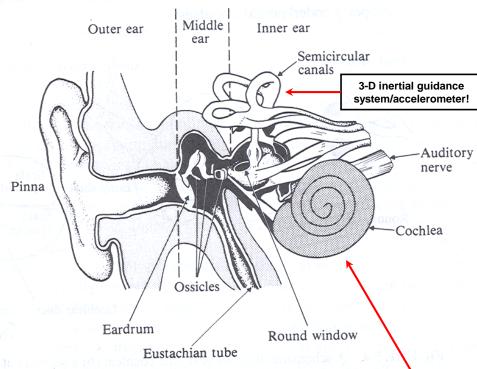
FIGURE 3.6. First 14 modes of an ideal membrane. The mode designation (m,n) is given above each figure and the relative frequency below. To convert these to actual frequencies, multiply by $(2.405/2\pi a)\sqrt{T/\sigma}$, where a is the membrane radius.

Wave Equation in 3-D:

$$\begin{split} & \nabla^2 p\left(\vec{r},t\right) = \frac{1}{c^2} \partial^2 p\left(\vec{r},t\right) \Big/ \partial t^2 \\ & f_{\ell m n}^{3-D} \propto \sqrt{\alpha \ell^2 + \beta m^2 + \gamma n^2} \quad \ell, m, n = 1, 2, 3 \dots \end{split}$$

This mathematical physics fact has <u>important</u> / <u>profound</u> consequences for the development of music and musical instruments by humans....

Human Hearing:



Pinna acts as ~ parabolic collector of sound

Mechanical amplification factor of

ear drum \Rightarrow ossicles (~ 1.3) \Rightarrow oval window ~ 26×

(A_{ear drum}/A_{oval window} ~ 20)

<u>Resonances</u> in the auditory canal (~ 2 cm long ~ open-closed organ pipe) boost ear's sensitivity in the ~ 2 - 5 KHz range

n.b. also explains e.g. midrange hearing loss due to excessively loud rock music...

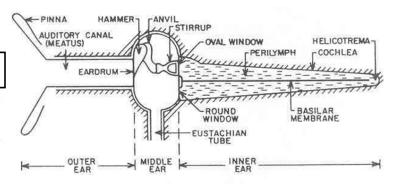
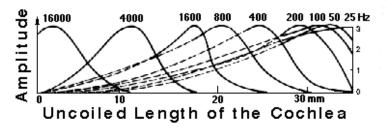


Fig. 1. Schematic diagram of the human ear, with the cochlea uncoiled.

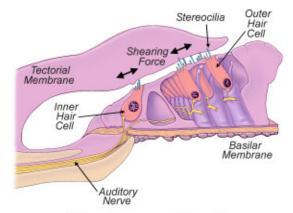


Nonlinear relationship between max amplitude A(f) vs. location along cochlea.

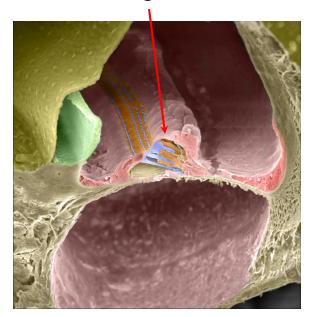
n.b. The <u>spiral</u> shape of the cochlea boosts sensitivity to low frequencies by ~ 20 dB ($\sim 100x$ in amplitude)!

D. Manoussaki, et al., Phys. Rev. Lett. 96, 088701 (2006)

The Organ of Corti & Inner/Outer Hair Cells, Stereocilia:

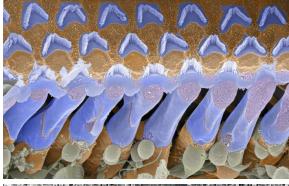


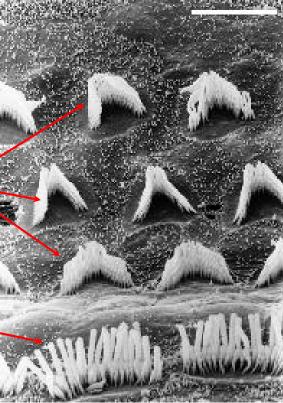
The Organ of Corti



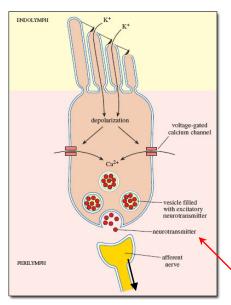
A triple-row of ~ 12,000 chevron-shaped <u>outer</u> hair cells – via their stereocilia act as <u>biological amplifiers</u>, boosting the sensitivity level of human hearing by ~ 40 dB (~ 10000x)!

~ 4000 <u>inner</u> hair cells – via their stereocilia generate the primary auditory signals sent along the auditory nerve to the brain





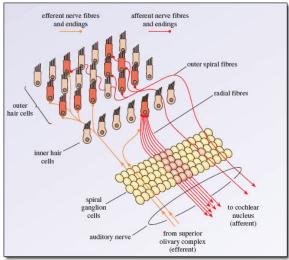
Action of Hair Cells, Auditory Nerve & Auditory Pathway to Brain:



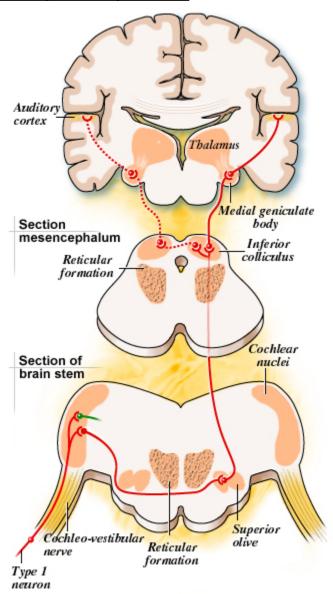
~ 95% of auditory nerve fibers (type I) are connected to ~ 4000 *inner* hair cells, each of which directs its output to up to ~ 10 type I auditory nerve fibers.

Type I auditory nerve fibers are bipolar and are mylenated (i.e. have nerve sheath) – boosts transmission speed of action potentials along nerve fiber by factor of up to ~ 300× over nonmylenated nerve fibers – evolutionarily very important – for our auditory startle reflex!

TRPA1 protein



~ 5% of auditory nerve fibers (type II) are connected to ~ 12,000 outer hair cells, are monopolar and are <u>not</u> mylenated (i.e. slow..)



Monaural Auditory Response to Two Pure Tones, Critical Band:

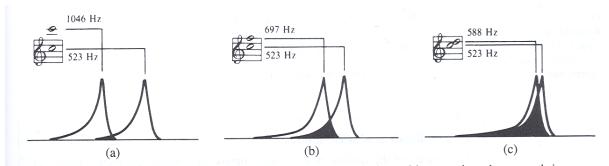
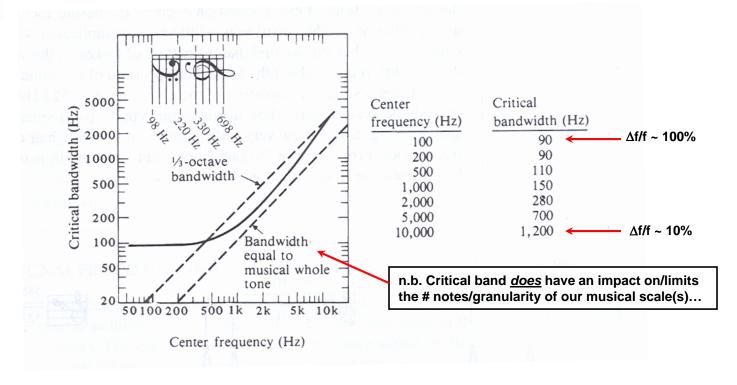
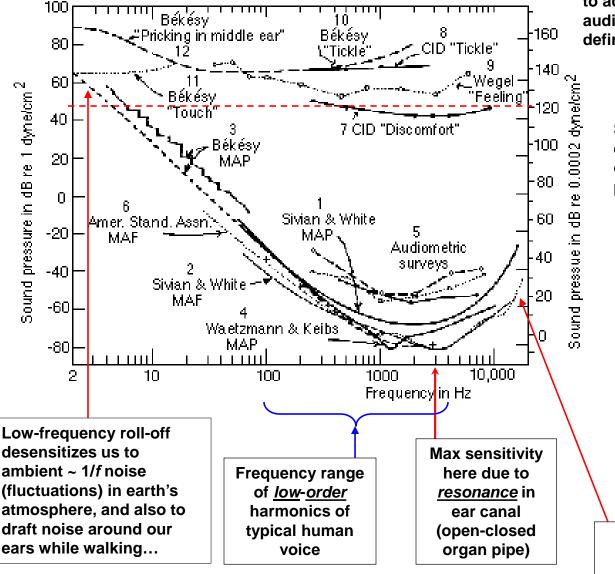


FIGURE 5.9 Frequency response curves for pairs of pure tones. As the interval between them decreases, their response curves show increasing overlap.



Sensitivity of Human Hearing vs. Frequency:



The human ear responds \sim logarithmically to acoustic <u>over-pressure</u>. The minimum audible RMS over-pressure (MAP) is defined at reference frequency f = 1 KHz:

$$p_o(f = 1 \text{ KHz}) = 2 \times 10^{-5} \text{ RMS Pascals}$$

 $SPL \equiv 10 \log_{10} (p/p_o)^2 \text{ deci-Bels } (dB)$

Since $p_{atm} = 10^5$ *Pascals*, humans can detect over-pressure variations of order ~ 1 part in 10^{10} of atmospheric pressure (n.b. dogs ~ $100 \times$ better)!

Corresponding minimum audible longitudinal particle velocity, longitudinal particle displacement and sound intensity at f = 1 KHz are:

$$u_o(f = 1 \text{ KHz}) = 4.8 \times 10^{-8} \text{ RMS m/s}$$

 $\xi_o(f = 1 \text{ KHz}) = 7.7 \times 10^{-12} \text{ RMS m} \leftarrow$
 $I_o(f = 1 \text{ KHz}) = 10^{-12} \text{ RMS Watts/m}^2$

n.b. typical size of an atom \sim few Angstroms (i.e. \sim few \times 10⁻¹⁰ m)!

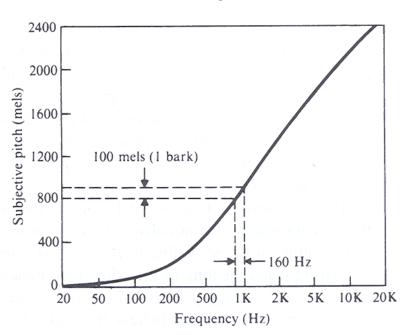
{Bohr radius of Hydrogen atom ~ ½ Angstrom}

Sensitivity at higher frequencies is needed for transients – *intelligibility* of consonants, plosive sounds

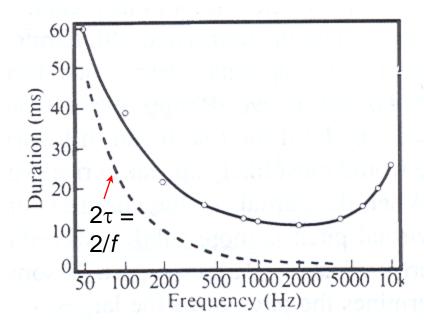
Our Perception of Frequency – <u>Pitch</u> – is {also} Non-Linear:

Only 3 decades of dynamic range in frequency: 20 Hz < f < 20 KHz

Define "units" associated with <u>subjective</u> pitch = **mels** ⇔ analogous to **Hz**.

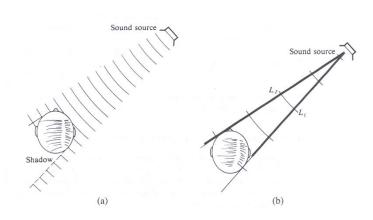


We also require a minimum time duration (min # cycles) in order to perceive a definite pitch:



Binaural Hearing and Sound Localization:

For frequencies between ~ 100 Hz < f < ~ 1.5 KHz, we use inter-aural arrival time difference information Δt (for impulse-type sounds) or equivalently, phase difference information $\Delta \phi = 2\pi \ (\Delta t/\tau)$ for periodic sounds for localizing source(s) of sounds:

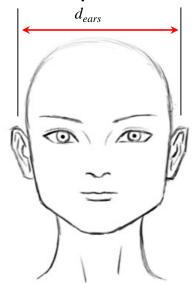


For frequencies above ~ 4 *KHz*, sound localization increasingly relies on sound intensity difference information (JND ~ 1 dB) — Our head casts a sound "shadow" on the "away" side...

At $f \sim 1$ KHz, \triangle SPL (L-R) ~ 8 dB; at $f \sim 10$ KHz, \triangle SPL (L-R) ~ 30 dB or more... Note that this spatial localization "algorithm" fails at <u>low</u> frequencies due to <u>sound</u> <u>diffraction</u> around our heads....

The localization "algorithm" also fails at certain <u>angles</u> and <u>frequencies</u> due to the acoustic analog of the Fresnel /Arago/Poisson "bright spot"!

Typical {adult} ear-ear separation distance is $d_{\rm ears} \sim 15$ cm. Corresponding maximum arrival time difference in air (@ NTP) is $\Delta t \sim d_{\rm ears}/v_{\rm air} \sim 440~\mu$ sec. We can easily localize sounds to within $\sim 5^{\circ}$ in horizontal plane in front of us $\Rightarrow \Delta t_{\rm min} \sim 12~\mu$ sec!



n.b. Human's have extremely difficult time localizing sounds e.g. in water $v_{\rm H2O} \sim 4.4 \times v_{\rm air}$, whereas e.g. dolphins, *etc.* have *no* such problems!

- ⇒ Dolphin hearing optimized for sound propagation in *water*, whereas our hearing is optimized for sound propagation in *air*!
- ⇒ Alien life forms: their hearing will be optimized for specifics of <u>their</u> environment and the sounds they make!

Forward orientation of our pinnae aids us {optimally} in localizing sounds in ~ horizontal plane in front of us (vertical & rearward sound localization degraded as a consequence).

Folds in the pinnae (unique to each human!) <u>enhance</u> our ability to localize sounds in the higher frequency region.

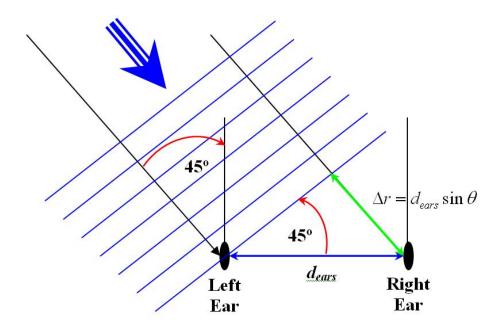
n.b. Long ago, our ancestors used to have *movable* ears (like donkeys)...

Localization of Sounds Using Phase/Inter-Aural Time-Difference Information:

One ear - not sensitive to absolute phase.

