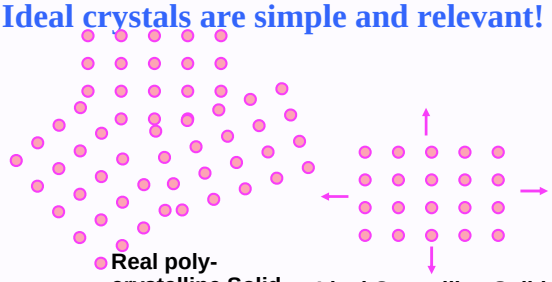
Lecture 2 - Structure of crystals

Solid State Physics 460- Lecture 2
Structure of Crystals
(Kittel Ch. 1)

See many great sites like "Bob's rock shop" with pictures and crystallography information on the web at
www.rockhounds.com/rockshop/xtal/index.html

Ideal crystals are simple and relevant!

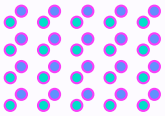


- Many solids are made of crystallites that are microscopic - but contain ~ 10^{20} atoms!

Crystals

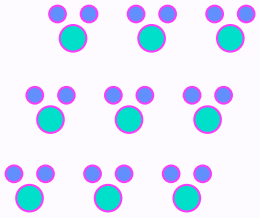
- A crystal is a repeated array of atoms
- Examples

Array of atoms
Each atom is identical



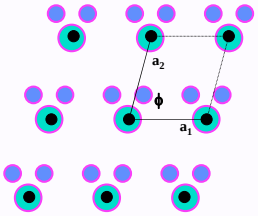
Array of atoms
Two types of atoms

Two Dimensional Crystals



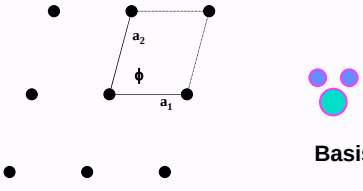
(Easier to draw in 2 dimensions – 3 dimensions later)

Two Dimensional Crystals



Lattice

Two Dimensional Crystals



Basis

Lattice

- Infinite number of possible crystals
- Finite number of possible crystal types

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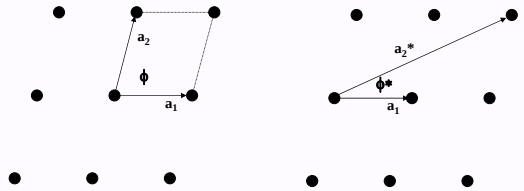
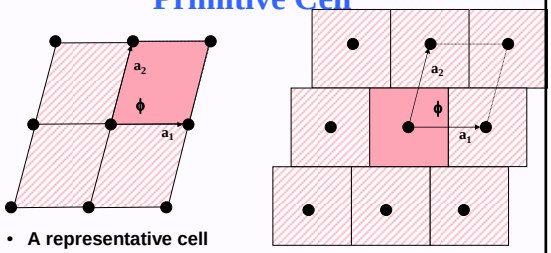
Lattices and Translations



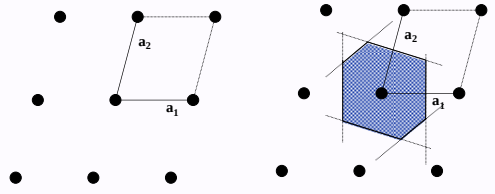
- The entire infinite lattice is specified by 2 primitive vectors a_1 and a_2 (also a_3 in 3-d)
- $T(n_1,n_2,...) = n_1 a_1 + n_2 a_2$ (+ $n_3 a_3$ in 3-d), where the n's are integers
- Note: the primitive vectors are not unique different vectors a_1 and a_2 can define the same lattice

Primitive Cell



- A representative cell
- Translation of a primitive cell fills space
- $T(n_1,n_2,...) = n_1 a_1 + n_2 a_2$ where the n's are integers
- Note: the primitive cells are not unique different cells can fill all space
- All primitive cells have the same are (volume)

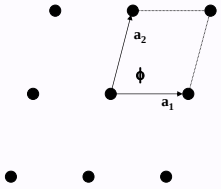
Two Dimensional Lattices Primitive Cell and Wigner-Seitz Cell



