Discovery of the W/2 and Higgs

The predictions of electroweak symmetry breaking were confirmed in spectacular Fashion with the discovery of the W and Z bosons at CERN in 1983, and the discovery of the Higgs boson in 2012. Today we will survey these processes, which took place at proton-proton colliders, and additionally examine the precision electroweak tests that can take place at electron-positron colliders. Throughout, we will exploit the simplifications of the narrow-width approximation to factorize production and decay:  $\sigma(initial state \rightarrow X \rightarrow final state) ~ \sigma(initial state \rightarrow X) \times Br(X \rightarrow fin(state))$ 

W production in pp collisions

From the W coupling to quarks, the following diagram exists:  

$$M_{u\bar{u}} = \frac{i9}{5\pi} V_{u\bar{u}} \overline{v(p_A)} \gamma^n (\frac{1-\gamma^5}{2}) u(p_u) \epsilon_u^n(p_w)$$

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As we saw when we discussed QCD, we need to weight this matrix element by the parton distribution Function of the proton, which counts quarks. At energies >100 GeV, the poton's quark content is mostly u and d value quarks, so this diagram suffices.

This is very similar to the t-6W diason we computed last week. Indeed, all that charges is  $V_{tb} \rightarrow V_{ud}$  and a  $\overline{v}$  instead of a  $\overline{u}$  spinor. But since the only difference is the sign of the quark mass term in the trace, and the terms proportional to  $m_t$  vanished, we can just borrow the result from last time, with a slightly different perfector:

 $\langle M|^2 \rangle = \frac{9^2}{12} |V_{ua}|^2 \left( p_u \cdot p_d + \frac{2(p_u \cdot p_w)(p_d \cdot p_w)}{mw^2} \right)$ average our spins

arraye over spins and wlors: 2x2 for spins, only 3 colors since W doesn't change quark color

This time, we have  $p_n + p_d = p_w$ . Defining  $(p_n + p_d)^2 = \hat{S}$ , the dot products are  $p_n \cdot p_d = \hat{S}$ ,  $p_n \cdot p_w = p_d \cdot p_w = \hat{m}_{12}^{*}$ , so  $(|m|^2) = \hat{T}_{12}^{*} |V_{nd}|^2 (\hat{S}_{12} + \hat{m}_{12}^{*})$ 

$$\sigma(u\overline{d} \Rightarrow w^{+}) = \frac{1}{2\hat{s}} \int dT_{1} \langle ln|^{2} \rangle \text{ where} \qquad [2]$$

$$\int dT_{1} = \int \frac{d^{3}\rho_{w}}{(ln)^{3}2E_{w}} (2\pi)^{+} \int^{(h)} (\rho_{w} + \rho_{d} - \rho_{w}) = 2\pi \delta(\hat{s} - m_{w}^{+})$$

$$(as we've alluded to before, 1-particle phase space has one unresolved  $\delta$ -function)
Therefore we can set  $\hat{s} = m_{w}^{-1}$  in the matrix element, giving
$$\sigma(u\overline{d} \Rightarrow w^{+}) = \frac{1}{NS} NT \left(\frac{g^{+}}{12} |V_{ud}|^{-} (m_{w}^{+})\right) \delta(\hat{s} - m_{w}^{-})$$

$$= \frac{T g^{-}}{12} |V_{ud}|^{2} \delta(\hat{s} - m_{w}^{-}) \text{ where } \alpha_{w} = \frac{g^{2}}{9\pi} (\text{ where "fine-structure constat"})$$$$

$$= \sum x_{1} = \frac{\sqrt{3}}{\sqrt{5}} e^{y}, \quad \text{Similarly } x_{1} = \frac{\sqrt{3}}{\sqrt{5}} e^{-y}$$
$$\frac{\partial(x_{1}, x_{2})}{\partial(\hat{s}, y)} = \frac{e^{y}}{\sqrt{5}} \frac{e^{-y}}{\sqrt{5}} = \frac{1}{2\sqrt{5}\sqrt{5}} = \frac{1}{5}$$
$$\frac{\sqrt{3}}{\sqrt{5}} e^{-y} = \frac{\sqrt{3}}{\sqrt{5}} = \frac{\sqrt{3}}{\sqrt{5}} = \frac{1}{5}$$

