Photon enission. $e^+e^- \rightarrow \mu^+\mu^- \gamma$

We now consider an O(a) correction to the process we studied last week. $\frac{e^{2}}{e^{2}}$
 $\frac{e^{2}}{e^{$ ext_{n-1} Photen polarization $Q^2 = (p_1+p_2)^2$) m^2 so we can ignore m_e , m_{μ} . $iM = i \frac{e^{2}}{a^{2}} \overline{V}(\rho_{x}) Y_{m} u(\rho_{1}) \overline{u}(\rho_{3}) \left[Y^{\prime} \frac{-i(\rho_{1}+\rho_{1})}{(\rho_{1}+\rho_{1})^{2}} (-iY^{\alpha}) + (-ieY^{\alpha}) \frac{i(\rho_{3}+\rho_{1})}{(\rho_{3}+\rho_{1})^{2}} Y^{\prime} \right] V(\rho_{1}) \epsilon_{\alpha}^{\beta}(\rho_{1})$

interact ferting proposator

defined in the mortal mathematics Let $S^{M^{d}} = -ie[Y^{\kappa} \frac{i(\rho_{3}+\rho_{1})}{(\rho_{3}+\rho_{1})^{2}}]Y^{M} - \gamma^{m} \frac{i(\rho_{4}+\rho_{1})}{(\rho_{4}+\rho_{1})^{2}}Y^{M} \Big]$ (not symmetric in m and a) Cross section after averaging over initial and sumving over final spins is $\sigma_{\gamma} = \frac{1}{2\alpha^2} \int d\pi \sqrt{|\mu|^2} = \frac{e^T}{2a^6} \int^{+V} X_{\gamma}$ $I_{\nu_1-\nu_2/4}$ a²=(2E,)(2E,) in CM frame w/ E = E = $\frac{\sqrt{a^2}}{2}$ L' is left half of the dingram! $L^{m'} = \frac{1}{4} \sum_{s,s} \overline{v}_s^{\prime}(\rho x) Y^{m} u_{s,s}(\rho_1) \overline{u}_{s,s}(\rho_1) Y^{v} v_{s,s}(\rho_2) = \frac{1}{4} T r L \rho_2 Y^{m} \rho_1' Y^{v} = \rho_1^{m} \rho_2^{v} + \rho_1^{v} \rho_2^{v} - \frac{1}{L} \alpha^{m} \rho_1^{mv}$ $X^{r\prime}$ is right halt, involving the photon: from $(\bar{u}Y)$ $X^{m\prime} = \int d\eta_{3} \sum_{s_{1},s_{2},\dots} \left[\overline{u}_{s_{3}}(\rho_{3}) \right] S^{m\alpha} v_{s_{1}}(\rho_{4}) \overline{v}_{s_{4}}(\rho_{1}) \int^{\beta\upsilon} u_{s_{3}}(\rho_{3}) \epsilon_{\alpha}^{\beta}(\rho_{1}) \epsilon_{\rho}(\rho_{1}) \int \right]$

Capologies for Use $\sum_{\text{pols.}} \epsilon_{\alpha}^{\phi}(\rho_{Y}) \epsilon_{\rho}(\rho_{Y}) \rightarrow -\eta_{\alpha,0}$. $X_{\text{mv}} = -\int d\Pi_{3}Tr[\phi_{3}S^{\text{max}}\phi_{4}S^{\text{min}}]$ height: Useful abuse

OF notation

Hint, we use the length of
$$
g
$$
 over 3-body phase space, d_1 , $e^{-\frac{1}{2}r}$, $\frac{d^2r}{dr^2} + \frac{d^2r}{dr} - \frac{1}{2}r$, $\frac{1}{2}r$, $(2\pi)^2$ Γ (Q- r) = $\frac{1}{2}r$ (P- r)

\nwhere $Q = f_1 f_1 f_2$.

\nLet's put off actually, including $x^{-\alpha}$ for α bit and see what the cross section looks like for a general limit state.

\nBy the *Wank* identity, we know $Q_n X^{-\alpha} = 0$, $A f_1$ or β have space in function 0 .

