Statics - TAM 211

Lecture 13 October 17, 2018

Announcements

- □ Upcoming deadlines:
- Friday (10/19)
 - Written Assignment 4
- Tuesday (10/23)
 - Prairie Learn HW5
- Quiz 2
 - Week of Oct 22

As announced during discussion section, you are encouraged and allowed to use your Casio calculator during PrairieLearn HWs and Quizzes.

☐ You should learn to solve a system of equations by hand using a calculator

□ PrairieLearn incorrect software issues:

 \Box Negative sign symbol (- vs. –)

□ Space between negative sign (-12 vs. - 12)

□ Solutions:

Always type in the negative sign symbol (-) into your PL answers for HW or Quiz.

Do not add space between negative symbol and number

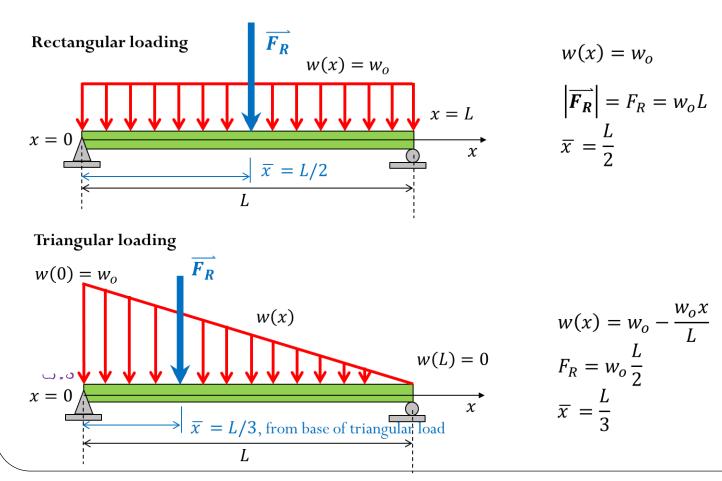
□ All students with these errors will be provided updated grades on Quiz 1. No credit for Quiz 2 and beyond.

Preparation for quiz:

- Practice PL HW on your own. Practice using a calculator.
- Monitor your time
- Read each question. Write givens, unknowns, draw FBD, write out equations
- HW reflections
 - What concepts did you struggle with?

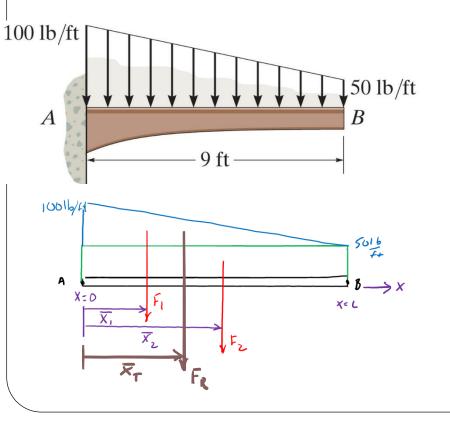
Recap: Distributed loads $F_R = \int_0^L w(x) \, dx \qquad \overline{x} = \frac{\int_0^L x \, w(x) \, dx}{\int_0^L w(x) \, dx} \qquad M_o = \overline{x} \, F_R$

Simple Shape Distributed loads



Recap: Superposition of simple shapes

- Divide complex distributed loads into multiple simple shapes of rectangles and/or triangles.
- Superimpose the resultant forces for each simple shape to determine the final composite resultant force.



