Statics - TAM 210 & TAM 211

Lecture 12 February 12, 2018

Announcements

- □ **READ** <u>Piazza</u> **posts!** If you had difficulty with Quiz 2, start reading and creating posts. There is a direct correlation with reviewing posts and quiz grade.
- ☐ Cumulative exam, Thursday, April 5, 7-9pm, 1 Noyes Lab
 - ☐ If you need DRES accommodation, send private message to instructors on Piazza with PDF of DRES letter. You must make your own arrangements at DRES testing facilities.
 - □ Conflict exam request: **MUST** send private message instructors on Piazza **now or at least 2 weeks before the exam date**. Only legitimate conflicts will be allowed. See <u>Information tab > Exam</u>
- ☐ Upcoming deadlines:
- Tuesday (2/13)
 - PL Homework 4
- Written Assignment 2 (2/15)
 - See <u>Schedule</u> page for assignment instructions
- Friday (2/16)
 - Mastering Engineering Tutorial 6

Recap: General procedure for analysis

- 1. Read the problem carefully; write it down carefully.
- 2. MODELTHE PROBLEM: Draw given diagrams neatly and construct additional figures as necessary.
- 3. Apply principles needed.
- 4. Solve problem symbolically. Make sure equations are dimensionally homogeneous
- 5. Substitute numbers. Provide proper units *throughout*. Check significant figures. Box the final answer(s).
- 6. See if answer is reasonable.

Most effective way to learn engineering mechanics is to solve problems!

Chapter 4: Force System Resultants

Goals and Objectives

- Discuss the concept of the <u>moment of a force</u> and show how to calculate it in two and three dimensions
- How to find the moment about a specified axis
- Define the <u>moment of a couple</u>
- Finding equivalence force and moment systems
- Reduction of <u>distributed loading</u>

Recap

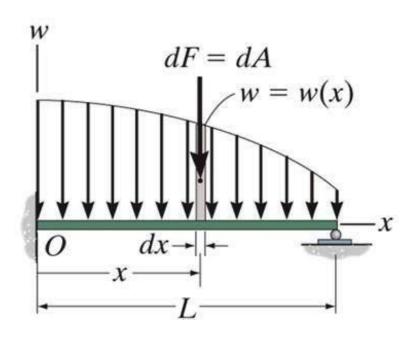
- Equivalent force system for distributed loading function w(x) with units of $\frac{\text{force}}{\text{length}}$.
- Find magnitude F_R and location \bar{x} of the equivalent resultant force for $\overline{F_R}$

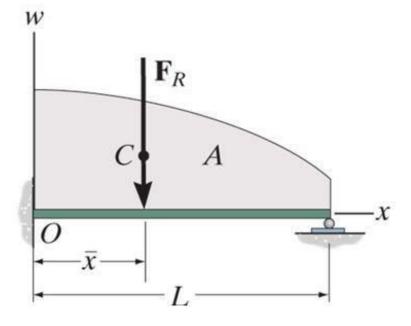
$$\left|\overrightarrow{F_R}\right| = F_R = \int_0^L dF = \int_0^L w(x) dx = A$$

$$M_o = \int_0^L x \ w(x) \ dx = \overline{x} F_R$$

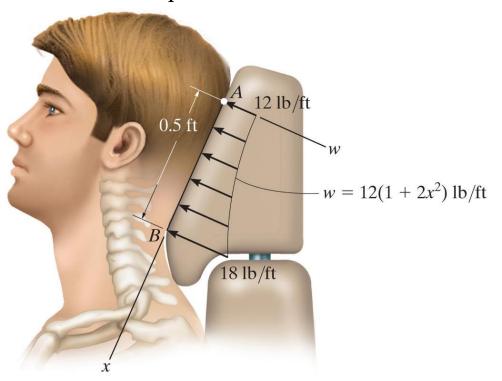
$$\overline{x} = \frac{M_o}{F_R} = \frac{\int_0^L x \ w(x) \ dx}{\int_0^L w(x) \ dx}$$

 $\bar{x} =$ **geometric center or centroid** of area A under loading curve w(x).

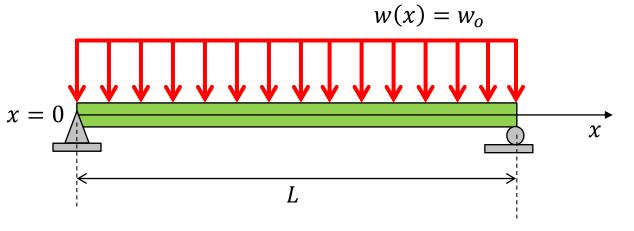




Find equivalent force and its location from point A for loading on headrest.



