Discovery of the W/2 and Higgs

The predictions of electroweak symmetry breaking were confirmed in spectacular Fashion with the discovery of the W and Z bosons at CERN in 1983, and the discovery of the Higgs boson in 2012. Today we will survey these processes, which took place at proton-proton colliders, and additionally examine the precision electroweak tests that can take place at electron-positron colliders. Throughout, we will exploit the simplifications of the narrow-width approximation to factorize production and decay: $\sigma(initial state \rightarrow X \rightarrow final state) ~ \sigma(initial state \rightarrow X) \times Br(X \rightarrow fin(state))$

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W production in pp collisions

From the W coupling to quarks, the following diagram exists:

$$M_{u\bar{u}} = \frac{i9}{5\pi} V_{u\bar{u}} \overline{v(p_A)} \gamma^n (\frac{1-\gamma^5}{2}) u(p_u) \epsilon_u^n(p_w)$$

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As we saw when we discussed QCD, we need to weight this matrix element by the parton distribution Function of the proton, which counts quarks. At energies >100 GeV, the poton's quark catent is mostly u and d value quarks, so this diagram suffices.

This is very similar to the $t \rightarrow 6W$ diason we computed last time. Indeed, all that charges is $V_{tb} \rightarrow V_{ud}$ and a \overline{v} instead of a \overline{u} spinor. But since the only difference is the sign of the quark mass term in the trace, and the terms proportional to m_t vanished, we can just borrow the result from last time, with a slightly different perfector:

 $\langle M|^2 \rangle = \frac{9^2}{12} |V_{ua}|^2 \left(p_u \cdot p_d + \frac{2(p_u \cdot p_w)(p_d \cdot p_w)}{mw^2} \right)$ average our spins

arraye over spins and wlors: 2x2 for spins, only 3 colors since W doesn't change quark color

This time, we have $p_n + p_d = p_w$. Defining $(p_n + p_d)^2 = \hat{S}$, the dot products are $p_n \cdot p_d = \hat{S}$, $p_n \cdot p_w = p_d \cdot p_w = \hat{m}_{12}^{*}$, so $(|m|^2) = \hat{T}_{12}^{*} |V_{nd}|^2 (\hat{S}_{12} + \hat{m}_{12}^{*})$

$$\sigma\left(u\overline{d} \Rightarrow w^{+}\right) = \frac{1}{2\hat{s}} \int d\overline{\eta}, \langle ln|^{2} \rangle \text{ where } \qquad \left[\frac{7}{2} \right]$$

$$\int d\overline{\eta}, = \int \frac{d^{3}\rho_{w}}{(4\pi)^{3}2E_{w}} (2\pi)^{+} \int^{(4)} (\rho_{w} + \rho_{d} - \rho_{w}) = 2\pi \delta\left(\hat{s} - m_{w}^{2}\right)$$

$$\left[\text{ as we've alluded to before, } 1 - particle phase space has one unresolved \overline{J} -function)
$$\text{Therefore we can set } \hat{s} = m_{w}^{2} \text{ in the matrix element, giving}$$

$$\sigma\left(u\overline{d} \Rightarrow w^{+}\right) = \frac{1}{4\hat{s}} S\pi\left(\frac{9^{2}}{12}|V_{ud}|^{-}(m_{w}^{2})\right) \delta\left(\hat{s} - m_{w}^{2}\right)$$

$$= \frac{\pi g^{2}}{12} |V_{ud}|^{2} \delta\left(\hat{s} - m_{w}^{2}\right) \text{ where } \alpha_{w} = \frac{9^{2}}{4\pi} \left(\text{ where "fine-structur constat"}\right)$$$$

$$\begin{aligned} \text{Integrating over POF's,} \\ \sigma(p\bar{p} \rightarrow w^{+}) &= \int dx_{1} dx_{2} \left(f_{u}(x_{1}) f_{\bar{d}}(x_{v}) \sigma(u(x_{1}\bar{P}_{1}) \bar{d}(x_{v}\bar{P}_{v}) \rightarrow w^{+}) + 1 \iff 2 \right) \\ \text{where } P_{1} \text{ and } P_{2} \text{ are the initial } p/\bar{p} \quad \text{4-momental.} \\ P_{1} &= \left(\frac{\sqrt{5}}{2}, 0, 0, \frac{\sqrt{5}}{2} \right), \quad P_{2} &= \left(\frac{\sqrt{5}}{2}, 0, 0, -\frac{\sqrt{5}}{2} \right) \quad \left(s \text{ not } 3! \text{ Protons have the Full conters} \right) \\ &= \mathcal{P}_{W} = x_{1} P_{1} + x_{2} P_{2} = \left((x_{1} + x_{v}) \frac{\sqrt{5}}{2}, 0, 0, (x_{1} - x_{v}) \frac{\sqrt{5}}{2} \right). \end{aligned}$$

