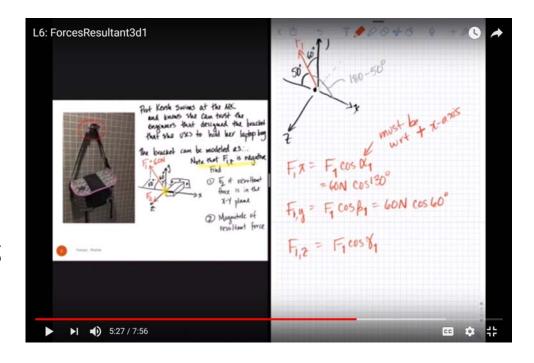
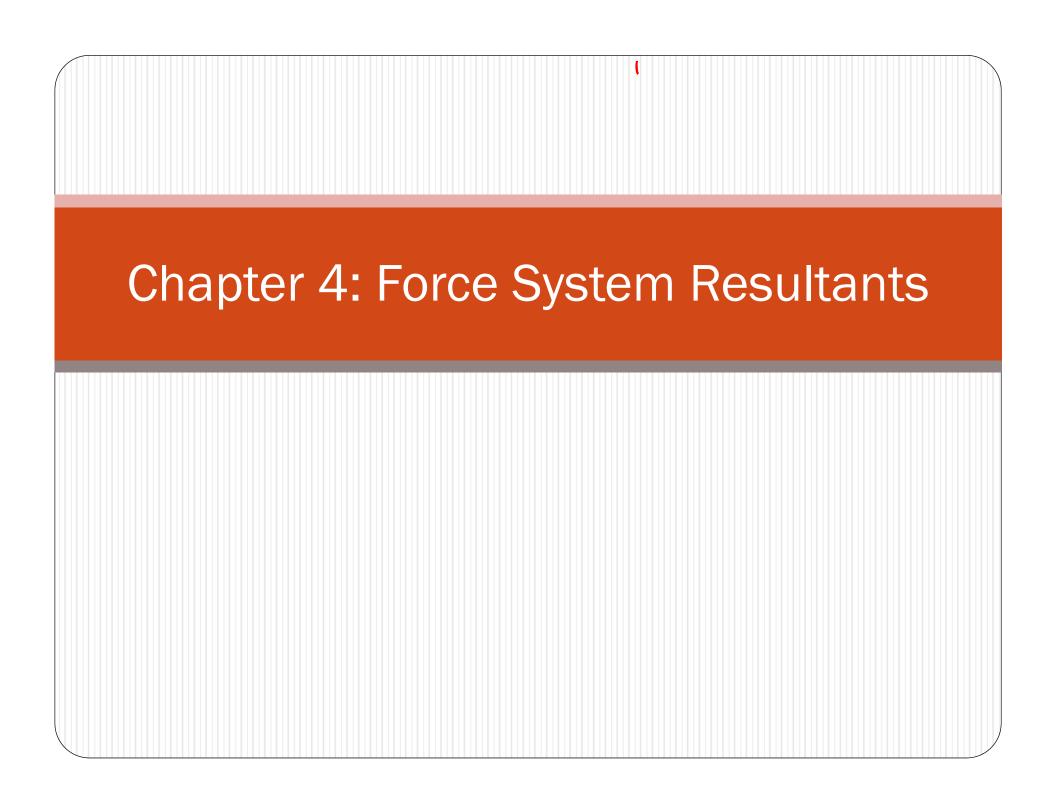
Statics - TAM 210 & TAM 211