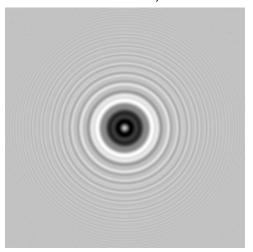
<u>Two</u> ears – sensitive to phase $\{= \text{time}\}\ \underline{differences}$ over frequency range of ~ 100 Hz < f < 1500 Hz.

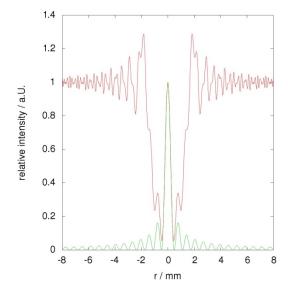
We humans can easily localize e.g. pure-tone/single frequency sounds {in this frequency range} with angular resolution of $\delta\theta \sim 5^{\circ}$, which corresponds to a time diff resolution of $\delta t \sim 12~\mu sec$ {also relevant for impulsive/transient sounds/sound pulses (consisting of a spectral <u>continuum</u> of frequencies)}



Acoustic Analog of the Optical Fresnel/Arago/Poisson Bright Spot:

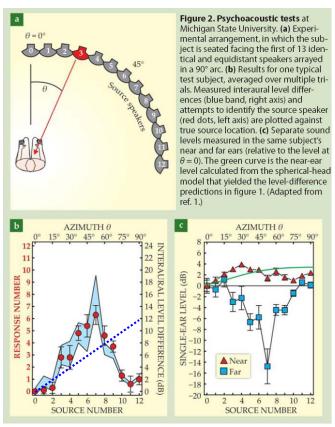
Circular obstacle, d = 1 mm





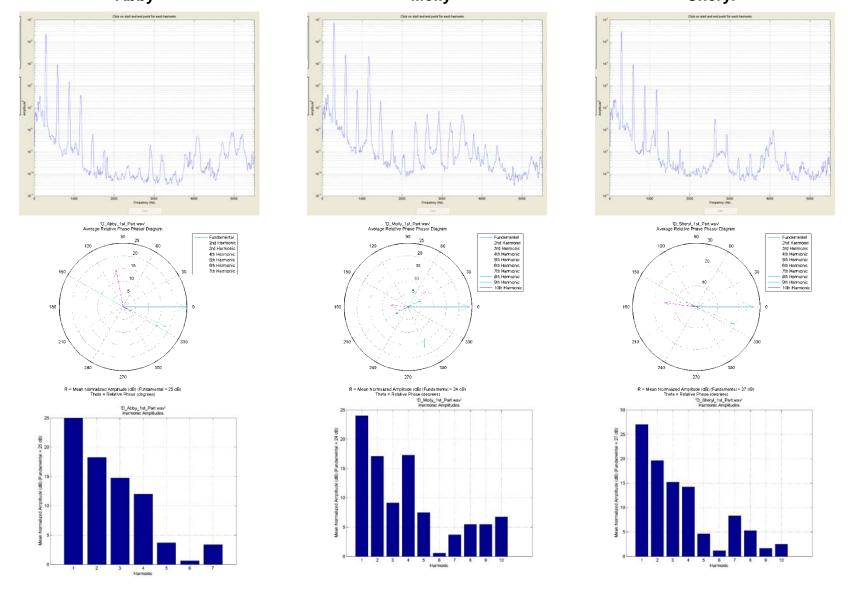
18
16
16
0 4000 Hz
0 3000 Hz
0 1500 Hz
0 500 Hz
0 500 Hz
0 100 Discrete di

Figure 1. Interaural level difference is a logarithmic measure of the ratio of sound intensities from a single source at the hearer's two ears. Calculated from a model of sound-wave diffraction around a spherical head, ILD is plotted, for various puretone frequencies, against the angle θ between the source direction in the horizontal plane and the direction in which the hearer faces. At frequencies well above 4 kHz, where diffraction becomes negligible, the ILD grows almost monotonically with θ and yields reliable source location. But all the curves shown here exhibit nonmonotonic effects of diffraction that can mislead the hearer. The 1500-Hz curve is particularly attractive for psychoacoustic tests of dif-90° fractive deception because itssingle prominent peak almost bisects the angular quadrant. (Adapted from ref. 1.)



Eric Macaulay, et al., (E.M'.s MSU PhD Thesis; former UIUC POM NSF Summer REU student - 2003!) "The Acoustical Bright Spot and Mislocalization of Tones By Human Listeners", J. Acoust. Soc. Am. 127, 1440-1449 (2010)

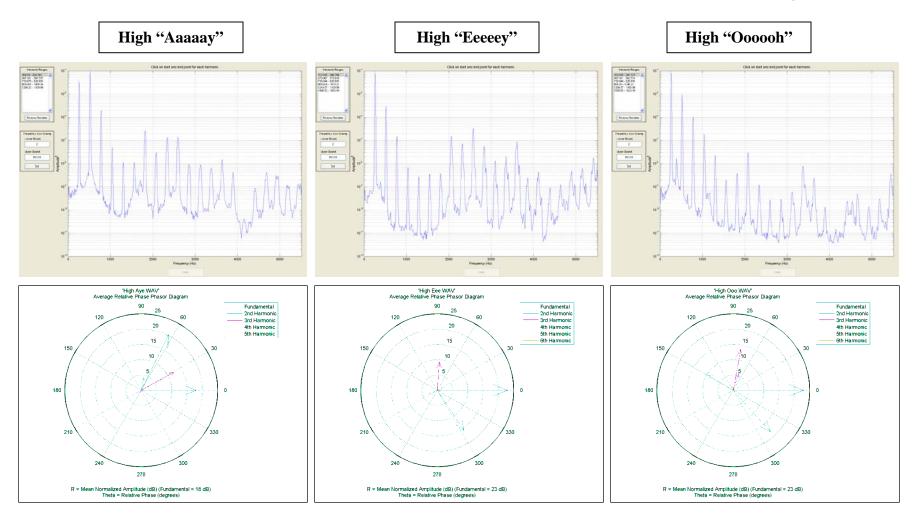
Harmonic Content of the Human Voice – First Human Musical Instrument: Comparison of 3 UIUC Physics 193POM/UIUC Women's Choir students singing D4 "Ooooh" (293.66 Hz): Abby Molly Cheryl



April 29, 2017

University of Toledo POM Talk

Harmonic Content of Vowels: John Nichols, P498POM Spring, 2010



The Phenomenon of <u>Consonance</u> & <u>Dissonance</u> – Pleasing & Displeasing Sounds – Why So??? Studied by Greek Philosopher Pythagoras (~ 500 BCE) – e.g. using the <u>monochord</u>:

Two frequencies (fundamentals) associated with the vibrating 1-D string segments (with common string tension T):

$$f_x = v/2x$$
 $f_{L-x} = v/2(L-x)$

Consonance occurs when frequency ratios

- = ratio of two low-order integers m:n
- ⇒ phase stable waveforms, e.g:

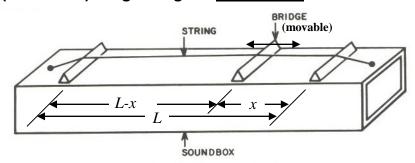
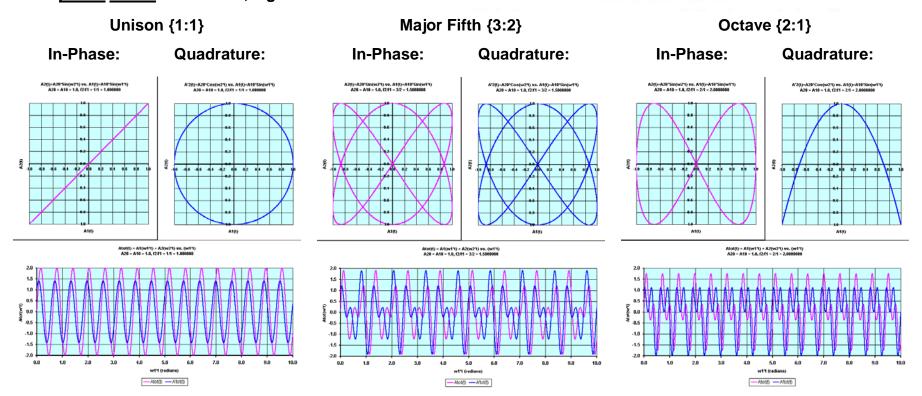


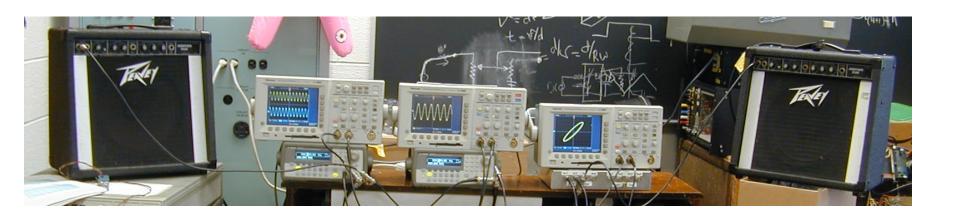
Fig. 1. The monochord.

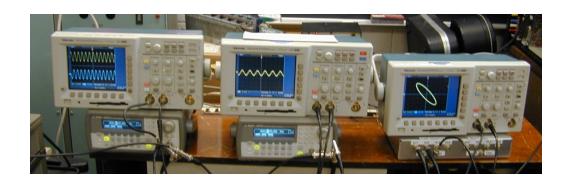


April 29, 2017

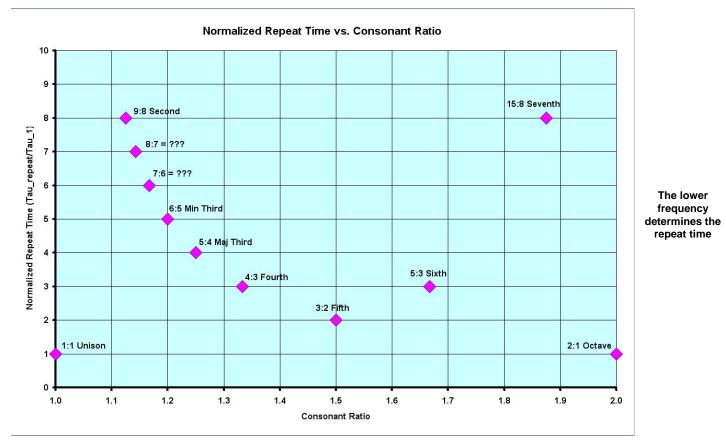
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Consonance/Dissonance Demo: hear/see/touch/feel...





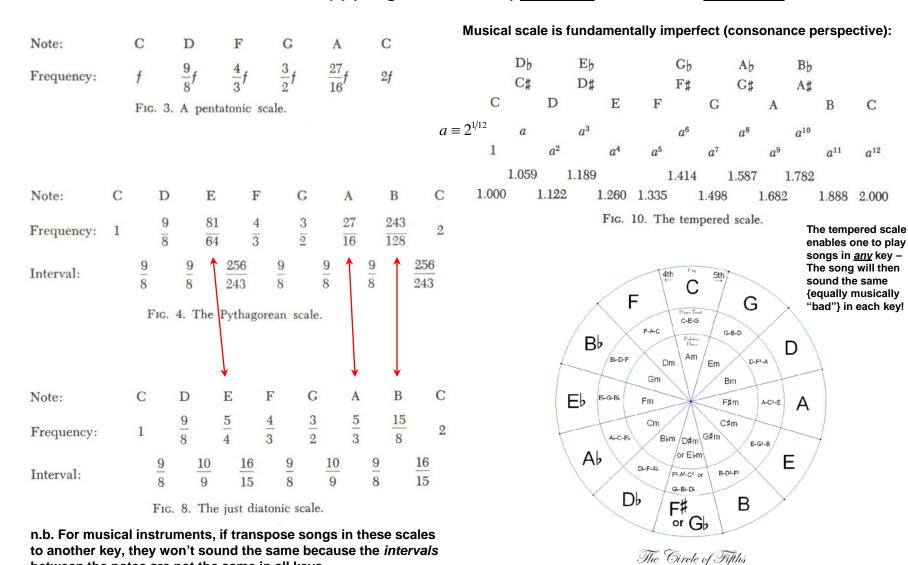
Consonant frequency intervals have <u>phase-stable</u> waveforms – with short repeat times – very easy for human ear to analyze:



No phase stability for dissonant/non-consonant/non-integer frequency ratios – repeat times can be infinitely long... requires more mental effort to analyze...

Our human brains have <u>separate</u> neural circuits for analyzing sounds to determine whether sounds are <u>consonant</u> {human voice-like sound – i.e. integer-related harmonics} vs. <u>dissonant</u> {not-human voice-like sound...} – the outputs of which are also wired into <u>different</u> emotional centers!

"Natural"notion of musical scale{s} (& e.g. circle of fifths) intimately connected to consonant intervals:



between the notes are not the same in all keys....

C

 a^{12}

2.000

B

 a^{11}

Consonance & Dissonance of Complex Tones – Just Diatonic Scale

Consonance of Harmonics - Just Diatonic Scale

Explanation: If two complex tones – e.g. two square or triangle waves and/or two musical tones with integer-related harmonics are superposed/added together – e.g as unison, $2^{\rm nd}$, minor $3^{\rm rd}$, $4^{\rm th}$, $5^{\rm th}$, ... octave in the just diatonic scale, the colored boxes in the tables below indicate the overlap of harmonics from the two sounds that will be <u>consonant</u> with each other. Thus, e.g. two complex tones in unison, a fifth apart or an octave apart are quite consonant with each other, whereas two complex tones that are e.g. a $2^{\rm nd}$ or a $7^{\rm th}$ apart are quite dissonant-sounding.