\nSo $X_{\mu\nu} = (Q_n Q_{\mu} - Q_{\mu\nu}) X(Q)$

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\nIn this form, $1^{-\alpha}X_{\mu\nu} = (Q_n - 4e^{-\alpha})X(Q_n^2)$, so $X(Q_n^2) = -\frac{1}{3}e^{-\alpha}T^{-\alpha}X_{\mu\nu}$

\nThus in f_1 , f_2 , f_3 , f_4 , f_5 , f_6 , f_7 , f_7 , f_8 , f_9 , <

There is a nice way to interpret this result, let's write

\n
$$
\begin{array}{rcl}\n\sigma_Y &= & \frac{4\pi\sigma_o}{\alpha} \times \frac{1}{2\alpha} \times {}^{IV}(-\eta_{\pi\nu}) & \text{where} & \alpha = \sqrt{\alpha^2}. \quad \text{Re decay rate} \\
0 &= & \frac{1}{2\alpha} \times {}^{IV}(-\eta_{\pi\nu}) & \text{where} & \alpha = \sqrt{\alpha^2}. \quad \text{Re decay rate} \\
0 &= & \frac{1}{2\alpha} \int d\pi \leq |M|^2 \geq 0 \\
\text{for a point of the right, } & \alpha = \frac{1}{2\alpha} \int d\pi \leq |M|^2 \geq 0 \\
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From HW 9, S+ t+u = $\sum m_i^2 \approx Q^2$ (you derived it for $p_i+p_k \rightarrow p_i+p_j$ but a similar result holds with appropriate minus signs for $Q \rightarrow P_3 r p + Y)$ $27 x + x + x$ = 2, take $x_r = 2-x_r-x_r$ so x_r and x_r are independent. Limits of integration: $t = 2t_3$ ipr = $2e_3E_r(1-cos\theta_{3r})$. $t_{min} = 0$ when $E_r = 0$; Limits of integration, $t = 2$ p; pr = $\sum E_{3} E_{r} (1 - \cos \theta_{3r})$, $t_{min} = 0$ when
track= 4Ez Ex when Cos θ_{3r} =1. If $E_{4} = 0$, $E_{3} = E_{r} = \frac{\alpha}{L}$, so $t_{max} = \alpha^{2}$ $22 x_{i_1} x_{i_2} \geq 0$, $x_{i_1} x_{i_2} \geq 1$

$$
\int d\Pi_{3} = \frac{Q^{2}}{128\pi^{3}} \int_{0}^{1} dx, \int_{1-x_{1}}^{1} dx_{2} \qquad (recall \text{ very similar form from } Hw3)
$$

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\int c [R_{3}S^{max}f_{4}S^{max}] = \frac{8e^{2}(x_{1}^{2}tx_{2}^{2})}{(1-x_{1})(1-x_{2})} \qquad (Although ex for ce l.4)
$$

\nThis diverges (open, times $(\int_{0}^{1} dx) dX_{1}x_{2} = 1$.

By the analysis above,
$$
x_i = 1
$$
 corresponds to the $\frac{1}{2}\pi/1-\cos\theta_{2x} = 0$.
\nThis can happen either if $Er = 0$ (a $\frac{1}{2}\pi/1-\cos\theta_{2x} = 0$)
\n(a $\frac{1}{2}\pi/1-\cos\theta_{2x} = 0$ (b $\frac{1}{2}\pi/1-\cos\theta_{2x} = 0$)
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L 10 More concrete interpretation an real experiment will have a finite eary resolution Eres and angular resolution Fres - Instead of Cutting off the integral with er, use Eve, and Eres instead. This is technically complicated, so we will justquote the answer ! o(ste - err)/EnLErs = (lue, [Iu(Ere, -1) - ...]+--) exclusive - Cross section (exactly / OvaL Gres photon) Focus on Inves If Q >> Eves, could be in a situation where In (EEes)(, and peturbation theory breaks down . Solution : Consider etem+n+ NV, ad don't restrict to a fixed number of photons . This is no conser ata fixed order in the coupling e, but corresponds better to the physical situation where distinguishing 2 vs. 3 vs- [↑] very Cow-energy photons isn't possible in practice. Inclusive cross sections ofte have better convergence properties. * Hw: emission of photon from initial state. Lessons - From this weele :

- · QFT gives infinities when you ask it dumb (unphysical) questions. By relating amplitudes to ^a physically measurable quantity, we always get finite results.
- · Singularities tend to appear beyond the lowest-orde diagrams. Resolving Den may require summing over several amplitudes cohrently. Singularities tend to appear begond the courspare
- electron magnetic moment is one example.