=>  $dx_1 dx_2 f(\hat{s} - m^2) = \frac{1}{5} d\hat{s} dY f(\hat{s} - m^2)$  $= \operatorname{r}(\rho\overline{\rho} \rightarrow w^{+}) = \frac{\pi^{2} \alpha_{w}}{3s} |V_{ua}|^{2} dY \left[ f_{u} \left( \frac{\alpha_{w}}{\sqrt{s}} e^{y} \right) f_{a} \left( \frac{\alpha_{w}}{\sqrt{s}} e^{y} \right) + f_{a} \left( \frac{\alpha_{w}}{\sqrt{s}} e^{y} \right) f_{u} \left( \frac{\alpha_{w}}{\sqrt{s}} e^{y} \right) \right]$  Note that once we know the W exists, this process can be used to measure the PDF's!

However, there are also QCD corrections from quotes entiting time-state gluons,  
SU 
$$\lceil w \Rightarrow j_{its} = \frac{\alpha_w M_w}{4} (1 + \frac{\alpha_s(m_w)}{\pi}) \left[ |V_{cs}|^2 + |V_{cs}|^2 + |V_{ud}|^2 + |V_{us}|^2 + |V_{ul}|^2 \right]$$
  
 $= 1.34 \text{ GeV}$   
 $\lceil tot = 2.085 \text{ GeV from POG, so predict Br (w \Rightarrow j_{its}) = \frac{\lceil w \Rightarrow j_{its} \rceil}{\lceil tot} = 64\%$ .  
Experimentally, Br (w  $\Rightarrow j_{efs}$ ) = 67.41%; not bad! (QCD corrections important)  
 $\lceil tot = leptonic decoy, no sum over colors:  $\lceil w \Rightarrow lv = \frac{\alpha_w M_w}{12}, equal for$   
 $e, M, T up to phase space effects for nonzero M_L. Again, well-supported by data.$$ 

Couples to all SM ternibus:  $\frac{h}{Z} = \frac{h}{F} + \frac{f}{F}$   $iM = \frac{ig}{\cos\theta_w} \left(T^3 Y^m \rho_L - Q \sin^2\theta_w Y^m\right) E_n(\rho_2)$   $= \frac{ig}{2\cos\theta_w} \left(T^3 Y^m (1-Y^5) - 2Q \sin^2\theta_w Y^m\right) E_n(\rho_2)$   $\equiv \frac{ig}{2\cos\theta_w} \left(C_V Y^m - C_A Y^n Y^5\right) E_n(\rho_2)$ 

Here,  $C_{v} \equiv T^{3} - 2\omega \sin^{2}\omega \text{ and } C_{A} \equiv T^{3} \text{ are "vector" and "axial-vector" couplings.}$ This may of writing things makes spino-products in 4-component notation lasier:  $[T_{V}^{n}Y^{5}V]^{+} = v^{+}Y^{5}(Y^{n})^{+}Y^{0}u = v^{+}Y^{5}Y^{0}Y^{n}u = -\overline{v}Y^{5}Y^{n}u = +\overline{v}Y^{n}Y^{5}u$ For trample, for f = e,  $T = -\frac{1}{2}$  and R = -1,  $C_{v} = -\frac{1}{2} + 2\sin^{2}\omega u$ ,  $C_{A} = -\frac{1}{2}$ . So  $< |M_{2} - 2ee|^{2} > = \frac{1}{3} \frac{2^{2}}{4\pi \omega^{2}\omega} \sum_{spins} \overline{v}(p)(c_{v}Y^{n} - c_{A}Y^{n}Y^{5})u(p_{i})\overline{u}(p_{i})(c_{v}Y^{v} - c_{A}Y^{v}Y^{5})v(p_{i})E_{i}(k)E_{i}(k)E_{i}(k)$ (setting me=0)  $= \frac{1}{3} \frac{2^{2}}{4\pi \omega^{2}\omega} Tr[P_{1}Y^{v}(c_{v} - c_{A}Y^{5})P_{1}Y^{n}(c_{v} - c_{A}Y^{5})](-\eta_{nv} + \frac{P_{2n}P_{2v}}{m_{2}^{*}})$  $= \frac{1}{3} \frac{2^{2}}{4\pi \omega^{2}\omega} Tr[P_{1}Y^{v}P_{1}Y^{n}(c_{v}^{*} + c_{A}^{*} - 2c_{v}c_{A}Y^{5})](-\eta_{nv} + \frac{P_{2n}P_{2v}}{m_{2}^{*}})$ 

