Statics - TAM 211

Lecture 7 September 26, 2018

Announcements

□ No classes September 29 – October 7 for National Day Holiday

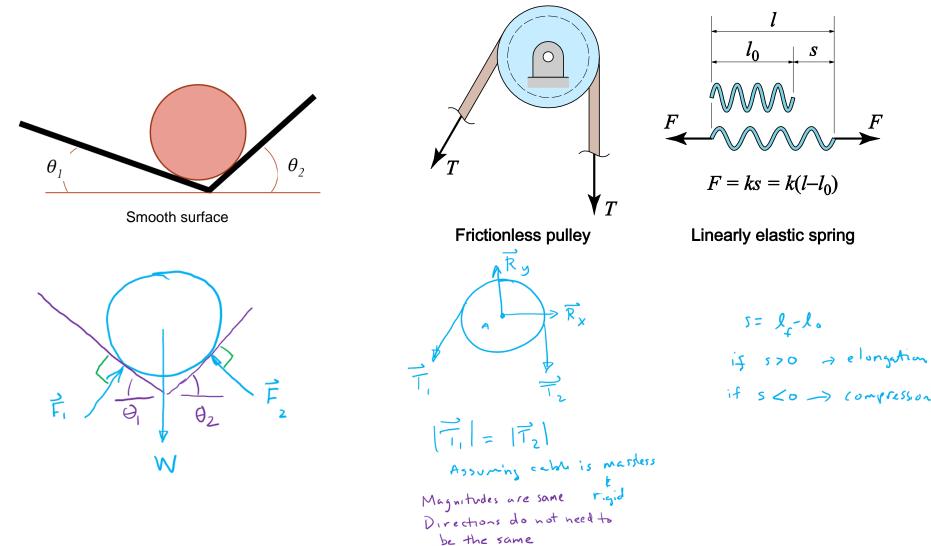
□ Upcoming deadlines:

- Thursday (9/28)
 - Quiz 1, 6-7 pm
 - Computer Lab (D211 for ME, D331 for CEE)
 - No personal calculator, must use computer
- Friday (Sept 28)
 - Written Assignment 2
- Tuesday (10/9)
 - Prairie Learn HW3



Recap: Idealizations

Smooth surfaces: regarded as frictionless; force is perpendicular to surfacePulleys: (usually) regarded as frictionless; tension around pulley is same on either side.Springs: (usually) regarded as linearly elastic; tension is proportional to *change* in length *s*.

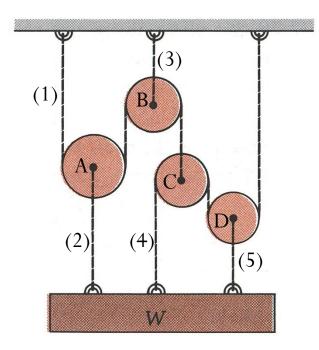


Recap: Equilibrium of a system of particles

Some practical engineering problems involve the statics of interacting or interconnected particles. To solve them, we use Newton's first law

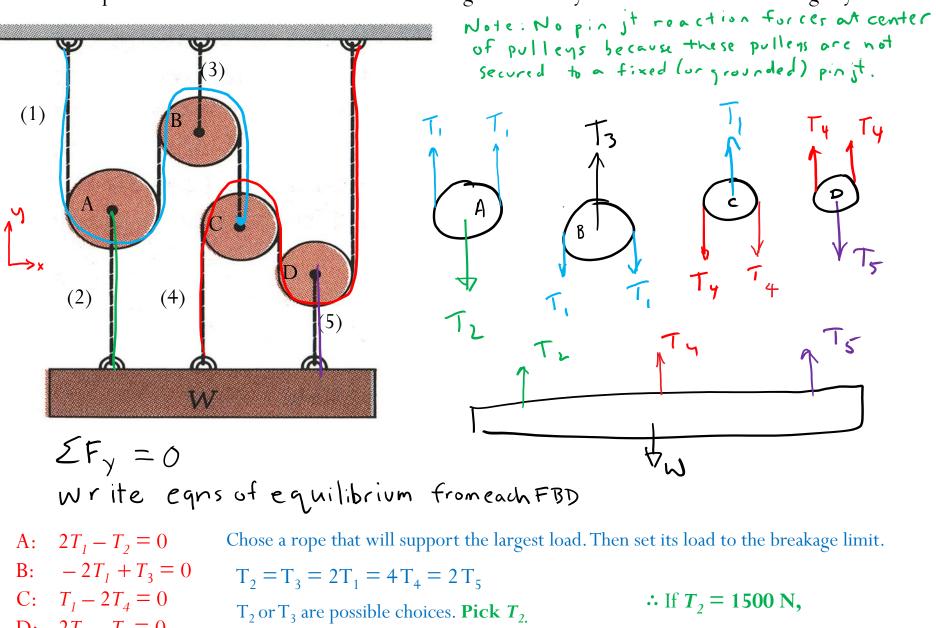
$\Sigma \mathbf{F} = \mathbf{0}$

on selected multiple free-body diagrams of particles or groups of particles.