Rectangular loading

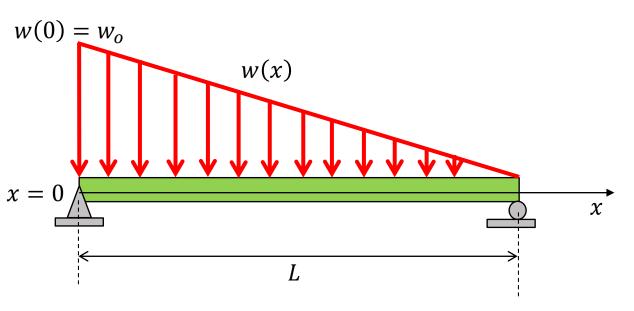


$$w(x) = w_o$$

$$\left|\overrightarrow{F}\right| = F = w_o L$$

$$\overline{x} = \frac{L}{2}$$

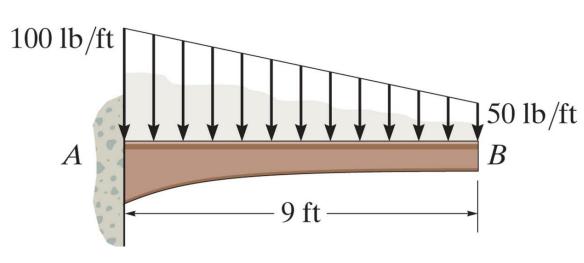
Triangular loading



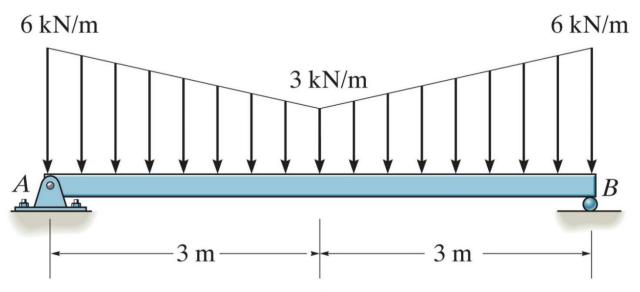
$$w(x) = w_o - \frac{w_o x}{L}$$

$$F = w_o \frac{L}{2}$$

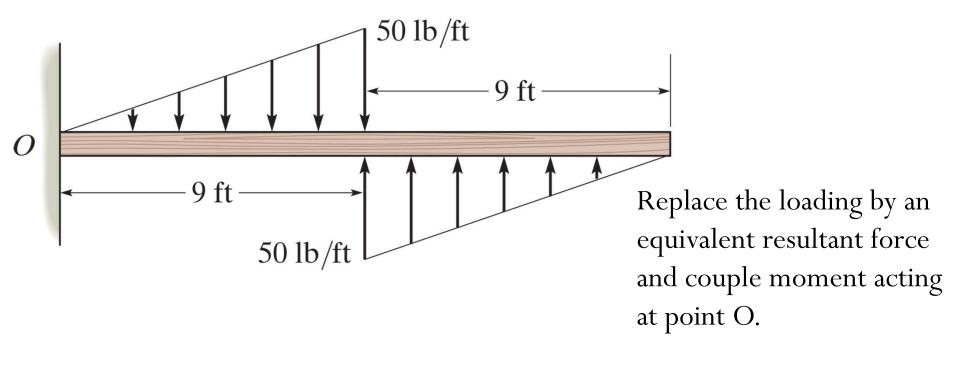
$$\overline{x} = \frac{L}{2}$$



Determine the magnitude and location of the equivalent resultant of this load.



6 kN/m Replace the distributed loading by an equivalent resultant force and couple moment acting at point A.



Chapter 5: Equilibrium of Rigid Bodies

Goals and Objectives

- Introduce the free-body diagram for a rigid body
- Develop the equations of equilibrium for a rigid body
- Solve rigid body equilibrium problems using the equations of equilibrium

Equilibrium of a Rigid Body

Static equilibrium:

$$\sum \vec{F} = 0$$
 (zero forces = no translation)

$$\sum (\overline{M}) = 0$$
 (zero moment = no rotation)

Maintained by reaction forces and moments

Forces from supports / constraints are exactly enough to produce zero forces and moments

Assumption of rigid body

Shape and dimensions of body remain **unchanged** by application of forces.

More precisely:

All **deformations of bodies** are small enough to be ignored in analysis.



