Colliders and defectors

How do we make elementary particles?  $E = nc^{2}$  plus QM? if you have enough energy, anything that <u>can</u> happen, will happen, unless forbidden by conservation laws For example, collide electrons and positrons?



If each bean has energy  $\frac{E}{2}$ , then the center-of-mass energy is E: we can create particles with total mass up to E (with total charge, lepton number, and barron number 0), QM (really QFT) tells us the probability of making a given set of Final-state particles. In particle physics we call this the matrix element  $M_{i\to f}$ , and next week we will see how to calculate it for some specific processes.

Cross sections

IF we have two colliding beams with cross-sectional area A and length L, scattering rate =  $\frac{events}{time} = n_A n_B A (|v_A - v_B| \sigma) \equiv L \sigma$ 

L is the luminosity and parameterizes the Flux of incoming particles.  
T is the scattering cross section which parameterizes the interaction strayth  

$$\Lambda_A$$
,  $\Lambda_B$  are the number densities of particles A and B in the beams.  
 $|V_A - V_B|$  is the relative velocity of the two beams. If the beams  
are relativistic  $(V_A \approx 1, V_B \approx 1)$ , this factor is  $|V_A - V_B| = 2$ . Despite  
appearances, this does not violate the velocity addition rule:  
it's formally defined as the "Moller velocity" and ensures the  
scattering rate is Lorentz-invariant with respect to boosts  
along the beam axis. (see Peskin & Schroeder Sec. 4.5 if you're cunious;  
Fermi's Golden Rule relates  $\sigma$  to  $M$ .  
 $\overline{\tau_{inf}} = \frac{1}{(2E_B)(2E_B)|_{V_A} - V_B|}$ 

4-momentum

Conservation

Sum over Finel

states: Loratz-

invariant phase

Space Note that or is not borentz-invariant, but transforms like an orea. Lorentz-inut, for boosts along beam axis. This is the key observable predicted by QFT: "effective area" of beens of particles A and B, taking into account the Fact that some collisions are rarer than others.

probabilities

are squals

of amplitudes

from relativistic

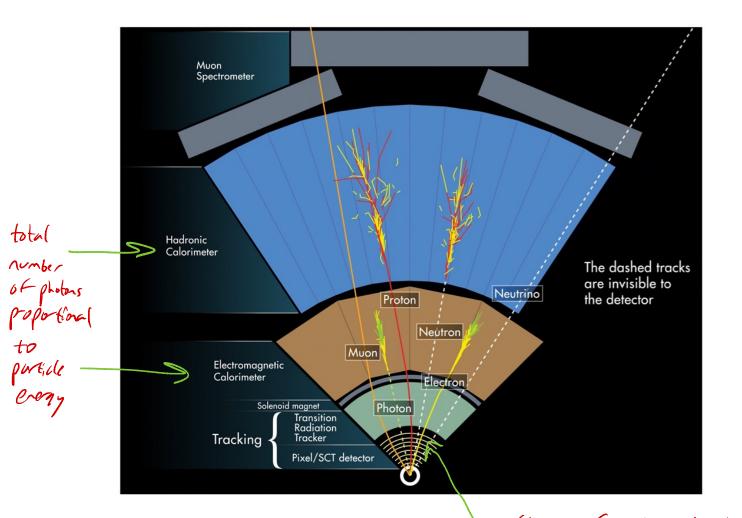
normalization of

initial and final

states

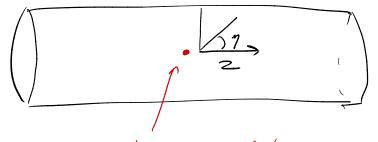
Units: 
$$\sigma$$
 is usually given in  $(SI prFix) > barns, where
 $1 \ barn = 10^{-24} \ cm^2$   
Luminosity is usually quoted in  $[preFix > barns]^{-1}/s$ , so for example  
a process with  $\sigma = 1 \ Fb = 10^{-15} \ barns$  at the LHC  $((n - 1pb^{-1}/s))$   
has a rate  $R = \mathcal{K}\sigma = 10^{-3}/s$ .$ 

How do we detect elementary particles? [] Two steps: measure an energy and/or momentum and then identify the particle by its mass and electric charge. Cross-section (view of the ATLAS defector.



Strips of silicon: church particles deposit small anomes of everys in each pixel, can leave tracks Entire detector is immersed in - myneth field (out of the page in inner region): measure momentum and choose by curvature radius R = 3 m x <u>P\_L [Gev]</u> (4 1B1[T] If we know E and p => know m, particle ID





interaction point

Basically spherical coordinates, but instead of O, use
pseudorapidity $y \equiv -\ln \tan \frac{e}{2}$
My this fung voriable? 2 related M=0 reasons:
· particle production is roughly
M=-00 M=00 M=-00 H=00 for massless particles
(Larkosk: 5.3)

Hard to detect particles which go very close to been direction (how do you avoid the beam?). As a result, often use transverse momentum  $p_T = \sqrt{p_x^2 + p_y^2} = \sqrt{p_z^2 - p_z^2}$ . Since all 3 components of spatial momentum must be conserved, Can infer existence of invisible particles from imbalance in  $p_T$ .  $P_{T_1} = \int_{T_2} \int_{T_1} \frac{1}{p_{T_2}} \int_{T_1} \frac{1}{p_{T_2}} \int_{T_2} \frac{1}{p_{T_2}}$ 

