## Statics - TAM 211

Lecture 13
October 17, 2018

## Announcements

$\square$ Upcoming deadlines:

- Friday (10/19)
- Written Assignment 4
- Tuesday (10/23)
- Prairie Learn HW5
- Quiz 2
- Week of Oct 22


## $\square$ Preparation for quiz:

$\square$ As announced during discussion section, you are encouraged and allowed to use your Casio calculator during PrairieLearn HWs and Quizzes.
$\square$ You should learn to solve a system of equations by hand using a calculator
$\square$ PrairieLearn incorrect software issues:
$\square$ Negative sign symbol (- vs. - )
Space between negative sign (-12 vs. - 12)
$\square$ Solutions:
$\square$ Always type in the negative sign symbol (-) into your PL answers for HW or Quiz.
$\square$ Do not add space between negative symbol and number
$\square$ All students with these errors will be provided updated grades on Quiz 1. No credit for Quiz 2 and beyond.

- Practice PL HW on your own. Practice using a calculator.
- Monitor your time
- Read each question. Write givens, unknowns, draw FBD, write out equations
- HW reflections
- What concepts did you struggle with?


## Recap: Distributed Ioads

$F_{R}=\int_{0}^{L} w(x) d x \quad \bar{x}=\frac{\int_{0}^{L} x w(x) d x}{\int_{0}^{L} w(x) d x} \quad M_{o}=\bar{x} F_{R}$

## Simple Shape Distributed Ioads



$$
w(x)=w_{o}
$$

$$
\left|\overrightarrow{\boldsymbol{F}_{\boldsymbol{R}}}\right|=F_{R}=w_{o} L
$$

$$
\bar{x}=\frac{L}{2}
$$

Triangular loading


$$
\begin{aligned}
& w(x)=w_{o}-\frac{w_{o} x}{L} \\
& F_{R}=w_{o} \frac{L}{2} \\
& \bar{x}=\frac{L}{3}
\end{aligned}
$$

## Recap: Superposition of simple shapes

- Divide complex distributed loads into multiple simple shapes of rectangles and/ or triangles.
- Superimpose the resultant forces for each simple shape to determine the final composite resultant force.
$100 \mathrm{lb} / \mathrm{ft}$


Use
(1) Sum of vertical forces: $\boldsymbol{F}_{R}=\Sigma \boldsymbol{F}_{i}$
(2 )Use sum of moments to find $\bar{X}_{T}$

$$
\bar{x}_{T}=\frac{\Sigma \bar{x}_{i} F_{i}}{F_{R}}
$$

## Chapter 5: Equilibrium of Rigid Bodies

## Goals and Objectives

- Introduce the free-body diagram for a rigid body
- Develop the equations of equilibrium for a 2D and 3D rigid body
- Solve rigid body equilibrium problems using the equations of equilibrium in 2D and 3D
- Introduce concepts of
- Support reactions for 2D and 3D bodies
- Two- and three-force members
- Constraints and statical determinacy


## Equilibrium of a Rigid Body

## Static equilibrium:

$\sum \overrightarrow{\boldsymbol{F}}=\mathbf{0}$ (zero forces = no translation)
$\sum(\overrightarrow{\boldsymbol{M}})=\mathbf{0}$ (zero moment $=$ no rotation)

## Maintained by reaction forces and moments

Forces from supports / constraints are exactly
 enough to produce zero forces and moments

## Assumption of rigid body

Shape and dimensions of body remain unchanged by application of forces.
More precisely:
All deformations of bodies are small enough to be ignored in analysis.


## Equilibrium of a Rigid Body

Equilibrium of a rigid body is of central importance in statics. We regard a rigid body as a collection of particles.
$\overrightarrow{\boldsymbol{F}_{i}}=$ resultant external force on particle $i$ $\overrightarrow{\boldsymbol{f}_{i j}}=$ internal force on particle $i$ by particle $j$ $\overrightarrow{\boldsymbol{f}_{i j}}=$ internal force on particle $j$ by particle $i$

Note that $\overrightarrow{\boldsymbol{f}_{i j}}=\overrightarrow{\boldsymbol{f}_{i j}}$ by Newton's third law.


