Discovery of the W/2 and Higgs

The predictions of electroweak symmetry breaking were confirmed in spectacular Fashion with the discovery of the W and Z bosons at CERN in 1983 and the discovery of the Higgs boson in 2012. Today we will survey these processes, which took place at proton-proton colliders, and additionally examine the precision electroweak tests that can take place at electron-positron colliders. Throughout, we will exploit the simplifications of the narrow-width approximation to factorize production and decay: $\sigma(initial state \rightarrow X \rightarrow final state) ~ \sigma(initial state \rightarrow X) \times Br(X \rightarrow final state)$

W production in pp collisions

From the W coupling to quarks, the following diagram exists:

$$M_{u\bar{u}} = \frac{i9}{5\pi} V_{u\bar{u}} \overline{v}(p_{A}) \Upsilon^{n}(\frac{1-\Upsilon^{5}}{2}) u(p_{u}) \varepsilon_{\mu}^{n}(p_{w})$$

As we saw when we discussed QCD, we need to weight this matrix element by the parton distribution Function of the poton, which counts quarks. At energies >100 GeV, the poton's quark content is mostly u and d value quarks, so this diagram suffices.

This is very similar to the t=6W diason we canputed last time. Indeed, all that charges is V_{tb} => Vud and a \overline{v} instead of a \overline{u} spinor. But since the only difference is the sign of the quark mass term in the trace, and the terms proportional to m_t vanished, we can just borrow the result from last time, with a slightly different perfector.

 $\langle |M|^2 \rangle = \frac{9^2}{12} |V_{ua}|^2 \left(p_u \cdot p_d + \frac{\gamma (p_u \cdot p_w)(p_d \cdot p_w)}{mw^2} \right)$ average over spins

arraye over spins and wlors: 2x2 for spins, only 3 colors since W doesn't change quark color

This time, we have $p_n + p_d = p_w$. Defining $(p_n + p_d)^2 = \hat{S}$, the dot products are $p_n \cdot p_d = \hat{S}$, $p_n \cdot p_w = p_d \cdot p_w = \hat{m}_{12}^{*}$, so $(|m|^2) = \hat{T}_{12}^{*} |V_{nd}|^2 (\hat{S}_{12} + \hat{m}_{12}^{*})$

$$\sigma(u\bar{d} \Rightarrow w^{+}) = \frac{1}{2\bar{s}} \int d\bar{\pi} \langle ln|^{2} \rangle \text{ where}$$

$$\int d\bar{\pi}_{l} = \int \frac{d^{3}\rho_{w}}{(4\pi)^{3}2E_{w}} (2\pi)^{4} \int^{(4)} (\rho_{w} + \rho_{w} - \rho_{w}) = 2\pi\sigma(\hat{s} - m_{w}^{2})$$

$$(as we've alluded to before, 1-particle phase space has one unresolved J -function)
Therefore we can set $\hat{s} = m_{w}^{2}$ in the matrix element, giving
$$\sigma(u\bar{d} \Rightarrow w^{+}) = \frac{1}{2\bar{s}} J\pi\left(\frac{g^{2}}{12}|V_{ud}|^{2}(m_{w}^{2})\right) \sigma(\hat{s} - m_{w}^{2})$$

$$= \frac{\pi g^{2}}{12} |V_{ud}|^{2} \sigma(\hat{s} - m_{w}^{2}) \text{ where } \alpha_{w} = \frac{g^{2}}{4\pi} (\text{ weak "Fine-structure constat"})$$$$

$$\begin{aligned} \text{Integrating over POF's,} \\ \sigma(p\bar{p} \rightarrow w^{+}) &= \int dx_{1} dx_{2} \left(f_{u}(x_{1}) f_{\bar{d}}(x_{\nu}) \sigma(u(x_{1}\bar{P}_{1}) \bar{d}(x_{\nu}\bar{P}_{\nu}) \rightarrow w^{+}) + 1 \iff 2 \right) \\ \text{where } P_{1} \text{ and } P_{2} \text{ are the initial } p/\bar{p} \quad \text{4-momental.} \\ P_{1} &= \left(\frac{\sqrt{5}}{2}, 0, 0, \frac{\sqrt{5}}{2} \right), \quad P_{2} &= \left(\frac{\sqrt{5}}{2}, 0, 0, -\frac{\sqrt{5}}{2} \right) \quad \left(s \text{ not } 3! \text{ Protens have the Full center} \right) \\ &= \sum_{\mu} P_{W} = x_{1} P_{1} + x_{2} P_{2} = \left((x_{1} + x_{\nu}) \frac{\sqrt{5}}{2}, 0, 0, (x_{1} - x_{\nu}) \frac{\sqrt{5}}{2} \right). \end{aligned}$$