Lecture 11 February 9, 2018

Announcements

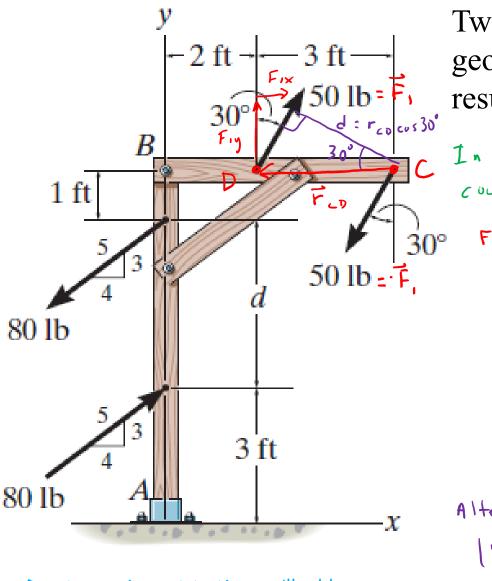
- □ Note there are videos of solving more sample problems under Schedule tab of course website
- ☐ Upcoming deadlines:
- Quiz 2 (2/7-9)
 - Reserve testing time at CBTF
 - Lectures 5-9
- Friday (2/9)
 - Mastering Engineering Tutorial 5
- Tuesday (2/13)
 - PL Homework 4





Goals and Objectives

- Discuss the concept of the <u>moment of a force</u> and show how to calculate it in two and three dimensions
- How to find the moment about a specified axis
- Define the moment of a couple
- Finding equivalence force and moment systems
- Reduction of <u>distributed loading</u>

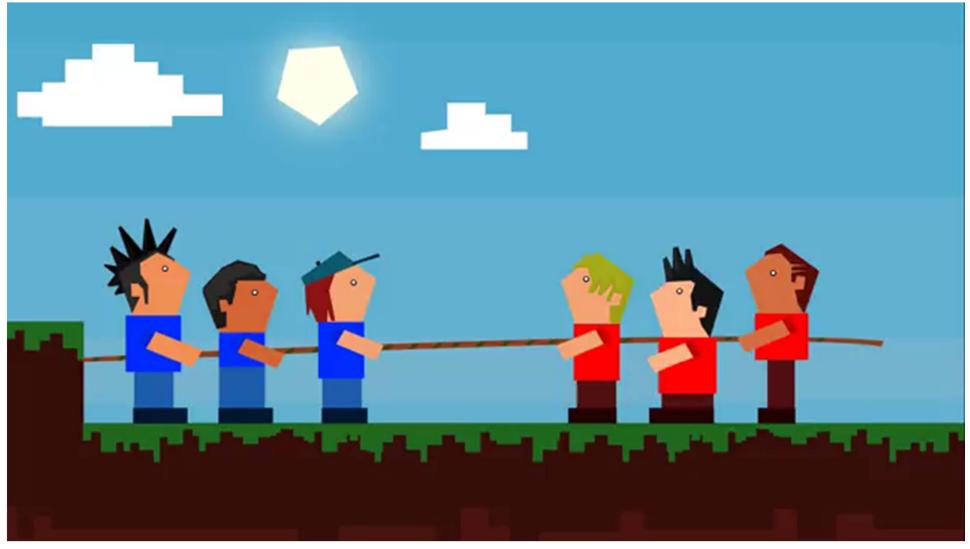


Due to running out to time, we'll address the typed problem statement in our next lecture. Hint to find M_R , need to also determine M_{lower} , such that $M_R = M_{upper} + M_{lower}$