The five ropes can each take 1500 N without breaking. How heavy can *W* be without breaking any?

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W:
$$T_2 + T_4 + T_5 - W = 0 \implies W = T_2 + 0.25 T_2 + 0.5 T_2$$

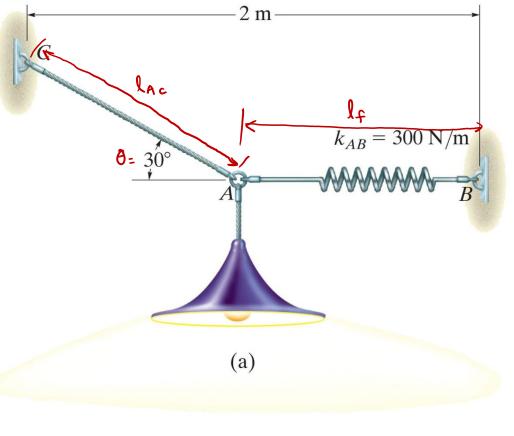
D.

Then W = 2625 N

Determine the required length of cord AC so that the 8-kg lamp can be suspended in the position shown.

The undeformed spring length is 0.4 m and has a stiffness of 300 N/m.

Given: M = 8kg, $l_0 = 0.4m$, $k_{a3} = 300$ N/m $\Theta = 30^{\circ}$ Find: l_{AC} Soln: FBD of A ZF_x : $F_s - F_{ac} \cos \theta = 0$ () ZF_y : $F_{ac} \sin \theta - mg = 0$ (2) $F_s = k_{ab} = k_{ab} (l_f - l_0)$ (3)



$$(3) int_{0} (1) : k_{AB}(l_{f} - l_{0}) - F_{Ac} \cos \theta = 0$$

$$insert (2) : k_{AB}(l_{f} - l_{0}) - (\frac{mg}{\sin \theta}) \cos \theta = 0$$

$$int_{0} = (\frac{mg}{k}) \frac{\cos \theta}{\sin \theta} + l_{0} = 0.853m$$

$$int_{0} = 0.853m$$

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Use geometrical constraint:
$$2m = l_f + l_{Ac} \cos \Theta$$

 $l_{Ac} = \frac{2m - l_f}{\cos \Theta} = [1.32m = l_{Ac}]$

3D force systems Use
$$\Sigma \overline{F_x} = 0, \Sigma \overline{F_y} = 0, \Sigma \overline{F_z} = 0$$

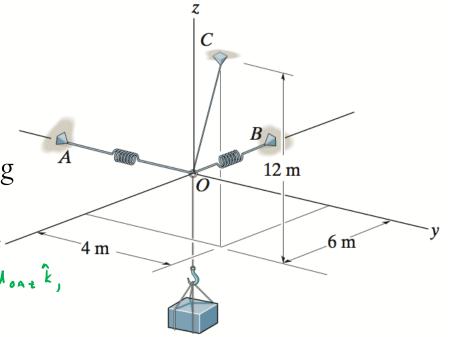
() Draw Find the tension developed in each cable
FBD Q A:
 $\overline{F_{A_B}}$ $\overline{F_{A_C}}$ $\overline{F_{A_C}}$
 $\overline{F_{A_B}}$ $\overline{F_{A_C}}$ $\overline{F_{$

Example – 3D

Determine the stretch in each of the two springs required to hold the 20-kg crate in the equilibrium position shown. Each spring has an unstretched length of 2 m and a stiffness of k = 360 N-m.

Check solution: If
$$\hat{u}_{0A} = U_{0Ax}\hat{i} + U_{0Ay}\hat{j} + U_{0A}$$

then $S_{0A} = \frac{F_{0c} U_{0Ay}}{k} = 218 \text{ mm}$
 $S_{0B} = \frac{F_{0c} U_{0Ax}}{k} = 327 \text{ mm}$



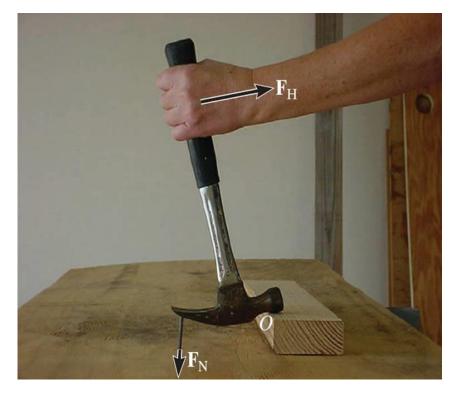
Chapter 4: Force System Resultants

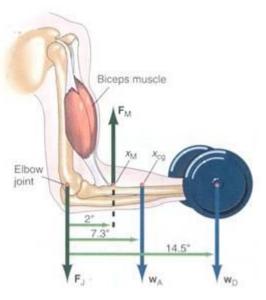
Goals and Objectives

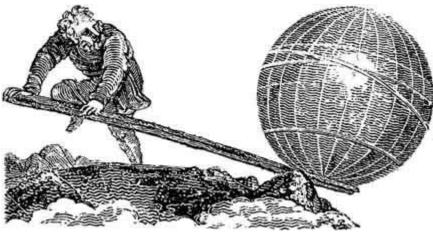
- Discuss the concept of the <u>moment of a force</u> and show how to calculate it in two and three dimensions
- How to find the <u>moment about a specified axis</u>
- Define the <u>moment of a couple</u>
- Finding <u>equivalence force and moment systems</u>
- Reduction of <u>distributed loading</u>