This looks more symmetric if we parameterize p_W in terms of rapidity Y: $p_W = (\sqrt{3}\cosh Y, 0, 0, \sqrt{3}\sinh Y)$ where $p_W^{-1} = \hat{s}$ (which we leave free for now) Charge variables $(x_{1,x_{2}}) \rightarrow (\xi, Y)$:

hange variables
$$(x_{1}, x_{2}) \rightarrow (x_{3}, y)$$
.
 $(x_{1}+x_{2}) \frac{\sqrt{5}}{2} + (x_{1}-x_{2}) \frac{\sqrt{5}}{2} = \sqrt{5} (\cosh Y + \sin h Y)$ (equating $\beta w^{0} + \beta w^{3}$ in both coordinates)
 $= \sum x_{1} = \frac{\sqrt{3}}{\sqrt{5}} e^{Y}$, $\sin \log Y = \frac{\sqrt{5}}{\sqrt{5}} e^{-Y}$
 $\frac{\partial(x_{1}, x_{2})}{\partial(\hat{s}, Y)} = \left| \begin{array}{c} \frac{e^{Y}}{2\sqrt{5}\sqrt{5}} & \frac{e^{-Y}}{2\sqrt{5}\sqrt{5}} \\ \frac{\sqrt{5}e^{Y}}{\sqrt{5}} & -\frac{\sqrt{5}e^{-Y}}{\sqrt{5}} \end{array} \right| = \frac{1}{5}$

 $= \int dx_{1} dx_{2} \int (\widehat{s} - n\omega^{2}) = \frac{1}{5} d\widehat{s} dY \int (\widehat{s} - n\omega^{2})$ $= \int \sigma(p\widehat{p} \rightarrow w^{+}) = \frac{\pi^{2} \alpha \omega}{35} |V_{ud}|^{2} \int dY \left[f_{u} \left(\frac{n\omega}{55} e^{2} \right) f_{\overline{u}} \left(\frac{n\omega}{55} e^{-2} \right) + f_{\overline{u}} \left(\frac{n\omega}{55} e^{2} \right) f_{\overline{u}} \left(\frac{n\omega}{55} e^{-2} \right) \right]$

Note that once we know the W exists, this process can be used to measure the PDF's!

W decays
Two kinds of decay processes, which look very different at collider.'
W⁺ W² "hadronic" (note mach, so w can't decy to the
Matrix elevants are very similar to the production matrix
elevants: only differences are lober sums and CKM elevants.
Hadronic: Sum -> average over W spins:
$$\frac{1}{2} \rightarrow 1$$

average > sum over quark spins: $\frac{1}{2} \rightarrow 1$
average > sum over quark colors: $\frac{1}{3} \rightarrow 3$
=> overall factor of 12 in the matrix elevant
Class = $\frac{1}{2} = \sqrt{\frac{1}{2\pi}} \frac{1}{2\pi} 4\pi \pi_{\rm elevant} = \frac{\pi_{\rm elevant}}{4} |V_{\rm el}|^{-1}$
However, there are also GCD corrections from quarks emitting find-state places
Sum $\frac{1}{2\pi} (1 + \frac{\pi_{\rm elevant}}{\pi}) [1/z_{\rm el}|^{-1} + 1/z_{\rm elevant}] = 1 + 1/z_{\rm elevant}]$
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Su $\lceil w \Rightarrow jres = \frac{\pi_{\rm elevant}}{\pi} (1 + \frac{\pi_{\rm elevant}}{\pi}) [1/z_{\rm elevant}] + 1/z_{\rm elevant}] + 1/z_{\rm elevant}] = 1 + 1/z_{\rm elevant}]$
For levant places of place of $\frac{1}{12\pi} \sqrt{12} \sqrt{12} - \frac{\pi_{\rm elevant}}{12\pi} = 62.1 + 1/z_{\rm elevant}]$
Experimentally, Br (w > jets) = 67.91 + 1/w_{\rm elevant}] (accorrections importat)
For levant decay, no sum over colors: $\lceil w \Rightarrow z = \frac{\pi_{\rm elevant}}{12\pi}, equal for
e. AN T up to phase space effects for nonzero matrix. Again, well-inspected by detaut.$

