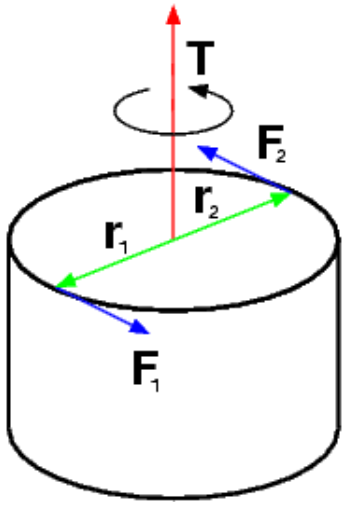
Statics - TAM 210 & TAM 211

Lecture 9

February 5, 2018

Announcements

- Upcoming deadlines:
- Tuesday (2/6)
  - PL Homework 3
- Quiz 2 (2/7-9)
  - Reserve testing time at CBTF
  - Lectures 5-9
- Friday (2/9)
  - Mastering Engineering Tutorial 5



https://fr.wikipedia.org/wiki/Couple_(physique)

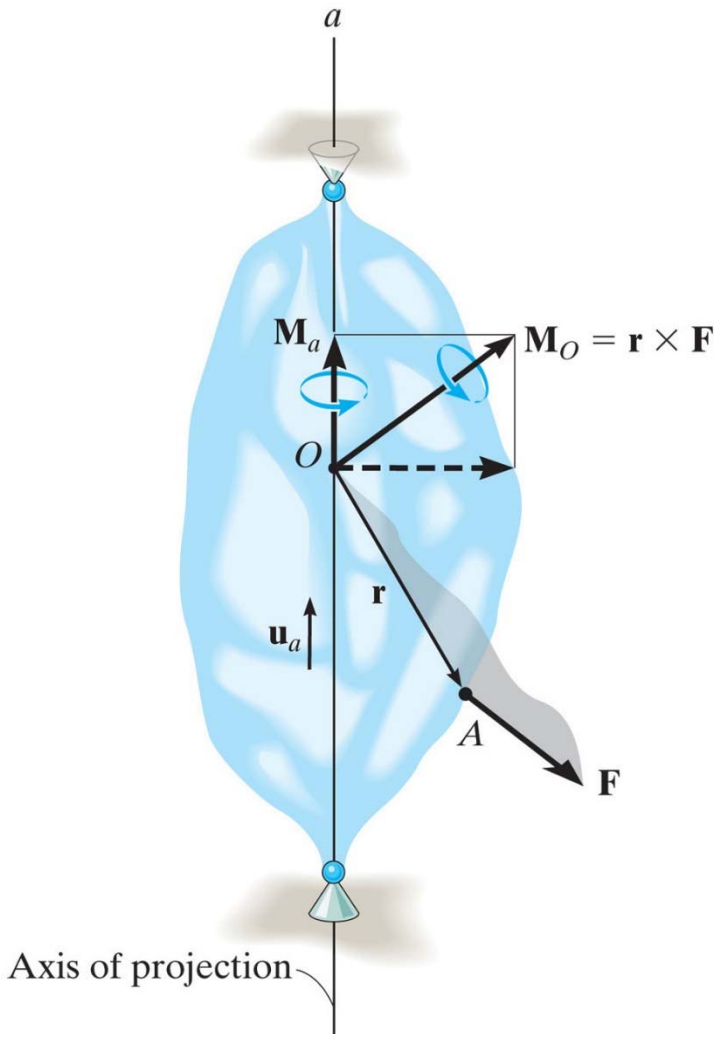
Chapter 4: Force System Resultants

Goals and Objectives

- Discuss the concept of the moment of a force and show how to calculate it in two and three dimensions
- How to find the moment about a specified axis
- Define the moment of a couple
- Finding equivalence force and moment systems
- Reduction of distributed loading

Recap: Moment of a force about a specified axis (Scalar Triple Product)

The magnitude of the projected moment about any generic axis *a* can be computed using the scalar triple product:



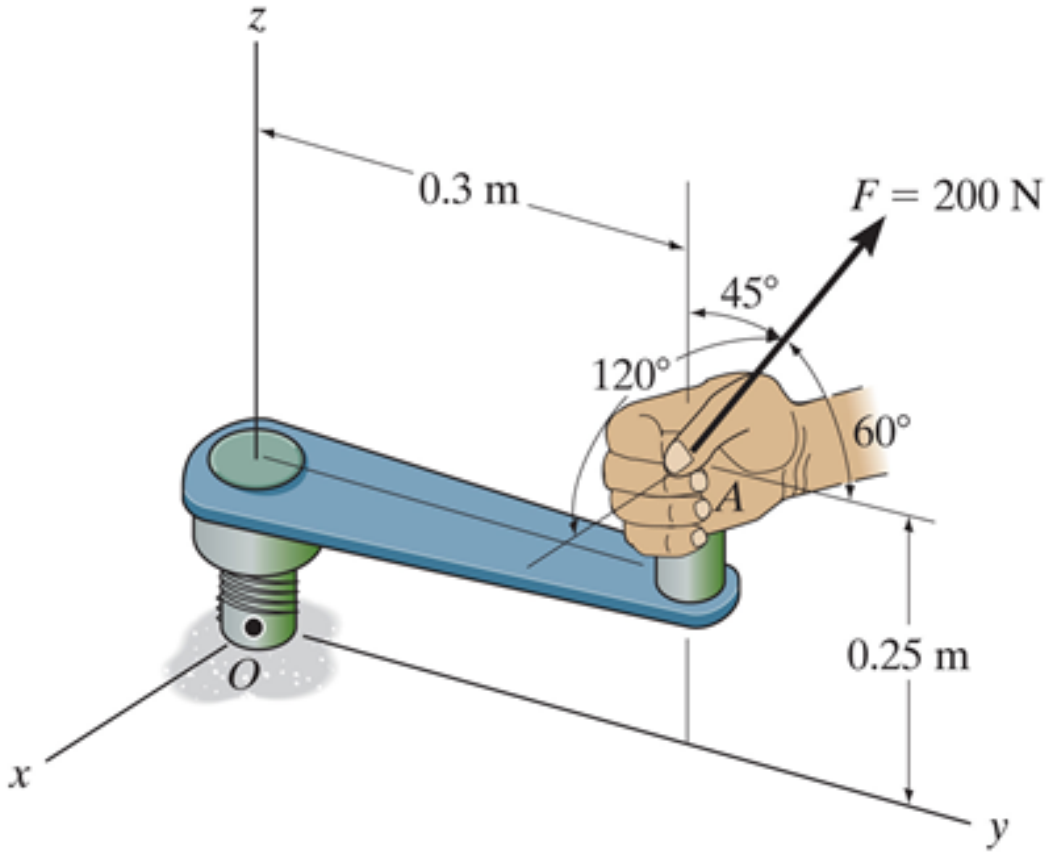
$$\left|\overrightarrow{\boldsymbol{M_a}}\right| = \overrightarrow{\boldsymbol{u_a}} \cdot \left(\vec{\boldsymbol{r}} \times \vec{\boldsymbol{F}}\right)$$

$$= \begin{vmatrix} u_{a_x} & u_{a_y} & u_{a_z} \\ r_x & r_y & r_z \\ F_x & F_y & F_z \end{vmatrix}$$

The direction of the projected moment about any generic axis *a* can be defined using :

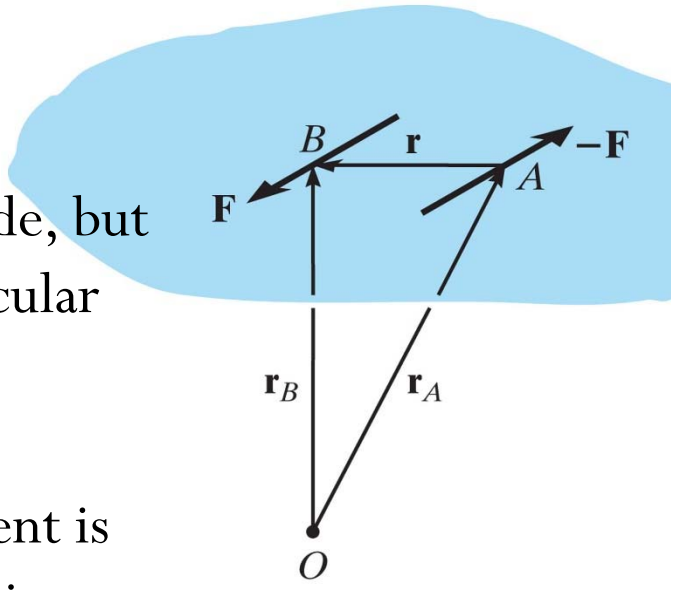
$$\overrightarrow{\boldsymbol{M_a}} = \left|\overrightarrow{\boldsymbol{M_a}}\right| \overrightarrow{\boldsymbol{u_a}}$$

where $\overrightarrow{\boldsymbol{u_a}}$ is the unit vector along axis *a*



A force is applied to the tool as shown. Find the magnitude of the moment of this force about the x axis.