Fundamental Frequency, $f_0 = 100 \text{ Hz}$

					Minor	Major					
	Unison	Second	???	???	3rd		Fourth	Fifth	Sixth	Seventh	Octave
Harmonic	C-C	D-C	???-C	???-C	E _b -C	E-C	F-C	G-C	A-C	B-C	C-C
#	1:1	9:8	8:7	7:6	6:5	5:4	4:3	3:2	5:3	15:8	2:1
1	100.0	112.5	114.3	116.7	120.0	125.0	133.3	150.0	166.7	187.5	200.0
2	200.0	225.0	228.6	233.3	240.0	250.0	266.7	300.0	333.3	375.0	400.0
3	300.0	337.5	342.9	350.0	360.0	375.0	400.0	450.0	500.0	562.5	600.0
4	400.0	450.0	457.1	466.7	480.0	500.0	533.3	600.0	666.7	750.0	800.0
5	500.0	562.5	571.4	583.3	600.0	625.0	666.7	750.0	833.3	937.5	1000.0
6	600.0	675.0	685.7	700.0	720.0	750.0	800.0	900.0	1000.0	1125.0	1200.0
7	700.0	787.5	800.0	816.7	840.0	875.0	933.3	1050.0	1166.7	1312.5	1400.0
8	800.0	900.0	914.3	933.3	960.0	1000.0	1066.7	1200.0	1333.3	1500.0	1600.0
9	900.0					1125.0					1800.0
10	1000.0	1125.0	1142.9	1166.7	1200.0	1250.0	1333.3	1500.0	1666.7	1875.0	2000.0
11	1100.0	1237.5	1257.1	1283.3	1320.0	1375.0	1466.7	1650.0	1833.3	2062.5	2200.0
12	1200.0	1350.0	1371.4	1400.0	1440.0	1500.0	1600.0	1800.0	2000.0	2250.0	2400.0
13	1300.0	1462.5	1485.7	1516.7	1560.0	1625.0	1733.3	1950.0	2166.7	2437.5	2600.0
14	1400.0					1750.0					2800.0
15	1500.0	1687.5	1714.3	1750.0	1800.0	1875.0	2000.0	2250.0	2500.0	2812.5	3000.0
16	1600.0					2000.0					3200.0
17	1700.0					2125.0					3400.0
18	1800.0	2025.0	2057.1	2100.0	2160.0	2250.0	2400.0	2700.0	3000.0	3375.0	3600.0
19	1900.0				•	2375.0					3800.0
20	2000.0	2250.0	2285.7	2333.3	2400.0	2500.0	2666.7	3000.0	3333.3	3750.0	4000.0
21	2100.0					2625.0					4200.0
22	2200.0						_				4400.0
23	2300.0					2875.0					4600.0
24	2400.0					3000.0					4800.0
25	2500.0				_	3125.0	_				5000.0
26	2600.0				_	3250.0					5200.0
27	2700.0					1					5400.0
28	2800.0										5600.0
29	2900.0										5800.0
30	3000.0										6000.0
31	3100.0					3875.0					6200.0
32	3200.0	3600.0	3657.1	3733.3	3840.0	4000.0	4266.7	4800.0	5333.3	6000.0	6400.0

Dissonance of Harmonics - Just Diatonic Scale

Explanation: If two complex tones – e.g. two square or triangle waves and/or two musical tones with integer-related harmonics are superposed/added together – e.g as unison, 2^{nd} , minor 3^{rd} , major 3^{rd} , 4^{th} , 5^{th} , ... octave in the just diatonic scale, the colored boxes in the tables below indicate the overlap of harmonics from the two sounds are within the critical band of the human ear and hence will be <u>dissonant</u> with each other. Thus, e.g. two complex tones in unison, a fifth apart or an octave apart are quite consonant with each other, whereas two complex tones that are e.g. a 2^{nd} or a 7^{th} apart are quite dissonant-sounding.

Fundamental Frequency, $f_0 = 100 \text{ Hz}$

					Minor						
		Second		???	3rd		Fourth			Seventh	
Harmonic	C-C	D-C		???-C		E-C	F-C	G-C	A-C	B-C	C-C
#	1:1	9:8	8:7	7:6	6:5	5:4	4:3	3:2	5:3	15:8	2:1
1	100.0				120.0				166.7		
2	200.0				240.0	250.0					400.0
3	300.0	337.5	342.9	350.0	360.0	375.0	400.0	450.0	500.0	562.5	600.0
4	400.0	450.0	457.1	466.7	480.0	500.0	533.3			750.0	800.0
5	500.0	562.5	571.4	583.3	600.0	625.0	666.7	750.0	833.3	937.5	1000.0
6	600.0	675.0	685.7	700.0	720.0	750.0	800.0	900.0	1000.0	1125.0	1200.0
7	700.0	787.5	800.0	816.7	840.0	875.0	933.3	1050.0	1166.7	1312.5	1400.0
8	800.0	900.0	914.3	933.3	960.0	1000.0	1066.7	1200.0	1333.3	1500.0	1600.0
9	900.0	1012.5	1028.6	1050.0	1080.0	1125.0	1200.0	1350.0	1500.0	1687.5	1800.0
10	1000.0	1125.0	1142.9	1166.7	1200.0	1250.0	1333.3	1500.0	1666.7	1875.0	2000.0
11	1100.0	1237.5	1257.1	1283.3	1320.0	1375.0	1466.7	1650.0	1833.3	2062.5	2200.0
12	1200.0	1350.0	1371.4	1400.0	1440.0	1500.0	1600.0	1800.0	2000.0	2250.0	2400.0
13	1300.0	1462.5	1485.7	1516.7	1560.0	1625.0	1733.3	1950.0	2166.7	2437.5	2600.0
14	1400.0	1575.0	1600.0	1633.3	1680.0	1750.0	1866.7	2100.0	2333.3	2625.0	2800.0
15	1500.0	1687.5	1714.3	1750.0	1800.0	1875.0	2000.0	2250.0	2500.0	2812.5	3000.0
16	1600.0	1800.0	1828.6	1866.7	1920.0	2000.0	2133.3	2400.0	2666.7	3000.0	3200.0
17	1700.0	1912.5	1942.9	1983.3	2040.0	2125.0	2266.7	2550.0	2833.3	3187.5	3400.0
18	1800.0	2025.0	2057.1	2100.0	2160.0	2250.0	2400.0	2700.0	3000.0	3375.0	3600.0
19	1900.0	2137.5	2171.4	2216.7	2280.0	2375.0	2533.3	2850.0	3166.7	3562.5	3800.0
20	2000.0	2250.0	2285.7	2333.3	2400.0	2500.0	2666.7	3000.0	3333.3	3750.0	4000.0
21	2100.0	2362.5	2400.0	2450.0	2520.0	2625.0	2800.0	3150.0	3500.0	3937.5	4200.0
22	2200.0	2475.0	2514.3	2566.7	2640.0	2750.0	2933.3	3300.0	3666.7	4125.0	4400.0
23	2300.0	2587.5	2628.6	2683.3	2760.0	2875.0	3066.7	3450.0	3833.3	4312.5	4600.0
24	2400.0	2700.0	2742.9	2800.0	2880.0	3000.0	3200.0	3600.0	4000.0	4500.0	4800.0
25	2500.0	2812.5	2857.1	2916.7	3000.0	3125.0	3333.3	3750.0	4166.7	4687.5	5000.0
26	2600.0		2971.4	3033.3	3120.0	3250.0	3466.7	3900.0	4333.3	4875.0	5200.0
27	2700.0						3600.0				5400.0
28	2800.0						3733.3				5600.0
29	2900.0						3866.7				5800.0
30	3000.0						4000.0				6000.0
31	3100.0						4133.3				6200.0
32	3200.0						4266.7				6400.0
JE	0230.0	0000.0	000111	0,000	00 10.0	.000.0	123011	100010	0000.0	000010	0.00.0

Universal $1/f^{\beta}$ "Noise" in Natural (and Man-Made) Systems:

There exists an ever-growing, long list of natural & man-made processes exhibiting "universal" $1/f^{\beta}$ <u>fluctuations</u> (aka "noise") where the exponent $0 < \beta < 2$:

⇒ Intimately connected to <u>fractals</u> (B. Mandebrodt, 1977)

Examples:

- Carbon-composition resistors, vacuum tubes, semiconducting devices
- Weather patterns (e.g. rainfall, annual flooding of the Nile River...)
- Radioactive decay(s)
- Traffic Flow, Financial Transactions, ...
- Signals in {mylenated} nerves ← important ramifications for human music!
- Human music!

• ...

For a comprehensive list of such processes, see e.g.

http://www.nslij-genetics.org/wli/1fnoise/index-by-category.html

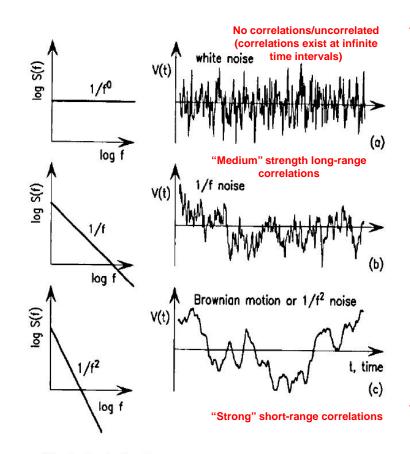


Fig. 3. Typical noises and their spectral densities $S_{\nu}(f)$.

R.F. Voss, "Random Fractals: Self Affinity in Noise, Music, Mountains, and Clouds" Physica D 38, p. 362-371 (1989).

White Noise "Music" is totally random -Unmusical

1/f Noise "Music" is interesting / engaging

Brown Noise "Music" is boring! -Too predictable!

Does Human Music Exhibit 1/f-Type Fluctuations?

YES INDEED! 3 Possible ways: Amplitude, Frequency & Tempo (Phase)!

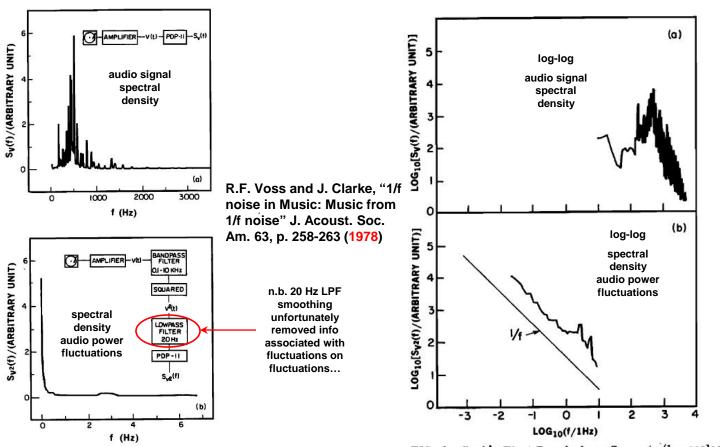


FIG. 2. Bach's First Brandenburg Concerto (linear scales). (a) Spectral density of audio signal, $S_Y(f)$ vs f; (b) spectral density of audio power fluctuations, $S_{Y^2}(f)$ vs f.

FIG. 3. Bach's First Brandenburg Concerto (log scales). (a) $S_V(f)$ vs f; (b) $S_{V^2}(f)$ vs f.

Audio Power (Amplitude) Fluctuations:

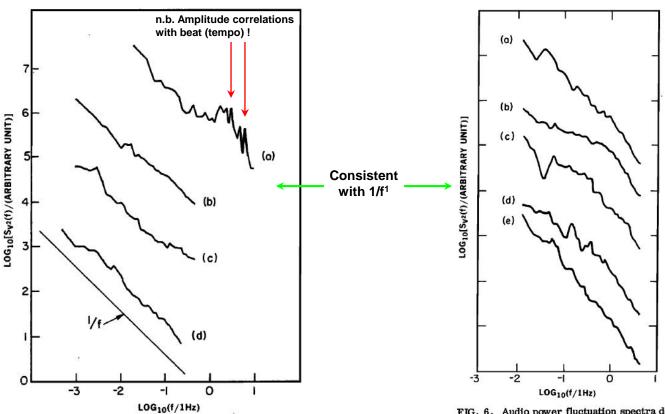


FIG. 4. Spectral density of audio power fluctuations, $S_{V^2}(f)$ vs f for (a) Scott Joplin piano rags; (b) classical radio station; (c) rock station; and (d) news and talk station.

FIG. 6. Audio power fluctuation spectra densities, $S_V^2(f)$ vs f for (a) Davidovsky's Synchronism I, II, and III; (b) Babbit's String Quartet number 3; (c) Jolas' Quartet number 3; (d) Carter's Piano concerto in two movements; and (e) Stockhausen's Momente.

Frequency Fluctuations:

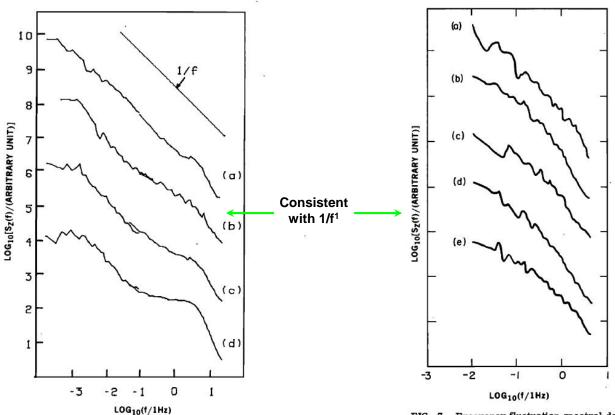


FIG. 5. Spectral density of frequency fluctuations, $S_Z(f)$ vs f for four radio stations (a) classical; (b) jazz and blues; (c) rock; and (d) news and talk.

FIG. 7. Frequency fluctuation spectral densities, $S_Z(f)$ vs f for (a) Davidovsky's Synchronism I, II, and III; (b) Babbit's String Quartet number 3; (c) Jolas' Quartet number 3; (d) Carter's Piano concerto in two movements; and (e) Stockhausen' Momente.

Frequency Fluctuations:

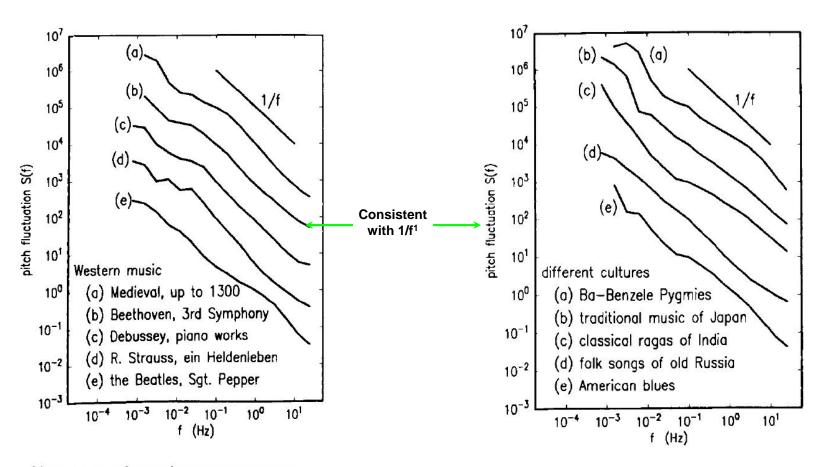
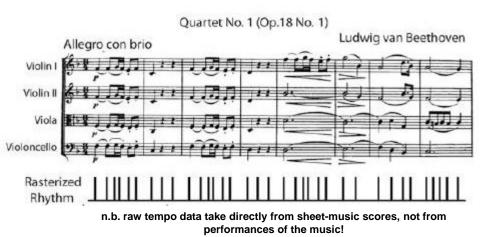


Fig. 4. Melody fluctuation spectral densities.

R.F. Voss, "Random Fractals: Self Affinity in Noise, Music, Mountains, and Clouds" Physica D 38, p. 362-371 (1989).