This looks more symmetric if we parameterize p_W in terms of rapidity Y: $p_W = (\sqrt{3}\cosh Y, 0, 0, \sqrt{3}\sinh Y)$ where $p_W^{-1} = \hat{s}$ (which we leave free for now) Charge variables $(x_{1,x_{2}}) \rightarrow (\xi, Y)$:

hange variables
$$(x_{1,x_{1}}) \xrightarrow{=} (x_{1,x_{1}}) \xrightarrow{=} (x_{1,x_{1}})$$

 $= \int dx_{1} dx_{2} \int (\widehat{s} - n\omega^{2}) = \frac{1}{5} d\widehat{s} dY \int (\widehat{s} - n\omega^{2})$ $= \int \sigma(p\widehat{p} \rightarrow w^{+}) = \frac{\pi^{2} \alpha \omega}{35} |V_{ud}|^{2} \int dY \left[f_{u} \left(\frac{n\omega}{55} e^{2} \right) f_{\overline{u}} \left(\frac{n\omega}{55} e^{-2} \right) + f_{\overline{u}} \left(\frac{n\omega}{55} e^{2} \right) f_{\overline{u}} \left(\frac{n\omega}{55} e^{-2} \right) \right]$

Note that once we know the W exists, this process can be used to measure the PDF's! 8 |

Even without knowing W mess precisely, can predict ratios of $\left[\begin{array}{c} q\\ p\\ ranching ratios:\\ Br(W^{+} \Rightarrow e^{i} U_{e}) \\ \overline{Rr(W^{+} \Rightarrow hedres)} = \frac{V_{3}}{(1+\frac{\alpha_{3}}{\pi})} \sum_{\substack{i \in W_{i} \\ i \neq M_{i} \\ j \neq dist}} = \frac{1}{6(1+\frac{\alpha_{3}}{\pi})} \sum_{\substack{i \in W_{i} \\ i \neq M_{i} \\ j \neq dist}} Since \sum_{i \in W_{i}} |V_{ij}|^{2} = 2$ Measurement of W mess is a little tricky! for 2-jet events, $(p_{ij}, r_{ij})^{2} = nw_{ij}$ but lots of QCD background. Instead, use transverse mass derived from (eptonic decays (important implications for recent COF W-mess repul!) $\frac{2}{1+\frac{1}{\pi}} \sum_{i \neq M_{ij}} (important implications for recent COF W-mess repul!)$

colliders, here we will focus on the decay modes. The Z boson Couples to all SM Fernions. $iM = \frac{19}{\cos\theta_{w}} \left(T^{3} Y^{m} P_{L} - Q \sin^{2}\theta_{w} Y^{m} \right) E_{m}(p_{2})$ $= \frac{ig}{2\cos\theta_{W}} \left(T^{\gamma}Y^{m}(1-\gamma^{5}) - 2\alpha\sin^{2}\theta_{W}Y^{n}\right) t_{m}(p_{2})$ $\equiv \frac{19}{2000} \left(C_V Y^m - C_A Y^n Y^5 \right) \mathcal{E}_n(\rho_2)$ Here, $C_V \equiv T^3 - 2 \cos in^2 \omega_w$ and $C_A \equiv T^3$ are "vector" and "axial-vector" couplings. This way or writing things makes spino-products in 4-component notation easier: $\left[\overline{u} \gamma^{n} \gamma^{5} v \right]^{+} = v^{+} \gamma^{5} (\gamma^{n})^{+} \gamma^{0} u = v^{+} \gamma^{5} \gamma^{0} \gamma^{n} u = - \overline{v} \gamma^{5} \gamma^{n} u = + \overline{v} \gamma^{n} \gamma^{5} u$ For example, for f = e, $T = -\frac{1}{2}$ and R = -1, $C_V = -\frac{1}{2} + 2\sin^2 \theta_W$, $C_A = -\frac{1}{2}$. $50 < \left[M_{2 \rightarrow ee}\right]^{2} = \frac{1}{3} \frac{2}{4\tau_{0}r_{0}} \underset{spins}{\leq} \overline{V(p)} \left(c_{v}r^{m} - c_{A}r^{m}r^{s}\right) u(p_{i})\overline{u(p_{i})} \left(c_{v}r^{v} - c_{A}r^{v}r^{s}\right) v(p_{i}) \in (A) \in (A)$ $(setting me=0) = \frac{1}{2} \frac{2^{2}}{q_{cos}^{2} \partial w} \operatorname{Tr}\left[P_{1}^{\prime} \gamma^{\prime} (c_{v} - c_{A} \gamma^{5}) p_{L}^{\prime} \gamma^{\prime} (c_{v} - c_{A} \gamma^{5})\right] \left(-\eta_{av} + \frac{p_{2a} p_{2v}}{m_{*}^{2}}\right)$ $= \frac{1}{3} \frac{2^{2}}{4c_{0}c_{0}} \operatorname{Tr}\left(p_{1}^{\prime} V^{\prime} p_{2}^{\prime} Y^{\prime} (c_{v} - c_{A}^{\prime} Y^{5})(c_{v} - c_{A}^{\prime} Y^{5})\right) \left(-\eta_{nv} + \frac{p_{2n}}{m} \frac{p_{2v}}{m}\right)$ $= \frac{1}{3} \frac{g^{2}}{4\pi \sigma_{5}^{2} \delta w} Tr \left[p_{1}^{\prime} \chi^{\prime} p_{2}^{\prime} \chi^{\prime \prime} \left(c_{V}^{2} + c_{A}^{2} - 2c_{V} c_{A}^{\prime} \chi^{5} \right) \right] \left(- \eta_{AV} + \frac{l_{2} p_{2}^{\prime} r_{2}}{m_{2}^{*}} \right)$

