Fegrant rules



 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$ 

 $\int$ 

Let's construct the Feyuman diagram for te lowest-order Contribution to  $e^+e^- \longrightarrow \mu^+\mu^-$ Ne lowest-o-de<br>
Ferindon;<br>
external states are "on-stell"<br>
internal lines are<br>
"virtual particles"

 $\frac{2}{\sqrt{2}}$  $\geq$ 

internal lines are



several things to note !

- · terms in brackets are Lorentz ↑-vectors, but all spinor indices have been Contracted. Macmoria: work backwards along fermion arrows.
- · Momentun conservation enforced at each retex : P, Pr flows into photon propagator, and this is equal to  $p_3 + p_4$ and this is equal to  $p_3 + p_4$  thous<br>number, which are call  $i$ M (i is convertional).
- · The final answer is a number ,

Recipe for computing cross sections ?

- · Write down all Feyuman diagrams at <sup>a</sup> given order in coupling <sup>2</sup> · Choose Spins *for exter*nal states<sub>,</sub> evaluate IMI<sup>2</sup>
- Integrate over Phase space to get o , or integrate over part of phase space to get a differential cross section  $\frac{d\sigma}{dx}$ , which gives a distribution in the variabless  $x$ . we for external states, evaluate  $|M|^{2}$ <br>were phose space to get  $\sigma$ , or integrate over<br>hase space to get a differential cross section do<br>es a distribution in the variables x.<br>were the outgoing in and the incoming  $e^{-i\Lambda$

In particular, we want to understand does - nth is the angle between the outgoing in and the incoming e in the center of momentum frame where  $\widehat{\rho}_{i}$ r  $=$  0

Exalina tiny the matrix element

\n
$$
M \approx \left[ \overline{v}_{n}(h) [L(eY^{n})u_{n}(h)] \left( \frac{-i \eta_{n}v}{(h^{n}h)^{n}} \right) \left[ \overline{u}_{n}(h) [L(eY^{n})u_{n}(h)] \right]
$$
\nFirst, need to specify spins, we will assume the initial  $e^{-\alpha x}e^{x}$  between  $\alpha e^{-\alpha x}$  by  $\alpha e^{x}$ .

\nAlso using the *detected* to the *int*  $\alpha$  to the *int*  $\alpha$ 

Now arrase over  $s_1$  and  $s_2$ . Once we write the indices explicitly, we can rearrange terms at will!

$$
\sum_{\begin{array}{l}5\\5\\2\end{array}} w_{s_1}(p_1)_{\beta} \overline{u}_{s_1}(p_1)_{\gamma} = (f_1 + n_e)_{\beta \gamma} \qquad \qquad \sum_{\begin{array}{l}e \text{prime,} \\ e(ect \text{on} / \text{positive,} \\ n_e \text{no.} \end{array}} p_1 \text{ and } p_2 \text{ (etc. } 6)
$$
\n
$$
\sum_{s_2} v_{s_2}(p_1)_{\sigma} \overline{v}_{s_2}(p_2)_{\alpha} = (f_2 - n_e)_{\sigma \alpha} \qquad \qquad \sum_{\begin{array}{l}n_{\alpha=55}\\n_{\alpha=55} \end{array}} e(ect \text{on} / \text{positive,} \text{momenta, } s_0)
$$
\n
$$
= \frac{1}{4} (f_2 - n_e)_{\sigma \alpha} Y_{\alpha \beta} (f_1 + n_e)_{\beta \gamma} Y_{\gamma \delta}^{\prime}
$$
\n
$$
= \frac{1}{4} [f_2((f_2 - n_e)Y_{\alpha} (f_1 + n_e)Y_{\beta})^{\prime}]
$$

Find step: integrate over phase space to obtain 
$$
\frac{d\sigma}{d\cos\theta}
$$
.  
\nLast week we saw that 2-body phase space took a  
\nparticularly simple form.  
\n $d\Pi_{\nu} = \frac{1}{16\pi^2} d\Omega = \frac{1/\rho e}{E_{\nu}}$   $\Theta(E_{\nu} - m_{\nu} - m_{\nu})$   
\n $d\sigma = \frac{1}{(k_{\mu} - \rho)\epsilon_{\mu} + \rho}$   $(1/11)^2 d\Pi_{\nu}$   
\n $\Gamma_{\nu} = \frac{1}{k_{\mu} - \rho} \sum_{\nu} (1/11)^2 d\Pi_{\nu}$   
\n $\Gamma_{\nu} = \frac{1}{k_{\mu} - \rho} \sum_{\nu} (1/11)^2 d\Pi_{\nu}$   
\n $\Gamma_{\nu} = \frac{1}{k_{\mu} - \rho} \frac{1}{k_{\mu$ 

Can also integrate over 6 to get total cross section.  $\sigma = \int \frac{d\sigma}{d\cos\sigma} d\cos\theta = \frac{\pi\alpha^2}{2E^2} \int_{-1}^{1} (1+x^2) dx = \frac{4\pi\alpha^2}{3E^2}$ For known E, can use this to measure x.