As with the quick decay, the XS trace is proportional to the [5  
antisymmetric tasor 
$$e^{n\sqrt{n/n}}$$
, so it vanishes when contracted with the  
polarization sum. The 4-vector products are identical to previous  
calculations, so we can just stip to the answer:  
 $\langle |M|D^{-} = \frac{2^{-}}{3\cos^{2}\omega} \left(P_{1}P_{2} + \frac{2(P_{1}P_{2})(P_{1}P_{2})}{n^{2}}\right) \left(c_{v}^{-} tc_{A}^{-}\right)$   
 $= \frac{2^{-m}n^{-}}{3ca^{2}\omega} \left(c_{v}^{-} tc_{A}^{-}\right)$   
 $T_{2acv}^{-} \frac{1}{2m} \left(IM_{2acv}^{-}\right)^{-} \right) = \frac{\alpha_{v}m_{2}}{3ca^{2}\omega_{v}} \left(c_{v}^{-} tc_{A}^{-}\right)$   
As with W's, this pedicts;  
· Equal backing Fractions into  $e/n/T$ , up to mass effects (a Hw)  
· hadraic decays enhanced by a factor of 3 for color, but also  
 $c_{v}^{-} rc_{A}^{-} = 1$  different! In the end, 70% to hadray vs. 30% to  
choosed (eptons + neutrinos.  
· Decay products are polarized! Indeed, W decay products are fully  
polarized (in massless approximation), since W only complets to L spinors,  
but Z decays are partially polarized, depending on fermion (o Hw)

· Easy to reconstruct mass of Z at ete collide: Look for events with ntm, m2=-(p\_m+p\_m)

## Discovery of the Higgs

Finally, let's examine the last piece of the Standard Model. For Huy you will calculate H=366 and H=3WW, 22. Since Higgs couplings are proportional to mass, we should try to produce it ad detect it with the heaviest initial-and final-state particles possible. However, pervesely,  $m_h < 2m_f$  and  $m_h < 2m_W$ , so decays into an-shell tops or gauge basans are kinematically forbidden. Even worse,  $m_b^2 0.02m_f$ , so decays to 6's are smaller by ~ 10<sup>4</sup>, and 2-jet events have an enormous QCD backsome! To find the Higgs at the LHC, experimentalists and theorists had to get creative. Tuo stratesies.

1)  $\frac{\partial FF-she'l}{\partial r}$  gause bosons,  $H \rightarrow Z Z^{*} \rightarrow m^{+} m^{-} m^{-}$   $h = 2 \sqrt{m^{2}}$   $h = - \sqrt{m^{2}}$   $h = - \sqrt{m^{2}}$  Here, one Z can be on-she'l, so $<math>(P_{m_{1}} + P_{m_{2}})^{*} = m^{2}_{Z}$ , and together,  $(P_{m_{1}} + P_{m_{2}} + P_{m_{1}})^{*} = m^{2}_{h}$ 

Indeed, this "golden channel" confirmed the initial thisges discovery, and with more data became the best channel to study the Higgs,

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2) photon and gluon complings g soos t t ----

The photon and gluon are massless, so there is no coupling to the Higgs in the Lagransian. However, such a coupling does exist at 1-loop, much like the anomalous magnetic moment diagram we studied. Calculating these diagrams is beyond the scope of this course, but note that they are both proportional to  $\frac{M_{t}}{V}$  when the loop consists of top quarks. This lets us exploit the large coupling to tops as a virtual particle. Indeed, in the first Higgs discovery analysis in 2012, the Higgs way mostly produced via gluon fusion (Left diagram) and detected via the diphoton channel (right diagram), through a small bump in the invariant mass distribution  $m_{TV}^{2} \equiv (P_{T}, tP_{T})^{2}$  at  $m_{h}^{2} \approx (125 \text{ GeV})^{2}$ .