

Maxwell's equations:

$$\begin{aligned}\vec{\nabla} \cdot \vec{D} &= \rho_f & \vec{\nabla} \cdot \vec{B} &= 0 \\ \vec{\nabla} \times \vec{E} &= -\frac{\partial \vec{B}}{\partial t} & \vec{\nabla} \times \vec{H} &= J_f + \frac{\partial \vec{D}}{\partial t} \\ \vec{D} &= \epsilon \vec{E} & \vec{H} &= \frac{1}{\mu} \vec{B}\end{aligned}$$

Wave equation:

$$\nabla^2 \psi(\vec{r}, t) = \frac{1}{v^2} \frac{\partial^2 \psi(\vec{r}, t)}{\partial t^2} \quad \text{Wave velocities: } \mathbf{v}_p = \frac{\omega}{\mathbf{k}}, \mathbf{v}_g = \frac{d\omega}{d\mathbf{k}}$$

Plane wave:

$$\vec{E}(\vec{r}, t) = \tilde{\vec{E}}_0 e^{i(\vec{k} \cdot \vec{r} - \omega t)} \quad \tilde{\vec{E}}_0 \cdot \vec{k} = 0 \quad \omega \tilde{\vec{B}}_0 = \vec{k} \times \tilde{\vec{E}}_0$$

Poynting vector:

$$\vec{S} = \vec{E} \times \vec{H}$$

Field energy:

$$U = \frac{1}{2} \vec{E} \cdot \vec{D} + \frac{1}{2} \vec{B} \cdot \vec{H}$$

Stress tensor:

$$T_{ij} = (E_i D_j - \frac{1}{2} \delta_{ij} \vec{E} \cdot \vec{D}) + (B_i H_j - \frac{1}{2} \delta_{ij} \vec{B} \cdot \vec{H})$$

Force density:

$$\vec{f} = \vec{\nabla} \cdot \vec{T} - \epsilon \mu \frac{\partial \vec{S}}{\partial t}$$

Continuity equation:

$$\vec{\nabla} \cdot \vec{J}_a = -\frac{\partial \rho_a}{\partial t}$$

Impedance:  $Z = \frac{V}{I}$

Electric dipole radiation:

$$\begin{aligned}\vec{E}(\vec{r}, t) &= \frac{\mu_0}{4\pi r} (\hat{r} \times (\hat{r} \times \ddot{\vec{p}})) = \frac{\mu_0 \ddot{\vec{p}}}{4\pi} \left( \frac{\sin \theta}{r} \right) \hat{\theta} & \vec{B}(\vec{r}, t) &= \frac{\hat{r} \times \vec{E}}{c} \\ \langle \vec{S} \rangle &= \left( \frac{\mu_0 p_0^2 \omega^4}{32\pi^2 c} \right) \frac{\sin^2 \theta}{r^2} \hat{r}\end{aligned}$$

Radiation from a point charge:  $\vec{E} = \frac{q}{4\pi\epsilon_0 (\vec{r} \cdot \vec{u})^3} (\vec{r} \times (\vec{u} \times \vec{a}))$ , where  $\vec{u} = c\vec{r} - \vec{v}$ .  $P = \frac{\mu_0 q^2 a^2}{6\pi c}$

Math:

Fourier analysis:  $\tilde{f}(z, t) = \int_{-\infty}^{+\infty} \tilde{A}(k) e^{i(kz - \omega t)} dk \quad \tilde{A}(k) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \left[ f(z, 0) + \frac{i}{\omega} \frac{\partial f(z, 0)}{\partial t} \right] e^{-ikz} dz$

$$\begin{aligned}e^{i\theta} &= \cos \theta + i \sin \theta & \vec{\nabla} \cdot (\vec{A} \times \vec{B}) &= \vec{B} \cdot (\vec{\nabla} \times \vec{A}) - \vec{A} \cdot (\vec{\nabla} \times \vec{B}) \\ \vec{\nabla} \times (f\vec{A}) &= f(\vec{\nabla} \times \vec{A}) - \vec{A} \times (\vec{\nabla} f) & \vec{\nabla} \times (\vec{A} \times \vec{B}) &= (\vec{B} \cdot \vec{\nabla}) \vec{A} - (\vec{A} \cdot \vec{\nabla}) \vec{B} + \vec{A}(\vec{\nabla} \cdot \vec{B}) - \vec{B}(\vec{\nabla} \cdot \vec{A}) \\ \vec{\nabla} \times (\vec{\nabla} \times \vec{A}) &= \vec{\nabla} \cdot (\vec{\nabla} \cdot \vec{A}) - \nabla^2 \vec{A}\end{aligned}$$

Spherical unit vectors:

$$\begin{aligned}\hat{r} &= \sin \theta \cos \phi \hat{x} + \sin \theta \sin \phi \hat{y} + \cos \theta \hat{z} \\ \hat{\theta} &= \cos \theta \cos \phi \hat{x} + \cos \theta \sin \phi \hat{y} - \sin \theta \hat{z} \\ \hat{\phi} &= -\sin \phi \hat{x} + \cos \phi \hat{y}\end{aligned}$$

Cylindrical unit vectors:

$$\begin{aligned}\hat{s} &= \cos \phi \hat{x} + \sin \phi \hat{y} \\ \hat{\phi} &= -\sin \phi \hat{x} + \cos \phi \hat{y}\end{aligned}$$