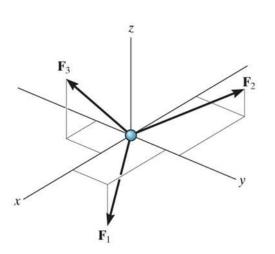


Equilibrium of a Rigid Body

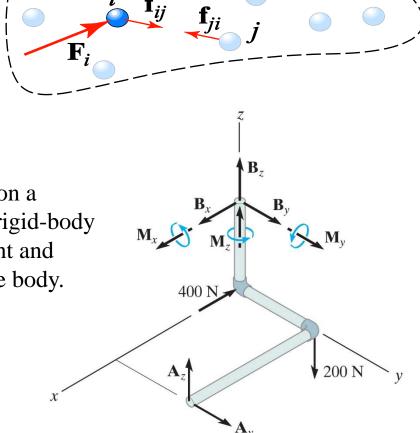
Equilibrium of a rigid body is of central importance in statics. We regard a rigid body as a collection of particles.

 $\overrightarrow{F_i} = \text{resultant external force on particle } i$ $\overrightarrow{f_{ij}} = \text{internal force on particle } i \text{ by particle } j$ $\overrightarrow{f_{ij}} = \text{internal force on particle } j \text{ by particle } i$

Note that $\overline{f_{ij}} = \overline{f_{ij}}$ by Newton's third law. Therefore the internal forces will not appear in the equilibrium equations.

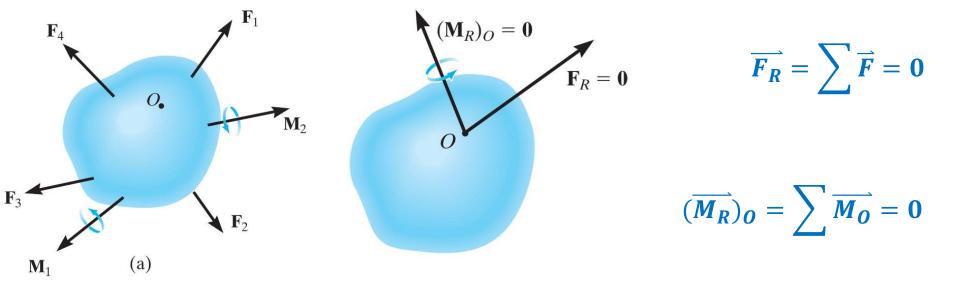


In contrast to the forces on a particle, the forces on a rigid-body are not usually concurrent and may cause rotation of the body.

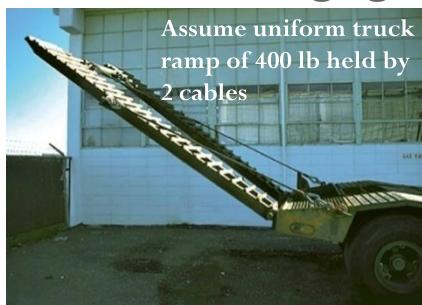


Equilibrium of a Rigid Body

We can reduce the force and couple moment system acting on a body to an equivalent resultant force and a resultant couple moment at an arbitrary point O.

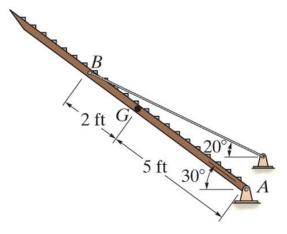


Process of solving rigid body equilibrium problems



2. Draw free body diagram showing ALL the external (applied loads and supports)

1. Create idealized model (modeling and assumptions)



3. Apply equations of equilibrium

$$\overrightarrow{F_R} = \sum_{i} \overrightarrow{F} = \mathbf{0}$$

$$(\overrightarrow{M_R})_A = \sum \overrightarrow{M_A} = \mathbf{0}$$

In this case, let's sum moments about pt A

Equilibrium in two-dimensional bodies

(Support reactions)



- If a support prevents the translation of a body in a given direction, then a force is developed on the body on that direction
- If a rotation is prevented, a couple moment is exerted on the body

Types of connectors

rocker

TABLE 5-1 Supports for Rigid Bodies Subjected to Two-Dimensional Force Systems Types of Connection Number of Unknowns Reaction (1) One unknown. The reaction is a tension force which acts away from the member in the direction of the cable. cable (2) One unknown. The reaction is a force which acts along or the axis of the link. weightless link (3) One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact. roller (4) One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.

Types of connectors

Types of Connection		Reaction	Number of Unknowns
(5) θ smooth contacting surface	F E		One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.
(6) Proller or pin in		or F	One unknown. The reaction is a force which acts perpendicular to the slot.
confined smooth slot (7) member pin connected to collar on smooth rod	θ	or θ	One unknown. The reaction is a force which acts perpendicular to the rod.

Types of connectors