Tempo (Phase) Fluctuations:



D.J. Levitin, P. Chordia, V. Menon, "Musical Rhythm Spectra From Bach to Joplin Obey a 1/f Power Law" www.pnas.org/cgi/doi/10.1073/pnas.1113828109

Used a multi-taper spectral analysis algorithm {commonly used in estimation of spike trains in neurobiology datasets} to analyze tempo data associated with past ~ 4 centuries of {western} music, totaling ~ 1800 movements from ~ 560 compositions across 16 sub-genres of human music...

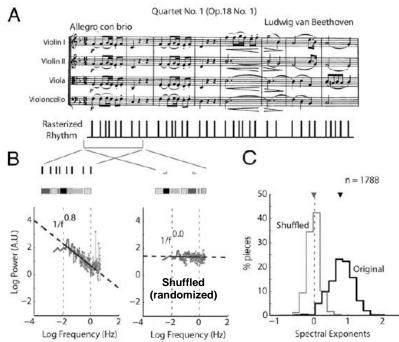


Fig. 2. Musical rhythm spectra obey a 1/f power law. (A) Rasterized rhythm representation (Lower) showing note onsets extracted from Beethoven's Quartet Op. 18. No. 1 (score, Upper). The representation shown is schematic: actual durations were extracted from the Humdrum kern format (Materials and Methods). (B) (Left) The spectrum of the rhythm raster from A has power that decays linearly (in a log-scale) with frequency as 1/f (gray dots). The slope of the spectrum (spectral exponent or β) is 0.8. Colored segments show the sequence of durations (internote intervals). Black line represents the linear fit to the spectrum in the frequency range of 0.01 to 1 Hz (delineated by dotted vertical gray lines). Dashed line represents extrapolation of the linear fit to other frequencies. (Right) The spectrum of a sequence with the note onsets shuffled randomly, keeping durations intact. The shuffled spectrum is flat ($\beta = 0.0$). Other conventions are as shown (Left). (C) Distribution of rhythm spectral exponents pooled across genres (black) obtained by linear fits to individual pieces across the population of 1,788 pieces analyzed. Gray: spectral exponent distribution for the corresponding shuffled rhythms. Inverted triangles represent the distribution median. Dashed vertical line: $\beta = 0$.

Tempo (Phase) Fluctuations – Different Types/Genres of Music:

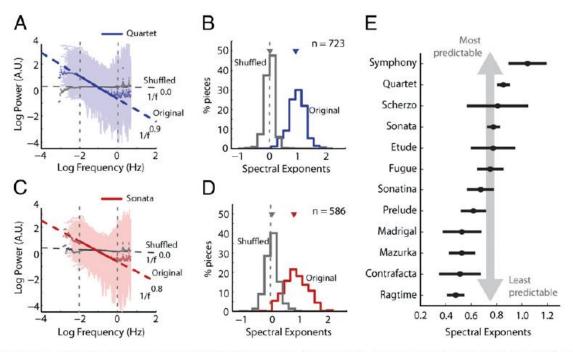


Fig. 3. The 1/f rhythm spectra are ubiquitous across genres. (A) Rhythm spectra for quartets. Average spectra (dark blue points) and linear fit (dark blue) to average spectrum in the frequency range of 0.01 to 1 Hz. Faded blue lines represent spectra of individual pieces. Gray data represent spectra of shuffled rhythms. Other conventions are as in Fig. 2B. (B) Distribution of rhythm spectral exponents obtained by linear fits to individual pieces (blue), and for the corresponding shuffled rhythms (gray). Inverted triangle represents median exponents. Dashed vertical line: $\beta = 0$. (C) Rhythm spectra for sonatas (red) and corresponding shuffled rhythms (gray). Other conventions are as in A. (D) Distribution of rhythm spectral exponents for sonatas (red) and corresponding shuffled rhythms (gray). Other conventions are as in B. (E) Distribution of rhythm spectral exponents for musical genres ordered from largest mean exponent to smallest. Larger exponents indicate correlations over longer timescales, and hence more predictable rhythms (vertical gray arrow). Circles are mean exponents, and error bars are 95% CI. Disjoint intervals indicate significantly different mean exponents (Tukey–Kramer HSD).

Tempo (Phase) Fluctuations – Different Composers:

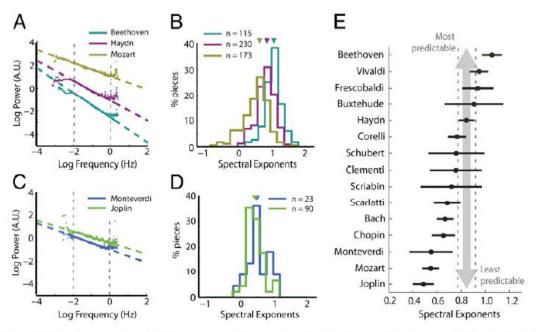


Fig. 4. Composers exhibit distinct 1/f rhythm spectra. (A) Average rhythm spectra for Beethoven (dark green), Haydn (violet), and Mozart (olive green): contemporary composers belonging to the Classical era (1750–1820). Other conventions are as in Fig. 3A. (B) Distribution of rhythm spectral exponents for compositions of Beethoven, Haydn, and Mozart. Color conventions are as in A. Other conventions are as in Fig. 3B. (C) Average rhythm spectra for Monteverdi (blue) and Joplin (green): composers separated by nearly three centuries of compositions. Other conventions are as in Fig. 3A. (D) Distribution of spectral exponents for compositions of Monteverdi and Joplin. Color conventions are as in C. Other conventions are as in Fig. 3B. (E) Distribution of spectral exponents for composers ordered from largest mean exponent to smallest. Spectral exponents of Haydn, for example (dotted vertical lines, 95% CI), are significantly different from those of Beethoven and Mozart (P < 0.05, Tukey–Kramer HSD). Other conventions are as in Fig. 3E.

- \Rightarrow It would be <u>extremely</u> interesting to carry out amplitude/frequency/tempo fluctuation analyses e.g. on <u>whale</u> songs and also songs from <u>other</u> singing animals! Do they <u>also</u> have $1/f^{\beta}$ structure??
- ⇒ Could potentially give us additional insight(s) as to what <u>alien</u> music (if exists) might sound like...

Turn the Physics Around – *Generate* "Music" from 1/f^β "Noise"!

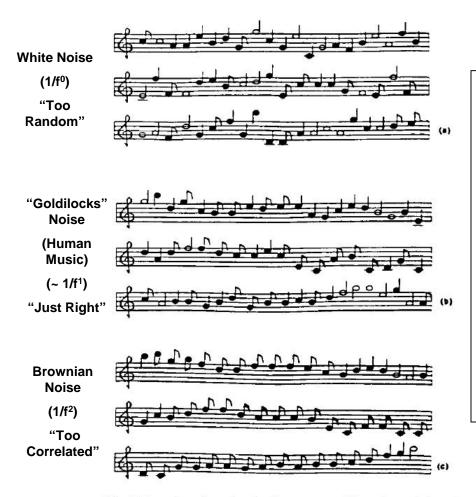


Fig. 5. Samples of stochastically composed fractal music based on the different types of noises shown in fig. 3. (a) "White" music is too random; (b) "1/f" music is the closest to actual music (and most pleasing) and (c) "brown" or $1/f^2$ music is too correlated.

Fluctuations of Fluctuations in Computer-Generated 1/f^β music:

A.) perfect beat/tempo $\tau = constant$

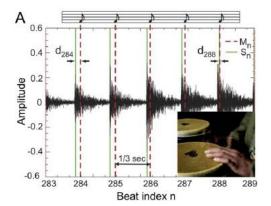
(*least* preferred)

B.) 1/f⁰ white noise fluctuations in beat/tempo (better)

C.) 1/f¹ noise fluctuations in beat/tempo

(bestlmost preferred!)

We humans appreciate / enjoy (some degree) of <u>complexity</u> in our music !!!



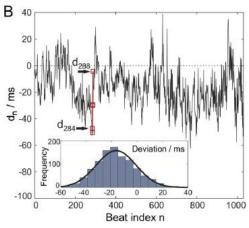


Figure 1. Demonstration of the presence of temporal deviations and LRC in a simple drum recording. A professional drummer (inset) was recorded tapping with one hand on a drum trying to synchronize with a metronome at 180 beats per minute (A). An excerpt of the recorded audio signal is shown over the beat index n at sampling rate 44.1 kHz. The beats detected at times S_n (green lines, see Methods) are compared with the metronome beats (red dashed lines). (B) The deviations $d_n\!=\!S_n\!-\!M_n$ fluctuate around a mean of -16.4 ms, i.e. on average the subject slightly anticipates the ensuing metronome clicks. Inset: The probability density function of the time series is well approximated by a Gaussian distribution (standard deviation 15.6 ms). Our main focus is on more complex rhythmic tasks, however (see Table 1). A detrended fluctuation analysis of $\{d_n\}$ is shown in Fig. 2C (middle curve).

doi:10.1371/journal.pone.0026457.g001

Musicians have fractal 1/f-noise in playing the actual music! Neural noise! We humans (definitely) prefer this!

The Musicality of a Chaotic "Leaky" Water Faucet

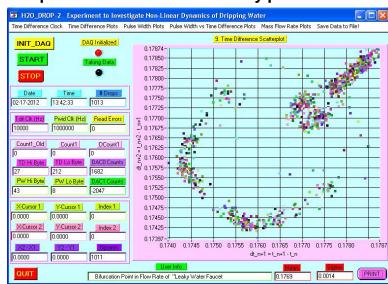
It has been extraordinarily difficult/frustrating to find/locate period-doubling/bifurcation critical water flow-rate point(s) using *visual* information of water drop time-differences from an oscilloscope trace...

Convert time differences between successive water drops into <u>audio</u> frequencies – sounds like jazz music !!! The human ear + brain makes it "trivial" to locate these bifurcation points! From the immediately previous

slides, now we understand why!



UIUC Physics 406 Chaotic "Leaky" Water Faucet Experiment



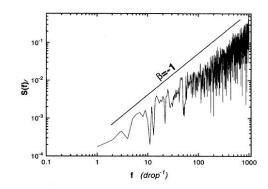
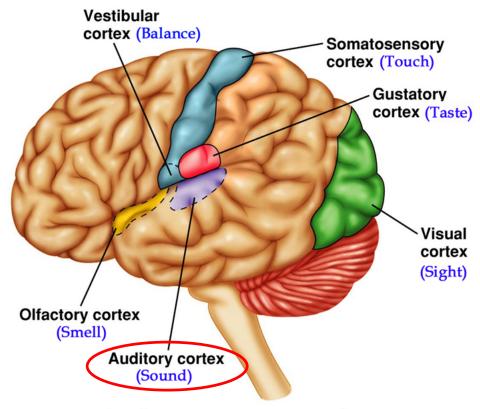


FIG. 4. Power spectra S(f) for the interval increments for the time series presented in Fig. 1. A straight line corresponding to the $\beta = -1$ curve is presented for comparison.

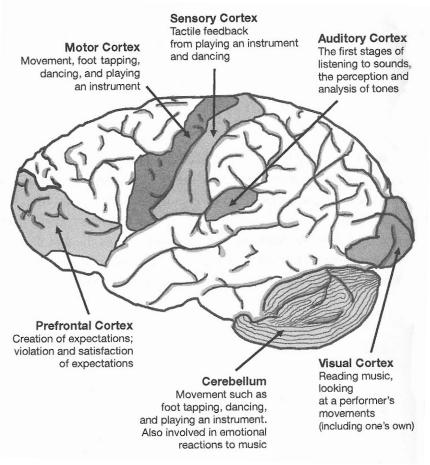
Basic Sensory Organization of the Human Brain:

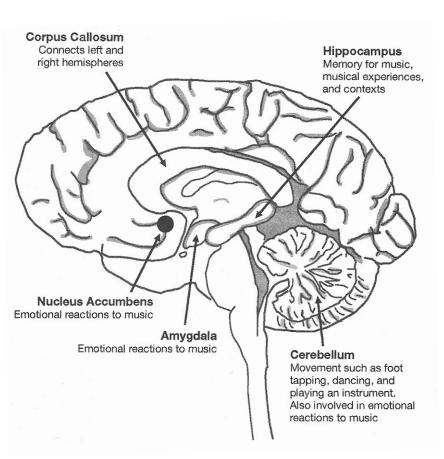


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Regions of the Human Brain Associated with Music:

Outside: Inside:





Tonotopic organization of the human auditory cortex – fMRI scans – pitch discrimination circuitry is geometrically laid out in ascending order – like keys on a piano!

D. Bilecen et al. | Hearing Research 126 (1998) 19-27

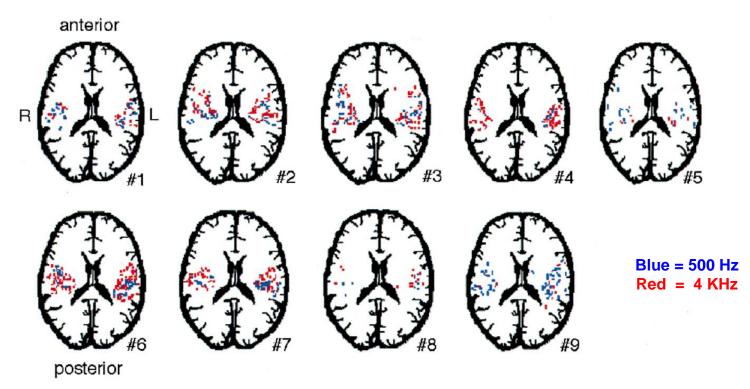
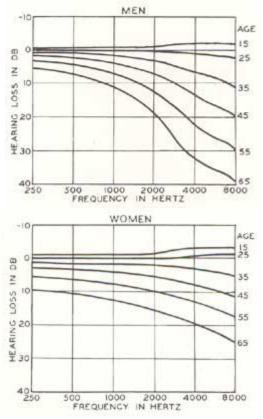


Fig. 5. Activated pixels in axial projection of all nine subjects. Blue pixels represent 500 Hz and red pixels 4000 Hz tone activated areas. All functional images were imposed on a schematic sketch. In general, high tone areas are located more frontally and closer to the medio-sagittal plane than the low tone activated areas.