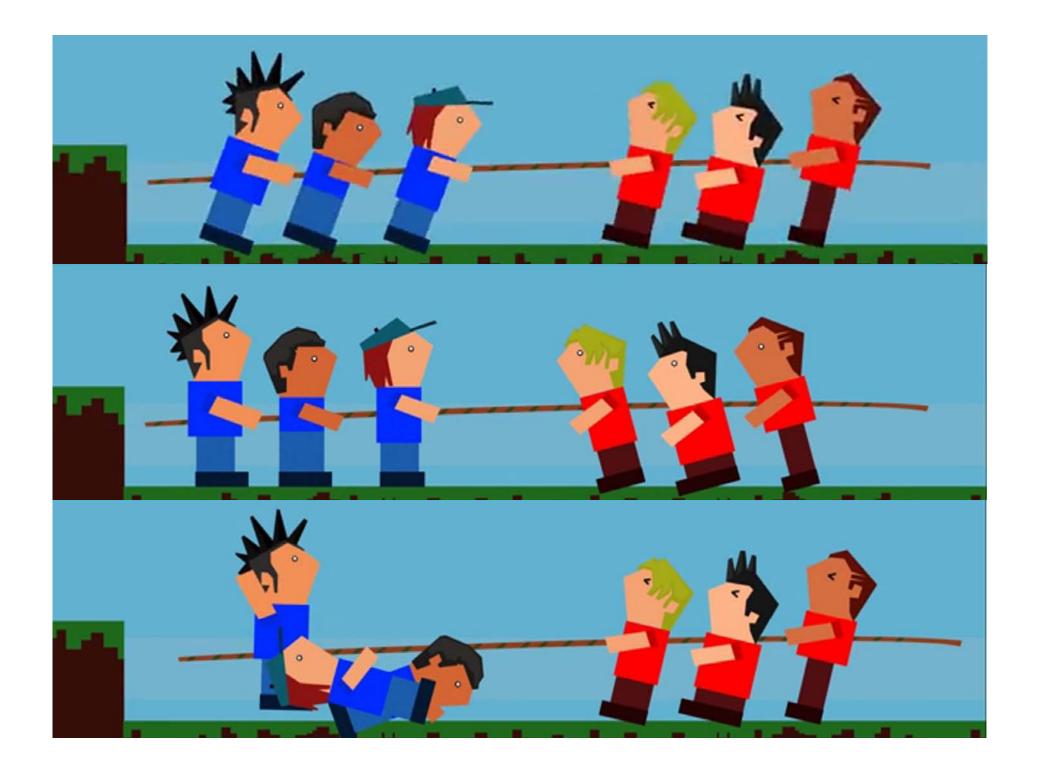
Two couples act on the beam with the geometry shown and d = 4 ft. Find the resultant couple

In response to student question about couple moment when T is not I to F: For upper beam, what is the Moment due to the solb force Couple? Find: Mupper Mugger = TXF = FCD XF, $= (-314 c) \times 50 (512300)$ + < 05 30j)16 = - 130 ft.16 k | Mupper | = d F where d is 1 distance Alternatively, = (|r col (0) 30° fl) (50 15) = (3 cos 30°) 50 ft.16 = 130 ft. 16 ccu (-k) Mupper = - 130 ft 16 k / same

Moving a force on its line of action



https://www.wikihow.com/Win-at-Tug-of-War



Moving a force on its line of action

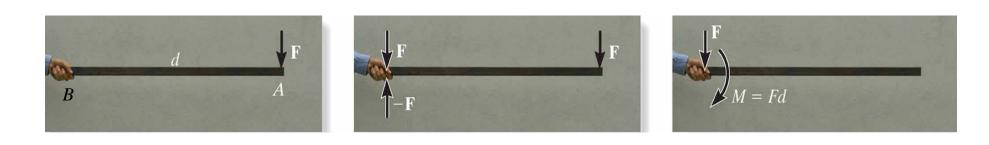


Moving a force from A to B, when both points are on the vector's line of action, does not change the **external effect**.

Hence, a force vector is called a **sliding vector**.

However, the **internal effect** of the force on the body does depend on where the force is applied.

Moving a force off of its line of action



The two force systems are equipollent since the resultant force is the same in both systems, and the resultant moment with respect to any point P is the same in both systems.

So moving a force off its line of action means you have to "add" a new couple. Since this new couple moment is a **free vector**, it can be applied at any point on the body.

Equipollent (or equivalent) force systems

A force **system** is a collection of **forces** and **couples** applied to a body.

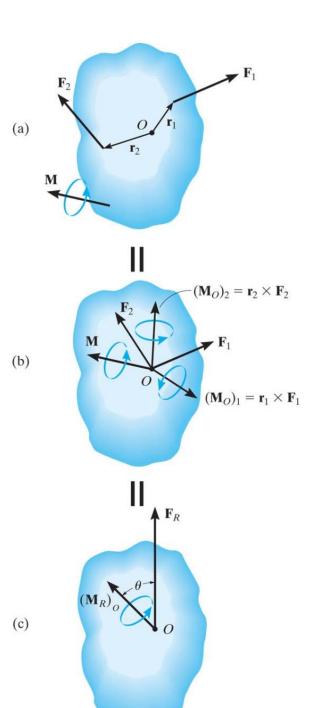
Two force systems are said to be **equipollent** (or equivalent) if they have the **same resultant force** AND the **same resultant moment** with respect to any point O.