As with top quive decy, the YS trace is propertional to the [10
antisymmetric tasor
$$e^{nval}$$
, so it vanishes when contracted with the
polarization sum. The 4-vector products are identical to previous
calculations, so we can just skip to the answer:
 $(1M1)^{T} = \frac{9^{T}}{3co^{3}cov} \left(\frac{P_{1}P_{2}}{P_{1}} + \frac{2(P_{1}P_{2})(P_{1}P_{2})}{nz^{4}}\right) \left(cv^{4}rc_{1}^{4}\right)$
 $= \frac{9^{2}mz^{2}}{3co^{3}cov} \left(cv^{2}rc_{1}^{4}\right)$
 $T_{2neir} = \frac{1}{2mz} \frac{1}{(cv^{2}rc_{1}^{4})}$
As with WS, this predicts:
 $equal banching Fractions into $e/n/T$, up to mass effects (a Hw)
 $hadvaric decays thenced by a factor of 3 for color, but also
 $cv^{2}rc_{1}^{4}$ is different! In the end, 70% to hadray VS. 30% to
choosed (eptons + neutrinos.
 $Decay products are polarized! Indeed, W decay products are fully
polarized (in massless approximation), since W only couples to L spinors,
but 2 decays are partially polarized, depending on femilar (a Hw)
 $Easy to reconstruct mass or Z at eter collider: look for
 $events with m^{2}m_{1}^{2} - (P_{1}rh_{1})^{2} (See plot on course webpage)$$$$$

Finally, let's examine the last piece of the Standard Model. For Huy, you will calculate H=> bb and H=> WW, 22. Since Higgs couplings are proportional to mass, we should try to produce it ad detect it with the heaviest initial-and final-state puticles possible. However, pervesely, $m_h < 2m_f$ and $m_h < 2m_W$, so decays into an experience to b's are smaller by $n 10^+$, and 2-jet events have an enormous QCD backsome! To find the Higgs at the LHC, experimentalists and theorists had to get creative. Tuo stratesies.

1) $0\overline{f}\overline{f}-s\overline{h}e^{(I)}$ gause bosons, $H \rightarrow Z Z^{\bullet} \rightarrow M^{+}\overline{m}\mu^{+}\overline{m}^{-}$ $-h - Z^{\bullet}$ Here, one Z can be on-shell, so $H^{\bullet}e^{(I)}$, $(P_{M_{1}}+P_{M_{2}})^{\bullet}=M_{2}^{2}$, and together, $T^{\bullet}e^{(I)}$, $(P_{M_{1}}+P_{M_{2}}+P_{M_{1}}+P_{M_{2}})^{\bullet}=M_{h}^{2}$

Indeed, this "golden channel" confirmed the initial tips discovery, and with more data became the best channel to study the Hipps,

2) photon and gluon complings g soos t t t t t t t t t t

The photon and gluon are massless, so there is no coupling to the Higgs in the Lagransian. However, such a coupling does exist at 1-loop, much like the anomalous magnetic moment diagram we studied. Colculating these diagrams is beyond the scope of this course, but note that they are both proportional to $\frac{M_{t}}{V}$ when the loop consists of top quarks. This lets us exploit the lage coupling to tops as a virtual particle. Indeed, in the first Higgs discovery analysis in 2012, the Higgs was mostly produced via gluon fusion (Left diagram) and detected via the diphoton channel (right diagram), through a small bump in the invariant mass distribution $m_{TV}^{N} \equiv (P_{T}, +P_{T})^{N}$ at $m_{L}^{L} \approx (125 \text{ GeV})^{2}$.

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