24

"Natural" hearing loss as we age — worse for men than for women; Can also be cause for tinnitus — the brain apparently generates "spurious" signals...



fMRI studies: Tonotopic reorganization of the auditory cortex in tinnitus:

10342 Psychology: Mühlnickel et al.

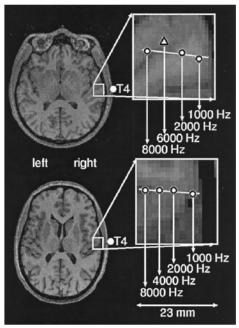


FIG. 1. A typical example of the tonotopic map is shown for a left ear tinnitus (*Upper*) and a control subject (*Lower*). Equivalent current dipoles elicited by auditory stimulation at the three standard and the tinnitus frequency in the tinnitus subject and the four standard frequencies in the healthy control are superimposed onto an axial slice of Brodman's area 41 of the right hemisphere. The line in the upper portion of the figure shows the trajectory of the dipole locations of the three standard tones (circles). The triangle (*Upper*) represents the location of the tinnitus frequency (6,000 Hz in this case). Note that the trajectory of the dipole locations of the four standard frequencies in the healthy control subject (circles, *Lower*) is linear, whereas the dipole of the affected frequency in the tinnitus subject diverges from the linear trajectory established by the three standard frequencies. The location of T₂ as well as the scale of measurement are marked.

Proc. Natl. Acad. Sci. USA 95 (1998)

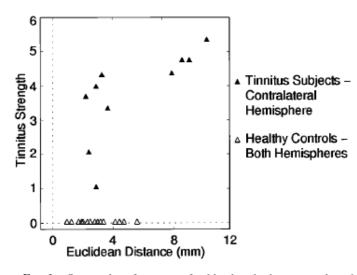


FIG. 2. Scatterplot of amount of subjective tinnitus strength and deviation of the tinnitus frequency from the tonotopic map in the contralateral hemisphere. A measure of deviation of the tinnitus frequency was obtained by determining the Euclidean distance between the trajectory of the standard tones and the location of the tinnitus frequency in tinnitus subjects or the corresponding comparison frequency in control subjects (see text). The tinnitus strength was assessed by the MTI. Greater subjective tinnitus strength was related to larger deviations from the trajectory of the standard frequencies. This figure suggests that there might not be a linear relationship between tinnitus and reorganization but rather a bimodal distribution of tinnitus sufferers with and without map distortions. The size of the sample studied is too small to clarify this point.

Music and the Human Brain:

Music is processed simultaneously in multiple regions of our brain – sequentially and in parallel – for frequency, amplitude/loudness, tempo/beat/rhythm, contour, as well as e.g. recalling memories of the same song and/or related songs – stored in <u>several</u> places in the brain – not just one place... explains <u>why</u> we have very robust recall of music! Alzheimer's patients remember songs/song lyrics <u>long</u> after forgetting everything else....

The outputs of these sound/music processing centers are also wired into our emotional centers in our brains – music <u>can</u> make us feel happy/sad/...

Various brain chemicals/neuro-transmitters are produced when listening to/participating in music:

<u>Serotonin</u> – produced by neurons of the raphe nuclei in the brain stem {regulates mood, appetite, sleep & metabolism}

<u>Dopamine</u> – released in nucleus accumbens {regulates emotions, mood, alertness and coordination of movement, aids in encoding of memory, and is also part of brain's pleasure and reward system – e.g. gamblers/drug addicts/chocoholics}. Its role in music was only recently discovered (V. Menon, D.J. Levitin, Neurolmage 28(1): 175-84, 2005).

Oxytocin – released by the pituitary gland, amygdala, ventromedial hypothalamus, septum and brain stem during communal singing, rituals & sexual arousal, enhances bonding & trust, reduces fear and/or apprehension, affects generosity by increasing empathy, ... Its role in music was also only recently discovered {1995, 2003, 2005}.

<u>Endorphins</u> – released by the pituitary gland & hypothalamus during singing, strenuous exercise, pain, orgasm, death – resembles opiates in analgesic (painkiller) ability and produces a sense of well-being...

Music increases our alertness – via modulation of <u>norepinephrine</u> and <u>epinephrine</u> (*aka* <u>adrenaline</u>)... Music also ameliorates the effects of stress – reduces <u>cortisol</u> levels (a hormone produced by stress).

The release of "feel-good" neuro-chemicals in human brain in response to playing / listening to music points to an ancient and evolutionarily beneficial connection to music, e.g. helps sooth/ease tensions/smooth over differences/forge social bonds/... helps to preserve/maintain/stabilize social structure of the group...

The release of these brain chemicals <u>also</u> boosts the immune system – humans stay healthier/fend off illness/disease – again improves the odds of one's survival!

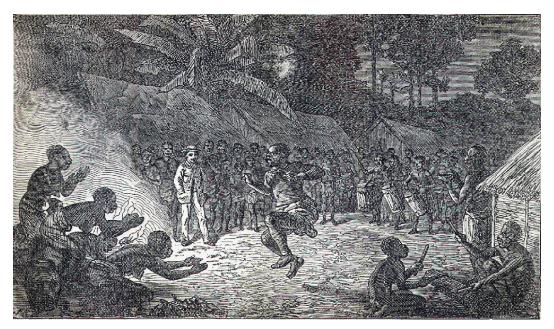
Production of "feel-good" neurotransmitters human brains in response to music evolutionarily beneficial to humans – individuals who didn't benefit from/have this response were at a disadvantage \Rightarrow reduced probability for passing on <u>their</u> genes. The humans who survived enjoyed/benefitted from music! \Leftarrow "positive" feedback mechanism!

Social interactions of early prehistoric tribes very likely coupled music, dance, food, celebration – benefitting everyone in group, also helping to ease tensions/squabbles, etc. – maintain stability of social structure of group...

Robust memory of music/song ⇒ effective tool e.g. for education of young – passing on of accumulated worldly knowledge – do's n' don'ts, how-to's, etc. from one generation to next, and also oral/musical preservation of early human culture's history...

n.b. <u>written</u> language developed <u>only</u> "very recently" (~ 6000 years ago – @ transition from hunter-gatherer to agrarian societies – initially to keep track of <u>transactions</u> of goods, etc. between members of society in that era...)

Earliest music presumably utilized only the human voice & e.g. clapping of hands, stomping of feet, etc. \Rightarrow naturally led to development of musical instruments such as early flutes, drums, etc. to accompany & thereby enhance such activities/ceremonies...



Early <u>humans</u>:

Likely entire group participated in music & dance celebrations...

Tradition still carried on today in many indigenous / native groups...

Mirror Neurons

- Mirror neuron = neuron that fires both when animal performs an action and when animal observes the same action by another {similar} animal.
- The neuron "mirrors" the behavior of the other animal, as though the observer were itself performing the action!
- Exist in the brains of humans, primates and also certain birds (e.g. Zebra Finch)
- Important for understanding the actions & intentions of others?
- Enables us to experience empathy for/understanding of others?
- Important for imitation & learning new skills?

A newborn macaque monkey imitating a human facial expression:





- Important for language acquisition?
- Important for learning in general?

 Incorporate this info into our teaching methods!
- Provides the physiological mechanism for perception-action coupling?
- Activate e.g. when watching movies, people playing sports games, performing music, ... e.g. many musicians listen just once to a new music composition and then perform it...
- Helps form/define the basis for a species' social behavior?
- Responsible for self-awareness/consciousness?
- Dysfunction/deficiency of mirror neurons associated with autism?

Genes for Language and Music:

Examination of fossil skulls reveals that Brodmann area 44 (BA44) – part of the frontal cortex {important for cognitive and perceptual tasks, as well as auditory motor imitation via <u>mirror neurons</u>} may well have been in place ~ 2 Myrs ago (i.e. <u>long</u> before Homo sapiens – first emerged ~ 200 Kyrs ago).

⇒ Neural mechanisms for *language* were in place long before they were fully exploited...

The FOXP2 gene (located on chromosome 7) is closely associated with human language – also existed in Neanderthals {recent DNA analysis!}. Chimpanzees and songbirds, such as the Zebra Finch {as well as other animals - e.g. fish, mice, crocodiles,...} have their own versions of the FOXP2 gene.



Brodmann area 44

<u>Microcephalin</u> is part of the human genome that encodes for brain development. A <u>genetic</u> <u>variant</u> of this gene emerged ~ 37,000 years ago – i.e. at the beginning of culturally modern humans, and coincides with the emergence of <u>tonal</u> languages and the appearance of artistic artifacts and bone flutes (earliest known manmade musical instruments) ...

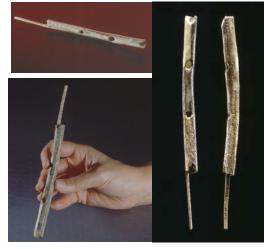
A <u>second</u> genetic variation of <u>microcephalin</u> arose ~ 5,800 yrs ago – coincides ~ with the first record of <u>written</u> language {Sumerian culture}, spread of agriculture, development of cities, ...

n.b. Social interactions can/do alter gene expression in the brain {and vice versa}!

⇒ ramifications for evolutionary forces operative in *today's modern world*???

The earliest known human-made musical instruments – Divje Babe flute (made from the femur bone of a bear) – found in cave nr. Cerkno, NW Slovenia in 1995, ~ 43,100 years old, and an ivory flute (made from woolly mammoth tusk) found in a mountain cave {Geissenklösterle}, near Ulm, SW Germany in 2004, ~ 37,000 years old:





n.b. other newer flutes (made from swan bones) were discovered earlier in this cave:

A bone drumstick was also found in this cave....

See/listen to YouTube video: https://www.youtube.com/watch?v=xn5ZygWxKmw

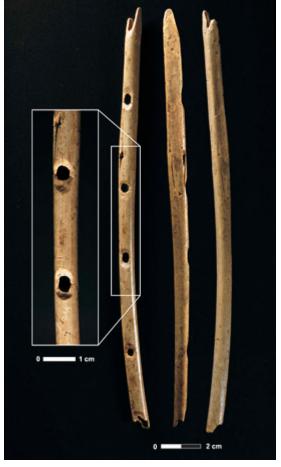
Another Bone Flute (Griffon vulture, > 35K yrs old) recently found in cave near Hohle Fels (SW Germany) in 2008:



n.b. An exact copy of this flute was made (via laser scan \Rightarrow 3-D printing), given to professional musician, who, after learning how to play it, was able to play "Amazing Grace" on it (in the key of D - uses the <u>white</u> notes on piano) and the German National Anthem – (uses both the white <u>and</u> black notes on piano)!!!

- ⇒ Evidence for 12-note natural/"consonant" musical scale in existence at <u>that</u> time, ~ 32,000 years before the Greeks !!!
- ⇒ Presumably, these early flutes were not <u>prototypes</u> i.e. they were used to play music in the everyday world of the humans who made them !!!

See/listen at: https://www.theguardian.com/music/2013/feb/15/ice-age-flute



Why do we have such strong/robust memories for music?

- * Compare ability to recall "everyday" memories vs. memory of favorite music.
- * Many people can easily recall whole songs, whole albums/CD's of their favorite music.
- * Compare e.g. the ability to remember/recall 5 names of people immediately after rapid-fire introduced to them at a party by host vs. musical memories.
- * "Everyday" memories are stored in <u>two</u> places in the brain the hippocampus (short term memory) and in the cortex (long term memory takes time for cortical neurons to "wire" themselves up).
- * Musical memories <u>are</u> more robust than "everyday" memories stored in <u>several</u> places in brain. Why? How?
- * Everyone has very vivid/clear memories e.g. of an event that occurred on a specific day/days in one's past. Recall e.g. the *earliest* such memories. Were there very strong emotions associated with whatever happened/occurred on each of those days? But we know that emotions produce brain chemicals {serotonin/dopamine/oxytocin/endorphins/...} apparently, such brain chemicals are important/required for the hard-wiring of our long-term memories!
- * If one has a "meh" emotional response to an event, very likely won't be able to remember it very long.
- * Can this-all then help explain why/how long before any written language existed the importance of human music as used in social group activities for the evolutionary benefit of homo sapiens in passing on worldly knowledge, wisdom, human history, *etc.* helping us to survive to the present day?

From the perspective of "survival of the fittest", <u>all</u> animals living on our planet are fundamentally / primarily interested in their <u>own</u> species, and secondarily in other species (e.g. as food/to keep from becoming food...)

We humans are <u>no</u> different in this regard. Our <u>anthropocentric</u> view of interest primarily in our own species is also reflected in our music - e.g. consonant intervals, musical scales, etc. as well as the sounds made by musical instruments that we have developed over the millennia....

It is <u>absolutely</u> not an accident that our musical instruments <u>mimic</u> the human voice – i.e. 1-D vibrating systems with integer-related harmonics $\{f_n = nf_1\}$ for overtones – some musical instruments succeed in this more closely than others, which can be viewed as ~ artistic abstractions of the human voice. Skilled musicians playing such instruments can evoke in us strong emotions as if we were listening to a human in agony/pain, joy/ecstasy, sorrow, etc. Tempo/timing – which parallels the temporal aspects of various human gestures/movements recently found to be critical in this regard, in terms of evoking human emotion(s) in response to music!

Similarly, it is also <u>not</u> an accident that {anharmonic $f_n \neq nf_1$ } 2-D percussion instruments – drums etc. are used to mimic the impulsive sounds associated with internal human <u>rhythms</u> – e.g. breathing, our heart beat, blood pulsing through our veins, etc.

Both classes {1-D and 2-D} of musical instruments can also be/have been used in musically artistic ways to mimic the characteristic voices, sounds made by animal species that are of secondary interest to us – e.g. the singing of birds, the roar of lions, howling of wolves, the clip-clop of horses hooves, etc.



April 29, 2017

University of Toledo POM Talk

Some Closing Comments:

- ⇒ <u>Nature vs. Nurture</u>: Infants & young children (< 8 yrs) undergo enormous development in their brains literally wiring the connections in their brains in a myriad of ways. Children deprived of sight/vision for any significant length of time (e.g. due to eye injury or infection) are at risk of life-long adverse impact because of this... Presumably, similar/analogous adverse effect(s) will occur if children grow up in environment completely *devoid* of all music those brain areas not used for nominally the processing of music will be wired for other uses... Will we eventually lose our "musical roots"? {e.g. Our bodies have lost the ability to <u>internally</u> produce vitamin C because of eating <u>fruit</u> in our diet Our bodies still do produce other vitamins, e.g. vitamin D, etc...}
- ⇒ Importance of music in fostering the development of our children, and synergy in their education
- ⇒ Musicians are especially interested in/focused on listening to/playing/creating music spend their lifetimes "wiring" their brains for auditory processing of sounds they can hear things that us "normal" humans do not (or at least much more acutely so). Similarly, artists wire their brains for visual processing of information, can see things us "normal" humans do not (or at least much more acutely so).
- ⇒ Information Overload: impact *short* and *long-term* on us humans (and other creatures e.g. whales, orcas, ... adverse effects/impact of our own noise pollution) living in the modern-day world, filling our heads 24/7 with overdoses of information & sounds coming at us seemingly from all directions, and at an ever-increasing pace? Human culture planet-wide is changing at <u>exponential</u> pace, far faster than human evolutionary time scales... what are the long-term implications of <u>this</u>?
- ⇒ The development of new technologies {e.g. fMRI, DNA sequencing, ...} in multiple areas of research has led to many exciting discoveries in the past few years, in terms of us gaining a better understanding of how human hearing works, and also the importance of music in our daily lives in the here-and-now, and helping to shed light on how this all came about i.e. our past why/how our own musical memory is <u>so</u> strong. Did music really play an important evolutionary role in our development, helping us to get from the stone age to where we are now???
- ⇒ The current picture on this topic is <u>far</u> from complete... However, more and more people appear to be getting involved & investigating as more becomes known the pace is accelerating.... The nature of this subject is such that it requires/would benefit greatly from multidisciplinary research/collaboration...
- ⇒ If intelligent life exists elsewhere in the universe, would such beings also have music in their culture?
 - What would their music sound like? Did their music play also an important role in their evolution?
 - Would their musical instruments also artistically mimic their own voices, their own internal rhythms?
- ⇒ Many, many things to think about, investigate & study! We live in exciting times in this regard!
- ⇒ Many questions remain to be answered, there is much still to be learned!
- ⇒ For you-all to remember everything in this colloquium talk, I should have sung everything to you-all, and we-all should have danced!!!