Use (1)Sum of vertical forces: $F_R = \Sigma F_i$ (2)Use sum of moments to find \bar{x}_T $\bar{x}_T = \frac{\Sigma \bar{x}_i F_i}{F_P}$

Chapter 5: Equilibrium of Rigid Bodies

Goals and Objectives

- Introduce the free-body diagram for a rigid body
- Develop the equations of equilibrium for a 2D and 3D rigid body
- Solve rigid body equilibrium problems using the equations of equilibrium in 2D and 3D
- Introduce concepts of
 - Support reactions for 2D and 3D bodies
 - Two- and three-force members
 - Constraints and statical determinacy

Equilibrium of a Rigid Body

Static equilibrium:

 $\sum \vec{F} = \mathbf{0} \text{ (zero forces = no translation)}$ $\sum (\vec{M}) = \mathbf{0} \text{ (zero moment = no rotation)}$

Maintained by reaction forces and moments

Forces from supports / constraints are exactly enough to produce zero forces and moments

Assumption of rigid body

Shape and dimensions of body remain **unchanged** by application of forces.

More precisely:

All **deformations of bodies** are small enough to be ignored in analysis.



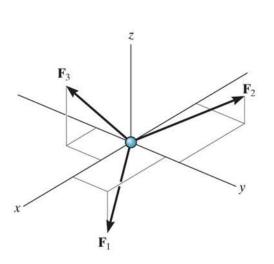


Equilibrium of a Rigid Body

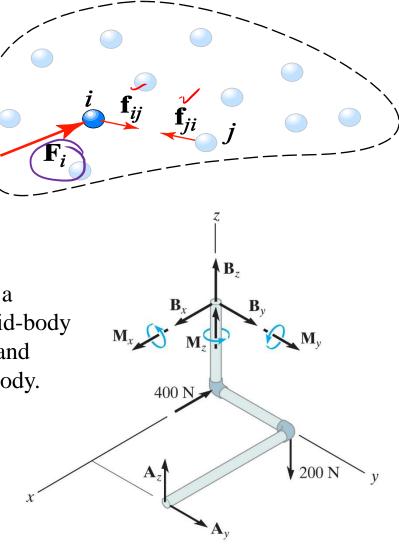
Equilibrium of a rigid body is of central importance in statics. We regard a rigid body as a collection of particles.

 $\overline{F_i} = \text{resultant external force on particle } i$ $\overline{f_{ij}} = \text{internal force on particle } i \text{ by particle } j$ $\overline{f_{ij}} = \text{internal force on particle } j \text{ by particle } i$

Note that $\overrightarrow{f_{ij}} = \overrightarrow{f_{ij}}$ by Newton's third law. Therefore the internal forces will not appear in the equilibrium equations.

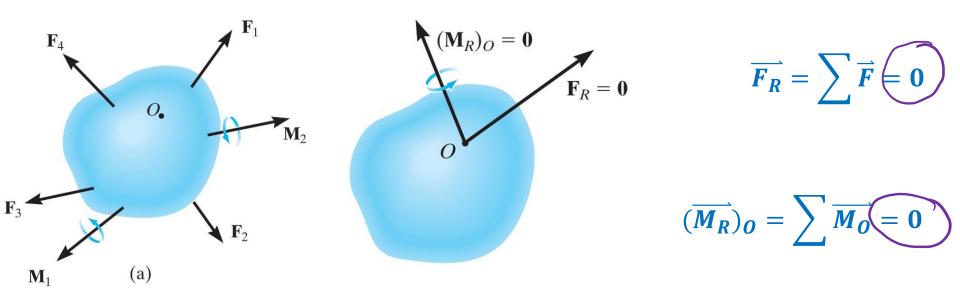


In contrast to the forces on a particle, the forces on a rigid-body are not usually concurrent and may cause rotation of the body.



Equilibrium of a Rigid Body

We can reduce the force and couple moment system acting on a body to an equivalent resultant force and a resultant couple moment at an arbitrary point O.