 $\begin{bmatrix} \overline{u} \ \gamma^{-} \gamma^{5} v \end{bmatrix}^{+} = v^{+} \gamma^{5} (\gamma^{-})^{+} \gamma^{0} u = v^{+} \gamma^{5} \gamma^{0} \gamma^{-} u = -\overline{v} \gamma^{5} \gamma^{-} u = +\overline{v} \gamma^{-} \gamma^{5} u$ For example, for f = e, $\overline{T} = -\frac{1}{2}$ and R = -1, $Cv = -\frac{1}{2} + 2\sin^{2} \theta u$, $c_{A} = -\frac{1}{2}$.

$$S_{\mathcal{D}} < |\mathcal{M}_{2 \rightarrow ce}|^{2} > = \frac{1}{3} \frac{2^{2}}{4\tau_{0}r_{0}} \underset{\text{spins}}{\mathbb{Z}} \overline{V(p)} (c_{v}Y^{m} - c_{A}Y^{m}Y^{s}) u(p_{i}) \overline{u(p_{i})} (c_{v}Y^{u} - c_{A}Y^{v}Y^{s}) v(p_{i}) \tilde{e}_{i}(p_{i}) \tilde{e}_$$

As with top quick decay, the YS trace is proportional to the [5]
antisymmetric tasor
$$e^{n\sqrt{n}R}$$
, so it varishes when contracted with the
polarization sum. The 4-vector products are identical to previous
calculations, so we can just stip to the answer:
 $(|M|)^{T} = \frac{9^{T}}{3co^{2}6u} \left(P_{1}P_{2} + \frac{2(P_{1}P_{2})(P_{1}P_{2})}{n_{2}}\right) \left(c_{v}^{T}tc_{A}^{T}\right)$
 $= \frac{9^{2}m_{2}^{T}}{3co^{2}6u} \left(c_{v}^{T}tc_{A}^{T}\right)$
 $T_{2nev} = \frac{1}{3co^{2}6u} \left(C_{v}^{T}tc_{A}^{T}\right)$
 $As with W's, this predicts;
 $equal bracking Fractions into $e/n/T$, up to mass effects (a Hw)
 $hadraic decays enhanced by a factor of 3 tor color, but also
 $c_{v}^{T}rc_{A}^{T}$ in different! In the end, 70% to hadray vs. 30% to
choosed (eptons + neutrinos.
 $Decay products are polarized ! Indeed, W decay products are fully
polarized (in massless approximation), since W only complets to L spinors,
but Z decays are partially polarized, depending on femion (a Hw)
 $\cdot Easy to reconstruct mess or Z at eter collider; look for$$$$$

events with
$$m^+m^-$$
, $m^-2^+ = (p_{n+}p_{n-})^2$

Discovery of the Higgs

Finally, let's examine the last piece of the Standard Model. For Huy you will calculate H=366 and H=3WW, 22. Since Higgs couplings are proportional to mass, we should try to produce it ad detect it with the heaviest initial-and final-state particles possible. However, pervesely, $m_h < 2m_f$ and $m_h < 2m_W$, so decays into an-shell tops or gauge bosons are kinemetically forbidden. Even worse, $m_b^2 0.02m_f$, so decays to 6's are smaller by ~ 10⁴, and 2-jet events have an enormous QCD backsome! To find the Higgs at the LHC, experimentalists and theorists had to get creative. Tuo stratesies.

1) $\frac{\partial FF-shell}{\partial f}$ gause bosons, $H \rightarrow Z Z^{*} \rightarrow m^{+} m^{-} m^{-}$ $h = Z^{+} M^{-}$ $h = Z^{+} M^{-$

Indeed, this "golden channel" confirmed the initial thisges discovery, and with more data became the best channel to study the Higgs,

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2) photon and gluon complings g soos t t ----

The photon and gluon are massless, so there is no coupling to the Higgs in the Lagransian. However, such a coupling does exist at 1-loop, much like the anomalous magnetic moment diagram we studied. Calculating these diagrams is beyond the scope of this course, but note that they are both proportional to $\frac{M_{t}}{V}$ when the loop consists of top quarks. This lets us exploit the lage coupling to tops as a virtual particle. Indeed, in the first Higgs discovers analysis in 2012, the Higgs was mostly produced via gluon fusion (Left diagram) and detected via the diphoton channel (right diagram), through a small bump in the invariant mass distribution $m_{TV}^{2} \equiv (P_{T_{1}} + P_{T_{2}})^{2}$ at $m_{L}^{2} \approx C125 \text{ GeV}^{2}$.