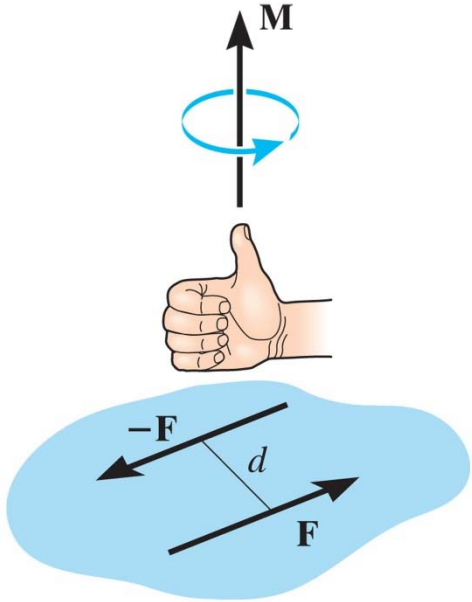
Moment of a couple



Couple: two parallel forces that have same magnitude, but opposite directions, and are separated by a perpendicular distance *d*.

- Resultant force is zero.
- Couple produces actual rotation, or if no movement is possible, tendency of rotation in a specified direction.

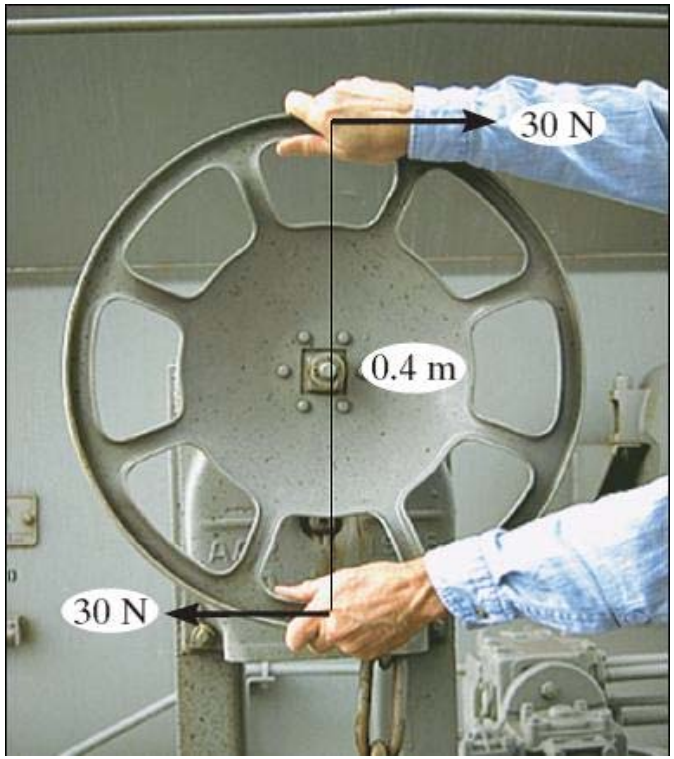
Moment produced by a couple is called **couple moment**.

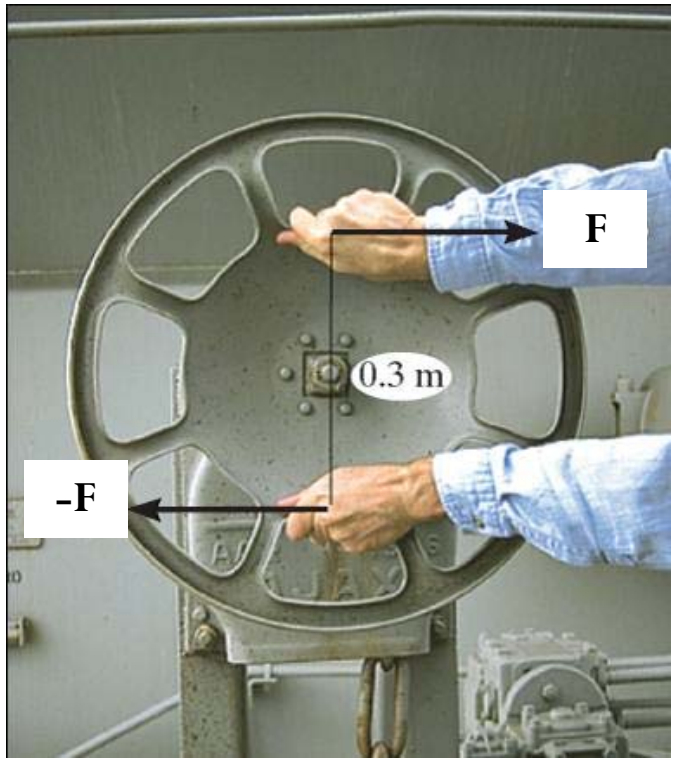


Sum of moments of both couple forces about **any** arbitrary point:

Couple moment is a **free vector**, i.e. is **independent** of the choice of O!

Equivalent couples



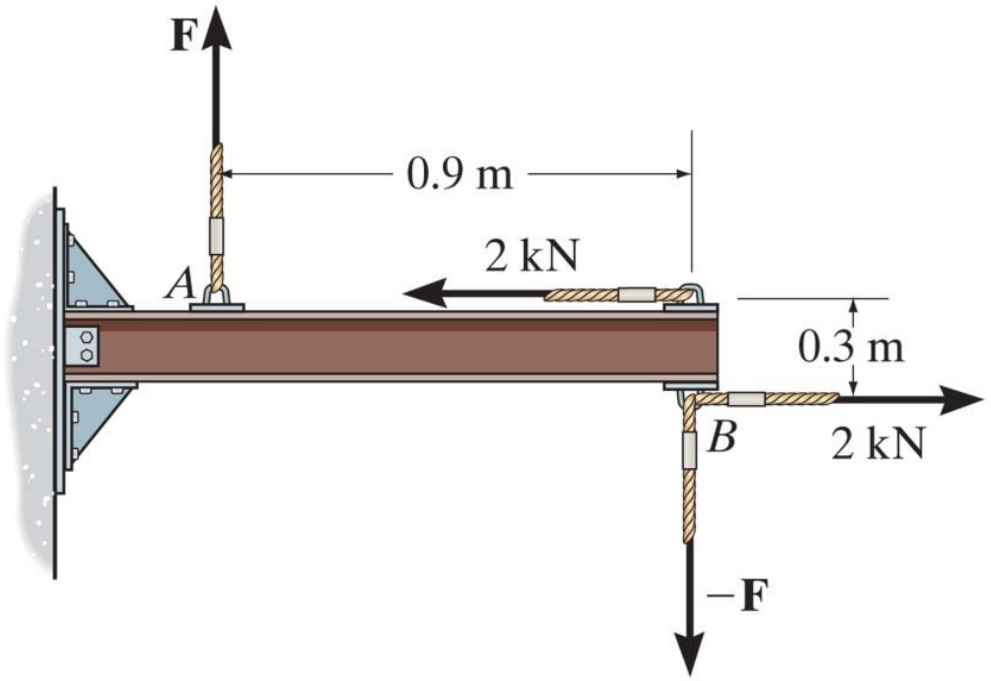


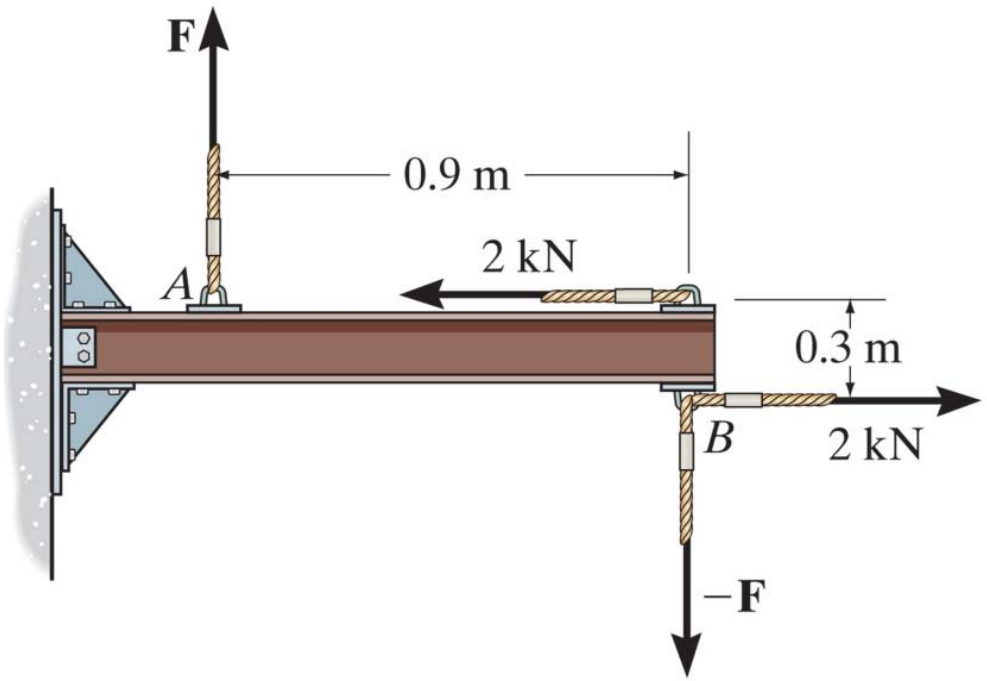
A torque or moment of 12 N·m is required to rotate the wheel.