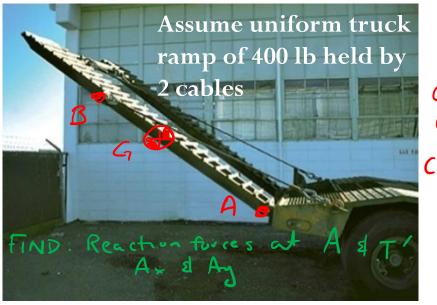


Recap: General procedure for analysis

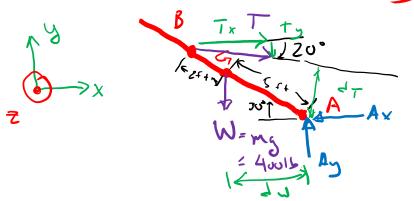
- 1. Read the problem carefully; write it down carefully.
- 2. MODELTHE PROBLEM: Draw given diagrams neatly and construct additional figures as necessary.
- 3. Apply principles needed.
- 4. Solve problem symbolically. Make sure equations are dimensionally homogeneous
- Substitute numbers. Provide proper units *throughout*. Check significant figures. Box the final answer(s).
- 6. See if answer is reasonable.

Most effective way to learn engineering mechanics is to *solve problems!*

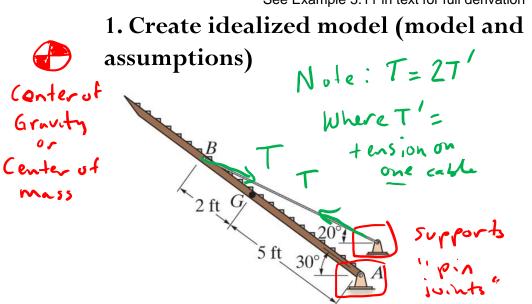
Process of solving rigid body equilibrium problems



2. Draw free body diagram showing <u>ALL</u> the external (applied loads and support reactions) $FBD \ of RAMP \ any$



This slide presents the basic approach for problem solving for this course (previous slide). Understand how to do this approach!



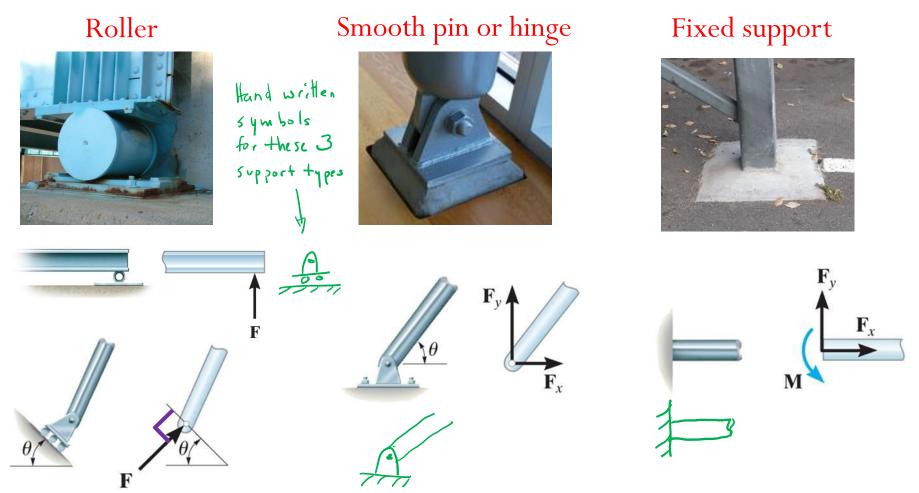
3. Apply equations of equilibrium $\overline{F_R} = \sum_{x} \overline{F} = 0$ $\underbrace{+}_{x} \leq F_x \leq -A_x + T_{cos} 20^\circ = 0$ $\underbrace{+}_{x} \leq F_y \circ A_y - \bigcup - T_{sin} 20^\circ = 0$

$$(\overline{M_R})_A = \sum \overline{M_A} = \mathbf{0}$$

Let's sum moments about pt A. <u>Pick pt to sum moments</u> <u>that eliminates as many unknowns as possible</u>.

