

Maxwell's equations:

$$\vec{\nabla} \cdot \vec{D} = \rho_f \quad \vec{\nabla} \cdot \vec{B} = 0$$

$$\mu \vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \quad \vec{\nabla} \times \vec{H} = J_f + \frac{\partial \vec{D}}{\partial t} \quad \vec{D} = \epsilon \vec{E} \quad \vec{H} = \frac{1}{\mu} \vec{B}$$

Wave equation:

$$\nabla^2 \psi(\vec{r}, t) = \frac{1}{v^2} \frac{\partial^2 \psi(\vec{r}, t)}{\partial t^2}$$

Wave velocities: $v_p = \frac{\omega}{k}, v_g = \frac{d\omega}{dk}$

Plane wave:

$$\vec{E}(\vec{r}, t) = \tilde{\vec{E}}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \quad \tilde{\vec{E}}_0 \cdot \vec{k} = 0 \quad \omega \tilde{\vec{B}}_0 = \vec{k} \times \tilde{\vec{E}}_0$$

Poynting vector:

$$\vec{S} = \vec{E} \times \vec{H}$$

Field energy:

$$U = \frac{1}{2} \vec{E} \cdot \vec{D} + \frac{1}{2} \vec{B} \cdot \vec{H}$$

Stress tensor:

$$T_{ij} = (E_i D_j - \frac{1}{2} \delta_{ij} \vec{E} \cdot \vec{D}) + (B_i H_j - \frac{1}{2} \delta_{ij} \vec{B} \cdot \vec{H})$$

Force density:

$$\vec{f} = \vec{\nabla} \cdot \vec{T} - \epsilon \mu \frac{\partial \vec{S}}{\partial t}$$

Continuity equation:

$$\vec{\nabla} \cdot \vec{J}_Q = -\frac{\partial \rho_Q}{\partial t}$$

Snell's Law: $\frac{\sin \theta_t}{\sin \theta_i} = \frac{n_i}{n_t}$

Boundary conditions:

$$\epsilon_1 E_{1\perp} - \epsilon_2 E_{2\perp} = \sigma_f; \quad B_{1\perp} = B_{2\perp}; \quad E_{1\parallel} = E_{2\parallel}; \quad \frac{1}{\mu_1} B_{1\parallel} - \frac{1}{\mu_2} B_{2\parallel} = K_f$$

Normal incidence on dielectric:

$$T \equiv \frac{I_t}{I_i} = \frac{\epsilon_2 v_2}{\epsilon_1 v_1} \left(\frac{E_t}{E_i} \right) = \frac{4n_1 n_2}{(n_1 + n_2)^2}$$

$$R \equiv \frac{I_r}{I_i} = \left(\frac{E_r}{E_i} \right) = \frac{(n_1 - n_2)^2}{(n_1 + n_2)^2}$$

Math:

Fourier analysis:

$$\tilde{f}(z, t) = \int_{-\infty}^{+\infty} \tilde{A}(k) e^{i(kz - \omega t)} dk \quad \tilde{A}(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left[f(z, 0) + \frac{i}{\omega} \frac{\partial f(z, 0)}{\partial t} \right] e^{-ikz} dz$$

$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$\vec{\nabla} \cdot (\vec{A} \times \vec{B}) = \vec{B} \cdot (\vec{\nabla} \times \vec{A}) - \vec{A} \cdot (\vec{\nabla} \times \vec{B})$$

$$\vec{\nabla} \times (f \vec{A}) = f (\vec{\nabla} \times \vec{A}) - \vec{A} \times (\vec{\nabla} f)$$

$$\vec{\nabla} \times (\vec{A} \times \vec{B}) = (\vec{B} \cdot \vec{\nabla}) \vec{A} - (\vec{A} \cdot \vec{\nabla}) \vec{B} + \vec{A} (\vec{\nabla} \cdot \vec{B}) - \vec{B} (\vec{\nabla} \cdot \vec{A})$$

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{A}) = \vec{\nabla} \cdot (\vec{\nabla} \cdot \vec{A}) - \nabla^2 \vec{A}$$

Spherical unit vectors:

$$\hat{r} = \sin \theta \cos \phi \hat{x} + \sin \theta \sin \phi \hat{y} + \cos \theta \hat{z}$$

$$\hat{\theta} = \cos \theta \cos \phi \hat{x} + \cos \theta \sin \phi \hat{y} - \sin \theta \hat{z}$$

$$\hat{\phi} = -\sin \phi \hat{x} + \cos \phi \hat{y}$$

Cylindrical unit vectors:

$$\hat{s} = \cos \phi \hat{x} + \sin \phi \hat{y}$$

$$\hat{\phi} = -\sin \phi \hat{x} + \cos \phi \hat{y}$$

$$\int_{-\infty}^{\infty} e^{-(z+ik)^2} dz = \sqrt{\pi}$$