If Interested: Suggested/Recommended Books for Further Reading:

- "This is Your Brain on Music The Science of Human Obsession", Daniel Levitin, Dutton, 2006.
- "The World in Six Songs", Daniel Levitin, Dutton, 2008.
- "The Singing Neanderthals The Origins of Music, Language, Mind and Body", Steven Mithen, Harvard University Press, 2007.
- "The Origins of Music", Nils Lennart Wallin, Björn Merker, Steven Brown, MIT Press, 2001.
- "Musicophilia Tales of Music and the Brain", Oliver Sachs, Alfred A. Knopf, Inc., 2007.

Website(s) for UIUC Acoustical Physics of Music/Musical Instruments Courses (if interested):

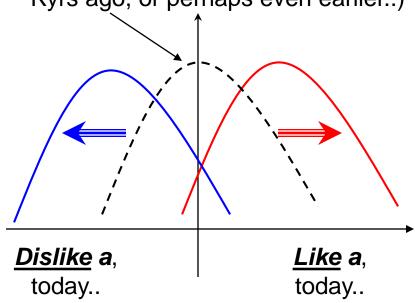
Much material posted/available online – lecture notes, experimental results, students semester project final reports, NSF Summer Research Experience for Undergraduates final reports, class pix, ...

Freshman "Discovery" Course: http://courses.physics.illinois.edu/phys193/ {less technical} Upper-Level Undergrad Physics Course: http://courses.physics.illinois.edu/phys406/ {more technical}

Why do humans <u>like</u> music? Is music <u>just</u> "auditory cheesecake" ??

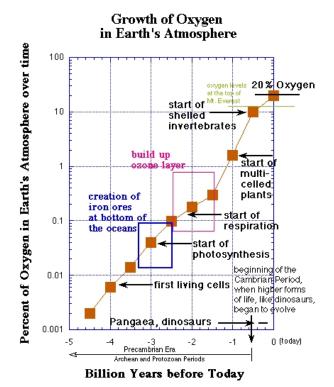
For <u>any</u> human attribute, *a*:

a, in ancient times.. ("t = 0" ~ 200 Kyrs ago, or perhaps even earlier..)

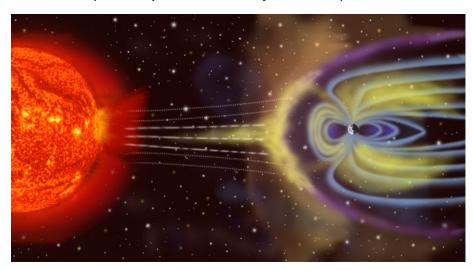


Did evolutionary "forces" – "survival of the fittest" shift (via feedback mechanisms / genetic mutations over the millennia) each generic human attribute \boldsymbol{a} from initial $\langle \boldsymbol{a} \rangle = 0$ to where it is today?

A (Very) Brief History of Planet Earth:



The earth's magnetic field (due to internal dynamo earth's outer core) shields planet from deadly solar X- & γ-radiation:



Photosynthesis of cyano-bacteria living in earth's oceans initially drove oxygenation of earth's atmosphere.

Further oxygenation of earth's atmosphere by stromatolites:



~ 4.5 Byrs ago: Solar System forms

~ 4.0 Byrs ago: late heavy bombardment in solar system ends;

The earth is in the "habitable zone", cools and {single-celled} life begins...

~ 3.5 Byrs ago: photosynthesis begins

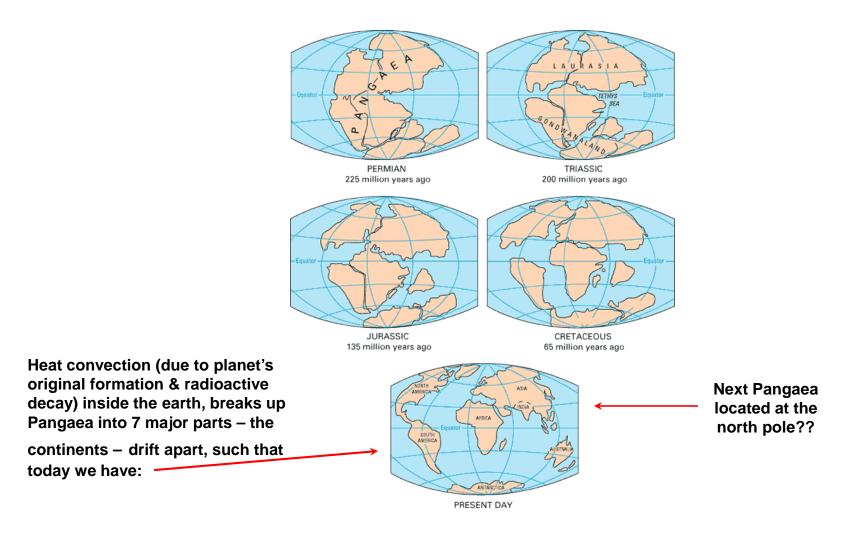
~ 2.3 Byrs ago: earth's atmosphere becomes oxygen rich;

The first "snowball earth" occurs... but eventually warms up again...

Ozone layer forms at the top of earth's atmosphere, enabling life to exist on land

- shielding it from harmful UV radiation.

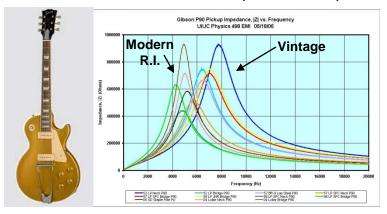
Breakup & formation of continents on earth – plate tectonics – appears to be cyclical; Pangaea – last supercontinent in the Permian epoch (~ 225 Myrs ago):



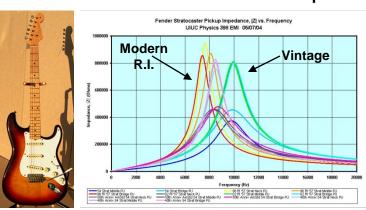
A Test of My Own Long-Term Musical Memories:

I played {electric} guitar in mid-60's – mid-70's; started playing again in ~ mid-90's: "Faithful" modern-day re-issues of vintage guitars didn't sound like the <u>real deal</u> to my ears... Due to false memories, or actual truth??? I explicitly checked:

Gibson P-90's in Les Pauls, Les Paul Jr, ...

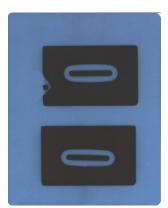


Fender Stratocaster Pickups

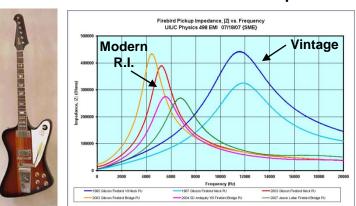


X-ray of P-90 PUs from '52 (top) vs. '98 R.I. (bottom) Gibson Les Paul Guitars:





Gibson Firebird Pickups

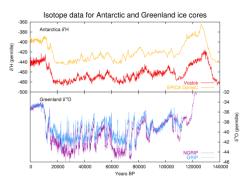


Connection Between Prehistoric Art and Music in Palæolithic Caves:

Grotte du Peche Merle {Blackbird Hill}, Caberets, Departement Lot, Southern France



Caves were a good place to live / camp out in during the last glacial period:



Red dots are markers for acoustic resonances !!!









Pech Merte 7.6 9 Act to Célé

Pech Merte 7.6 9 Act to Célé

Pech Merte 7.6 9 Act to Célé

Le Loi Act to Calarc

Paintings dated ~ 20,000 - 25,000 yrs old ⇒







La Grotte du Portel, Ariège Pyrenees, Southern France:

Acoustical resonance properties of this cave recently studied by Prof. legor Reznikoff & his University Paris/Nanterre research team.



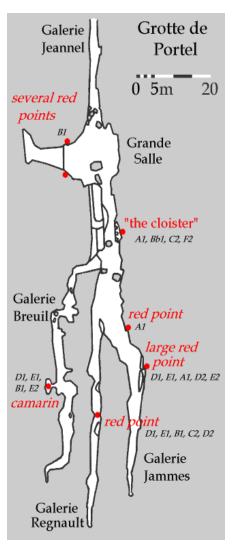
Paeleolithic man would have explored caves by dull light of torches, and using his voice like sonar/echo-location to navigate around corners, avoid holes, explore nooks/crannies of the cave...

Reznikoff's team discovered that the red dots in this cave were <u>markers</u> of acoustic resonances – and were very often within ~ 1-2 meters of paintings in the cave.

Brought in trained vocalist to map out the acoustic resonances.

Also discovered that by modulating the harmonic content and amplitude, some acoustic resonances sounded very similar to those made by the animals painted on the nearby wall – i.e. animal paintings also a <u>marker</u> for humans to make the animal's sound !!!





Fourier Analysis:

A continuous, finite (i.e. mathematically well-behaved) but otherwise arbitrary $\underline{periodic}$ function of time, F(t) can be $\underline{exactly}$ represented by an $\underline{infinite}$ series of sines & cosines of harmonics of fundamental:



Jean-Baptiste Joseph Fourier 1768-1830

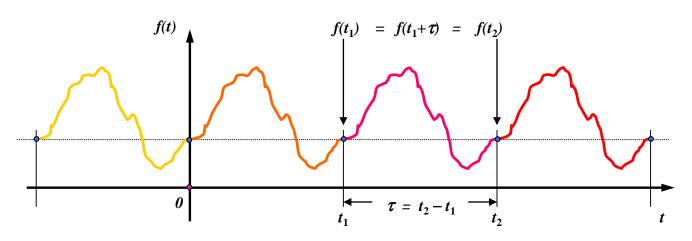
$$F(t) = a_o + a_1 \cos \omega_1 t + a_2 \cos \omega_2 t + a_3 \cos \omega_3 t + \dots$$

$$+ b_1 \sin \omega_1 t + b_2 \sin \omega_2 t + b_3 \sin \omega_3 t + \dots$$

$$= \frac{1}{2} a_o + \sum_{n=1}^{\infty} a_n \cos \omega_n t + \sum_{n=1}^{\infty} b_n \cos \omega_n t \qquad \text{where: } \omega_n \equiv 2\pi f_n$$

$$a_o = \frac{1}{\tau} \int_{t=0}^{t=\tau} F(t) dt \qquad a_n = \frac{1}{\tau} \int_{t=0}^{t=\tau} F(t) \cos \omega_n t dt \qquad b_n = \frac{1}{\tau} \int_{t=0}^{t=\tau} F(t) \sin \omega_n t dt$$

Fourier {aka Harmonic} Analysis of Periodic Waveforms:



$$f(t) = a_o + \sum_{n=1}^{\infty} a_n \cos \omega_n t - \sum_{n=1}^{\infty} b_n \sin \omega_n t \quad (\omega_n = 2\pi f_n, \quad f_n = nf_1)$$

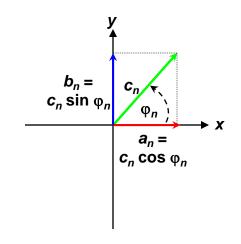
$$a_n = \frac{1}{\tau} \int_0^{\tau} f(t') \cos \omega_n t' dt' \quad b_n = \frac{1}{\tau} \int_0^{\tau} f(t') \sin \omega_n t' dt'$$

$$\underline{Define}: \quad a_o \equiv c_o \quad a_n \equiv c_n \cos \varphi_n \quad b_n \equiv c_n \sin \varphi_n \quad \varphi_n = \tan^{-1}(b_n/a_n)$$

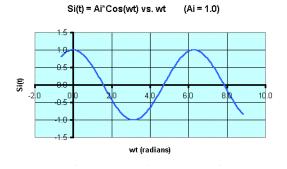
$$f(t) = c_o + \sum_{n=1}^{\infty} c_n \cos(\omega_n t + \varphi_n) = \sum_{n=0}^{\infty} c_n \cos(\omega_n t + \varphi_n) \quad (\omega_o = \varphi_o \equiv 0)$$

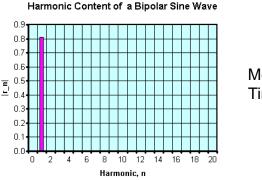
$$c_n = \frac{1}{\tau} \int_0^{\tau} f(t') \cos(\omega_n t' + \varphi_n) dt'$$

$$\underline{Complexify}: \quad \tilde{f}(t) = \sum_{n=0}^{\infty} c_n e^{i(\omega_n t + \varphi_n)} \quad c_n = \frac{1}{\tau} \int_0^{\tau} \tilde{f}(t') e^{i(\omega_n t' + \varphi_n)} dt'$$



Basic Musical Waveforms:

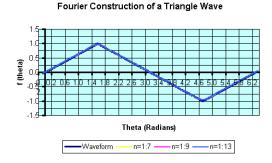


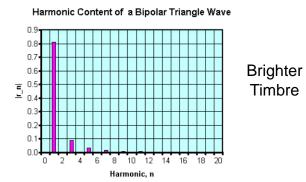


Mellow Timbre

Symmetrical Triangle Wave:

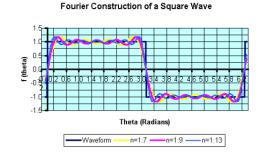
Sine/Cosine Wave:

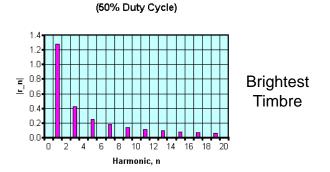




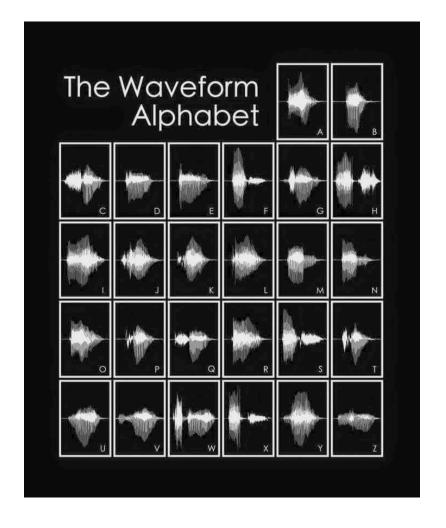
Harmonic Content of a Bipolar Square Wave

Symmetrical Square Wave:





Alphabet - Time Domain Waveforms:



Early Waveform Synthesizers:



Greek Hydraulus (water organ):
Ctesibius of Alexandria, 3rd century BCE



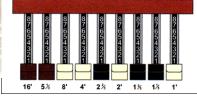
Pipe Organs: 2nd century ACE – present











Hammond Organ: 1934 - present

Telharmonium Mk-I,II & III, NYC: Thaddeus Cahill 1897-1916

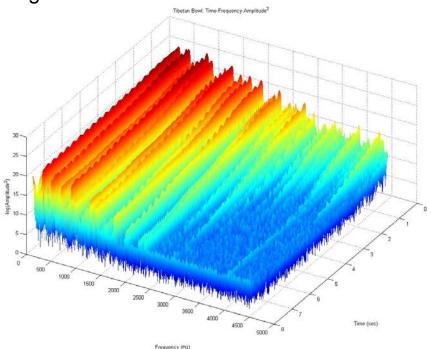
Some Experimental Results from the UIUC Physics of Music/Musical Instruments Lab...