Phase space

To compute cross sections, we need to sum over all Final states => integrate over all q-momenta consistent al Poincaré invariance

15

Translation invariance => 4-momentum conservation (Noether's Theorem)

$$\int d T_{A} = \int \left\{ \frac{1}{(1+1)} \frac{d^{2} p_{i}}{(2\pi)^{4}} 2\pi \int (p_{i}^{2} - m_{i}^{2}) \Theta(p_{i}^{0}) \right\} (2\pi)^{4} \int (p_{A} + p_{B} - \hat{z}_{p_{i}}) \int (p_{A} + p_{B} - p_{A}) \int (p_{A} + p_{A}) \int (p$$

The Dris are convertionally attacked to ATT but they do matter - doi't forget then!

We can perform the  $p^{\circ}$  integral for each  $i_{j}$  using  $\mathcal{J}(p_{i}^{*}-n_{i}^{*}) = \mathcal{J}((p_{i}^{\circ})^{*}-p^{*}-n_{i}^{*})$  and  $\mathcal{J}(q_{i}) = \mathcal{J}((p_{i}^{\circ})^{*}-p^{*}-n_{i}^{*})$ 

$$\begin{split} \mathcal{J}(f(x)) &= \frac{1}{|f'(x_0)|} \int (x - x_0) & \text{killed by } \mathcal{O}(\rho_i^\circ) \\ &= \mathcal{J}\left(\rho_i^2 - n_i^2\right) = \frac{1}{2\sqrt{\rho_i^2 + n_i^2}} \left( \mathcal{J}\left(\rho_i^\circ - \sqrt{\rho_i^2 + n_i^2}\right) + \mathcal{J}\left(\rho_i^\circ + \sqrt{\rho_i^2 + n_i^2}\right) \right) \end{split}$$

=> 
$$\int dp_{i}^{\circ} \int (p_{i}^{2} - m_{i}^{2}) \Theta(p_{i}^{\circ}) f(p_{i}^{\circ}) = \frac{1}{2E_{i}} f(E_{i}) w/E_{i} = \int \vec{p}_{i}^{2} + m_{i}^{2}$$

$$= \sum \int \int \int \pi_{n} = \int \int \int \frac{1}{|i|} \frac{d^{3} \rho_{i}}{(2\pi)^{3}} \frac{1}{2E_{i}} (2\pi)^{4} \int^{(4)} \left( \frac{\rho_{A} + \rho_{B}}{\rho_{i} - \frac{2}{i}} \frac{\rho_{i}}{\rho_{i}} \right)$$

$$\rho_{i}^{0} = E_{i}$$

16 For 2-particle phase space, can do nost of the integrals. (HW 4", 3-paticle phase space.) Consider the process P, + P2 -> P3+P4 (relabelling to match Schwartz 5.1) in the center-oF-mass frame where Pi+Pr= (Ecn, 0).  $P_1$   $P_2$  $P_2$  $dT_{2} = \frac{d^{3} p_{3}}{(2\pi)^{3}} \frac{1}{2\epsilon_{3}} \frac{d^{3} p_{4}}{(2\pi)^{3}} \frac{1}{2\epsilon_{4}} \frac{d^{3} p_{4}}{(2\pi)^{3}} \frac{1}{2\epsilon_{4}} (2\pi)^{4} \int (p_{1} + p_{2} - p_{3} - p_{4})$ Use J'(P,+P,-P,-P,) = J'(0-P3-P4) to do d'f4 integal! Sets \$\$ = - \$\$. Then, write d'P3 = \$\$ df3 d. D, where ds2 is the differential solid angle for P3 in spherical coordinates. Collecting the  $2\pi i_{5}$  and relabeling  $P_{3} = P_{f}$  chansed signs to converse.  $d\pi_{2} = \frac{1}{16\pi^{2}} d\Omega \int dP_{f} \frac{P_{f}^{2}}{E_{E}E_{a}} \mathcal{J}(E_{3} + E_{q} - E_{cm}) \mathcal{J}(A) = \mathcal{J}(-x)$ where  $E_3 = \sqrt{p_F^2 + n_3^2}$ ,  $E_q = \sqrt{p_F^2 + n_q^2}$ . (hange variables pf -> X(pr)= E3(pp)+ E4(pr) - Ecm Jacobian:  $\frac{dx}{dpr} = \frac{2pr}{2\sqrt{pr^2 + m_1^2}} + \frac{2pr}{2\sqrt{pr^2 + m_1^2}} = \frac{pr}{E_1} - \frac{pr}{E_2} = \frac{E_3 + E_4}{E_3 - E_4} pr$ J-function enforces E3 + Eq = Ecn, 50  $dT_{1_{2}} = \frac{1}{16\pi^{2}} d\Omega \int dx \frac{P_{F}(x)}{E_{cm}} J(x) = \frac{1}{16\pi^{2}} d\Omega \frac{IP_{F}I}{E_{cm}} \Theta(E_{cm} - m_{3} - m_{4})$   $m_{T}^{+}m_{F} - E_{cm}$ wher IPFI is the solution to X(PF)=0 enforces our begy treshold condition (usually casiv to use boratz dot product tricks) from earlier