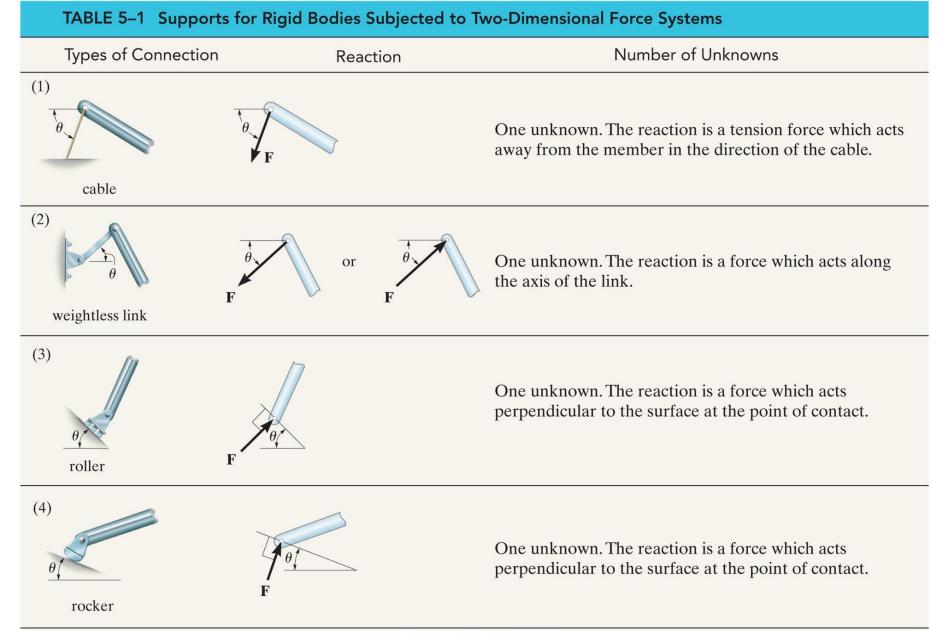
+)
$$ZM_{A}$$
: + $W(d_{u}) - T(d_{T}) = 0$ 3

Equilibrium in <u>two-dimensional</u> bodies (Support reactions)

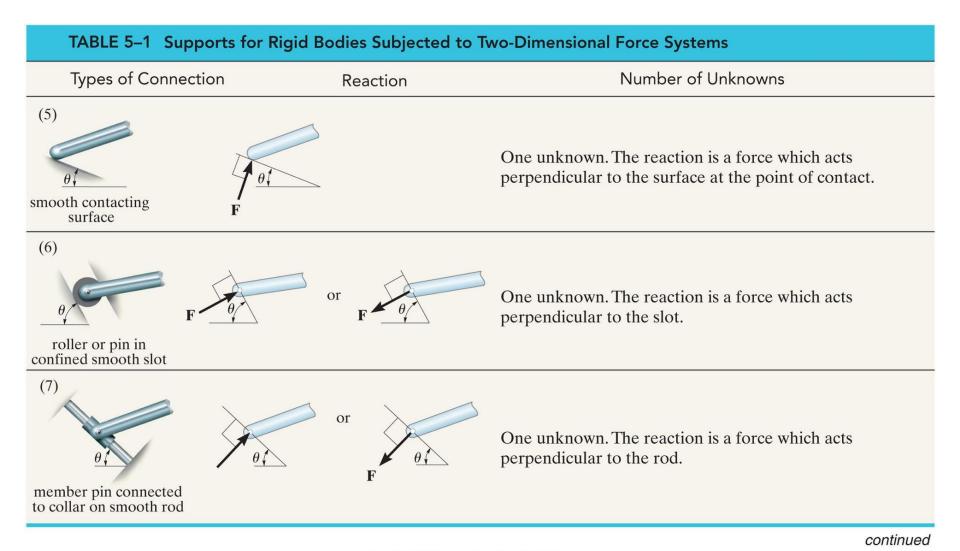


- If a support prevents the translation of a body in a given direction, then a force is developed on the body on that direction
- If a rotation is prevented, a couple moment is exerted on the body

Types of connectors



Types of connectors



Copyright ©2016 Pearson Education, All Rights Reserved

Types of connectors