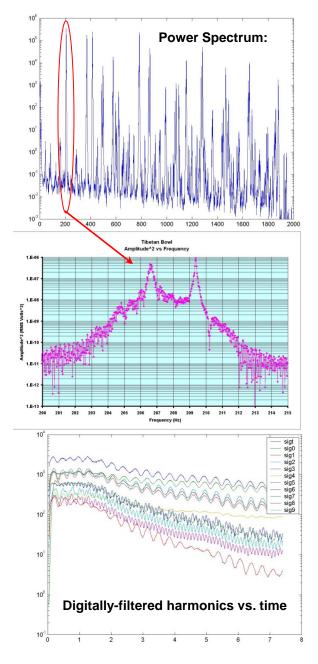
Phase-Sensitive Analysis of Sounds

Complex Sound Field Measurements

Some Experimental Results from UIUC Physics of Music/Musical Instruments Course(s):

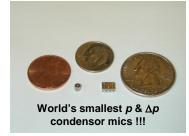
Analyze the harmonic content (amplitude, frequency <u>and</u> phase info vs. time) of quasisteady complex sounds produced by musical instruments, human voice, etc. using 24-bit digital audio recorder + reference omnidirectional condensor mic ⇒ .wav file e.g. Tibetan Bowl:





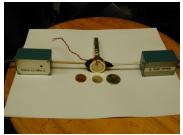
Frequency-Domain Measurements of Complex Harmonic/Periodic Sound Fields

Complex sound field at point in space uniquely determined if simultaneously measure pressure p and particle velocity \vec{u} (= <velocity> of air molecules, spatially averaged over an infinitesimal volume element d^3V).

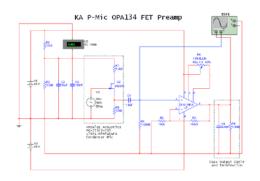


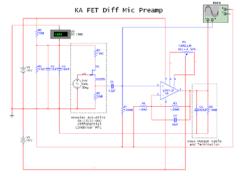


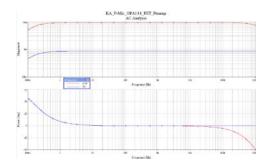


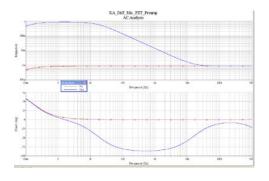


April 29, 2017









1-D Euler Eqn for
$$\frac{inviscid}{fluid flow:}$$
 $\frac{\partial \tilde{u}_z(z,t)}{\partial t} = -\frac{1}{\rho_o} \frac{\partial \tilde{p}(z,t)}{\partial z}$

Integrate:

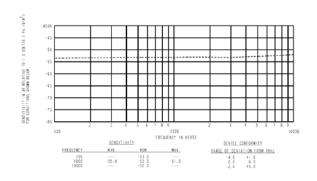
$$\rho_o = 1.204 \, kg/m^3$$
 for air @ *NTP*

$$\frac{\partial \tilde{u}_{z}(z,t)}{\partial t} = -\frac{1}{\rho_{o}} \frac{\partial \tilde{p}(z,t)}{\partial z} \qquad \rho_{o} = 1.204 \, kg/m^{3} \text{ for air } @ NTP$$

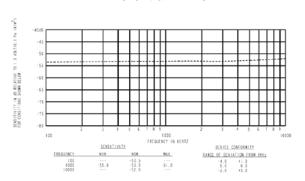
$$\tilde{u}_{z}(z,t) = -\frac{1}{\rho_{o}} \int_{-\infty}^{t} \frac{\partial \tilde{p}(z,t')}{\partial z} dt' \simeq -\frac{1}{\rho_{o} \Delta z} \underbrace{\int_{-\infty}^{t} \Delta \tilde{p}(z,t') dt'}_{op-amp integrator}$$

Sensitivity & Absolute Calibration of *p/u*-Mics

Omni-directional Condensor P-mic



Differential P-mic



Calibrate Mics e.g. in $SPL = 94.0 \, dB$ sound field:

$$SPL = 94.0 \ dB = 20 \log_{10}(p/p_{ref}) = 20 \log_{10}(u_z/u_{ref})$$

 $\Rightarrow p = 1.0 \ RMS \ Pascals, \ u_z = 2.42 \ RMS \ mm/sec$

Typical Mic Sensitivities:

$$S_{p-mic} \sim 280 \ RMS \ mV/RMS \ Pa$$

$$S_{u-mic} \sim 90 \text{ RMS } mV/\text{RMS } Pa^*, 1.0 \text{ RMS } Pa^* = 2.42 \text{ RMS } mm/\text{sec}$$

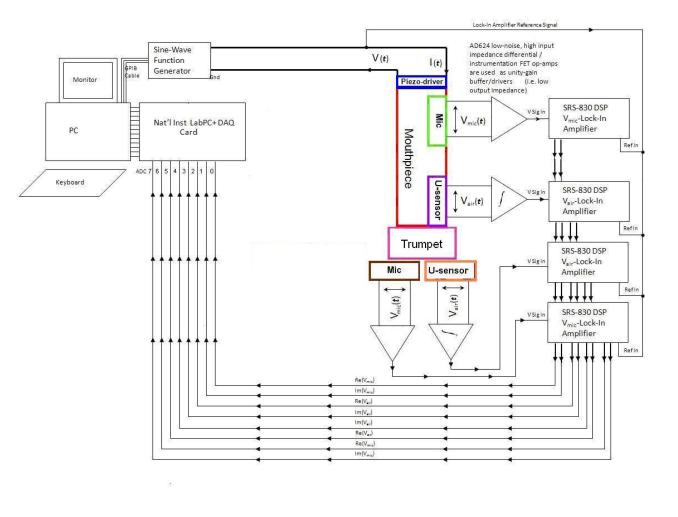
$$p_{ref}(f = 1 \text{ KHz}) = 2 \times 10^{-5} \text{ RMS Pascals}$$

 $u_{ref}(f = 1 \text{ KHz}) = 4.8 \times 10^{-8} \text{ RMS m/s}$

Extech SPL Calibrator



Block Diagram of PC-Based DAQ System



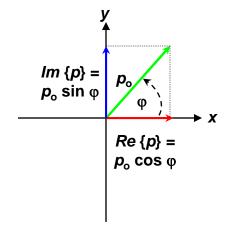
Lock-in Amplifiers (LIA's) measure the in-phase (="Real") and 90° out-of phase {aka "quadrature"} (="Imaginary") amplitude components (w.r.t. reference sine-wave function generator signal, e.g.

$$p(t) = p_0 \cos(\omega t + \varphi)$$
$$= p_0 \cos \omega t \cos \varphi$$

$$-p_{o} \sin \omega t \sin \varphi$$

$$Re\{p\} = p_o \cos \varphi$$

$$Im\{p\} = p_0 \sin \varphi$$



Time Domain (instantaneous pressure/particle velocity):

Use e.g. Digital Oscilloscope/Digital Recorder to Measure:

$$p(\vec{r},t) = p_o(\omega)\cos[\omega t + \varphi_p(\omega)]$$
 n.b. phase-referenced w.r.t.
$$u_z(\vec{r},t) = u_{o_z}(\omega)\cos[\omega t + \varphi_{u_z}(\omega)]$$
 sine-wave fcn generator Complexify:

$$\tilde{p}(\vec{r},t) = p_o(\omega)e^{i(\omega t + \varphi_p(\omega))} = FT\left\{\tilde{p}(\vec{r},\omega)\right\}$$

$$\tilde{u}_z(\vec{r},t) = u_{o_z}(\omega)e^{i(\omega t + \varphi_{u_z}(\omega))} = FT\left\{\tilde{u}_z(\vec{r},t)\right\}$$
Compute:

Compute:

$$\xi_{z}(\vec{r},t) = \int \tilde{u}_{z}(\vec{r},t) dt = \frac{1}{i\omega} \tilde{u}_{z}(\vec{r},t)$$

$$a_{z}(\vec{r},t) = \frac{\partial \tilde{u}_{z}(\vec{r},t)}{\partial t} = i\omega \tilde{u}_{z}(\vec{r},t)$$

$$\tilde{Z}_{z}(\vec{r},t) = \tilde{p}(\vec{r},t)/\tilde{u}_{z}(\vec{r},t) = I.I.R.(\vec{r},t)$$

$$\tilde{I}_{z}(\vec{r},t) = \frac{1}{2} \tilde{p}(\vec{r},t) \cdot \tilde{u}_{z}(\vec{r},t)$$

$$= \frac{1}{2} p_{o}(\omega) \cdot u_{o_{z}}(\omega) e^{i[\varphi_{p}(\omega) - \varphi_{u_{z}}(\omega)]} \left[1 + e^{-2i[\omega t + \varphi_{p}(\omega)]} \right]$$

$$= \frac{1}{2} I_{o_{z}}(\omega) e^{i\varphi_{I_{z}}(\omega)} \left[1 + e^{-2i[\omega t + \varphi_{p}(\omega)]} \right]$$

$$w(\vec{r},t) = \frac{1}{4 \sigma c^{2}} |\tilde{p}(\vec{r},t)|^{2} + \frac{1}{4} \rho_{o} |\tilde{u}_{z}(\vec{r},t)|^{2}$$

Frequency Domain:

Use e.g. LIA (and/or Spectral Analysis Techniques) to Measure:

$$\tilde{p}(\vec{r},\omega) = p_o(\omega)e^{i(\omega t + \varphi_p(\omega))} = FT\{\tilde{p}(\vec{r},t)\} \quad \{Pascals\}$$

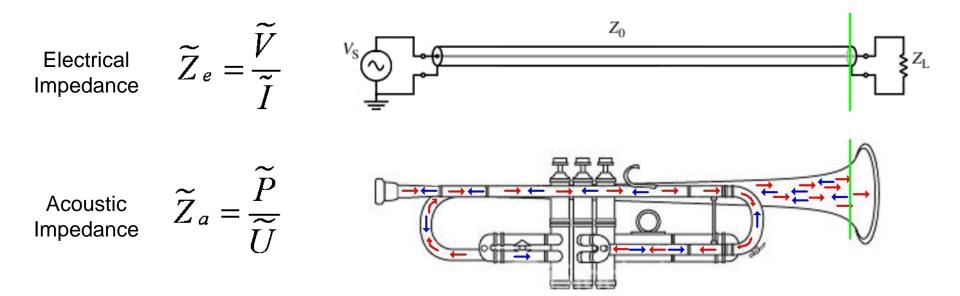
$$\tilde{u}_z(\vec{r},\omega) = u_{o_z}(\omega)e^{i(\omega t + \varphi_{u_z}(\omega))} = FT\{\tilde{u}_z(\vec{r},t)\} \quad \{mm/sec\}$$
Compute:

$$\begin{split} \xi_{z}\left(\vec{r},\omega\right) &= \int \tilde{u}_{z}\left(\vec{r},\omega\right) dt = \frac{1}{i\omega} \tilde{u}_{z}\left(\vec{r},\omega\right) \; \{mm\} \\ a_{z}\left(\vec{r},\omega\right) &= \frac{\partial \tilde{u}_{z}\left(\vec{r},\omega\right)}{\partial t} = i\omega \tilde{u}_{z}\left(\vec{r},\omega\right) \; \{mm/sec^{2}\} \\ \tilde{Z}_{z}\left(\vec{r},\omega\right) &= \tilde{p}\left(\vec{r},\omega\right) / \tilde{u}_{z}\left(\vec{r},\omega\right) \; \{Acoustic \; Ohms\left(Pa-sec/m\right)\} \\ &= \frac{1}{2} p_{o}\left(\omega\right) \cdot u_{o_{z}}\left(\omega\right) e^{i\left[\varphi_{p}(\omega)-\varphi_{u_{z}}(\omega)\right]} = Z_{o_{z}} e^{i\varphi_{Z_{z}}(\omega)} \\ \tilde{I}_{z}\left(\vec{r},\omega\right) &= \frac{1}{2} \tilde{p}\left(\vec{r},\omega\right) \cdot \tilde{u}_{z}^{*}\left(\vec{r},\omega\right) \; \{Watts/m^{2}\} \\ &= \frac{1}{2} p_{o}\left(\omega\right) \cdot u_{o_{z}}\left(\omega\right) e^{i\left[\varphi_{p}(\omega)-\varphi_{u_{z}}(\omega)\right]} = I_{o} e^{i\varphi_{I_{z}}(\omega)} \\ w(\vec{r},\omega) &= \frac{1}{4 \alpha c^{2}} \left|\tilde{p}\left(\vec{r},\omega\right)\right|^{2} + \frac{1}{4} \rho_{o} \left|\tilde{u}_{z}\left(\vec{r},\omega\right)\right|^{2} \{Joules/m^{3}\} \end{split}$$

Real part of complex *I*, *Z* associated with propagating sound

Imaginary part of complex *I*, *Z* associated with *non-propagating* sound energy (e.g. in "near-field" r $<< \lambda$ of sound source, or e.g. in SWT (where $Re\{I, Z\} \sim 0$))

Acoustic Impedance Analogous to Electrical Impedance

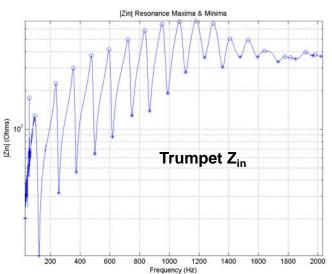


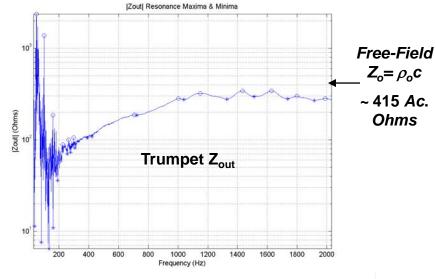
Impedance mismatch @ bell end means wave reflection, constructive interference of standing waves @ mouthpiece reinforces buzzing of player's lips!