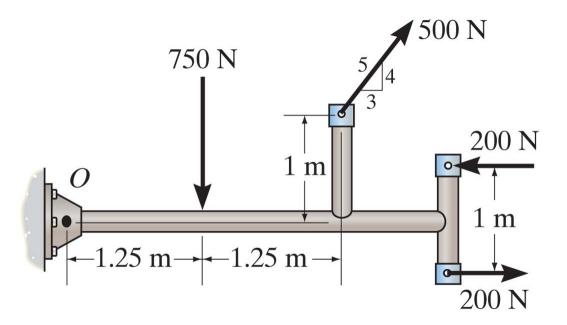
Reducing a force system to a single resultant force F_R and a single resultant couple moment $(M_R)_o$:

$$\overrightarrow{F_R} = \Sigma F_{\chi} \hat{\boldsymbol{i}} + \Sigma F_{y} \hat{\boldsymbol{j}} + \Sigma F_{z} \hat{\boldsymbol{k}}$$

$$|\overrightarrow{F_R}| = \sqrt{F_{\chi}^2 + F_{y}^2 + F_{z}^2} \qquad \theta = \tan^{-1} \frac{F_{opp}}{F_{adj}}$$

$$(M_R)_{o} = \sum M_{o} + \sum M$$

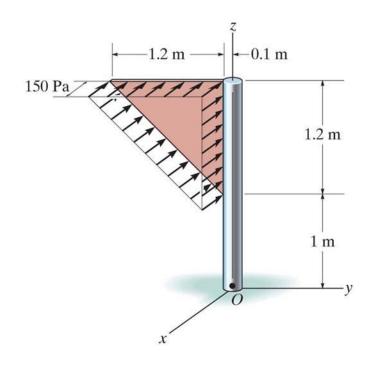




Replace the forces and couple system acting on the member by an equivalent force and couple moment acting at point O.

Reduction to a simple distributed load

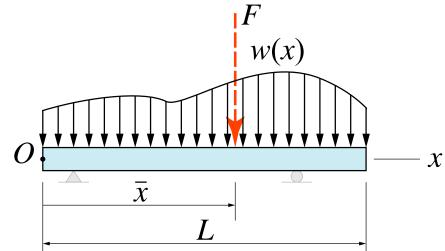




The lumber places a distributed load (due to the weight of the wood) on the beams. To analyze the load's effect on the steel beams, it is often helpful to reduce this distributed load to a single force. How would you do this?

To be able to design the joint between the sign and the sign post, we need to determine a single equivalent resultant force and its location.

Reduction to a simple distributed load



In structural analysis, often presented with **distributed load** w(x) (force/unit length) and need to find equivalent loading F.

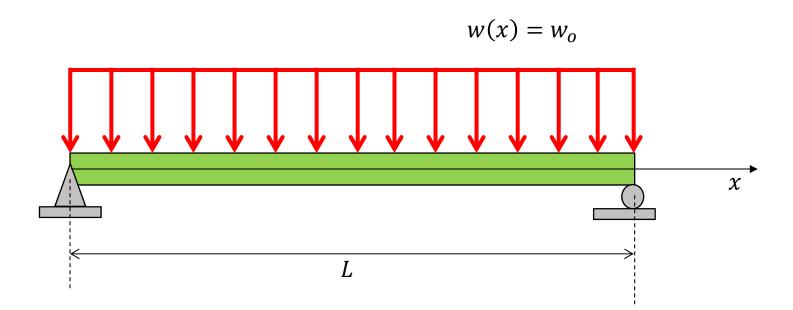
Ex: winds, fluids, weight on body's surface.

By equipollence, we require that $\sum \mathbf{F}$ be the same in both systems, i.e.,

and $\sum M_P$ with respect to any point P be the same in both systems, i.e.,

Combining both equations gives:

Rectangular loading



Triangular loading