Would F be greater or less than 30 N?

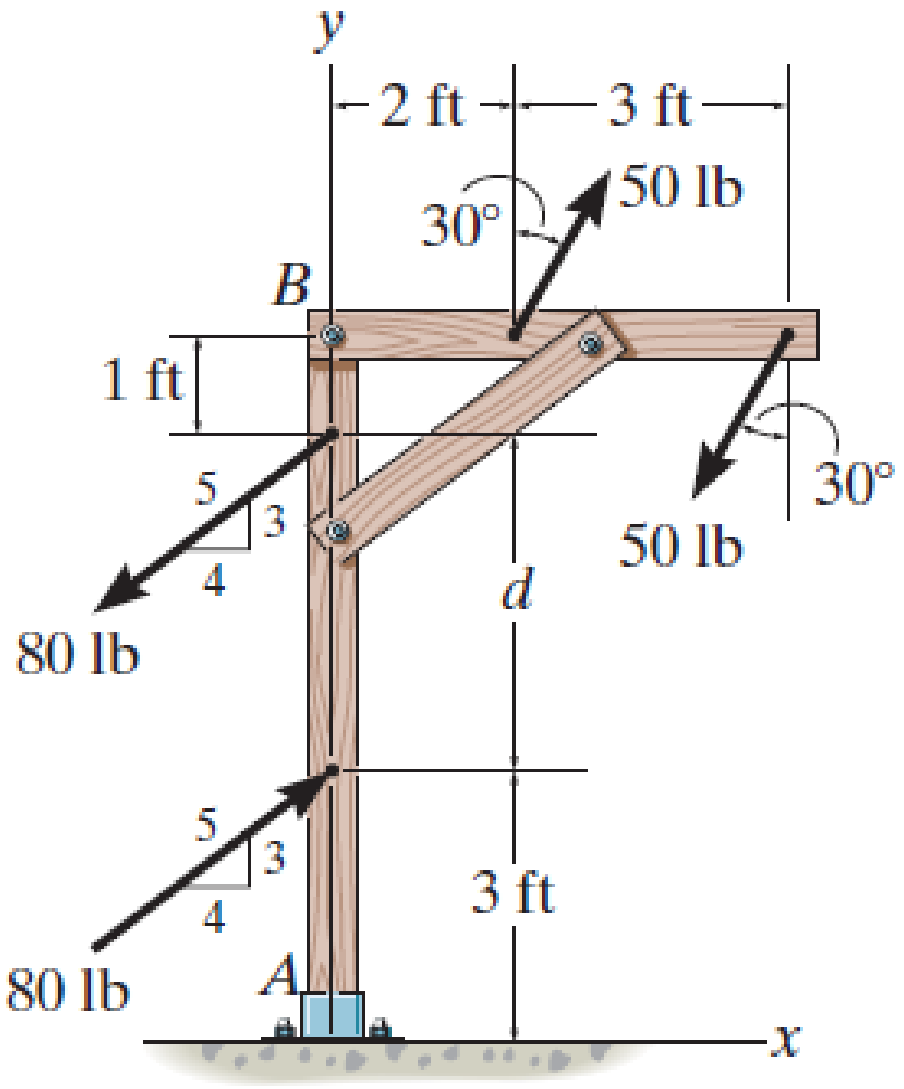
Resultant Couple Moment

Since couple moments are vectors, their resultant is due to vector addition:





Two couples act on the beam with the geometry shown. Find the magnitude of F so that the resultant couple moment is 1.5 kN·m clockwise.



Two couples act on the beam with the geometry shown and d = 4 ft. Find the resultant couple