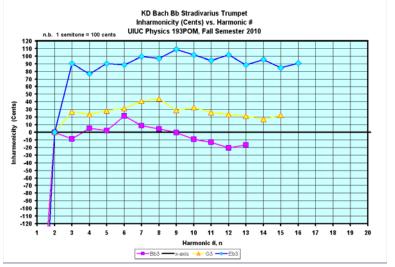
|Zin| maxima (pressure maxima, particle velocity minima occur for constructive interference) corresponds to standing waves, i.e. playable notes!

Measure input & output impedances Z(f) = p(f)/u(f) of brass/wind instruments \Rightarrow Maxima of $Z_{in}(f)$ defines which notes are playable on the instrument:





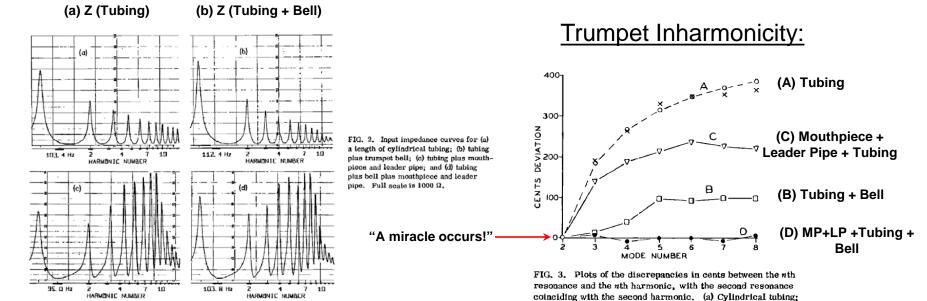




April 29, 2017

University of Toledo POM Talk

Acoustical Properties of Individual Components of Trumpet J. Backus, JASA 60, 460-80, 1976



(d) Z (MP+LP +Tubing + Bell)

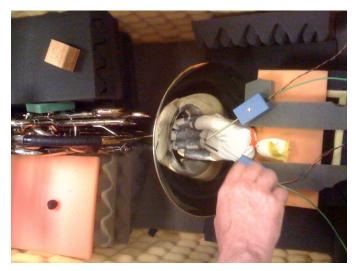
n.b. The design of the trumpet – centuries old instrument {1500 BCE; valves added ~ 1793) {as well as many other musical instruments} didn't have the benefit of the modern scientific knowledge of acoustics that we have today – musical solution(s) arrived at iteratively, by persistent effort(s) !!!

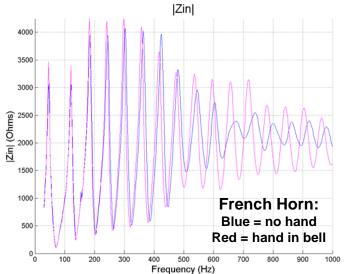
(b) tubing plus bell; (c) tubing plus leader pipe and mouthpiece; and (d) tubing plus bell plus leader pipe and mouthpiece.

(c) Z (Mouthpiece +

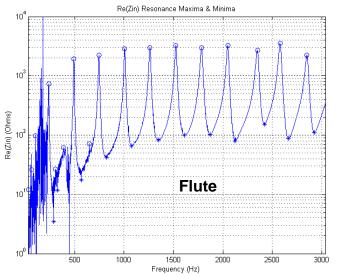
Leader Pipe + Tubing)

Have Measured Acoustic Properties of {Many Other} Other Brass/Wind Instruments, e.g.

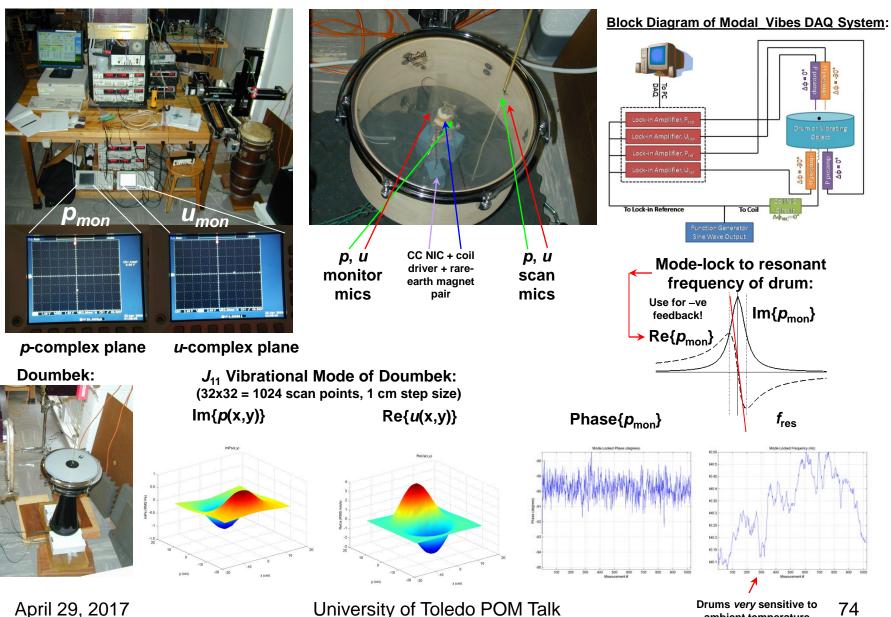








<u>UIUC P406POM Modal Vibes DAQ Experiment</u>: <u>Phase-Sensitive Near-Field Acoustic Holography!</u>

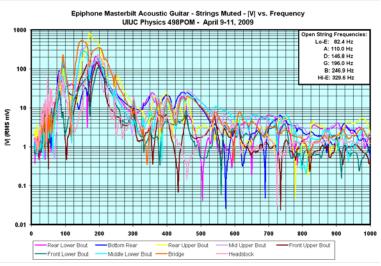


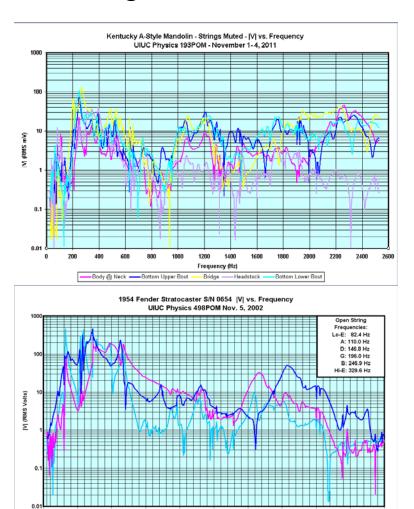
University of Toledo POM Talk

ambient temperature changes!

Mechanical Modal Vibrations of Stringed Instruments:



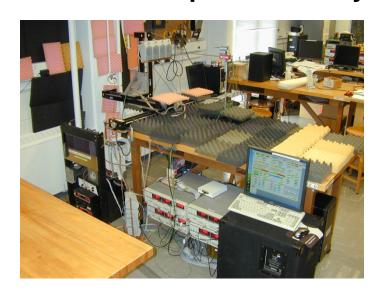


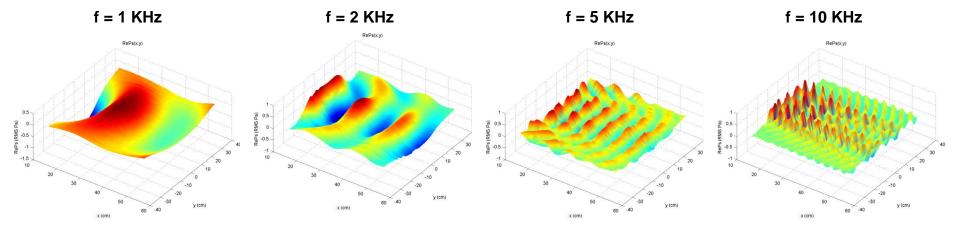


Body at Neck Heel -

Body at Bridge Headstock

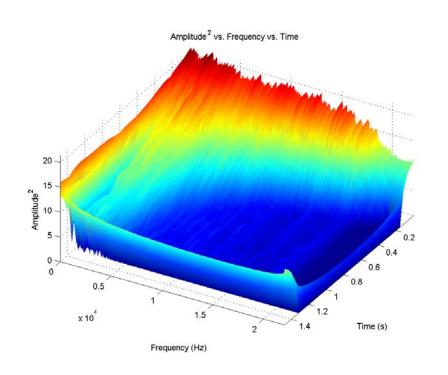
Complex Sound Field of Loudspeakers/Arrays of Loudspeakers:

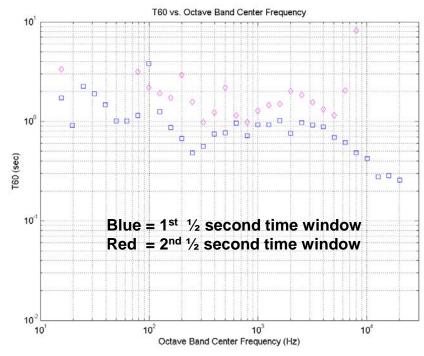




Auditorium/Room Acoustics:

Inject white noise (flat frequency spectrum) into a room, allow it to equilibrate, then adiabatically rapidly shut off sound source and measure exponential decay rate of sound vs. frequency (32 1/3-octave bands):





Recording Studio, UIUC School of Music

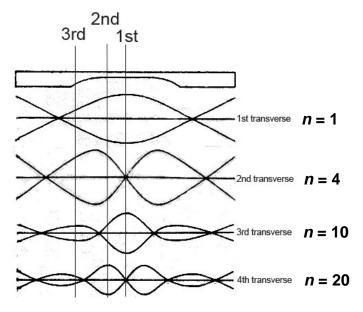
$$T_{60} \equiv -\frac{1}{2} \ln \left(10^{-6} \right) \cdot \tau_p \simeq 6.91 \tau_p$$

Time for sound to fall to 1 millionth of initial intensity $(\Delta SIL = -60 \text{ dB} = 10log_{10}(I_{final}/I_{init})$

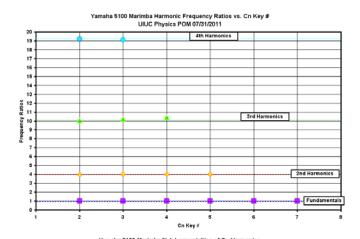
Marimba Studies:

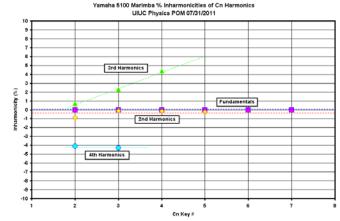


Mallet strike location – varies harmonic content/tone:



Sculpting of underside of marimba bar tunes bar, and harmonic content: 1 (fund), 4th, 10th & 20th...



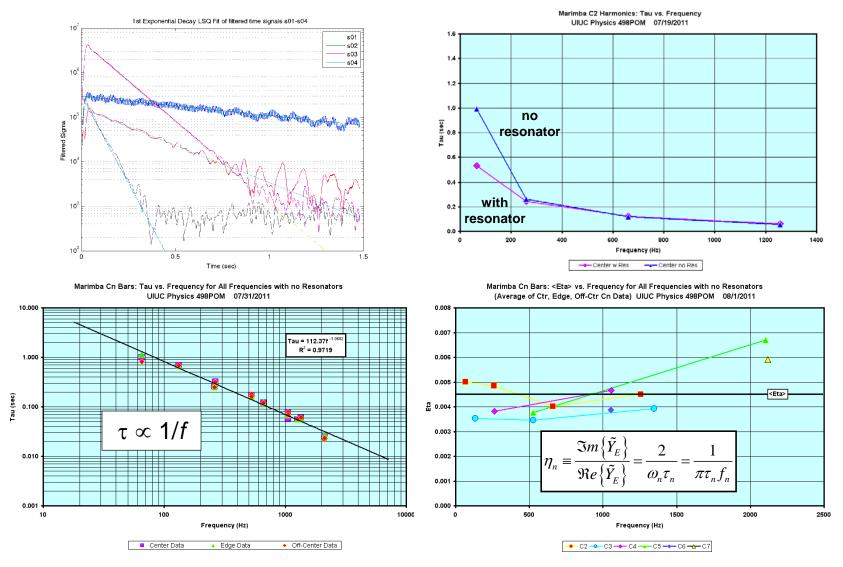


Resonators underneath marimba = open-closed organ pipe, matched to fundamental of each bar.

$$f_n = nf_1$$
, $n = 1,3,5,7...$ {odd harmonics}

⇒ Boosts fundamental

Marimba Studies – Measurement of the decay time(s) of harmonics of the C_n marimba bars (n = 2.7) and extraction of absorption coefficient η of rosewood



Fun with Spectral Analysis of (Any Kind of/YOUR Favorite) Music: Use e.g. AUDACITY (free-ware)

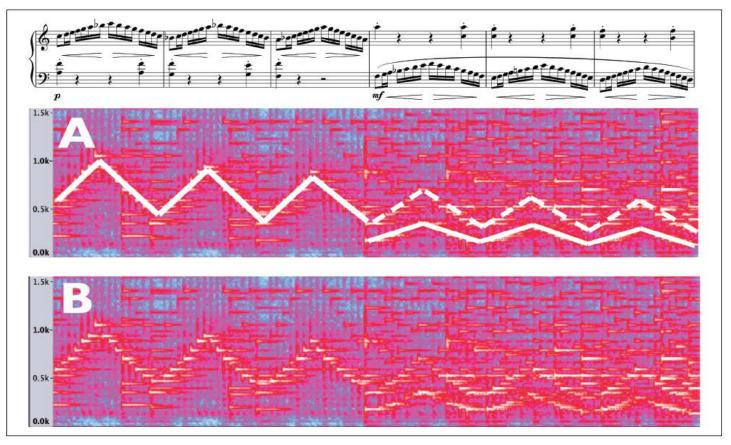


Figure 2. Underneath a standard score view, a spectrogram presents the false transition from Mozart K545. Image (A) is marked to help notice the octaves in unmarked image (B), which presents one reason listeners comfortably adapt to octave jumps. The top image (A) marks the fundamental pitch with a solid white line, which jumps down one octave halfway through the passage. When the line jumps, the dashed line makes clear that the overtone at the octave continues the original line

See e.g. Matthew D. Thibeault paper at: http://gmt.sagepub.com/content/25/1/50