One possible Primitive Cell Wigner-Seitz Cell -- Unique

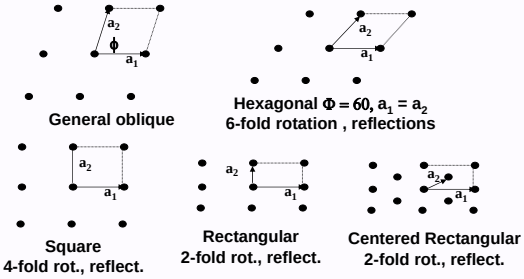
- All primitive cells have same area (volume)
- Wigner Seitz Cell is most compact, highest symmetry cell possible
- Also same rules in 3 dimensions

Possible Two Dimensional Lattices



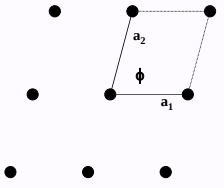
- Special angles ϕ = 90 and 60 degrees lead to special crystal types
- In addition to translations, the lattice is invariant under rotations and/or reflections

Possible Two Dimensional Lattices



- These are the only possible special crystal types in two dimensions

More on Two Dimensional Lattices



- Why is it imposible to have a crystal with a five-fold rotation symmetry?
- Why is the centered square not a special type?

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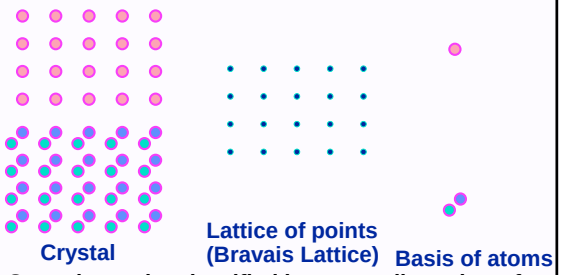
Classification of Crystal Structures

- Crystal structures classified by:
- Translation symmetry
  - Only the Bravais lattice
  - Limited number of possible Bravais lattice types
- Rotation, Inversion, reflection symmetry
  - Depends upon basis
  - Limited number of possible crystal types
- Examples in 2 dimensions
  - (3 dimensions later)
- See Kittel for lists of possible translation types.
  - See other crystallography references for lists of all possible crystal types

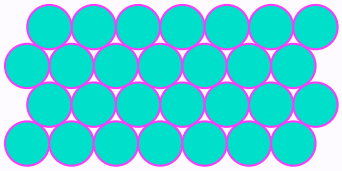
Summary at this point

- A crystal is a repeated array of atoms
- Crystal ⇔ Lattice + Basis



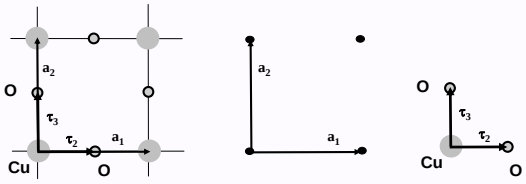
- Crystals can be classified into a small number of types – See text for more details

Examples of Crystals
Close packing of spheres in a 2-d crystal



- Each sphere has 6 equal neighbors
- Close packing for spheres
- Hexagonal symmetry (rotation by 60 degrees)
- Actually occurs for rare gas atoms (spherical) on a flat surface

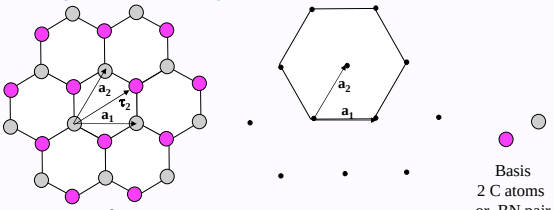
Crystalline layers with >1 atom basis



CuO_2 Square Lattice Square Lattice CuO_2 Basis

- One CuO_2 layer in the High Tc superconductors
- Square lattice
- One basis unit on each site

Crystalline layers with >1 atom basis



Honeycomb Lattice
(graphene or BN layer) Hexagonal Lattice

- A single layer of graphitic carbon (graphene)
  - The two atoms in the cell are both Carbon
- A single layer of hexagonal boron nitride (BN)
  - The two atoms in the cell are B and N

Next Time

- More on Crystal Lattices - Continue Kittel, Ch. 1
- 3 Dimensions
- Lattice planes
- Examples of crystals