Therefore the internal forces will not appear in the equilibrium equations.


In contrast to the forces on a particle, the forces on a rigid-body are not usually concurrent and may cause rotation of the body.


## Equilibrium of a Rigid Body

We can reduce the force and couple moment system acting on a body to an equivalent resultant force and a resultant couple moment at an arbitrary point O .


$$
\begin{gathered}
\overrightarrow{F_{R}}=\sum \vec{F}=0 \\
\left(\overrightarrow{M_{R}}\right)_{o}=\sum \overrightarrow{M_{0}}=0
\end{gathered}
$$

## Recap: General procedure for analysis

1. Read the problem carefully; write it down carefully.
2. MODEL THE PROBLEM: Draw given diagrams neatly and construct additional figures as necessary.
3. Apply principles needed.
4. Solve problem symbolically. Make sure equations are dimensionally homogeneous
5. Substitute numbers. Provide proper units throughout. Check significant figures. Box the final answer(s).
6. See if answer is reasonable.

Most effective way to learn engineering mechanics is to solve problems!

Process of solving rigid body equilibrium problems

2. Draw free body diagram showing ALL the external (applied loads and support reactions) $F B D$ of RAMP dally


This slide presents the basic approach for problem solving for this course (previous slide). Understand how to do this approach!
3. Apply equations of equilibrium

$$
\begin{aligned}
& \overrightarrow{\boldsymbol{F}_{\boldsymbol{R}}}=\sum+\overrightarrow{\boldsymbol{F}}=\mathbf{0} \\
& \quad \pm \sum F_{x}:-A_{x}+T \cos 20^{\circ}=0 \\
& \quad+\uparrow \sum F_{y}: A_{y}-W-T_{\sin } 20^{\circ}=0 \text { (2) } \\
& \left(\overrightarrow{\boldsymbol{M}_{\boldsymbol{R}}}\right)_{A}=\sum \overrightarrow{\boldsymbol{M}_{A}}=\mathbf{0}
\end{aligned}
$$

Let's sum moments about pt A. Pick pt to sum moments that eliminates as many unknowns as possible.

$$
\begin{equation*}
+\sum \sum M_{A}:+W\left(d_{\omega}\right)-T\left(d_{T}\right)=0 \tag{3}
\end{equation*}
$$

3 Unknowns $\left(A_{x}, A_{y}, T^{\prime}\right)$, 3 equations $(1-3)$ $\Rightarrow$ Determinate system $\therefore$ Can solve.

## Equilibrium in two-dimensional bodies (Support reactions)



Smooth pin or hinge


Fixed support


- If a support prevents the translation of a body in a given direction, then a force is developed on the body on that direction
- If a rotation is prevented, a couple moment is exerted on the body


## Types of connectors

TABLE 5-1 Supports for Rigid Bodies Subjected to Two-Dimensional Force Systems


cable
(2)

weightless link
(3)


One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.
(4)


One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.

## Types of connectors

TABLE 5-1 Supports for Rigid Bodies Subjected to Two-Dimensional Force Systems
Types of Connection Reaction Number of Unknowns


One unknown. The reaction is a force which acts perpendicular to the surface at the point of contact.
(6)


One unknown. The reaction is a force which acts perpendicular to the slot.
roller or pin in confined smooth slot
(7)


One unknown. The reaction is a force which acts perpendicular to the rod.
member pin connected
to collar on smooth rod


## Types of connectors

## TABLE 5-1 Continued

Types of Connection Reaction Number of Unknowns
(8)

or


Two unknowns. The reactions are two components of force, or the magnitude and direction $\phi$ of the resultant force. Note that $\phi$ and $\theta$ are not necessarily equal [usually not, unless the rod shown is a link as in (2)].

Two unknowns. The reactions are the couple moment and the force which acts perpendicular to the rod.
member fixed connected to collar on smooth rod
(10)

or


Three unknowns. The reactions are the couple moment and the two force components, or the couple moment and the magnitude and direction $\phi$ of the resultant force.

[^0]
[^0]:    fixed support