Moment of a force

The **moment of a force about a point** provides a measure of the **tendency for rotation** (sometimes called a torque).



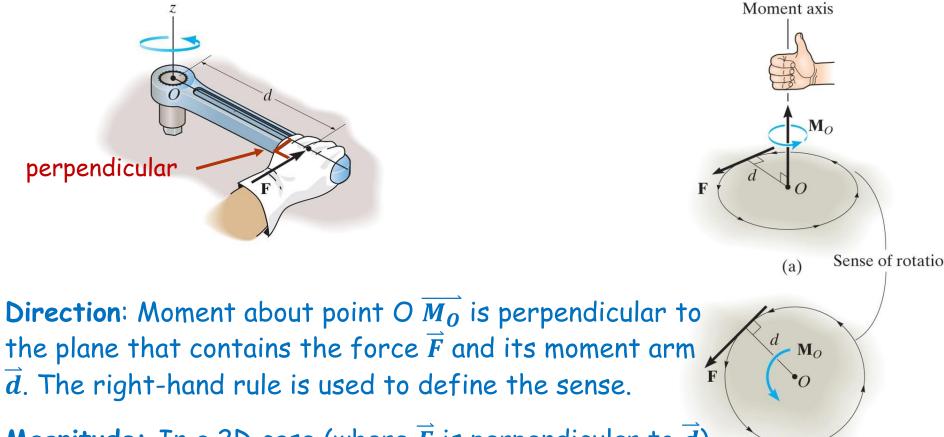




Moment 1.A very brief period of time. An exact point in time. 2. Importance. 3. A turning effect produced by a force acting at a distance on an object. Oxford Dictionary

Moment of a force – <u>scalar formulation</u>

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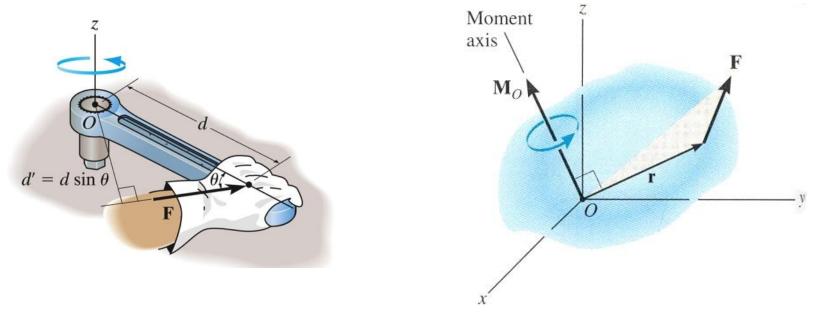


(b)

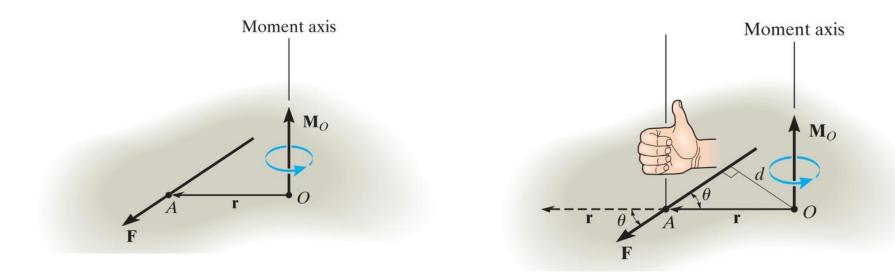
Magnitude: In a 2D case (where \vec{F} is perpendicular to \vec{d}), the magnitude of the moment about point O is $M_O = F d$

Moment of a force – vector formulation The moment of a force \vec{F} about point O, or actually about the moment axis passing through O and perpendicular to the plane containing O and \vec{F} , can be expressed using the cross (vector) product, namely:

where \vec{r} is the position vector directed from O to any point on the line of action of \vec{F} .



Moment of a force – vector formulation



Use cross product: $\overline{M_O} = \overline{r} \times \overline{F}$ Direction: Defined by right hand rule.

 $\overrightarrow{M_O} = \overrightarrow{r} \times \overrightarrow{F}$

Magnitude:

 $M_{O} = \left| \overrightarrow{\boldsymbol{M}_{O}} \right|$

